

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				

Pearson Edexcel International Advanced Level

Friday 12 January 2024

Morning (Time: 1 hour 30 minutes) **Paper reference** **WFM01/01**

Mathematics

International Advanced Subsidiary/ Advanced Level

Further Pure Mathematics F1

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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1.

$$\mathbf{M} = \begin{pmatrix} 2k + 1 & k \\ k + 7 & k + 4 \end{pmatrix} \text{ where } k \text{ is a constant}$$

(a) Show that \mathbf{M} is non-singular for all real values of k .

(3)

(b) Determine \mathbf{M}^{-1} in terms of k .

(2)



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Question 1 continued

Lined area for writing answers.

(Total for Question 1 is 5 marks)



$$f(z) = 2z^3 + pz^2 + qz - 41$$

The complex number $5 - 4i$ is a root of the equation $f(z) = 0$

- (2)

(d) Determine the area of this triangle.

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Question 2 continued

Lined area for writing the answer to Question 2.



Question 2 continued

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Question 2 continued

Lined area for writing answers.

(Total for Question 2 is 9 marks)



3. The hyperbola H has equation $xy = c^2$ where c is a positive constant.

The point $P\left(ct, \frac{c}{t}\right)$, where $t > 0$, lies on H .

The tangent to H at P meets the x -axis at the point A and meets the y -axis at the point B .

- (a) Determine, in terms of c and t ,

(i) the coordinates of A ,

(ii) the coordinates of B .

(4)

Given that the area of triangle AOB , where O is the origin, is 90 square units,

- (b) determine the value of c , giving your answer as a simplified surd.

(2)



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Question 3 continued

Lined area for writing the answer to Question 3.

(Total for Question 3 is 6 marks)



4.

$$\mathbf{A} = \begin{pmatrix} 1 & 0 \\ 0 & 3 \end{pmatrix}$$

- (a) Describe the single geometrical transformation represented by the matrix \mathbf{A} . (2)

The matrix **B** represents a rotation of 210° anticlockwise about centre $(0, 0)$.

- (b) Write down the matrix \mathbf{B} , giving each element in exact form. (1)

The transformation represented by matrix **A** followed by the transformation represented by matrix **B** is represented by the matrix **C**.

- (c) Find \mathbf{C} . (2)

The hexagon H is transformed onto the hexagon H' by the matrix C .

- (d) Given that the area of hexagon H is 5 square units, determine the area of hexagon H' (2)



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Question 4 continued

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(Total for Question 4 is 7 marks)



5. The quadratic equation

$$2x^2 - 3x + 7 = 0$$

has roots α and β

Without solving the equation,

(a) write down the value of $(\alpha + \beta)$ and the value of $\alpha\beta$

(1)

(b) determine the value of $\alpha^2 + \beta^2$

(2)

(c) find a quadratic equation which has roots

$$\left(\alpha - \frac{1}{\beta^2}\right) \text{ and } \left(\beta - \frac{1}{\alpha^2}\right)$$

giving your answer in the form $px^2 + qx + r = 0$ where p , q and r are integers to be determined.

(6)



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Question 5 continued

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Question 5 continued

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Question 5 continued

Lined area for writing the answer to Question 5.

(Total for Question 5 is 9 marks)



6. (i)

$$f(x) = x - 4 - \cos(5\sqrt{x}) \quad x > 0$$

- (a) Show that the equation $f(x) = 0$ has a root α in the interval $[2.5, 3.5]$ (2)
- (b) Use linear interpolation once on the interval $[2.5, 3.5]$ to find an approximation to α , giving your answer to 2 decimal places. (2)

(ii)

$$g(x) = \frac{1}{10}x^2 - \frac{1}{2x^2} + x - 11 \quad x > 0$$

- (a) Determine $g'(x)$. (2)

The equation $g(x) = 0$ has a root β in the interval $[6, 7]$

- (b) Using $x_0 = 6$ as a first approximation to β , apply the Newton–Raphson procedure once to $g(x)$ to find a second approximation to β , giving your answer to 3 decimal places.



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Question 6 continued

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Question 6 continued

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Question 6 continued

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(Total for Question 6 is 8 marks)



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Question 7 continued

Lined area for writing the answer to Question 7.

(Total for Question 7 is 7 marks)



8. (a) Use the standard results for summations to show that, for all positive integers n ,

$$\sum_{r=1}^n r(2r^2 - 3r - 1) = \frac{1}{2}n(n+1)^2(n-2) \quad (4)$$

- (b) Hence show that, for all positive integers n ,

$$\sum_{r=n}^{2n} r(2r^2 - 3r - 1) = \frac{1}{2}n(n-1)(an+b)(cn+d)$$

where a, b, c and d are integers to be determined.

(4)



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Question 8 continued

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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 8 marks)



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Question 9 continued

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(Total for Question 9 is 6 marks)



10. (i) Prove by induction that for $n \in \mathbb{Z}^+$

$$\begin{pmatrix} 5 & -1 \\ 4 & 1 \end{pmatrix}^n = 3^{n-1} \begin{pmatrix} 2n+3 & -n \\ 4n & 3-2n \end{pmatrix} \quad (5)$$

(ii) Prove by induction that for $n \in \mathbb{Z}^+$

$$f(n) = 8^{2n+1} + 6^{2n-1}$$

is divisible by 7

(5)



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Question 10 continued

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Question 10 continued

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Question 10 continued

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Question 10 continued

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(Total for Question 10 is 10 marks)

TOTAL FOR PAPER IS 75 MARKS

