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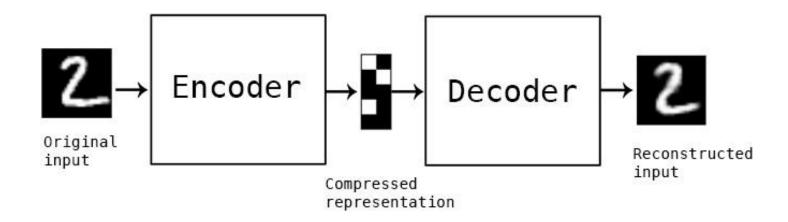
KDD 2019

Keywords

Variational Autoencoder, Generative Adversarial Network, Representation Learning, Semi-Supervised Classification



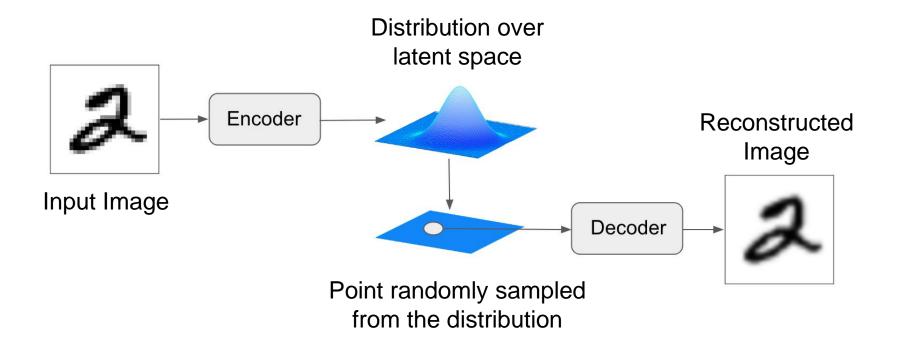
Autoencoders (AEs)



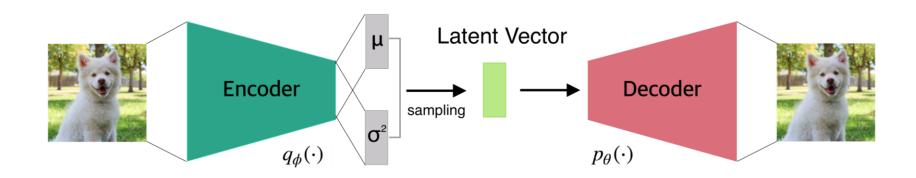
$$\min_{\phi,\theta} L_{rec} = \min \frac{1}{n} \sum_{i=1}^{n} \| \mathbf{x}_i - g_{\theta}(f_{\phi}(\mathbf{x}_i)) \|^2$$



Variational Autoencoders (VAEs)



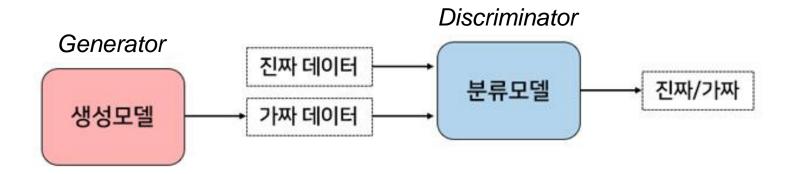
Variational Autoencoders (VAEs)



$$L = -E_{z \sim q(z|x)} \left[\log p(x|z) \right] + D_{KL} \left(q\left(z|x \right) || p\left(z \right) \right)$$



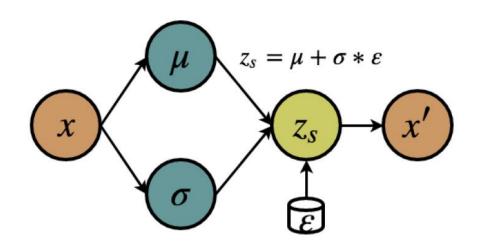
GAN (Generative Adversarial Network)



$$\min_{G} \max_{D} V(D,G) = E_{x \sim p_{data}(x)}[log D(x)] + E_{z \sim p_{z}(z)}[log(1 - D(G(z))]$$



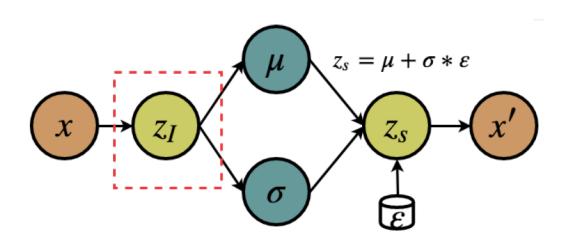
Motivation - Why VAE++.



(a) Standard VAE



Motivation - Why VAE++.



(b) VAE++



Motivation

□ Why VAE++ needs the Semi-supervised GAN.

To reduce the information loss between the two latent representations z_I and z_S to guarantee the learned z_I is representative.

□ Why Semi-supervised GAN needs the VAE++.

To provide a meaningful prior distribution that can represent the distribution of the input data.



Related Work



VAE for Semi-supervised Learning Semi-supervised GAN Combination of VAE and GAN



Proposed Method

1. To focus on **semi-supervised classification** instead of generation.

2. To attempt to learn an **exclusive latent representation** instead of a stochastic sampled representation.

3. To works on improvement of latent space instead of data space.



Methodology



Preliminary

Input dataset
$$(N = N_L + N_U)$$
 $\mathbf{x}_i^L \in \mathbb{R}^M$ $\mathbf{y}_i \in \mathbb{R}^K$ Labelled Samples $(\mathbf{X}^L, \mathbf{Y}^L) = \{(\mathbf{x}_1^L, \mathbf{y}_1), (\mathbf{x}_2^L, \mathbf{y}_2), \cdots, (\mathbf{x}_{N_L}^L, \mathbf{y}_{N_L})\}$ Unlabelled Samples $\mathbf{X}^U = \{\mathbf{x}_1^U, \mathbf{x}_2^U, \cdots, \mathbf{x}_{N_U}^U\}$ $\mathbf{x}_i^U \in \mathbb{R}^M$

- 1. To learn a latent representation which is rich of distinguishable information.
- 2. To build an encoder to provide an **embedding or feature representation** which allows accurate classification even with limited observations.



VAE

The VAE maps the input

observation x to a compressed code z_s , and decodes it to reconstruct the observation. The latent representation is calculated through the reparameterization trick [16]:

$$z_s = \mu_{\boldsymbol{x}} + \sigma_{\boldsymbol{x}} * \boldsymbol{\varepsilon} \tag{1}$$

with $\varepsilon \sim \mathcal{N}(0, 1)$ to impose the posterior distribution of the latent code on $\underline{p(z_s|x)} \sim \mathcal{N}(\mu_x, \sigma_x^2)$. μ_x and σ_x denote the expectation and standard deviation of the posterior distribution of z_s , which are learned from x. For the efficient generation and reconstruction, VAE imposes the code z_s on a prior Gaussian distribution:

$$\bar{p}(z_s) = \mathcal{N}(z_s|0,I)$$

Through minimizing the reconstruction error between x and x' and restricting the distribution of z_s to approximate the prior distribution $\bar{p}(z_s)$, VAE is supposed to learn the representative latent code z_s which can be used for classification or generation.



Limitation of Standard VAE

$$z_s = g(\mu_{\mathbf{x}}, \sigma_{\mathbf{x}}, \boldsymbol{\varepsilon})$$

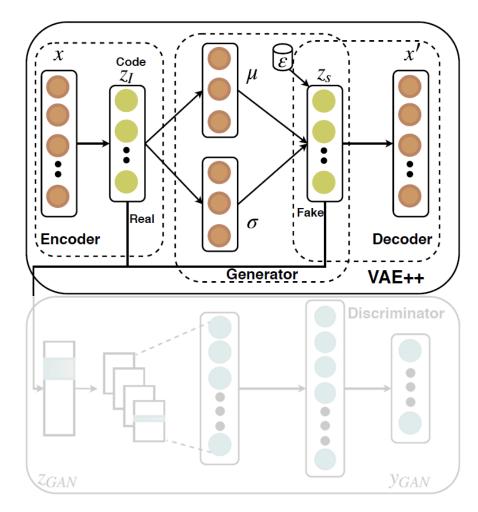
 $z_s = g(\mu_{\boldsymbol{x}}, \sigma_{\boldsymbol{x}}, \boldsymbol{\varepsilon})$ The learned latent code is not **exclusive**.

The latent code z_s is determined by two factors.

the prior distribution of observation $\bar{p}(x)$ the stochastically sampled data $\pmb{\varepsilon}$



AVAE - VAE++





VAE++ – Encoder and Generator

non-linear transformation
$$p_{\boldsymbol{\theta}_{en}}(\boldsymbol{z}_{I}|\boldsymbol{x}) = f(\boldsymbol{z}_{I};\boldsymbol{x},\boldsymbol{\theta}_{en})$$

$$\downarrow$$
encoder parameters exclusive latent code $z_{I} \in \mathbb{R}^{D}$

$$z_s = \mu(z_I) + \sigma(z_I) * \varepsilon$$



VAE++ - Decoder and Loss

non-linear rendering
$$p_{\theta_{de}}(x'|z_s) = f'(x';z_s,\theta_{de})$$

$$p_{\theta_{de}}(x'|z_s) = f'(x';z_s,\theta_{de})$$
reconstructed observation

decoder parameters

$$\mathcal{L}_{VAE} = -\mathbb{E}_{\boldsymbol{z}_{s} \sim p_{\boldsymbol{\theta}_{en}}(\boldsymbol{z}_{s}|\boldsymbol{x})}[\log p_{\boldsymbol{\theta}_{de}}(\boldsymbol{x}'|\boldsymbol{z}_{s})] + KL(p_{\boldsymbol{\theta}_{en}}(\boldsymbol{z}_{s}|\boldsymbol{x})||\bar{p}(\boldsymbol{z}_{s}))$$



VAE++

$$z_s = \mu(z_I) + \sigma(z_I) * \varepsilon$$

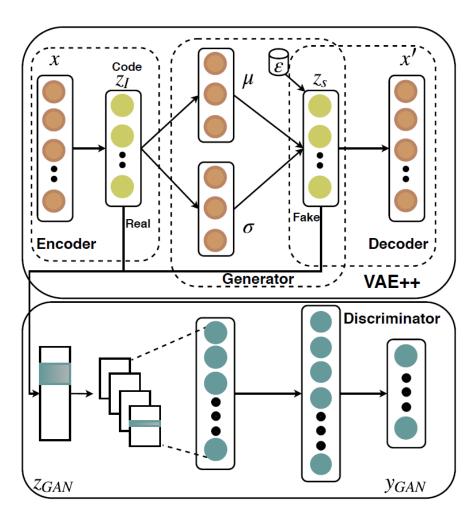
From equation (2), we can observe that the expectation and standard deviation of z_s and z_I are invariant. In particular, for a specific sample x_i , the corresponding z_{si} and z_{Ii} have the same statistical characteristics. Thus, we have

$$z_s \leftarrow \mu(z_I), \sigma(z_I), \varepsilon$$

which indicates that the generated z_s is affected by both the distribution (or statistic characteristics) of z_I and the prior distribution $\bar{p}(z_s)$ (or ε). In summary, the z_s inherits the statistical characteristics of z_I .



AVAE





□ Generator

For labelled observations $m{x}^L
ightharpoonup m{z}_I^L \in \mathbb{R}^D$, $m{z}_s^L \in \mathbb{R}^D$

For unlabelled observations $oldsymbol{x}^U
ightharpoonup oldsymbol{z}_I^U \in \mathbb{R}^D, \ oldsymbol{z}_s^U \in \mathbb{R}^D$

$$\boldsymbol{y} \in \mathbb{R}^{K} \quad \Longrightarrow \quad \boldsymbol{y}_{GAN} \in \mathbb{R}^{K+1}$$

K possible classes to K + 1 possible classes regarding generated fake samples



Discriminator

input of the discriminator
$$q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN}) = h(m{y}_{GAN};m{z}_{GAN},m{arphi})$$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN}) = h(m{y}_{GAN};m{z}_{GAN},m{arphi})$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN},m{arphi})$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN},m{arphi})$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN},m{arphi})$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN},m{arphi})$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN},m{arphi})$
 $q_{m{arphi}}(m{y}_{GAN}|m{z}_{GAN},m{arphi})$



$$\mathcal{L}_{label} = -\mathbb{E}_{\boldsymbol{z}_{GAN}, \boldsymbol{y}_{GAN} \sim p_{j}}[log\boldsymbol{q}_{\boldsymbol{\varphi}}(\boldsymbol{y}_{GAN}|\boldsymbol{z}_{GAN}, \boldsymbol{y}_{GAN} < K + 1)]$$

$$\mathcal{L}_{unlabel} = -\mathbb{E}_{\boldsymbol{z}_{GAN} \sim p_{\boldsymbol{\theta}en}(\boldsymbol{z}_{I}|\boldsymbol{x})}[log(1 - \boldsymbol{q}_{\boldsymbol{\varphi}}(\boldsymbol{y}_{GAN} = K + 1|\boldsymbol{z}_{GAN}))]$$

$$-\mathbb{E}_{\boldsymbol{z}_{GAN} \sim p_{\boldsymbol{\theta}en}(\boldsymbol{z}_{S}|\boldsymbol{x})}[log(\boldsymbol{q}_{\boldsymbol{\varphi}}(\boldsymbol{y}_{GAN} = K + 1|\boldsymbol{z}_{GAN}))]$$

$$\mathcal{L}_{GAN} = w_1 * flag * \mathcal{L}_{label} + w_2 * (1 - flag) * \mathcal{L}_{unlabel}$$
 w_1, w_2 : weight $flag = \begin{cases} 1 & labelled \\ 0 & unlabelled \end{cases}$



If the specific observation is labelled, we calculate the labelled loss function. Otherwise, we calculate the unlabelled loss function. From empirical experiments, we observe that the $\mathcal{L}_{unlabel}$ is much easier to converge than \mathcal{L}_{label} and the real/fake classification accuracy is much higher than the K classes classification accuracy. To encourage the optimizer to focus on the former part which is more difficult to converge, we set $w_1 = 0.9$ and $w_2 = 0.1$

The discriminator receives z_{GAN} as input and extracts the dependencies through CNN filters. Two fully connected layers follow the convolutional layer for dimension reduction. At last, a softmax layer is employed to work on the low-dimension features to estimate the log normalization of the categorical probability distribution which is output as y_{GAN} .

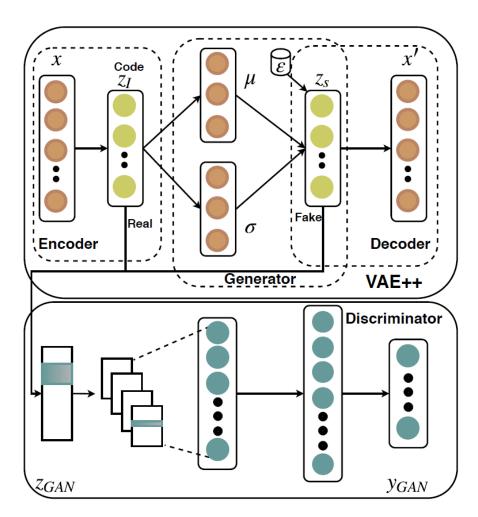


ALGORITHM 1: Adversarial Variational Embedding

```
Input: labelled observations (X^L, Y^L) and unlabelled observations X^U
Output: Representation z_I
  1: Initialize network parameters \theta_{en}, \theta_{de}, q_{\varphi}
 2: for x \in \{X^L, X^U\} do
  3: z_I \leftarrow x
  4: \mu, \sigma \leftarrow z_I
  5: Sampling \varepsilon from \mathcal{N}(0, I)
  6: \mathbf{z}_{S} = \mu(\mathbf{z}_{I}) + \sigma(\mathbf{z}_{I}) * \boldsymbol{\varepsilon}
 7: x' \leftarrow z_s
  8: \mathcal{L}_{VAE} \leftarrow \mathbf{x}, \mathbf{x}', p(\mathbf{z}_{S}|\mathbf{x})
 9: for z_I, z_s, \boldsymbol{y} \in Y^L do
        \boldsymbol{y}_{GAN} \leftarrow z_I, z_S
               \mathcal{L}_{GAN} \leftarrow \boldsymbol{y}_{GAN}, \boldsymbol{y}
          end for
           Minimize \mathcal{L}_{VAE} and \mathcal{L}_{GAN}
14: end for
15: return z_I
```



AVAE





Experiments



Experiments – (1) Activity Recognition

Experiment Setup

- PAMAP2 dataset Cycling, standing, walking, lying and running.
- The time window is set as 10 with 50% overlapping.
- Training set 80%, testing set 20%

Application-related State-of-the-arts

- Chen et al. [6] adopt an attention mechanism to select the Guo et al. [12] exploit the diversity of base classifiers to conmost distinguishable features from the activity signals and send them to a CNN structure for classification.
- Lara et al. [18] apply both statistical and structural detectors features to discriminate among activities.
- struct a good ensemble for multimodal activity recognition, and the diversity measure is obtained from both labelled and unlabelled data.
- Zhang et al. [40] combine deep learning and the reinforcement learning scheme to focus on the crucial dimensions of the signals.



Experiments – (2) Neurological Diagnosis

□ Experiment Setup

- TUH dataset EEG data (Epileptic seizure state and normal state)
- The sampling rate is set as 250Hz
- Select 12,000 samples from each of 18 subjects.

■ Application-related State-of-the-arts

- Ziyabari et al. [41] adopt a hybrid deep learning architecture, including LSTM and stacked denoising Autoencoder, which integrates temporal and spatial context to detect the epileptic seizure.
- Harati et al. [13] demonstrate that a variant of the filter bankbased approach, coupled with first and second derivatives, provides a reduction in the overall error rate.
- Schimeister et al. [32] attempt to improve the performance of seizure detection by combining deep ConvNets with training strategies such as exponential linear units.
- Goodwin et al. [11] combine RNN with access to textual data in EEG reports in order to automatically extracting word-and report-level features and infer underspecified information from EHRs (electronic health records).

Experiments – (3) Image Classification

Experiment Setup

- To evaluate the representation learning ability in images.
- MNIST dataset Handwritten(0-9) digital images.
- 50,000 for training, 10,000 for testing.

Application-related State-of-the-arts

- Augustus [26] proposes a semi-supervised GAN (SGAN) by forcing the discriminator network to output class labels.
- Springenberg [34] proposes CatGAN to modify the objective Miyato et al. [23] propose a regularization method based on function taking into account the mutual information between observation and the prediction distribution.
- Weston et al. [36] apply kernel methods for a nonlinear semisupervised embedding algorithm.
 - virtual adversarial loss: a new measure of local smoothness of the conditional label distribution given the inputs.



Experiments – (4) Recommender System

□ Experiment Setup

- Yelp dataset Restaurant attributes(13) and ratings(1-5)
- A unseen business's attributes as input data and predict the possible ratings from the potential customers.

■ Application-related State-of-the-arts

- Pazzani et al. [27] summarizes basic content-based recommendation approaches, from which we select the cosine similaritybased nearest neighbour method as our fundamental baseline.
- Rendle [30] proposes the original implementation of factorization machine(FM) which is capable of incorporating item features with explicit feedbacks. We concatenate only the item indication vector and its feature after each user indication vector following the format in [30].
- He et al. [14] enhances the original FM using deep neural networks to learn high-order interactions between different item features.
- Chen et al. [5] applies feature- and item-level attention on item features, which is capable of emphasizing on the most important features.



Experiments – Algorithm-related SOTA

- M2. [15] proposes a probabilistic model that describes the data as being generated by a latent class variable in addition to a continuous latent representation.
- Adversarial Autoencoders (AAE). [21] employs the GAN to perform variational inference by matching the aggregated posterior of the hidden representation of the autoencoder.
- Ladder Variational Autoencoders (LVAE). [33] proposes an inference model which recursively corrects the generative distribution by a data dependent likelihood.
- Auxiliary Deep Generative Models (ADGM). [20] extends deep generative models with auxiliary variables, which improves the variational approximation.



Semi-supervised Classification Accuracy(1)

Table 1: Overall comparison of semi-supervised classification accuracy (%) on activity recognition. All the baselines and our approach are working on the same dataset and sharing the same experiment settings for each specific application.

Dataset	Rate (%)	Algorithm-related State-of-the-art				App	lication-relate	ed State-of-the	e-art	I	Ours		
		M2	AAE	LVAE	ADGM	[6]	[18]	[12]	[40]	VAE (µ)	VAE	VAE++	AVAE
	20	64.83±0.16	63.67±0.23	69.82±0.69	67.31±0.45	72.31±0.16	70.95±0.08	67.31±0.14	76.68±0.31	58.43±0.13	76.51±0.53	78.12±0.55	78.63±0.38
Activity	40	68.92±0.23	76.83 ± 0.25	76.43 ± 0.19	78.21 ± 0.38	80.51±0.21	75.38 ± 0.12	77.28 ± 0.21	80.15±0.16	62.74±0.12	78.78 ± 0.22	80.88 ± 0.38	81.37±0.29
Recognition	60	72.35 ± 0.21	77.39 ± 0.19	78.69 ± 0.27	79.34±0.29	80.29±0.21	76.89 ± 0.05	79.69 ± 0.15	82.49 ± 0.33	67.85±0.08	79.63 ± 0.29	81.94±0.19	84.91±0.17
(PAMAP2)	80	75.88 ± 0.35	78.28 ± 0.11	81.41±0.23	80.38 ± 0.16	82.12±0.16	79.95 ± 0.18	81.65±0.09	83.56 ± 0.11	73.43±0.06	81.75 ± 0.17	82.08 ± 0.26	85.56±0.21
	100	77.59 ± 0.17	80.79 ± 0.14	84.39 ± 0.18	83.66±0.16	83.64±0.12	81.96±0.11	82.38 ± 0.13	84.59 ± 0.24	76.85±0.00	82.37 ± 0.25	83.29 ± 0.18	86.41±0.06

Note: If the compared method can not deal with unsupervised samples, it will be trained only by the supervised samples.

Table 2: Overall comparison of semi-supervised classification accuracy (%) on neurological diagnosis

Dataset	Rate (%)	Algorithm-related State-of-the-art					lication-relate	d State-of-the	e-art	I	Ours		
		M2	AAE	LVAE	ADGM	[41]	[13]	[32]	[11]	$VAE(\mu)$	VAE	VAE++	AVAE
	20	71.28±0.16	80.13±0.95	82.31±0.19	86.32±0.12	87.66±0.23	86.38±0.36	82.19±0.24	86.33±0.21	80.58±0.69	86.37±0.24	0.86±0.53	93.69±0.16
Neurological	40	75.32±0.16	82.95±0.26	84.38±0.16	86.99 ± 0.05	89.25±0.19	91.58±0.35	84.21±0.08	89.25±0.34	81.35±0.24	89.69 ± 0.27	91.28±0.25	94.32±0.28
Diagnosis	60	76.32±0.29	86.21±0.52	87.51±0.26	87.65±0.16	91.28±0.37	92.58±0.26	85.36±0.32	90.38±0.24	82.59±0.63	90.58 ± 0.27	92.87±0.31	95.21±0.21
(TUH)	80	79.65±0.37	88.53 ± 0.28	89.56±0.25	88.05 ± 0.12	92.59±0.26	93.25±0.31	85.16±0.24	91.59±0.16	83.21±0.21	91.69±0.35	93.96±0.28	97.86±0.26
	100	82.59±0.31	89.58±0.25	90.25±0.21	88.65 ± 0.26	93.32±0.18	94.29 ± 0.25	86.42±0.26	92.4±0.25	84.21±0.65	92.38 ± 0.41	94.65±0.24	98.13±0.32

supervision rate

$$N^L/(N^L + N^U)$$



Semi-supervised Classification Accuracy(2)

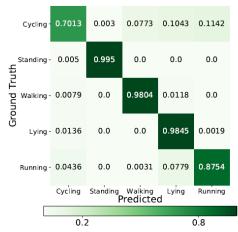
Table 3: Overall comparison of semi-supervised classification accuracy (%) on image classification

Dataset	Rate (%)	Algorithm-related State-of-the-art				Application-related State-of-the-art				A	Ours		
		M2	AAE	LVAE	ADGM	[26]	[34]	[36]	[23]	$VAE(\mu)$	VAE	VAE++	AVAE
	20	93.22±0.62	90.25±0.25	93.25±0.26	89.61±0.27	95.23±0.34	94.25±0.13	94.58±0.25	92.96±0.28	91.58±0.24	92.31±0.53	93.59±0.31	95.12±0.19
Image	40	93.25 ± 0.34	93.21±0.23	93.28 ± 0.46	91.58±0.25	95.27±0.53	95.56 ± 0.08	95.21±0.26	93.21±0.56	93.65±0.21	94.21±0.19	94.68 ± 0.28	96.43±0.35
Classification	60	96.24±0.51	96.35±0.27	95.34±0.21	93.21±0.34	96.38±0.22	96.54±0.08	96.48±0.32	96.28±0.57	94.89±0.21	95.34±0.14	96.42±0.25	97.21±0.21
(MNIST)	80	98.19±0.25	95.32 ± 0.37	96.11±0.52	95.01±0.15	97.82±0.11	97.21±0.13	97.86±0.34	97.63±0.15	96.78±0.25	97.63±0.15	98.71±0.16	99.79±0.12
	100	98.65±0.21	$0.98.25 \pm 0.61$	96.35±0.26	95.38 ± 0.82	99.21±0.26	98.64 ± 0.27	99.06±0.22	98.53 ± 0.17	97.41±0.18	98.35±0.09	99.67 ± 0.23	99.85±0.11

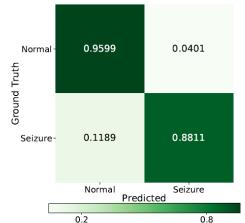
Table 4: Overall comparison of semi-supervised classification accuracy (%) on recommender system

Dataset	Rate (%)	Algorithm-related State-of-the-art					lication-relate	ed State-of-the	e-art	I	Ours		
		M2	AAE	LVAE	ADGM	[27]	[30]	[14]	[5]	VAE (µ)	VAE	VAE++	AVAE
		66.42±0.17	58.27±0.35	66.35±0.36	54.27±0.38	40.55±0.27	47.58±0.36	65.99±0.62	66.21±0.24	64.28±0.12	64.39±0.62	65.58±0.37	70.19±0.87
Recommender	20	69.36±0.37	61.55±0.62	68.16±0.24	55.35 ± 0.26	40.28±0.32	48.65 ± 0.27	67.53±0.31	66.59±0.29	64.37±0.25	67.23±0.95	71.05±0.29	72.21±0.35
System	40	72.58±0.19	62.15±0.39	68.59 ± 0.93	57.63 ± 0.23	42.15±0.16	50.95 ± 0.24	66.58±0.29	67.95±0.38	67.56±0.35	69.58±0.37	72.19 ± 0.62	75.34±0.35
(Yelp)	60	72.39±0.64	62.89 ± 0.62	74.28 ± 0.37	58.34±0.15	43.21±0.15	52.15±0.38	67.65±0.31	68.23±0.15	69.25±0.18	71.39 ± 0.56	73.21 ± 0.58	78.54±0.38
	80	74.58±0.62	63.51±0.86	72.59 ± 0.36	59.58 ± 0.23	45.86±0.22	54.10 ± 0.12	68.03 ± 0.17	70.61 ± 0.25	73.24±0.68	73.28 ± 0.69	76.53 ± 0.28	79.38±0.59

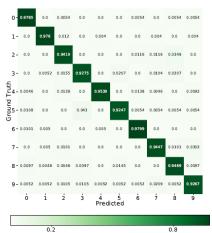
Confusion Matrix



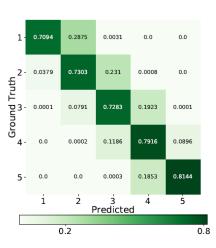
(a) Confusion matrix of PAMAP2



(b) Confusion matrix of TUH



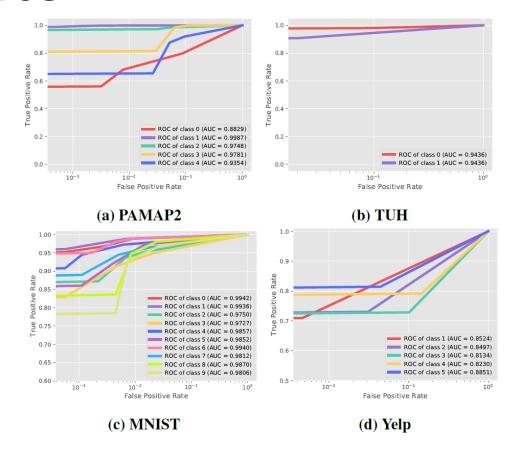
(c) Confusion matrix of MNIST



(d) Confusion matrix of Yelp

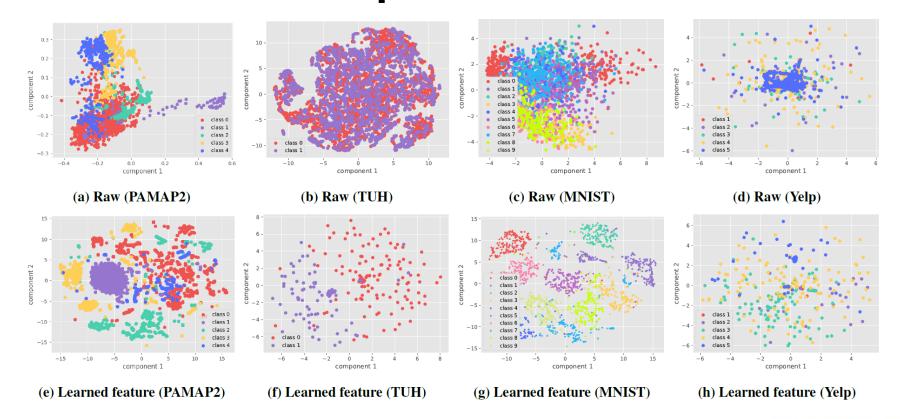


ROC curves





Visualization Comparison





Convergence Curve

