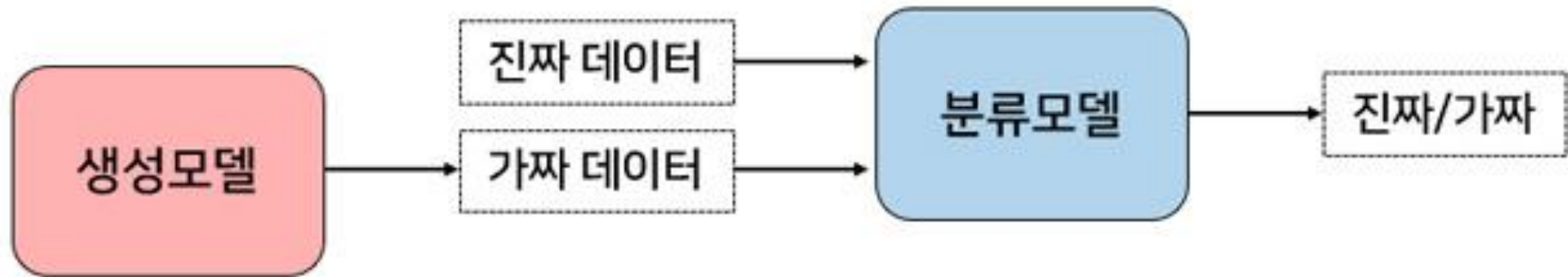


# Enhancing Collaborative Filtering with Generative Augmentation

KDD'19

# GAN

## □ Generative Adversarial Network



$$\min_G \max_D V(D, G) = E_{x \sim p_{data}(x)} [\log D(x)] + E_{z \sim p_z(z)} [\log(1 - D(G(z)))]$$

# Data Augmentation



# Preliminaries

First, we introduce some important notations used throughout the paper. Let  $\mathcal{U}$  and  $\mathcal{V}$  be the sets of all users and items, and let  $M$  and  $N$  be their sizes, respectively. We define the interaction between user  $u$  and item  $v$  in the dataset  $C$  as:

$$c = \begin{cases} 1, & u \text{ likes } v; \\ 0, & u \text{ dislikes } v; \\ \emptyset, & \text{unvisited} \end{cases} \quad (1)$$

# Preliminaries

we consider pure CF as a prediction task. Given a user  $u \in \mathcal{U}$  and an item  $v \in \mathcal{V}$ , the score for  $u$  likes  $v$  is estimated by  $f(u, v, c; \mathbf{P}, \mathbf{Q})$ , where  $f$  is a non-linear function and can be implemented by a deep neural nets,  $\mathbf{P}$  and  $\mathbf{Q}$  are matrices to map users and items into a joint latent space, respectively.  $\mathbf{P}$  and  $\mathbf{Q}$  are left out to make the notations more compact when no ambiguity arises. Then, the probability of  $c = 1$  is measured by the Sigmoid function:

$$P(c = 1) = \frac{\exp(f(u, v, c = 1))}{1 + \exp(f(u, v, c = 1))} \quad (2)$$

# Preliminaries

When an item  $v$  is sampled from the real data, we use  $y = 1$  or  $y = 0$  to represent that user  $u$  likes it ( $c = 1$ ) or not ( $c = 0$ ). Similarly, when an item  $v$  is from the generator (i.e., fake item), we instead use  $y = 3$  or  $y = 2$  to represent the same meaning. Next, we briefly introduce how this labeling system supports the two-phase training. In Phase I, since we always train the generator and discriminator under the same class and user (i.e.,  $c$  is fixed), the label  $y$  that discriminator needs to map an input item into is confined to  $\{0, 2\}$  when  $c = 0$ , or  $\{1, 3\}$  when  $c = 1$ , depending on where  $v$  is from.



# Preliminaries

the discriminator just behaves like a normal pure CF method except that it would map a  $(u, v)$  pair into both  $y = 0$  and  $y = 2$  if  $u$  dislikes  $v$ , otherwise, it is mapped into both  $y = 1$  and  $y = 3$ . As such, we extend the original pure CF score function  $f$  introduced above to enable this multi-label objective, in this way, the score for label  $i$  can be measured by  $f(u, v, y)$  where  $y \in \{0, 1, 2, 3\}$ , and Sigmoid in Eq. 2 is replaced by Softmax:

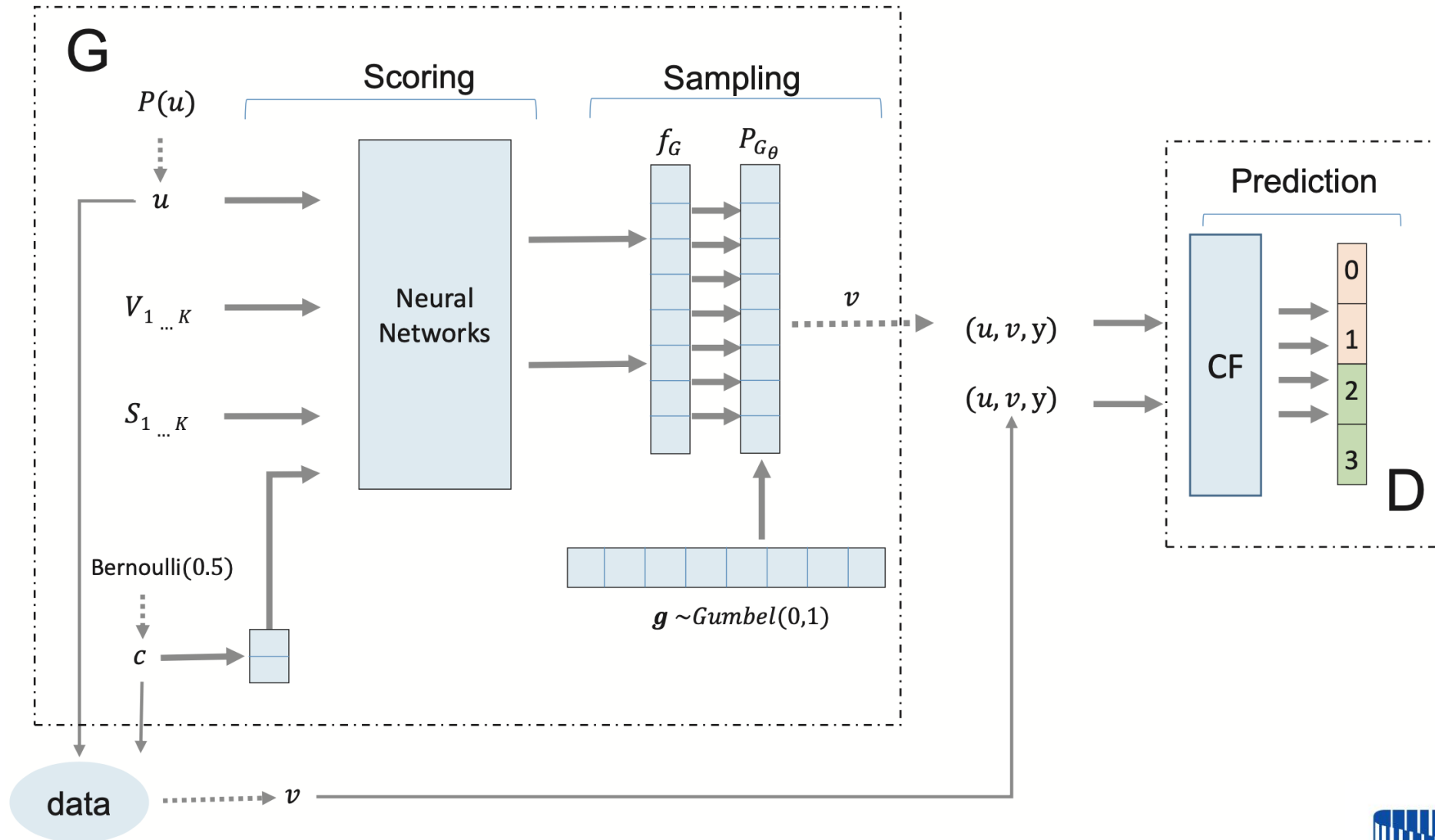
$$P(y = i) = \frac{\exp(f(u, v, y = i))}{\sum_{j=0}^3 \exp(f(u, v, y = j))} \quad (3)$$

# Model Overview

AugCF has two major components: the generator (denoted as  $G_\theta$ ) and the discriminator (denoted as  $D_\phi$ ) with parameters  $\theta$  and  $\phi$  respectively. The generator as a data augmentor can generate high-quality and reliable  $(u, v, c)$  tuples while the discriminator plays two roles in the model. First, it distinguishes between a real tuple sampled from  $C$  and a fake tuple generated by  $G_\theta$ . Then, it further acts as a pure CF method to predict whether  $u$  likes a given  $v$  or not.



# AugCF



# Phase I: Data Augmentation

$$\theta^*, \phi^* = \min_{\theta} \max_{\phi} (\mathbb{E}_{(u, v, y) \sim P_C(v|u, c)} \log[D_{\phi}(v, y|u, c), y \in \{0, 1\}] \\ + \mathbb{E}_{(u, v, y) \sim P_{G_{\theta}}(v|u, c)} \log[D_{\phi}(v, y|u, c), y \in \{2, 3\}])$$

$$* \min_G \max_D V(D, G) = E_{x \sim p_{data}(x)}[\log D(x)] + E_{z \sim p_z(z)}[\log(1 - D(G(z)))]$$

# Phase I: Data Augmentation

## □ Discriminator

Given an item under a user and a class, the discriminator needs to discriminate whether it is real or fake. According to Eq. 4, the objective for training the discriminator in Phase I is:

$$\phi_I^* = \max_{\phi}(L_D^I) \quad (5)$$

where

$$L_D^I = \mathbb{E}_{(u,v,y) \sim P_C(v|u,c)} \log[D_{\phi}(v, y|u, c), y \in \{0, 1\}] + \mathbb{E}_{(u,v,y) \sim P_{G_{\theta}}(v|u,c)} \log[D_{\phi}(v, y|u, c), y \in \{2, 3\}]$$

where  $D_{\phi}(v, y|u, c)$  estimates whether an item is fake or real conditioning on a specific class  $c$  and a user  $u$ , which is achieved by constraining the probability  $P$  to  $c$  and  $u$ :

$$D_{\phi}(v, y|u, c) = P(y|v; u, c) = \frac{\exp(f(u, v, y))}{\sum_{i=0}^3 \exp(f(u, v, y = i))} \quad (6)$$

# Phase I: Data Augmentation

## □ Generator

First, we sample a user  $u$  from  $\mathcal{U}$  based on this subsampling strategy:

$$P(u) = 1 - \sqrt{\frac{t}{h(u)}} \quad (7)$$

where  $h(u)$  is the frequency of user  $u$  (i.e., number of  $u$ 's interactions) and  $t$  is a predefined threshold. In this way, the less active users have higher probabilities to be sampled.

# Phase I: Data Augmentation

## □ Generator

We only randomly sample  $K$  of them, denoted as  $\mathcal{V}_u = \{v_1, \dots, v_K\}$ , and their associated side information is denoted as  $\mathcal{S}_u = \{\mathcal{S}_1, \mathcal{S}_1, \dots, \mathcal{S}_K\}$ . Following these steps,  $u$ ,  $c$ ,  $\mathcal{V}_u$  and  $\mathcal{S}_u$  are fed into  $G_\theta$ , obtaining a point-wise probability distribution  $P_{G_\theta}(v_i|u, c)$ :

$$P_{G_\theta}(v_i|u, c) = \frac{\exp f_G(u, v_i, \mathcal{S}_i, c)}{\sum_{j=1}^K \exp f_G(u, v_j, \mathcal{S}_j, c)} \quad (8)$$

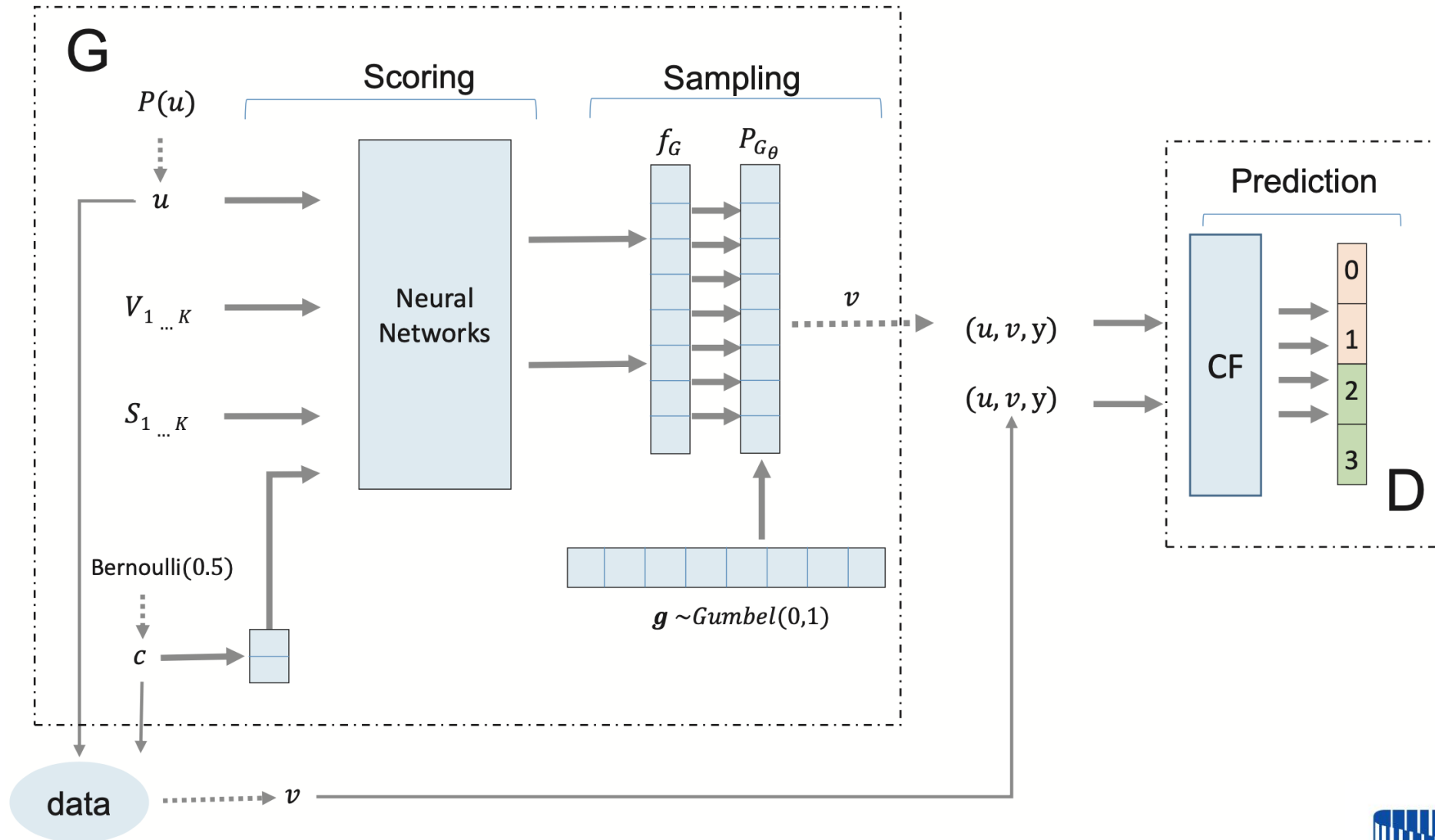
# Phase I: Data Augmentation

## □ Generator

$$\begin{aligned}\theta^* &= \min_{\theta} ((\mathbb{E}_{(u, v, y) \sim P_C(v|u, c)} \log[D_{\phi}(v, y|u, c), y \in \{0, 1\}] + \\ &\quad \mathbb{E}_{(u, v, y) \sim P_{G_{\theta}}(v|u, c)} \log[D_{\phi}(v, y|u, c), y \in \{2, 3\}]) \\ &= \max_{\theta} (\underbrace{\mathbb{E}_{(u, v, y) \sim P_{G_{\theta}}(v|u, c)} \log[D_{\phi}(v, y|u, c), y \in \{0, 1\}]}_{\text{denoted as } L_G^I})\end{aligned}$$



# AugCF



# Phase II: Pure Collaborative Filtering

$$\phi^* = \max_{\phi} ( \underbrace{\mathcal{L}_R + \mathcal{L}_G}_{\text{denoted as } L_D^{II}} ) \quad (10)$$

where,

$$\mathcal{L}_R = \mathbb{E}_{(u,v,y) \sim P_C} \log[D_{\phi}(y|u,v) + D_{\phi}(y'|u,v), y \in \{0,1\}, y' \in \{2,3\}]$$

,

$$\mathcal{L}_G = \mathbb{E}_{(u,v,y) \sim P_{G_{\theta^*}}} \log[D_{\phi}(y|u,v) + D_{\phi}(y'|u,v), y \in \{2,3\}, y' \in \{0,1\}]$$

and

$$D_{\phi}(y|u,v) = P(y|u,v) = \frac{\exp(f(u,v,y))}{\sum_{i=0}^3 \exp(f(u,v,y=i))}$$

# End-to-End Training

Specifically, let  $\mathbf{g}$  be a  $K$ -dimensional noise vector, where  $g_1, \dots, g_K$  are i.i.d sampled from  $Gumbel(0, 1)^2$ . We then obtain the sampled item  $\mathbf{v}$  in one-hot representation, i.e., the position of  $v$  in this one-hot vector is 1 while the other elements are 0, using the arg max operation using the Gumbel-Max trick [28]:

$$\mathbf{v} = \text{one\_hot} \left( \arg \max_i \left[ \log P_{G_\theta}(v_i) + g_i \right] \right) \quad (11)$$

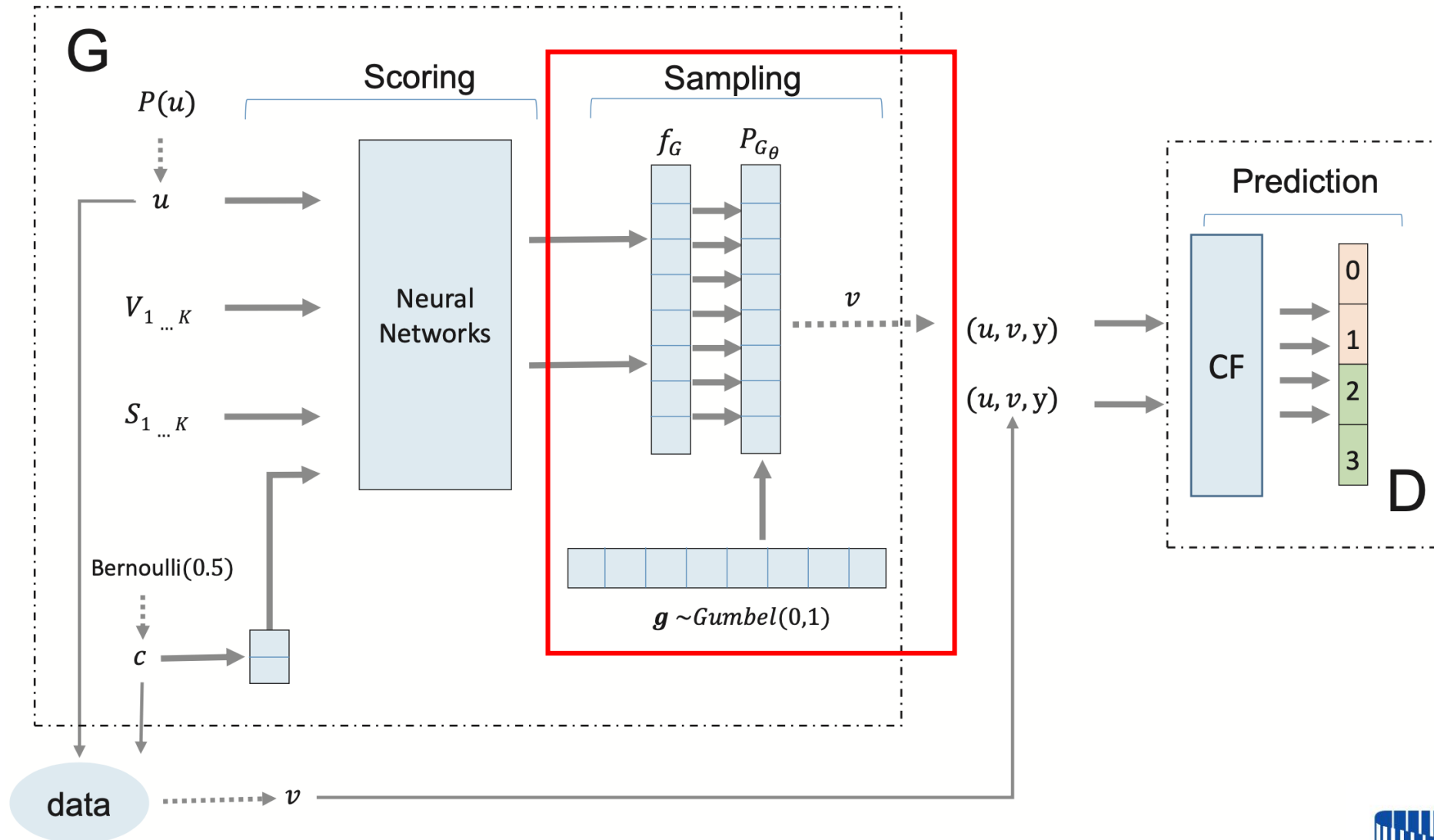
# End-to-End Training

Since the arg max operation, again, is not differentiable, the continuous and differentiable softmax function is replaced to approximate it, which is called Gumbel-Softmax [20]. Finally, we obtain an approximate one-hot representation of the sampled item  $\mathbf{v}$ , i.e.,

$$v_i = \frac{\exp((\log P_{G_\theta}(v_i) + g_i)/\tau)}{\sum_{j=1}^K \exp((\log P_{G_\theta}(v_j) + g_j)/\tau)} \quad \text{for } i = 1, \dots, K \quad (12)$$

where  $\tau$  is a hyper-parameter called temperature, and when it approaches 0, samples from the Gumbel-Softmax distribution become one-hot and the Gumbel-Softmax distribution becomes identical to the multinomial distribution  $P_{G_\theta}$ .

# AugCF



# Algorithm

```
19 for each epoch in Phase II do
20    $\mathcal{B}_{gen} = \emptyset; \mathcal{B}_{real} = \emptyset;$  //sets for generated and real data
21    $G_{\theta^*}$  generates a batch of tuples, adding to  $\mathcal{B}_{gen};$ 
22   Add a batch of tuples sampled from  $C$  to  $\mathcal{B}_{real};$ 
23   Update  $D_{\phi}$  with both  $\mathcal{B}_{gen}$  and  $\mathcal{B}_{real}$  based on Eq. 14;
24 end
```

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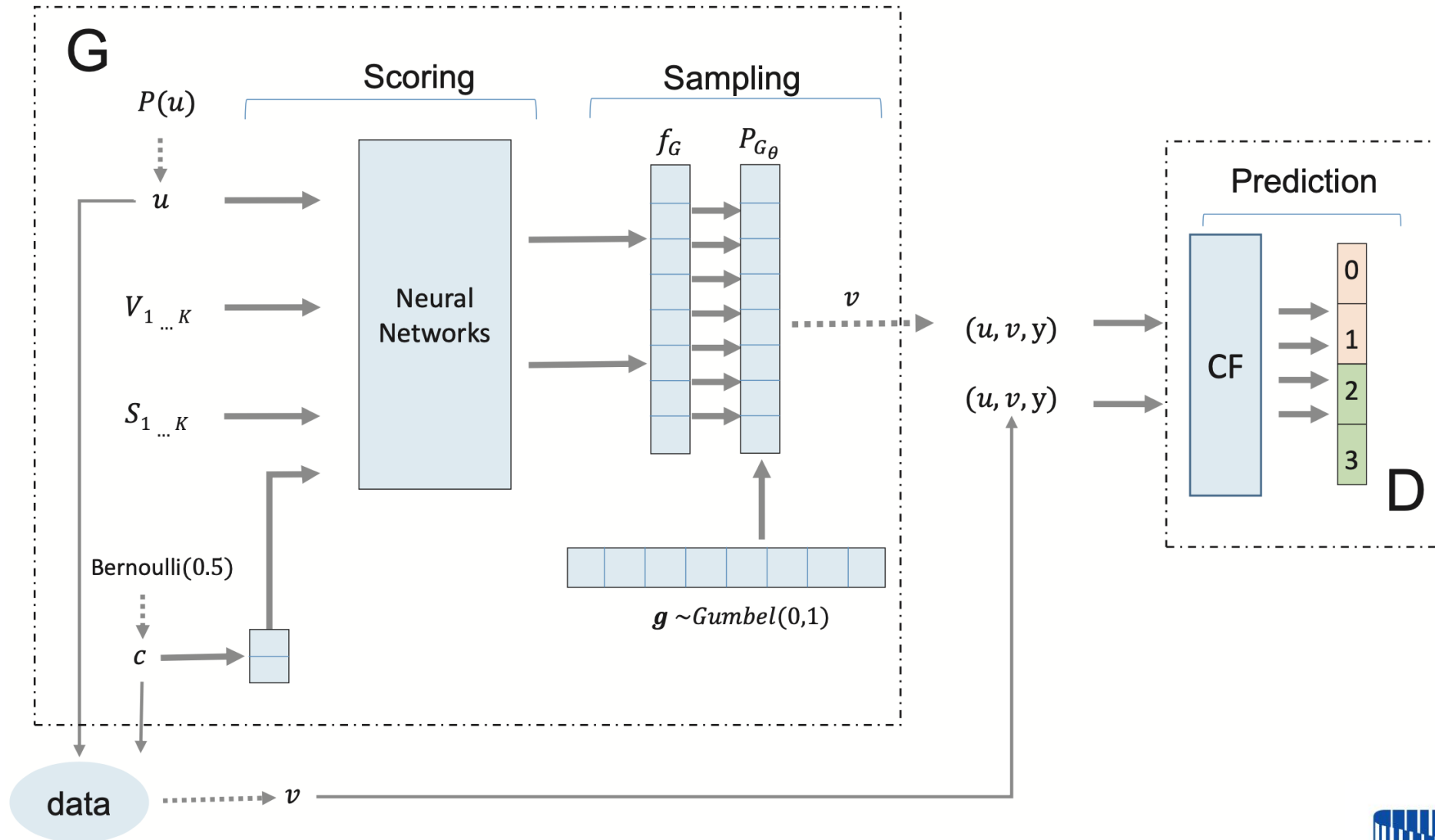
## Algorithm 1: AugCF Training Algorithm

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```
1 INPUT: Training data  $C$  and side information  $\mathcal{S}$ , pre-trained
   generator  $G_{\theta}$ , number of epochs in Phase I and Phase II and
   batch size  $J$ ;
2 OUTPUT: An augmented  $C$  and  $G_{\theta^*}$  and  $D_{\phi^*}$ ;
3 for each epoch in Phase I do
4    $\mathcal{B}_{gen} = \emptyset; \mathcal{B}_{real} = \emptyset;$  //sets for generated and real data
5   Sample a batch of users  $u_1, \dots, u_J$  based on Eq. 7;
6   Sample a batch of binary classes  $c_1, \dots, c_J \sim \text{Bern}(0.5);$ 
7   for every  $u, c$  in batch do
8      $G_{\theta}$  generates a distribution  $P_{G_{\theta}(v|(u,c))}$  over  $K$ 
       unvisited items based on Eq. 8;
9     Sample a  $K$ -dimensional  $\mathbf{g} \sim \text{Gumbel}(0, 1);$ 
10    Obtain an approximate fake item  $v$  based on Eq. 12;
11    Construct a fake tuple  $(u, v, y)$  where  $y = c + 2;$ 
12    Add this  $(u, v, y)$  to  $\mathcal{B}_{gen};$ 
13    Randomly sample an item  $v$  from  $C$  given  $u$  and  $c;$ 
14    Construct a real tuple  $(u, v, y)$  where  $y = c;$ 
15    Add this  $(u, v, y)$  to  $\mathcal{B}_{real};$ 
16  end
17  update  $G_{\theta}$  and  $D_{\phi}$  with  $\mathcal{B}_{gen}$  and  $\mathcal{B}_{real}$  based on Eq. 13;
18 end
```



# AugCF



# Applications

## □ Content-Based AugCF (DeepCoNN)

$$f_G(u, v_i, \mathcal{S}_i, c) = \hat{w}_0 + \sum_{i=1}^{|\hat{z}|} \hat{w}_i \hat{z}_i + \sum_{i=1}^{|\hat{z}|} \sum_{j=i+1}^{|\hat{z}|} \langle \hat{\mathbf{b}}_i, \hat{\mathbf{b}}_j \rangle \hat{z}_i \hat{z}_j$$

## □ Sparse Feature-Based AugCF (Wide & Deep)

$$f_G(u, v_i, \mathcal{S}_i, c) = \mathbf{w}_{wide}^T [\mathbf{x}, \phi(\mathbf{x})] + \mathbf{w}_{deep}^T a^{(l_f)} + b$$

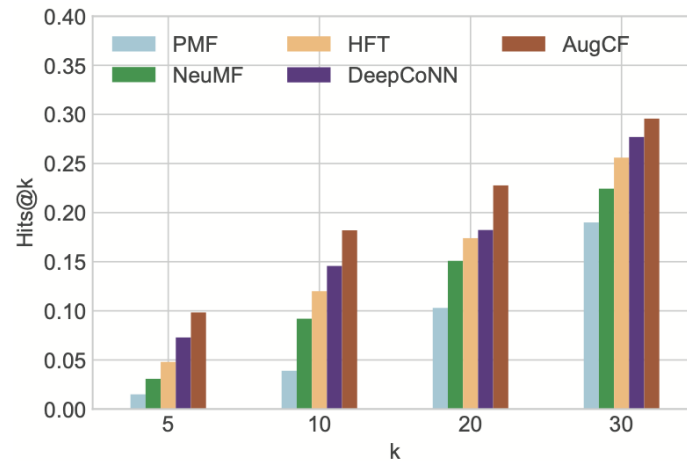
# Datasets

## Content-Based

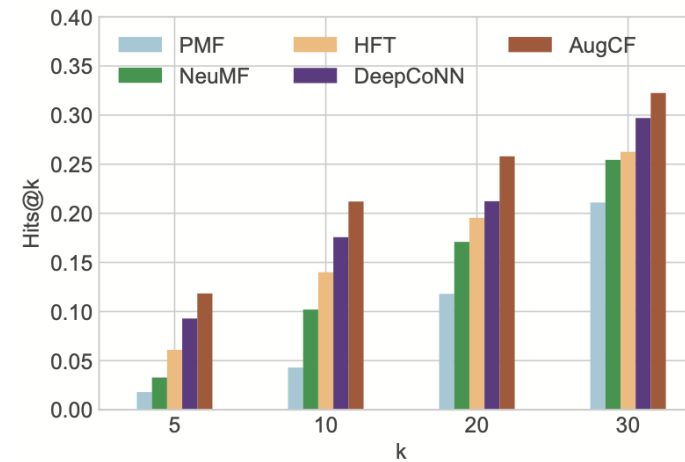
Dataset	#Users	#Items	#Interactions	#Features	Sparsity
Electronics	192,403	63,001	1,689,188	N/A	0.014%
Health	38,609	18,534	346,355	N/A	0.048%
Beauty	22,363	12,101	198,502	N/A	0.073%
Games	24,303	10,672	231,780	N/A	0.089%
Movielens	6,040	3,706	1,000,209	9,812	4.47%
Frappe	957	4,082	288,609	5,382	7.39%

## Sparse Feature-Based

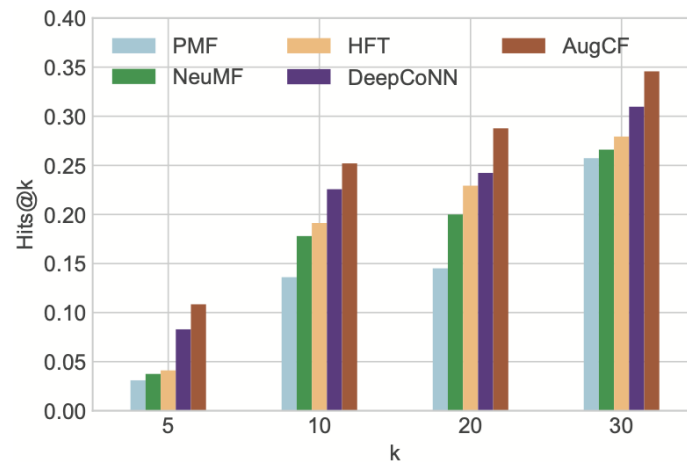
# Experiments



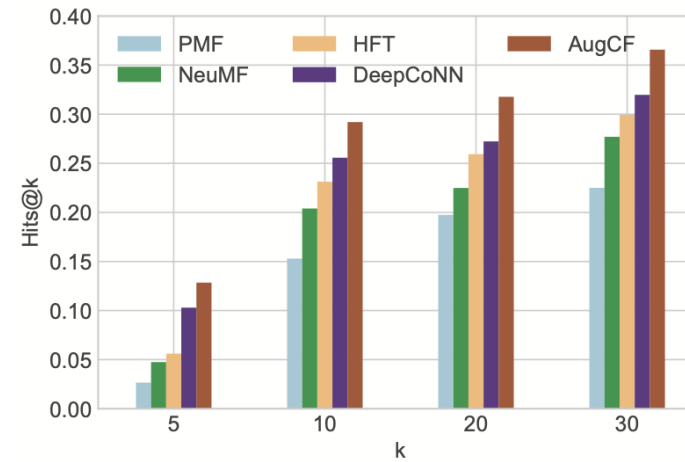
(a) Electronics



(b) Health

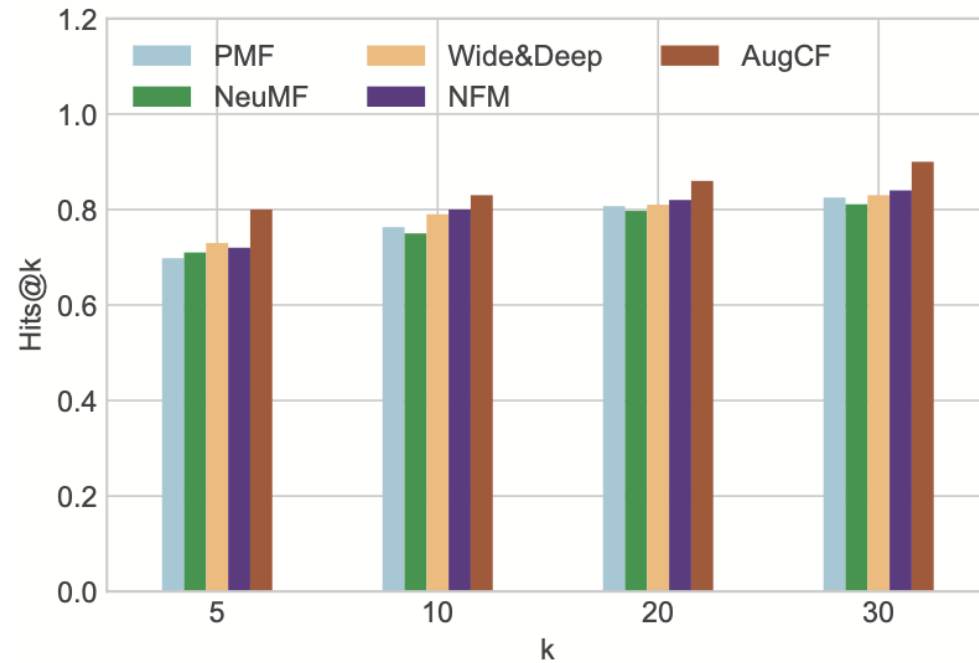


(c) Beauty

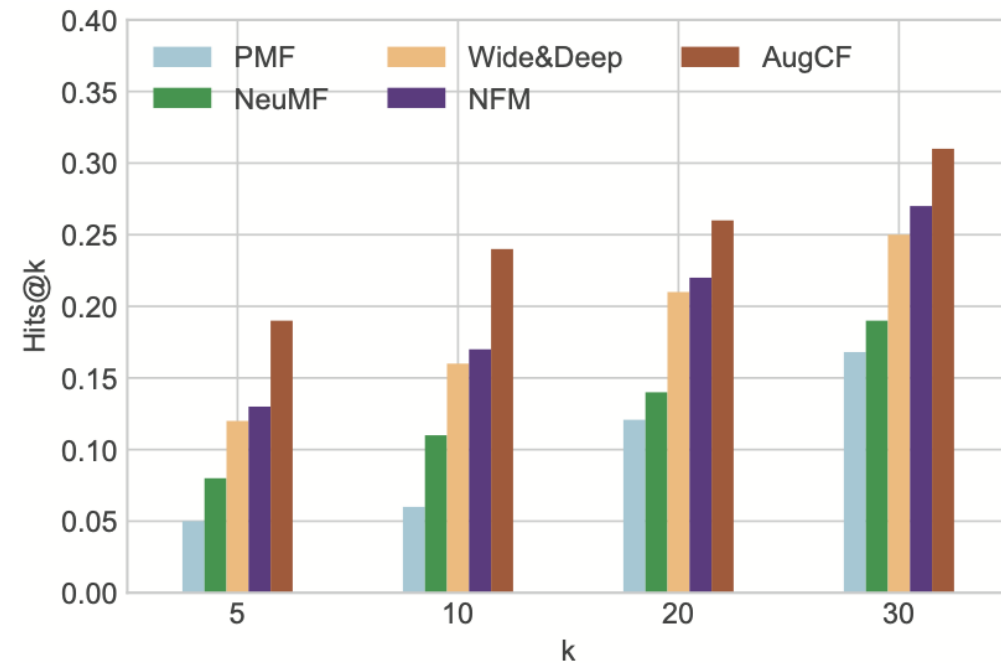


(d) Games

# Experiments



(a) Frappe



(b) Movielens