

# Air quality project : Time Series Analysis

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## Preliminary

Our project consists of time series analysis using R programming language. Our data set contains the responses of a gas mutisensor device deployed on the field in an Italian city, in a significantly polluted area, at road level. The data set contains 9358 instances of hourly averaged responses from an array of 5 metal oxide chemical sensors embedded in an Air Quality Chemical Multisensor Device. Data were recorded from March 2004 to February 2005.

```
## Loading required package: Rcpp

## ##
## ## Amelia II: Multiple Imputation
## ## (Version 1.7.6, built: 2019-11-24)
## ## Copyright (C) 2005-2020 James Honaker, Gary King and Matthew Blackwell
## ## Refer to http://gking.harvard.edu/amelia/ for more information
## ##

dim(data)

## [1] 9471 17

str(data)

## 'data.frame': 9471 obs. of 17 variables:
## $ Date : chr "10/03/2004" "10/03/2004" "10/03/2004" "10/03/2004" ...
## $ Time : chr "18.00.00" "19.00.00" "20.00.00" "21.00.00" ...
## $ CO.GT. : chr "2,6" "2" "2,2" "2,2" ...
## $ PT08.S1.CO. : int 1360 1292 1402 1376 1272 1197 1185 1136 1094 1010 ...
## $ NMHC.GT. : int 150 112 88 80 51 38 31 31 24 19 ...
## $ C6H6.GT. : chr "11,9" "9,4" "9,0" "9,2" ...
## $ PT08.S2.NMHC.: int 1046 955 939 948 836 750 690 672 609 561 ...
## $ NOx.GT. : int 166 103 131 172 131 89 62 62 45 -200 ...
## $ PT08.S3.NOx. : int 1056 1174 1140 1092 1205 1337 1462 1453 1579 1705 ...
## $ NO2.GT. : int 113 92 114 122 116 96 77 76 60 -200 ...
## $ PT08.S4.NO2. : int 1692 1559 1555 1584 1490 1393 1333 1333 1276 1235 ...
## $ PT08.S5.O3. : int 1268 972 1074 1203 1110 949 733 730 620 501 ...
## $ T : chr "13,6" "13,3" "11,9" "11,0" ...
## $ RH : chr "48,9" "47,7" "54,0" "60,0" ...
## $ AH : chr "0,7578" "0,7255" "0,7502" "0,7867" ...
## $ X : logi NA NA NA NA NA NA ...
## $ X.1 : logi NA NA NA NA NA NA ...
```

Attribute	Description
Date	Date (DD/MM/YYYY)
Time	Time (HH.MM.SS)
CO(GT)	True hourly averaged concentration CO in mg/m <sup>3</sup> (reference analyzer)
PT08.S1(CO)	PT08.S1 (tin oxide) hourly averaged sensor response (nominally CO targeted)
NMHC(GT)	True hourly averaged overall Non Metanic Hydro Carbons concentration in microg/m <sup>3</sup> (reference analyzer)
C6H6(GT)	True hourly averaged Benzene concentration in microg/m <sup>3</sup> (reference analyzer)
PT08.S2(NMHC)	PT08.S2 (titania) hourly averaged sensor response (nominally NMHC targeted)
NOx(GT)	True hourly averaged NOx concentration in ppb (reference analyzer)
PT08.S3(NOx)	PT08.S3 (tungsten oxide) hourly averaged sensor response (nominally NOx targeted)
NO2(GT)	True hourly averaged NO2 concentration in microg/m <sup>3</sup> (reference analyzer)
PT08.S4(NO2)	PT08.S4 (tungsten oxide) hourly averaged sensor response (nominally NO2 targeted)
PT08.S5(O3)	PT08.S5 (indium oxide) hourly averaged sensor response (nominally O3 targeted)

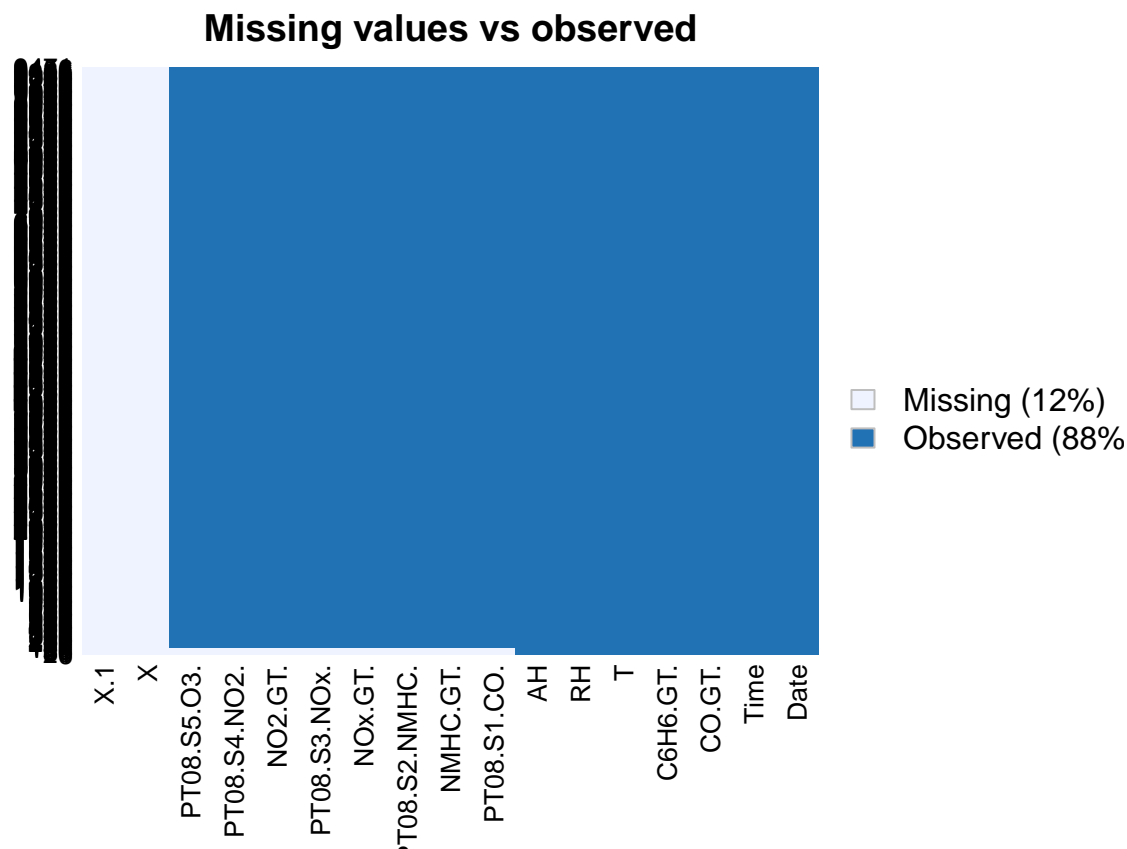
Attribute	Description
T	Temperature in °C
RH	Relative Humidity (%)
AH	AH Absolute Humidity

## I)-Cleaning and preprocessing

### 1) Data cleaning

As we can see in the `str(dim)` output, our data contains missing values, some are directly reported as NA and others have been assigned to -200. It also contains a certain number of numeric variables that are characters which makes it not directly exploitable and some numbers have commas within them. For all these reasons, we had to clean our data set first so that we can exploit it afterwards.

```
missmap(data, main = "Missing values vs observed")
```



We remove X1 and X because they have no data within them, also we compute the necessary changes so that our data is exploitable afterwards.

We noticed that NMHC contains a lot of -200 values, so we preferred to delete along with all the lines that contain -200.

```
summary(data$NMHC.GT.)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## -200.0  -200.0  -200.0  -159.1  -200.0  1189.0
```

```
str(data)
```

```
## 'data.frame':    6941 obs. of  14 variables:
## $ Date           : Date, format: "2004-03-10" "2004-03-10" ...
## $ Time           : chr  "18.00.00" "19.00.00" "20.00.00" "21.00.00" ...
## $ CO.GT.         : num  2.6 2 2.2 2.2 1.6 1.2 1.2 1 0.9 0.7 ...
## $ PT08.S1.CO.    : int  1360 1292 1402 1376 1272 1197 1185 1136 1094 1066 ...
## $ C6H6.GT.       : num  11.9 9.4 9 9.2 6.5 4.7 3.6 3.3 2.3 1.1 ...
## $ PT08.S2.NMHC.  : int  1046 955 939 948 836 750 690 672 609 512 ...
## $ NOx.GT.        : int  166 103 131 172 131 89 62 62 45 16 ...
## $ PT08.S3.NOx.   : int  1056 1174 1140 1092 1205 1337 1462 1453 1579 1918 ...
## $ NO2.GT.        : int  113 92 114 122 116 96 77 76 60 28 ...
## $ PT08.S4.NO2.   : int  1692 1559 1555 1584 1490 1393 1333 1333 1276 1182 ...
## $ PT08.S5.O3.    : int  1268 972 1074 1203 1110 949 733 730 620 422 ...
## $ T              : num  13.6 13.3 11.9 11 11.2 11.2 11.3 10.7 10.7 11 ...
## $ RH             : num  48.9 47.7 54 60 59.6 59.2 56.8 60 59.7 56.2 ...
## $ AH             : num  0.758 0.726 0.75 0.787 0.789 ...
```

Now that our data is nearly clean, we chose to consider the daily concentration of the different gases our main focus of study by taking the average of the concentrations observed daily.

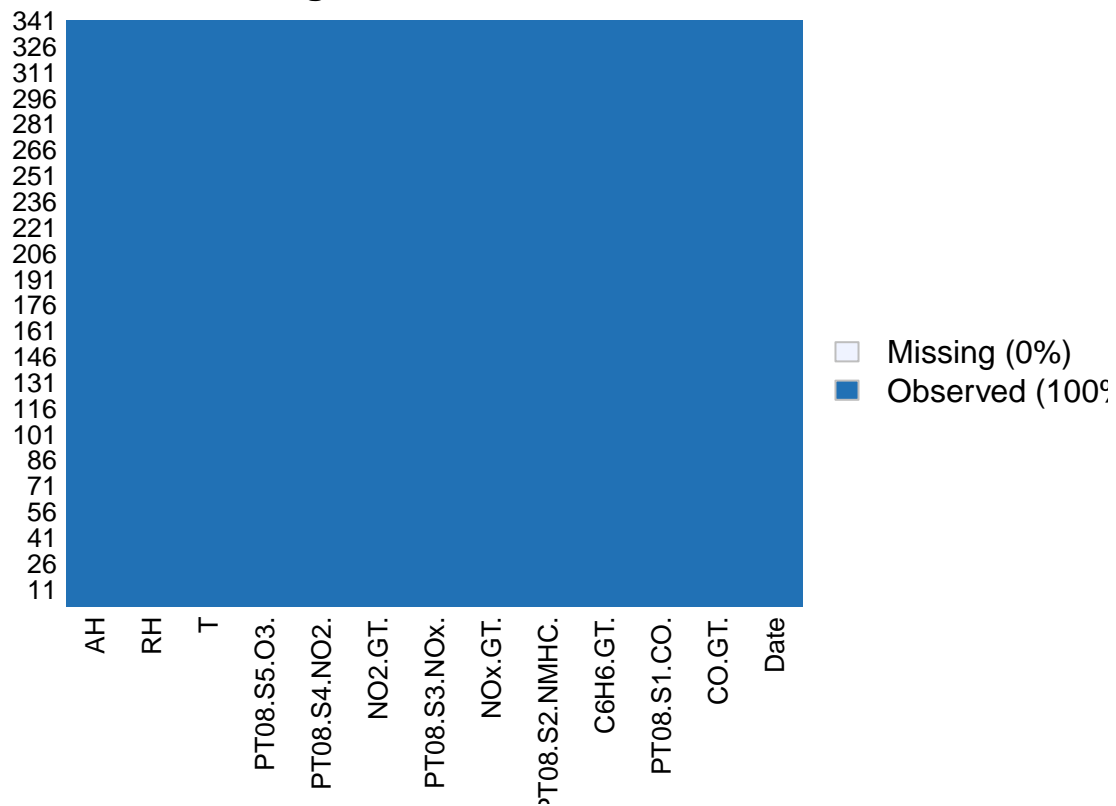
We obtain 341 observations of 13 variables.

```
str(daily_data)
```

```
## 'data.frame':    341 obs. of  13 variables:
## $ Date           : Date, format: "2004-03-10" "2004-03-11" ...
## $ CO.GT.         : num  1.97 2.31 2.9 2.74 2.47 ...
## $ PT08.S1.CO.    : num  1316 1265 1309 1346 1372 ...
## $ C6H6.GT.       : num  8.45 8.57 12.67 11.38 9.84 ...
## $ PT08.S2.NMHC.  : num  912 880 1036 1010 951 ...
## $ NOx.GT.        : num  132 150 181 188 150 ...
## $ PT08.S3.NOx.   : num  1167 1233 1053 978 999 ...
## $ NO2.GT.        : num  109 103 120 120 112 ...
## $ PT08.S4.NO2.   : num  1546 1551 1651 1614 1608 ...
## $ PT08.S5.O3.    : num  1096 923 1121 1269 1241 ...
## $ T              : num  12 9.8 11.8 13.4 16.4 ...
## $ RH             : num  54.9 64.4 49.6 49.9 47.6 ...
## $ AH             : num  0.766 0.778 0.667 0.734 0.848 ...
```

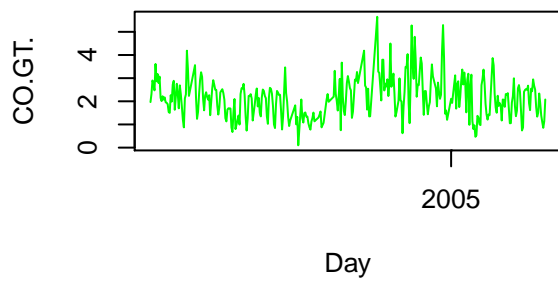
```
misssmap(daily_data, main = "Missing values vs observed")
```

## Missing values vs observed

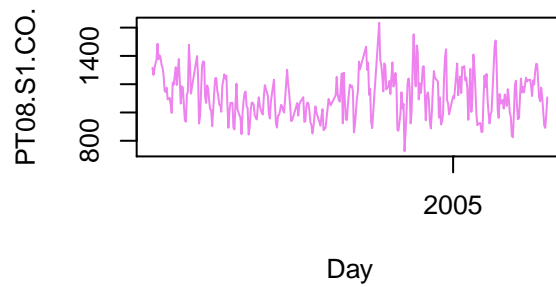


data is all observed now, we can start plotting it to visualize what our data set looks like.

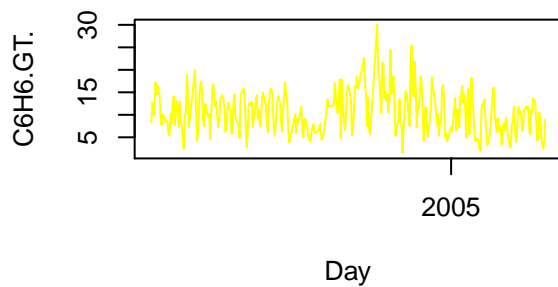
**CO.GT. concentration**



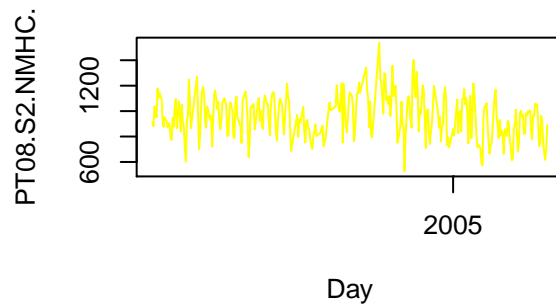
**PT08.S1.CO. concentration**

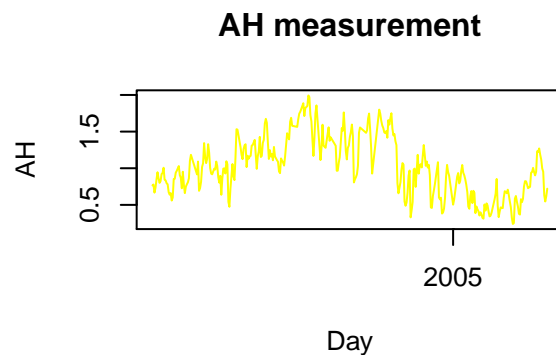
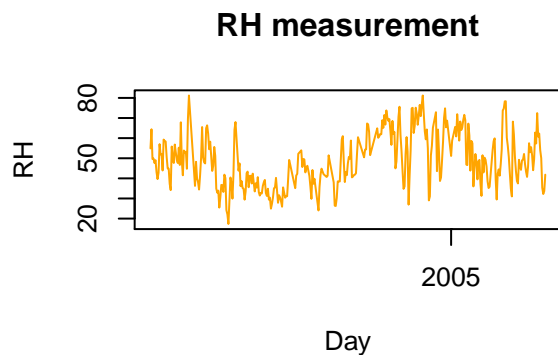
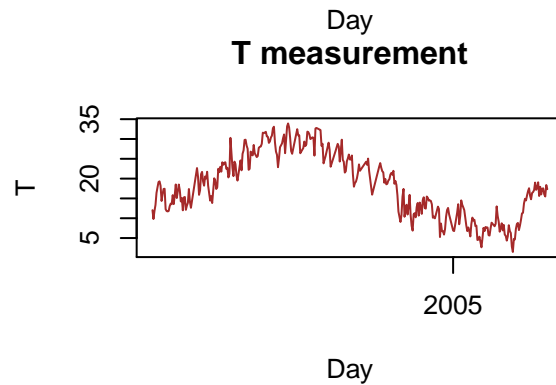
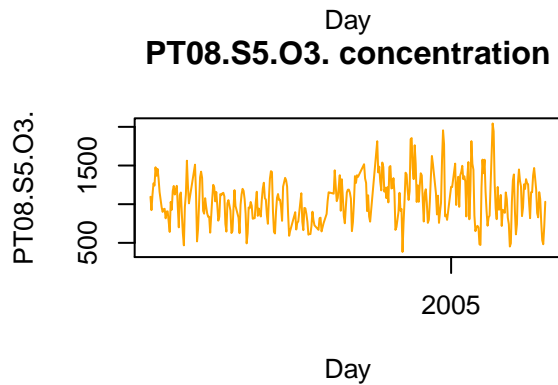
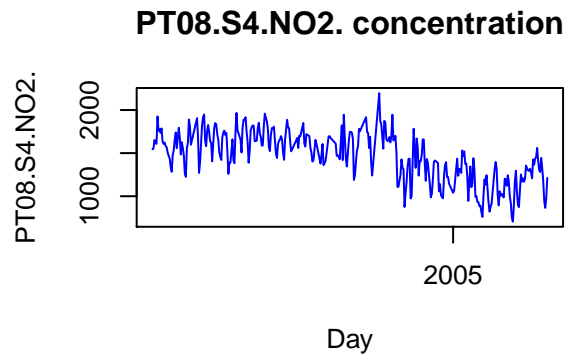
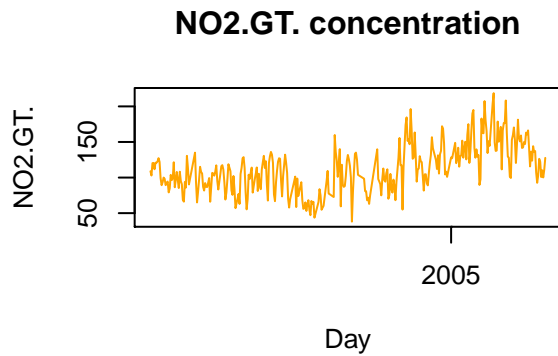
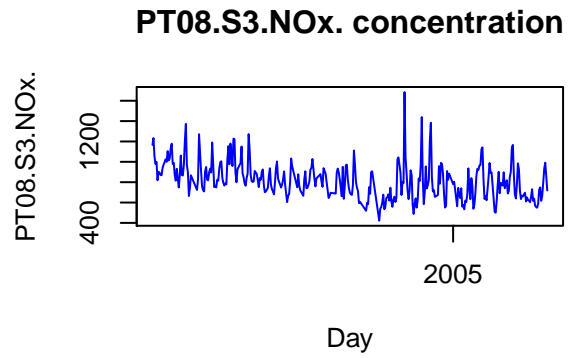
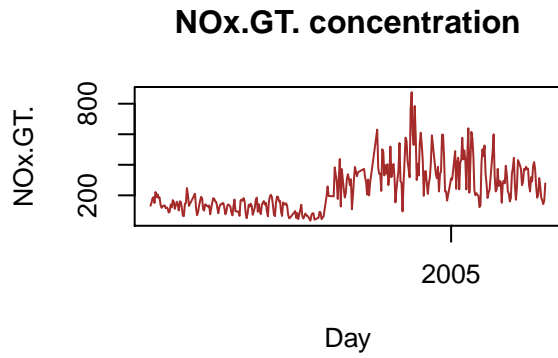


**C6H6.GT. concentration**



**PT08.S2.NMHC. concentration**





The variables starting with PT are the responses of the sensors measuring the concentration of the gas concerned. When investigating our data and by doing some research on air pollution, we found that the main air pollutants belong to the nitrogen oxides family (NOx). Thus, we wanted to see the relation between this gas concentration and the other ones. A linear regression was run between the NOx concentration and the

other gases.

```
summary(reg)

##
## Call:
## lm(formula = daily_data$PT08.S3.NOx. ~ +daily_data$PT08.S1.CO. +
##     daily_data$PT08.S2.NMHC. + daily_data$PT08.S4.NO2. + daily_data$PT08.S5.O3. +
##     daily_data$T + daily_data$RH + daily_data$AH)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -182.43  -60.67  -12.99   32.68  736.42
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1499.58349    73.78298   20.324 < 2e-16 ***
## daily_data$PT08.S1.CO.    -0.30643     0.09141   -3.352 0.000894 ***
## daily_data$PT08.S2.NMHC.   -0.46111     0.10894   -4.233 2.99e-05 ***
## daily_data$PT08.S4.NO2.     0.51459     0.05633    9.135 < 2e-16 ***
## daily_data$PT08.S5.O3.    -0.26128     0.06138   -4.256 2.70e-05 ***
## daily_data$T             -4.07044     3.05090   -1.334 0.183057
## daily_data$RH             -0.70990     1.08830   -0.652 0.514660
## daily_data$AH            -263.09360    48.56193   -5.418 1.16e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 95.89 on 333 degrees of freedom
## Multiple R-squared:  0.714, Adjusted R-squared:  0.708
## F-statistic: 118.8 on 7 and 333 DF,  p-value: < 2.2e-16
```

We will build the NOx concentration a time series because it comes from sensor measurements, thus noise will be modeled accordingly. Since it is linearly related to the other gases (except for the temperature, relative humidity and absolute humidity that we will exclude from our study), we preferred to focus on the NOx model.

## 2) Data preprocessing

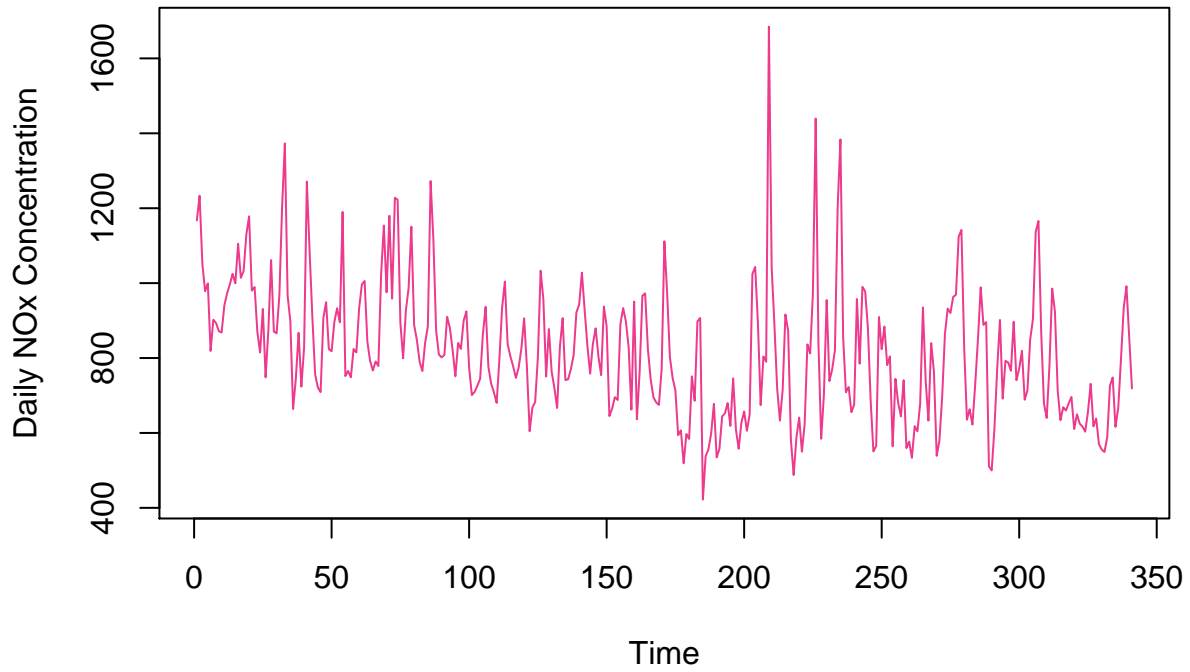
We count one PT08.S3.NOx observation per day for 341 days. We suppose that our time series follows an additive model :

$$D_t = S_t + T_t + X_t$$

Where

$(S_t)_t$  the seasonality ,  $(T_t)_t$  the trend and  $(X_t)_t$  is assumed to be stationary

We obtain this representation :

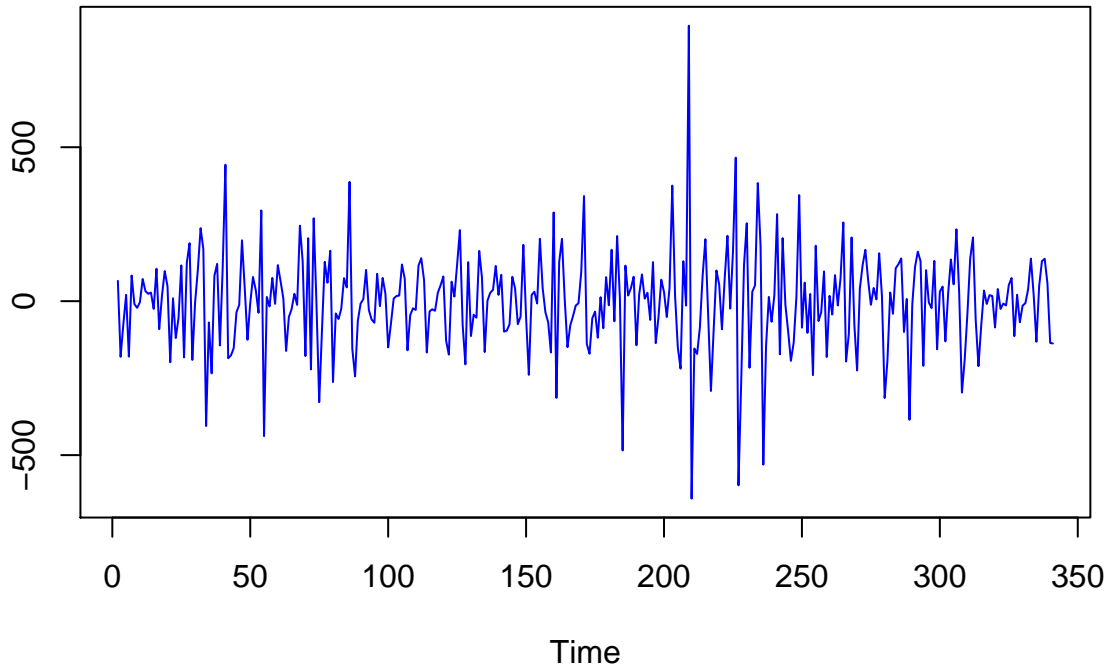


Before building any model, we have to stationarise it first by removing the seasonal and trend components.

$$X_t = D_t - T_t - S_t$$

So we use differencing :

$$D_t - D_{t-1}$$



We want to make sure of the stationarity of our series, so we use the Augmented Dickey-Fuller Test that tests the null hypothesis that a unit root is present in a time series sample.



We obtain these results :

```
## Warning in adf.test(ts_stat_PT08.S3.N0x.): p-value smaller than printed p-value
##
## Augmented Dickey-Fuller Test
##
## data: ts_stat_PT08.S3.N0x.
## Dickey-Fuller = -11.962, Lag order = 6, p-value = 0.01
## alternative hypothesis: stationary
```

Since our p-value is smaller than 0.01, we reject the null hypothesis with level of confidence of 99%

## II)-Model fitting on the time series of interest

- 1) MA model
- 2) AR model
- 3) ARMA model
- 4) Residuals
- 5) GARCH model
- 6) Prediction intervals for the 10 most recent data

## III)-Training on the times series of interest using explanatory times series

- 1) Preprocessing
- 2) Time varying coefficients
- 3) QLIK
- 4) Prediction

## IV) Conclusion