spaceTimeWindow Library

Technical Manual

Version 1.0 (Draft) | OpenFOAM v2512

Boundary Data Extraction • **Time Interpolation** • **Optional Encryption**

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Contents

1   Introduction

The `spaceTimeWindow` library enables extraction and reconstruction of spatial subsets from Large Eddy Simulation (LES) and transient RANS simulations in OpenFOAM. This technique allows researchers to:

- Extract a region of interest from a full-domain simulation

- Store time-varying boundary conditions efficiently

- Reconstruct the flow within the subset using pre-computed boundary data

- Optionally encrypt boundary data for secure distribution

The library consists of four main components:

1. **spaceTimeWindowExtract** — Function object for boundary data extraction during simulation

2. **spaceTimeWindowInitCase** — Utility for reconstruction case initialization

3. **spaceTimeWindow** — Pure Dirichlet boundary condition for applying extracted data

4. **spaceTimeWindowInletOutlet** — Flux-based boundary condition (recommended for unsteady flows)

1.1   Requirements

- OpenFOAM v2512 (openfoam.com) or compatible ESI-OpenCFD version

- C++17 compatible compiler (GCC 7+ or Clang 5+)

- Optional: libsodium for encryption support

- Optional: MPI for parallel execution

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1.2   Building the Library

```
1  # Navigate to source directory
2  cd openfoam-spaceTimeWindow
3
4  # Build library and utilities
5  ./Allwmake
6
7  # Or with encryption support (requires libsodium)
8  ./Allwmake  # Auto-detects libsodium if installed
```

Listing 1: Building spaceTimeWindow

For manual building with encryption:

```
1  cd src/spaceTimeWindow
2  export FOAM_USE_SODIUM=1 && wmake
3
4  cd applications/utilities/preProcessing/spaceTimeWindowInitCase
5  export FOAM_USE_SODIUM=1 && wmake
6
7  cd ../spaceTimeWindowKeygen
8  export FOAM_USE_SODIUM=1 && wmake
```

Listing 2: Manual build with encryption

2 Concept: Space-Time Window Extraction and Reconstruction

This section introduces the fundamental concepts behind space-time window extraction and reconstruction. Understanding these concepts is essential before diving into the technical implementation details.

2.1 The Challenge of Large-Scale CFD Simulations

Modern computational fluid dynamics (CFD) simulations, particularly Large Eddy Simulations (LES) and Direct Numerical Simulations (DNS), generate enormous amounts of data. A typical industrial LES simulation might involve:

- Meshes with 10^7–10^9 cells

- Thousands of timesteps

- Multiple field variables (velocity, pressure, turbulence quantities)

- Terabytes to petabytes of raw output data

Storing and post-processing this data is often impractical. The space-time window approach addresses this by extracting only the data needed to reconstruct the flow in a *region of interest* at a later time.

2.2 The Space-Time Window Concept

A **space-time window** is a bounded region in both space (a 3D box) and time (a time interval) from which we extract the information necessary to reconstruct the flow field. The key insight is that we only need:

1. **Initial conditions**: The complete field state at one timestep (t_0)

2. **Boundary data**: Time-varying values on the boundary of the spatial region

Figure 1 illustrates this concept. The extraction box (blue) defines a spatial subset of the full domain (gray). During simulation, we record the field values on the boundary of this box at every timestep, creating a complete "boundary history" that can later drive a reconstruction simulation.
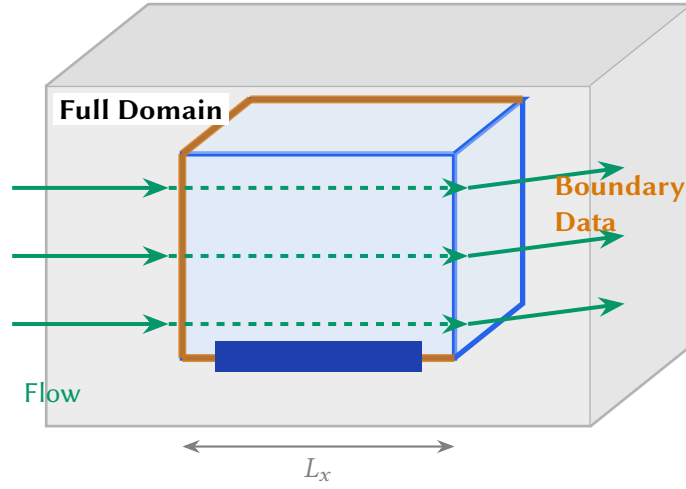
Figure 1: Space-time window extraction: A bounding box (blue) defines the region of interest within the full computational domain (gray). Boundary data (orange) is recorded at every timestep as the flow passes through.
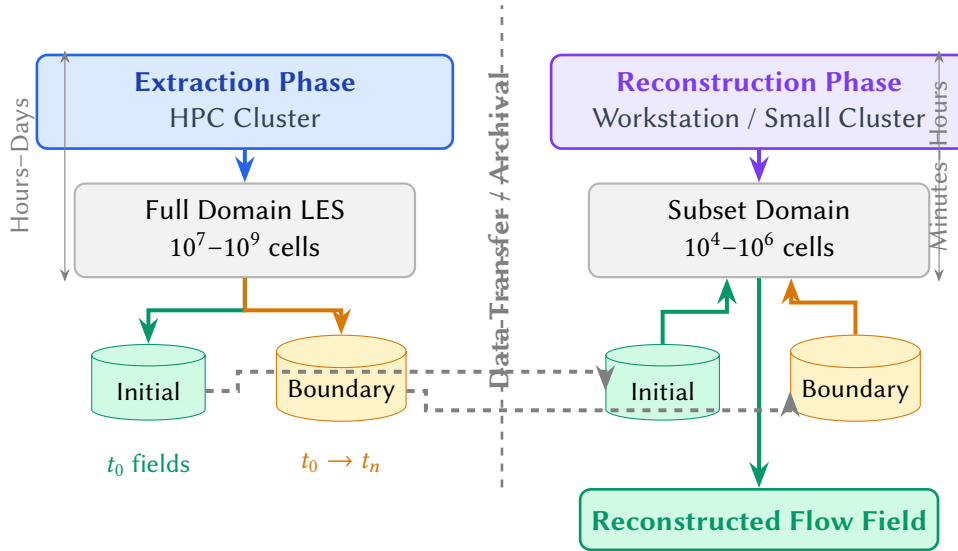
Figure 2: Two-phase workflow: The extraction phase runs on HPC resources and produces compact data files. The reconstruction phase can run on modest hardware, reproducing the flow in the region of interest.

2.3 Extraction and Reconstruction Workflow

The workflow consists of two distinct phases that can be separated in time and computational resources, as shown in fig. 2.

2.3.1 Extraction Phase (HPC)

During the original simulation on high-performance computing resources:

1. The `spaceTimeWindowExtract` function object monitors the simulation

2. At the start time (t_0), it extracts the complete field state within the bounding box

3. At every timestep, it interpolates field values to the boundary faces and stores them

4. The output is a compact dataset: initial conditions + time-varying boundary data

2.3.2 Reconstruction Phase (Offline)

Later, on more modest computational resources:

1. The `spaceTimeWindowInitCase` utility creates a complete simulation case

2. The subset mesh is extracted from the original

3. Boundary conditions are configured to read the stored boundary data

4. The solver runs, reproducing the flow within the extraction box

> **✓ Tip**
>
> The reconstruction phase typically requires 100–10,000× fewer computational resources than the original simulation, making it feasible to run on a workstation or laptop.

2.4 Parallel Execution with MPI Domain Decomposition

Large-scale CFD simulations invariably run in parallel using MPI (Message Passing Interface). The computational domain is divided among multiple processors, each handling a subset of the mesh. The spaceTimeWindow library handles both serial and parallel execution transparently.

Figure 3 illustrates how domain decomposition affects the extraction process. The extraction box may span multiple processor domains, requiring coordination to gather boundary data from all relevant processors.

2.4.1 How Parallel Extraction Works

In parallel mode, the extraction process operates as follows:

1. **Local identification**: Each processor identifies which of its cells fall within the extraction bounding box

2. **Local extraction**: Each processor extracts field values for its local portion of the boundary

3. **Global gathering**: Boundary data is gathered to the master processor using MPI collective operations

Parallel Extraction: Domain Decomposition with 8 MPI Processes
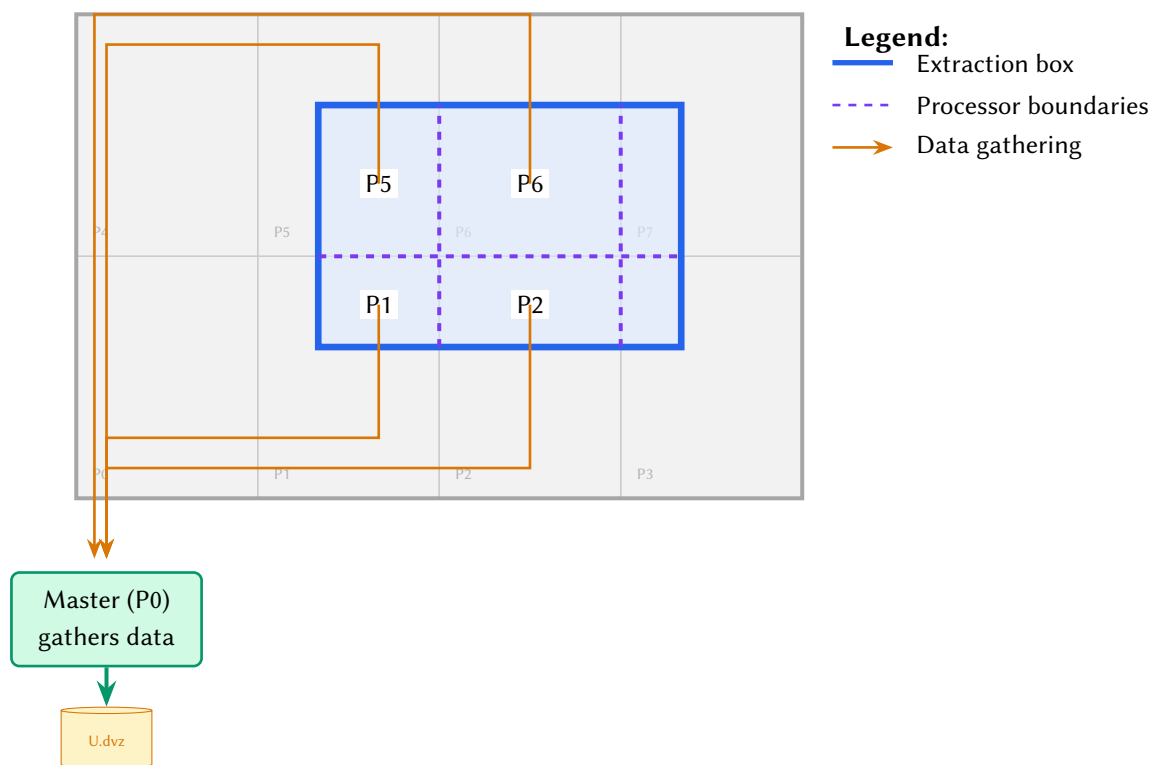
Figure 3: Domain decomposition in parallel simulations. The extraction box (blue) spans multiple processor domains. Each processor extracts its local contribution, and data is gathered to the master process for writing unified boundary data files.

4. **Unified output**: The master processor writes a single, consolidated boundary data file for each timestep

Figure 4 shows the detailed data flow during the extraction process. The `spaceTimeWindowExtract` function object runs on each MPI process, extracting local contributions that are then gathered and merged into unified output files.
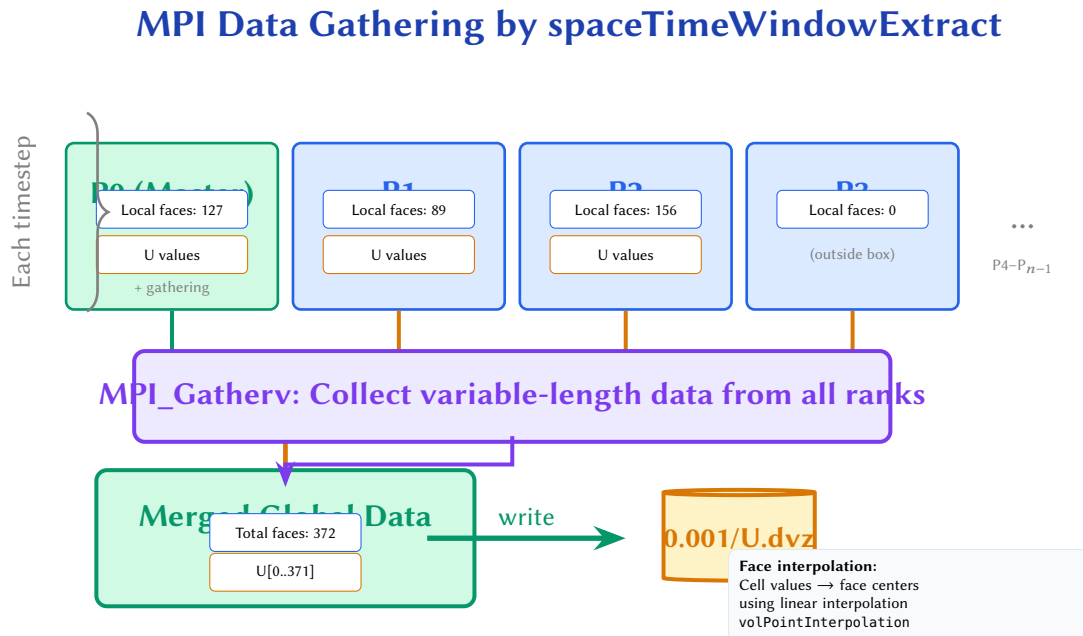
Figure 4: Detailed MPI data gathering during parallel extraction. Each processor runs the `spaceTimeWindowExtract` function object, which identifies local boundary faces, interpolates field values to face centers, and participates in a collective gather operation. The master processor (P0) writes the merged data to a single file per timestep.

This approach ensures that:

- The reconstruction case is **decomposition-independent**—the same boundary data works regardless of how the original simulation was parallelized

- Output files are compact and self-contained, with no processor-specific information

- The reconstruction can run in serial or with a different parallel decomposition

> **ℹ Note**
>
> In parallel mode, mesh information is not written during extraction. Instead, the extraction box parameters are stored, and `spaceTimeWindowInitCase` creates the subset mesh from reconstructed fields. Run `reconstructPar -time <startTime>` on the source case before initializing the reconstruction case.

2.5 Data Storage: Initial Fields and Boundary Data

The extracted data consists of two distinct components, illustrated in fig. 5.
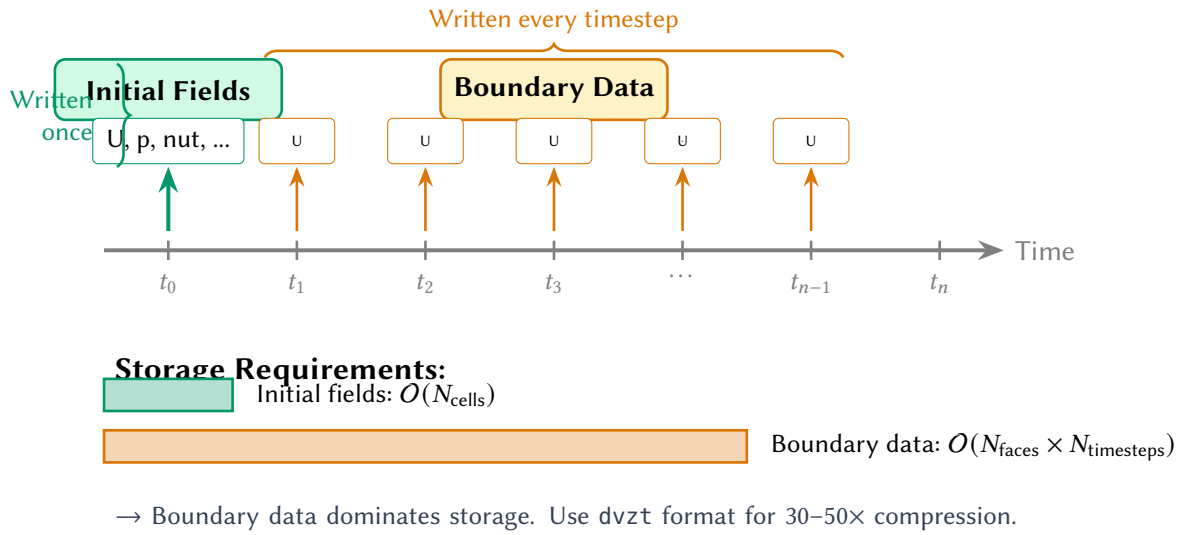
Figure 5: Data storage structure: Initial fields are written once at t_0, while boundary data is accumulated at every timestep. Compression is critical for the boundary data component.

2.5.1 Initial Fields

The initial fields provide the starting state for reconstruction:

- **What**: Complete volumetric data (U, p, turbulence quantities) within the extraction box

- **When**: Written once at the extraction start time (t_0)

- **Format**: Standard OpenFOAM field format (ASCII)

- **Size**: Proportional to number of cells in the subset, typically megabytes

2.5.2 Boundary Data

The boundary data provides the time-varying boundary conditions:

- **What**: Face-interpolated field values on the boundary of the extraction box

- **When**: Written at every timestep throughout the simulation

- **Format**: Configurable (ASCII, binary, or compressed `dvz`/`dvzt`)

- **Size**: Proportional to (number of boundary faces) × (number of timesteps)

> △ **Warning**
>
> Boundary data accumulates rapidly during long simulations. For a typical LES with 10^4 boundary faces and 10^4 timesteps, uncompressed ASCII data can reach tens of gigabytes. The `dvzt` compression format reduces this by 30–50×.

2.6 Why Reconstruction Works

The reconstruction is possible because the governing equations (Navier-Stokes for incompressible flow) are well-posed with appropriate boundary conditions. Mathematically, if we denote:

- $\Omega \subset \mathbb{R}^3$: the extraction box domain

- $\partial\Omega$: the boundary of the extraction box

- $\mathbf{u}(\mathbf{x}, t)$: the velocity field

- $p(\mathbf{x}, t)$: the pressure field

Then knowing $\mathbf{u}(\mathbf{x}, t_0)$ for $\mathbf{x} \in \Omega$ (initial condition) and $\mathbf{u}(\mathbf{x}, t)$ for $\mathbf{x} \in \partial\Omega$, $t \in [t_0, t_n]$ (boundary data) is sufficient to uniquely determine $\mathbf{u}(\mathbf{x}, t)$ for all $\mathbf{x} \in \Omega$, $t \in [t_0, t_n]$.

The reconstruction achieves "bit-reproducible" results when:

1. Time interpolation is disabled (`timeInterpolationScheme none`)

2. The reconstruction runs with the same timestep as extraction

3. The same solver settings and numerical schemes are used

With time interpolation enabled (recommended for practical use), the reconstruction closely approximates the original solution, with errors controlled by the interpolation scheme (linear or cubic Catmull-Rom spline).

2.7 Automatic Boundary Condition Configuration

A key feature of the spaceTimeWindow library is the **automatic configuration** of boundary conditions during offline reconstruction. When you run `spaceTimeWindowInitCase`, the utility analyzes the extracted data and configures appropriate boundary conditions for each field—no manual setup required.

Figure 6 illustrates the automatic configuration process that occurs when setting up a reconstruction case on a laptop or desktop computer.

2.7.1 Resolution-Independent Reconstruction

The reconstruction can run at **different mesh resolutions** than the original extraction. This enables several important use cases:

- **Coarser mesh**: Faster turnaround for exploratory analysis or debugging

- **Finer mesh**: Higher resolution studies without re-running the expensive global simulation

- **Same resolution**: Bit-reproducible reconstruction for validation

Figure 7 shows how the `spaceTimeWindow` boundary condition automatically handles resolution differences at runtime.

2.7.2 Time Interpolation at Runtime

Similarly, the boundary condition handles **time interpolation** automatically when the reconstruction timestep differs from the extraction timestep (which is common with adaptive timestepping). Figure 8 illustrates the temporal interpolation process.

Automatic B ██████████████████████████ **dowInitCase**

Extracted Data
boundaryData/

U.dvz (velocity)

points

extractionMetadata

spaceTimeWindowInitCase
1. Read extraction metadata
2. Detect available fields
3. Check mesh resolution
4. Determine BC types:
   - Vector + data → InletOutlet
   - Scalar + data → zeroGradient
   - No data → zeroGradient

Configured Case
Ready to run!

0.0001/U

0.0001/p

0.0001/nut

system/controlDict

Automatic Boundary Condition Assignment (oldInternalFaces patch)

Field	Condition	Assigned BC
U (velocity)	Has boundaryData + -inletOutletBC	`spaceTimeWindowInletOutlet`
p (pressure)	No boundaryData	`zeroGradient`
nut, k, ω	Scalar fields	`zeroGradient`

Figure 6: Automatic boundary condition configuration during case initialization. The `spaceTimeWindowInitCase` utility analyzes extracted data and automatically assigns appropriate boundary conditions based on field type and data availability.

Extraction Mesh

(from HPC simulation)

7 faces

U data stored

Coarser

-coarsenLevel 1

2 faces

Area-weighted averaging

Same Resolution

(default)

7 faces

Direct 1:1 mapping

Finer

-refineLevel 1

14 faces

Barycentric
(Delaunay triangulation)

coarsen

same

refine

At runtime:
The `spaceTimeWindow` BC automatically detects resolution mismatch and applies appropriate spatial interpolation **on-the-fly**.
No preprocessing required!

Figure 7: Resolution-independent reconstruction: The `spaceTimeWindow` boundary condition automatically handles mesh resolution differences between extraction and reconstruction. Spatial interpolation is performed on-the-fly during the simulation.
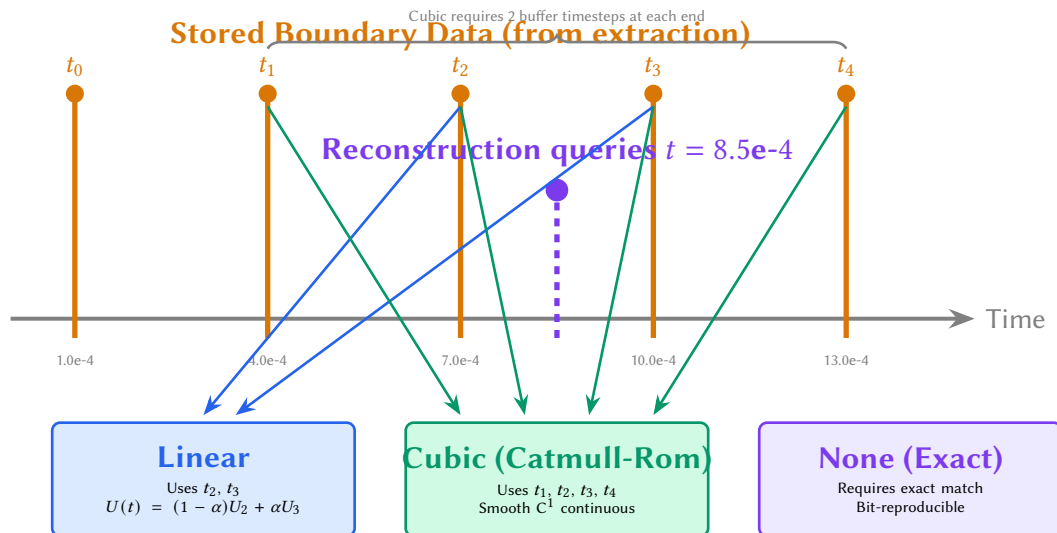
Figure 8: Time interpolation during reconstruction. When the solver requests field values at times not exactly matching stored timesteps, the boundary condition interpolates using linear (2 points) or cubic Catmull-Rom (4 points) schemes. Cubic interpolation provides smooth derivatives, essential for adaptive timestepping.

> ✓ **Tip**
>
> The combination of automatic spatial and temporal interpolation means you can:
>
> - Run reconstruction on a laptop with a coarser mesh for quick visualization
>
> - Use adaptive timestepping (`adjustTimeStep yes`) without worrying about timestep alignment
>
> - Later refine the mesh for detailed analysis without re-extracting data
>
> All interpolation happens transparently at runtime—no preprocessing steps required.

3 Encryption of Boundary Data

The spaceTimeWindow library supports X25519 asymmetric encryption using libsodium sealed boxes. This allows secure distribution of simulation data where:

- Extraction uses only the **public key**

- Reconstruction requires the **private key**

- Data cannot be decrypted without the private key

3.1 Key Generation

Generate a keypair using the provided utility:

```
spaceTimeWindowKeygen
# Output:
# Public key:  fqzYQ0U8j27tFEr5WzEMylbvXYP+9CAyk0JhwwZ2rwg=
```

```
4   # Private key: QgzxB5b+DGPQH8exbWDe18n4Kv0nu5gqljI2RPBCwl4=
5   #
6   # IMPORTANT: Store the private key securely!
```

Listing 3: Generating encryption keys

> △ **Warning**
>
> The private key must be stored securely and never committed to version control. Anyone with the private key can decrypt all boundary data encrypted with the corresponding public key.

3.2 Secure Key Storage

The private key should be stored using one of the following methods:

- **Hardware security keys**: YubiKey, Nitrokey, or similar FIDO2/PIV-capable devices provide the strongest protection. The private key never leaves the hardware token.

- **Secure password managers**: KeePassXC, 1Password, Bitwarden, or similar tools with strong master passwords and optional hardware key integration.

- **Encrypted vaults**: GPG-encrypted files or OS keychains (macOS Keychain, GNOME Keyring, Windows Credential Manager).

> ✓ **Tip**
>
> For maximum security, generate the keypair on an air-gapped machine, store the private key on a hardware token, and only transfer the public key to the HPC system.

3.3 Encrypted Extraction

Add the public key to your extraction configuration in `system/controlDict`:

```
1   functions
2   {
3       extractSubset
4       {
5           type            spaceTimeWindowExtract;
6           libs            (spaceTimeWindow);
7
8           box             ((0.05 -0.25 0.01) (0.90 0.25 0.38));
9           outputDir       "../subset-case";
10          fields          (U p nut);
11
12          writeFormat     deltaVarint;
13
14          // Enable encryption with public key
15          publicKey       "fqzYQ0U8j27tFEr5WzEMylbvXYP+9CAyk0JhwwZ2rwg=";
16
17          writeControl    timeStep;
18          writeInterval   1;
```

```
19        }
20    }
```

Listing 4: Encrypted extraction configuration

Encrypted files have the `.enc` extension (e.g., `U.dvz.enc` for compressed and encrypted data).

3.4 Decryption During Case Initialization

When running `spaceTimeWindowInitCase` on encrypted data, you will be prompted for the private key:

```
1   cd subset-case
2   spaceTimeWindowInitCase -sourceCase ../source-case
3   # Enter private key (base64): [input not echoed]
```

Listing 5: Decrypting boundary data

The utility automatically:

1. Derives the public key from the private key

2. Decrypts all `.enc` files in boundaryData

3. Removes encrypted files after successful decryption

3.5 Security Properties

- **Sealed box encryption**: Anonymous sender, only recipient can decrypt

- **X25519 key exchange**: 128-bit security level

- **XSalsa20-Poly1305**: Authenticated encryption

- **No plaintext on disk**: Encryption occurs before writing

3.5.1 Cryptographic Foundations

The encryption uses elliptic curve Diffie-Hellman on Curve25519. Key generation produces a private scalar s and public point (eq. (1)):

$$P_{\mathrm{pub}} = s \cdot G \tag{1}$$

where G is the curve's base point. The discrete logarithm problem makes recovering s from P_{pub} computationally infeasible.

Sealed Box Construction   For each encryption, a sealed box generates an ephemeral keypair $(e, e \cdot G)$ and computes a shared secret:

$$K = \mathrm{BLAKE2b}(e \cdot P_{\mathrm{recv}}) = \mathrm{BLAKE2b}(e \cdot s_{\mathrm{recv}} \cdot G) \tag{2}$$

The ciphertext is constructed as shown in eq. (3):

$$C = (e \cdot G) \| \mathrm{XSalsa20\text{-}Poly1305}_K(M) \tag{3}$$

where M is the plaintext boundary data and $\|$ denotes concatenation. The ephemeral public key $(e \cdot G)$ is prepended to allow decryption.

Decryption   The recipient computes the same shared secret using their private key (eq. (4)):

$$K = \text{BLAKE2b}(s_{\text{recv}} \cdot (e \cdot G)) \tag{4}$$

By the associativity of scalar multiplication on elliptic curves (eq. (5)):

$$s_{\text{recv}} \cdot (e \cdot G) = e \cdot (s_{\text{recv}} \cdot G) = e \cdot P_{\text{recv}} \tag{5}$$

This ensures both parties derive the same key K without ever transmitting it.

Security Level   X25519 provides approximately 128 bits of security. Breaking the encryption requires either:

- Solving the elliptic curve discrete logarithm problem (ECDLP): $O(2^{128})$ operations

- Brute-forcing the symmetric key: $O(2^{256})$ operations for XSalsa20

3.6 Ethical Considerations and HPC Transparency

Most high-performance computing (HPC) centers require full transparency regarding the simulations performed on their infrastructure. For this reason, **encryption support is an optional compile-time feature** controlled by the `FOAM_USE_SODIUM` flag. Centers may choose not to enable this functionality.

It is important to understand what encryption does and does not protect:

- **What is protected**: The time-varying boundary field data in `constant/boundaryData`. When downloaded, this data is sealed and cannot be read without the private key.

- **What is NOT protected**: The test case setup (mesh, dictionaries, initial conditions) remains unencrypted. Anyone can re-run the global simulation to regenerate the boundary data—encryption does not prevent this.

The practical security model relies on the following observations:

1. Re-running the global simulation to obtain internal fields is **computationally expensive** and requires HPC resources. Such jobs are recorded in the scheduler logs, providing an audit trail.

2. Offline recalculation on a personal workstation is typically infeasible due to computational cost.

3. If file permissions on HPC scratch directories are misconfigured and the user chooses not to write timestep data from the global simulation, other users can only copy the unencrypted test case setup—not the valuable boundary data.

> **i Note**
>
> The encryption feature is designed for protecting intellectual property during data distribution, not for hiding simulations from HPC administrators. Always comply with your computing center's acceptable use policies.

3.7 Protection Against Malware and Ransomware

The spaceTimeWindow approach offers an additional security benefit: by storing only the minimal data required for reconstruction, the valuable simulation results can be protected against malware and ransomware attacks.

3.7.1 Secure Archival Strategy

The reconstruction case contains only:

- The subset mesh (`constant/polyMesh`)

- Encrypted boundary data (`constant/boundaryData/*.enc`)

- Initial fields for one timestep

- Configuration dictionaries

This minimal dataset (typically a few gigabytes) can be stored on:

- **Write-Once Read-Many (WORM) media**: Optical discs (M-DISC), tape archives with WORM capability, or cloud storage with object lock/immutability settings (AWS S3 Object Lock, Azure Immutable Blob Storage).

- **Secure vaults**: Hardware-encrypted drives kept offline, or institutional secure storage with access controls and audit logging.

- **Air-gapped backups**: Disconnected storage that cannot be reached by network-based malware.

3.7.2 Security Model

1. **Encrypted boundary data is immutable**: Once written to WORM storage, the encrypted files cannot be modified or deleted by malware.

2. **Private key stored separately**: The decryption key resides on a hardware token or secure password manager, not on the same system as the data.

3. **Reconstruction is always possible**: Even if the HPC system or workstation is compromised, the archived data remains intact and can be decrypted on a clean system.

4. **Minimal attack surface**: The small archive size makes backup and verification practical, unlike terabyte-scale full simulation outputs.

> ✓ **Tip**
>
> For critical simulations, archive the encrypted reconstruction case to WORM storage immediately after extraction completes. The full simulation data can then be deleted from HPC scratch space, eliminating the risk of data loss from ransomware or accidental deletion.

4   Boundary Condition Approaches

The library provides two approaches for applying boundary conditions on the extraction boundary (`oldInternalFaces`):

4.1   Inlet-Outlet BC (`-inletOutletBC`) — Recommended for Unsteady Flows

Uses `spaceTimeWindowInletOutlet` BC which applies:

- **Velocity (U)**: Flux-based switching — Dirichlet (prescribed value) at inflow faces, zero-Gradient at outflow faces

- **All scalar fields (p, nut, k, epsilon, omega)**: zeroGradient

This approach is **physically correct** for unsteady turbulent flows because:

- Turbulent flows have instantaneous velocity fluctuations that can reverse direction locally

- Vortex shedding, recirculation zones, and turbulent eddies cause portions of the boundary to alternate between inflow and outflow

- Prescribing fixed values at outflow faces is non-physical (information should leave the domain freely)

- The flux-based switching automatically adapts to the instantaneous flow direction at each face

```
1  spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
```

Listing 6: Using inlet-outlet BC

4.2   Fixed Outlet Direction (`-outletDirection`)

Creates a separate `outlet` patch from faces at one edge of the extraction box:

- **oldInternalFaces**: Pure Dirichlet BC (`spaceTimeWindow`) on all remaining faces

- **outlet**: Pressure relief patch with `inletOutlet` for U and `zeroGradient` for p

Use when the mean flow direction is well-defined and outflow always occurs at a known location.

```
1  spaceTimeWindowInitCase -sourceCase ../source-case -outletDirection "(1 0 0)"
```

Listing 7: Using fixed outlet direction

> **△ Warning**
>
> These options are mutually exclusive. Using both `-inletOutletBC` and `-outletDirection` together produces an error with guidance.

4.3   Boundary Condition Assignment Logic

For each field in the initial time directory, `spaceTimeWindowInitCase` assigns BCs according to Table 1.

This ensures fields without time-varying data automatically get appropriate BCs.

Table 1: Boundary condition assignment logic

In boundaryData?	-inletOutletBC?	Field Type	BC Applied
Yes	Yes	vector (U)	`spaceTimeWindowInletOutlet`
Yes	Yes	scalar	`zeroGradient`
Yes	No	any	`spaceTimeWindow` (Dirichlet)
No	any	any	`zeroGradient`

Extraction Phase
Full-domain simulation with `spaceTimeWindowExtract`

↓

Case Setup Phase
Run `spaceTimeWindowInitCase`

↓

Reconstruction Phase
Subset simulation with `spaceTimeWindow` BC
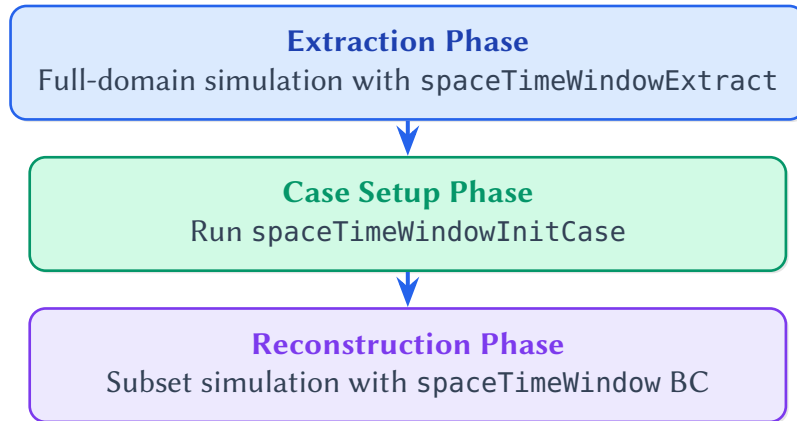
Figure 9: Space-time window reconstruction workflow

5 Workflow Overview

The space-time window reconstruction workflow is strictly sequential, as shown in fig. 9.

5.1 Serial Workflow

```
# 1. Run extraction during simulation
cd source-case
pimpleFoam    # With spaceTimeWindowExtract function object

# 2. Initialize reconstruction case (recommended: inlet-outlet BC)
cd ../subset-case
spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC

# 3. Run reconstruction
pimpleFoam
```

Listing 8: Complete serial workflow

In serial mode:

- Mesh and initial fields are written directly to the output directory

- Boundary data is written at every timestep

- The extractor forces field writes at t_1 and t_2 (for interpolation buffers)

> **i Note**
>
> In serial mode, the extractor writes internal fields only at t_0 (extraction start). The t_1 and t_2 internal fields are **not** automatically saved. If you need linear interpolation starting at t_1, ensure your `writeInterval` captures t_1, or use parallel mode which forces writes at t_0, t_1, and t_2.

5.2 Parallel Workflow

1. Run the original simulation in parallel with extraction enabled

2. Run `reconstructPar` for the desired start timestep (t_2 for cubic interpolation)

3. Run `spaceTimeWindowInitCase -sourceCase <path> -inletOutletBC`

4. Run the solver on the subset case (serial or parallel)

```
1   # Step 1: Run parallel extraction
2   cd source-case
3   mpirun -np 4 pimpleFoam -parallel
4   # Extraction automatically forces writes at t_0, t_1, t_2
5
6   # Step 2: Reconstruct fields at cubic-safe start time (t_2)
7   reconstructPar -time 0.0002
8
9   # Step 3: Initialize subset case (recommended: inlet-outlet BC)
10  cd ../subset-case
11  spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
12
13  # Step 4: Run reconstruction
14  pimpleFoam
```

Listing 9: Complete parallel workflow

In parallel mode:

- Boundary data from all processors is gathered to master and written as single files

- The extractor forces field writes at t_0, t_1, and t_2 for interpolation buffers (t_0 only in parallel)

- Only extraction box parameters are written (not mesh) — `spaceTimeWindowInitCase` creates the mesh

- `reconstructPar` must be run at the reconstruction start time (t_2) to provide source fields

6   Configuration Reference

6.1 Extraction Configuration

The extraction function object is configured in `system/controlDict` within the `functions` sub-dictionary. The available parameters are listed in table 2.

```
1   functions
2   {
3       extractSubset
4       {
5           type              spaceTimeWindowExtract;
6           libs              (spaceTimeWindow);
7
8           // Bounding box: ((minX minY minZ) (maxX maxY maxZ))
9           // Must be fully internal to domain
10          box               ((0.05 -0.25 0.01) (0.90 0.25 0.38));
11
12          outputDir       "../subset-case";
13
14          // Fields for time-varying boundary data (written every timestep)
15          fields          (U);                // Typically just velocity
16
17          // Fields for initial conditions (optional, defaults to 'fields')
18          initialFields   (U p nut);         // More fields for IC
19
20          // Write format: ascii, binary, deltaVarint, or dvzt
21          writeFormat     dvzt;              // Recommended: best compression
22
23          // Precision for deltaVarint/dvzt (default: 6)
24          deltaVarintPrecision  6;
25
26          // Keyframe interval for dvzt (default: 20)
27          dvztKeyframeInterval  20;
28
29          // Gzip compression (ignored for deltaVarint/dvzt)
30          writeCompression off;
31
32          // Optional encryption
33          // publicKey     "base64-encoded-public-key";
34
35          // Time window (optional)
36          // timeStart     0.0;
37          // timeEnd       1.0;
38
39          writeControl    timeStep;
40          writeInterval   1;
41      }
42  }
```

Listing 10: Complete extraction configuration

6.2 Initial Fields vs Boundary Data Fields

The extraction can separate which fields are used for:

- **Initial conditions** (`initialFields`): Fields written to the start time directory for solver initialization

Table 2: Extraction parameters

Parameter	Type	Required	Description
box	pointPair	Yes	Extraction bounding box
outputDir	fileName	Yes	Output case directory
fields	wordList	Yes	Fields for time-varying BC (boundary-Data)
initialFields	wordList	No	Fields for initial conditions (default: same as fields)
writeFormat	word	No	`ascii`, `binary`, `deltaVarint`, or `dvzt`
deltaVarintPrecision	label	No	Decimal digits (default: 6)
dvztKeyframeInterval	label	No	Keyframe interval for dvzt (default: 20)
writeCompression	switch	No	Gzip compression (ignored for deltaVarint/dvzt)
publicKey	string	No	Base64 public key for encryption
timeStart	scalar	No	Extraction start time
timeEnd	scalar	No	Extraction end time

- **Time-varying boundary data** (`fields`): Fields written to `boundaryData/` for time-varying BCs

This allows extracting more fields for initial conditions (e.g., `U p nut k omega`) while only storing time-varying data for velocity:

```
// In extraction function object
fields          (U);                 // Only U for time-varying BC (saves
    storage)
initialFields   (U p nut);           // More fields for initial conditions
```

Listing 11: Field selection strategy

Fields NOT in `boundaryData` automatically get `zeroGradient` BC on `oldInternalFaces`.

> ✓ **Tip**
>
> For unsteady turbulent flows with `-inletOutletBC`, the recommended approach is to extract only velocity (`U`) for boundary data while including all turbulence fields for initial conditions. This works because pressure and turbulence quantities use zeroGradient (no BC data needed), reducing storage by approximately 66%.

6.3 Boundary Condition Configuration

6.3.1 spaceTimeWindowInletOutlet (Recommended)

Flux-based boundary condition that reads pre-computed velocity values and applies them only at inflow faces. The parameters are listed in table 3.

```
boundaryField
{
    oldInternalFaces
    {
```

```
5            type                    spaceTimeWindowInletOutlet;
6            dataDir                 "constant/boundaryData";
7            phi                     phi;        // Flux field name
8            allowTimeInterpolation  true;
9            timeInterpolationScheme cubic;      // or "linear" or "none"
10           value                   uniform (0 0 0);
11       }
12   }
```

Listing 12: spaceTimeWindowInletOutlet configuration

How it works:

1. At each timestep, reads velocity values from boundaryData (with optional time interpolation)

2. Computes flux through each face: $\phi_f = \mathbf{U}_f \cdot \mathbf{S}_f$

3. For inflow faces ($\phi < 0$): applies prescribed velocity from boundaryData

4. For outflow faces ($\phi \geq 0$): applies zeroGradient (extrapolates from interior)

Table 3: spaceTimeWindowInletOutlet parameters

Parameter	Type	Default	Description
dataDir	fileName	constant/boundaryData	Path to boundary data
phi	word	phi	Name of flux field
allowTimeInterpolation	bool	false	Permit interpolation for missing timesteps
timeInterpolationScheme	word	linear	none, linear, or cubic

6.3.2 spaceTimeWindow (Pure Dirichlet)

Pure Dirichlet boundary condition that prescribes values on all faces regardless of flow direction. The parameters are listed in table 4.

```
1   boundaryField
2   {
3       oldInternalFaces
4       {
5           type                    spaceTimeWindow;
6           dataDir                 "constant/boundaryData";
7           fixesValue              true;       // Tells adjustPhi these values
                                                   are fixed
8           allowTimeInterpolation  true;
9           timeInterpolationScheme cubic;
10          reportFlux              true;
11          value                   uniform (0 0 0);
12      }
13  }
```

Listing 13: spaceTimeWindow configuration

Use this for:

- Scalar fields when not using `-inletOutletBC`

- Situations where fixed values are explicitly desired on all faces

Table 4: spaceTimeWindow parameters

Parameter	Type	Default	Description
dataDir	fileName	constant/boundaryData	Path to boundary data
fixesValue	bool	true	Report to adjustPhi that values are fixed
allowTimeInterpolation	bool	false	Enable time interpolation
timeInterpolationScheme	word	linear	none, linear, or cubic
reportFlux	bool	false	Print net flux through patch (velocity only)
setAverage	bool	false	Adjust field average
offset	Type	Zero	Offset value

6.4 Case Initialization Options

The `spaceTimeWindowInitCase` utility accepts command-line options (see table 5):

```
# Recommended: inlet-outlet BC for unsteady turbulent flows
spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC

# Alternative: fixed outlet direction for steady-mean flows
spaceTimeWindowInitCase -sourceCase ../source-case -outletDirection "(1 0 0)"

# With mass flux correction (optional, ensures exact mass conservation)
spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
    -correctMassFlux
```

Listing 14: spaceTimeWindowInitCase usage

> ⚠ **Warning**
>
> `-inletOutletBC` and `-outletDirection` are mutually exclusive. Using both together produces an error with guidance on which option to choose.

6.5 Mesh Coarsening and Refinement

The reconstruction mesh can be coarsened or refined relative to the extraction mesh (table 6). This enables running reconstructions at different resolutions than the original simulation.

Table 5: spaceTimeWindowInitCase options

Option	Type	Description
-sourceCase	directory	Source case where extraction ran (required)
-extractDir	directory	Directory with extracted data (default: cwd)
-inletOutletBC	flag	**Recommended.** Use flux-based inlet-outlet BC for U, zero-Gradient for scalars
-outletDirection	vector	Create fixed outlet patch in given direction (e.g., "(1 0 0)")
-outletFraction	scalar	Fraction of box extent for outlet region (default: 0.1)
-correctMassFlux	flag	Apply least-squares mass flux correction to boundaryData
-initialFields	list	Override initial fields list (e.g., "(U p nut k)")
-refineLevel	label	Refine mesh N times (spatial interpolation at runtime)
-coarsenLevel	label	Coarsen mesh N times (spatial interpolation at runtime)
-overwrite	flag	Overwrite existing files

```
1  # Refine mesh (finer than extraction)
2  spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -refineLevel 1
3
4  # Coarsen mesh (coarser than extraction)
5  spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -coarsenLevel 1
6
7  # Multiple levels
8  spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -refineLevel 2
```

Listing 15: Mesh resolution options

Table 6: Mesh resolution options

Option	Type	Description
-refineLevel	label	Refine mesh N times (each level splits cells ×8)
-coarsenLevel	label	Coarsen mesh N times (each level merges cells)

> ⚠ **Warning**
>
> -refineLevel and -coarsenLevel are mutually exclusive. Use only one at a time.

6.5.1 Spatial Interpolation Algorithms

When the reconstruction mesh differs from the extraction mesh, spatial interpolation is required for boundary data. The spaceTimeWindow boundary conditions handle this automatically at runtime using different algorithms depending on the resolution change.

Refinement: Barycentric Interpolation with 2D Delaunay Triangulation   When the target mesh has more faces than the source (refinement), the algorithm triangulates source face centers using the Bowyer-Watson algorithm, as illustrated in fig. 10. For each target face center, the enclosing triangle is found and barycentric weights are computed. If the target point lies outside all triangles (which can happen because the extracted submesh uses original

cells from the source case and may have irregular boundaries), the algorithm finds the nearest triangle by centroid distance and uses clamped barycentric coordinates. This provides smooth C^0 continuous interpolation.

Given a target point p inside a triangle with vertices v_1, v_2, v_3, the barycentric coordinates $(\lambda_1, \lambda_2, \lambda_3)$ satisfy eq. (6):

$$p = \lambda_1 v_1 + \lambda_2 v_2 + \lambda_3 v_3, \quad \text{where} \quad \lambda_1 + \lambda_2 + \lambda_3 = 1 \tag{6}$$

The weights are computed from signed triangle areas (eq. (7)):

$$\lambda_1 = \frac{A(p, v_2, v_3)}{A(v_1, v_2, v_3)}, \quad \lambda_2 = \frac{A(v_1, p, v_3)}{A(v_1, v_2, v_3)}, \quad \lambda_3 = \frac{A(v_1, v_2, p)}{A(v_1, v_2, v_3)} \tag{7}$$

where the signed area of a 2D triangle is given by eq. (8):

$$A(a, b, c) = \frac{1}{2} \left[(b_x - a_x)(c_y - a_y) - (c_x - a_x)(b_y - a_y) \right] \tag{8}$$

The interpolated field value at the target point is then (eq. (9)):

$$\phi(p) = \lambda_1 \phi_1 + \lambda_2 \phi_2 + \lambda_3 \phi_3 \tag{9}$$

Barycentric Interpolation (Refinement)

● Source face centers
✕ Target face center
— Delaunay triangles

$v_{\text{target}} = w_1 v_1 + w_2 v_2 + w_3 v_3$
where $w_1 + w_2 + w_3 = 1$
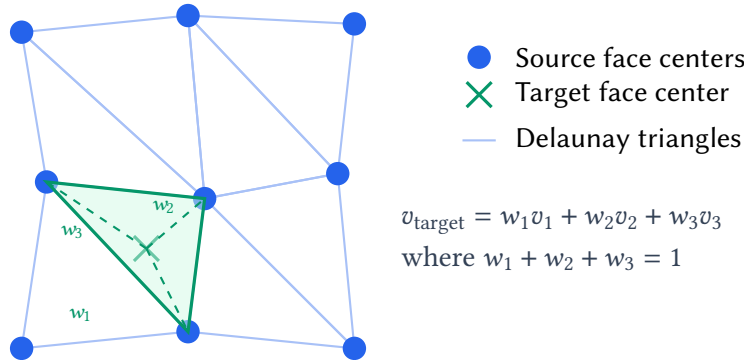
Figure 10: Barycentric interpolation for mesh refinement: source face centers (blue) are triangulated, and each target point (green) is interpolated using barycentric weights from the enclosing triangle

Coarsening: Area-Weighted Averaging When the target mesh has fewer faces than the source (coarsening), an octree is built from source points for efficient spatial lookup, as shown in fig. 11. For each target face, all source points within a search radius are found and averaged with equal weights. If no points are found, the search radius is progressively expanded. This ensures conservation of integral quantities.

For a target point p with search radius r, define the set of contributing source points (eq. (10)):

$$\mathcal{S}(p, r) = \{i : \|x_i - p\| \le r\} \tag{10}$$

The interpolated value is the arithmetic mean of all contributing sources (eq. (11)):

$$\phi(p) = \frac{1}{|\mathcal{S}|} \sum_{i \in \mathcal{S}} \phi_i \tag{11}$$

If $|\mathcal{S}| = 0$, the search radius is expanded by a factor $\alpha > 1$ (typically $\alpha = 1.5$) and the search is repeated (eq. (12)):

$$r \leftarrow \alpha \cdot r \quad \text{until} \quad |\mathcal{S}(\boldsymbol{p}, r)| > 0 \tag{12}$$

The octree provides $\mathcal{O}(\log N)$ lookup complexity for finding points within the search radius, making the algorithm efficient even for large meshes.

Figure 11: Area-weighted averaging for mesh coarsening: all source face centers (blue) within the search radius of each target point (orange) are averaged with equal weights

2D Projection by Box Face   The interpolation is performed on 2D point clouds, as illustrated in fig. 12. Points are grouped by which face of the extraction bounding box they belong to (6 planar surfaces: $\pm X$, $\pm Y$, $\pm Z$), then projected to 2D by dropping the constant coordinate. This exploits the box geometry while handling the irregular face distribution that arises from extracting a submesh with original cell shapes.
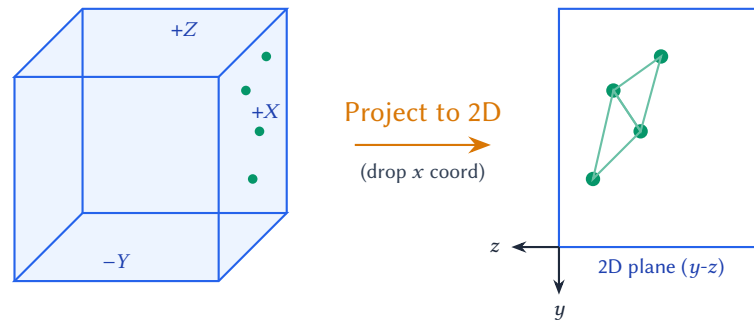
Figure 12: Points on each box face are projected to 2D for triangulation. The constant coordinate (perpendicular to the face) is dropped, enabling efficient 2D algorithms

6.5.2 Initial Field Interpolation

Initial fields are also interpolated when mesh resolution changes (see figs. 13 and 14):

- **Refinement**: Uses `mapFields` with cell-center interpolation (fig. 13)

- **Coarsening**: Uses volume-weighted averaging of source cells (fig. 14)

mapFields Cell-Center Interpolation (Refinement)

Source (coarse)   Target (fine)

Each target cell interpolates from neighboring source cells
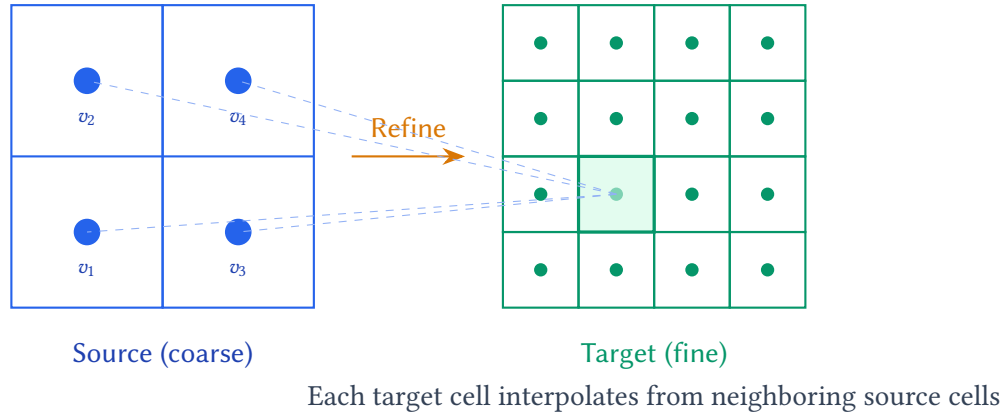
Figure 13: Initial field refinement using mapFields: target cell values are interpolated from surrounding source cell centers using distance-weighted averaging

Volume-Weighted Averaging (Coarsening)

Source (fine)   Target (coarse)

$$v_{\text{target}} = \frac{\sum_i V_i \cdot v_i}{\sum_i V_i}$$
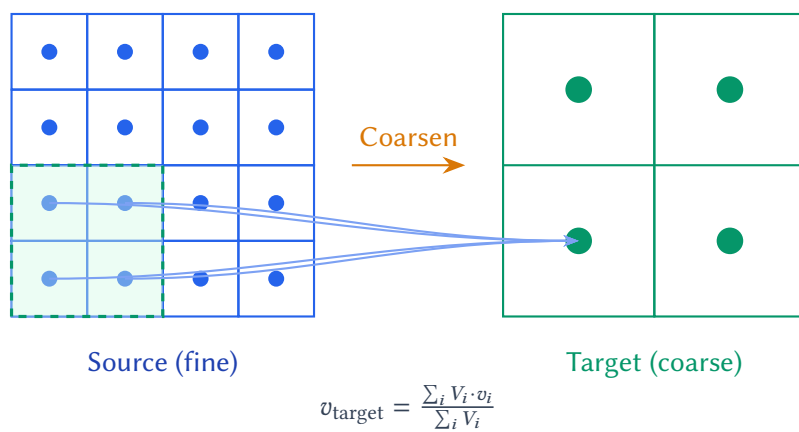
Figure 14: Initial field coarsening using volume-weighted averaging: source cell values within each target cell region are averaged weighted by their volumes

> **i Note**
>
> Spatial interpolation introduces smoothing, particularly for coarsening. For turbulent flows, this may affect small-scale structures. Consider the trade-off between computational cost and resolution fidelity.

What spaceTimeWindowInitCase creates:

1. `system/controlDict` — With matching solver, deltaT, adjustTimeStep from extraction

   - `startTime` set to t_2 (third timestep) for cubic interpolation buffer
   - `endTime` set to t_{n-2} (third-to-last) for cubic interpolation buffer

2. `system/fvSchemes`, `system/fvSolution` — Copied from source case (with pRefPoint added)

3. `constant/` files — All physics properties copied (mandatory for fidelity)

4. Initial field files with appropriate BCs based on options and boundaryData availability

7 Data Storage Format

7.1 Directory Structure

The extraction creates the following directory structure:

```
outputDir/
    constant/
        polyMesh/                # Subset mesh
            points
            faces
            owner
            neighbour
            boundary
            extractionBox        # (parallel only)
        boundaryData/
            oldInternalFaces/
                points               # Face centres
                extractionMetadata   # Settings and timestep list
                0.0001/
                    U                # or U.dvz or U.dvz.enc
                    p
                    nut
                0.0002/
                    ...
    0.0001/                          # Initial fields (serial only)
        U
        p
        nut
```

Listing 16: Extracted data structure

7.2 Boundary Data Compression

The `writeFormat` parameter controls how boundary data files are written, with compression ratios summarized in table 7.

Table 7: Compression comparison

Format	Extension	Typical Size	Notes
ASCII	(none)	100%	Human-readable
Binary	(none)	~50%	OpenFOAM native
ASCII + gzip	.gz	~10%	Compressed
Binary + gzip	.gz	~8%	Compressed
deltaVarint	.dvz	~2.7%	High compression, self-contained
dvzt	.dvzt	~2.4%	Best compression, recommended

7.2.1 Delta-Varint Codec (DVZ)

Specialized codec optimized for CFD boundary data (see figs. 15 and 16):

1. **Component-major ordering**: Groups similar values (all U_x, then U_y, then U_z)

2. **Spatial delta encoding**: Stores differences between consecutive face values within the same timestep

3. **Quantization**: Rounds to configurable precision

4. **Varint encoding**: Variable-length integer encoding

5. **Zigzag encoding**: Efficient signed integer representation

DVZ Encoding Pipeline

1. Raw Data (face-major):

| $U_{x,0}$ | $U_{y,0}$ | $U_{z,0}$ | $U_{x,1}$ | $U_{y,1}$ | $U_{z,1}$ | $U_{x,2}$ | $U_{y,2}$ | $U_{z,2}$ |

2. Component-major reorder:

| $U_{x,0}$ | $U_{x,1}$ | $U_{x,2}$ | $U_{y,0}$ | $U_{y,1}$ | $U_{y,2}$ | $U_{z,0}$ | $U_{z,1}$ | $U_{z,2}$ |

all x all y all z

3. Spatial delta encoding:

| v_0 | δ_1 | δ_2 | v_0 | δ_1 | δ_2 | v_0 | δ_1 | δ_2 | $\delta_i = v_i - v_{i-1}$

4. Quantize → Zigzag → Varint:

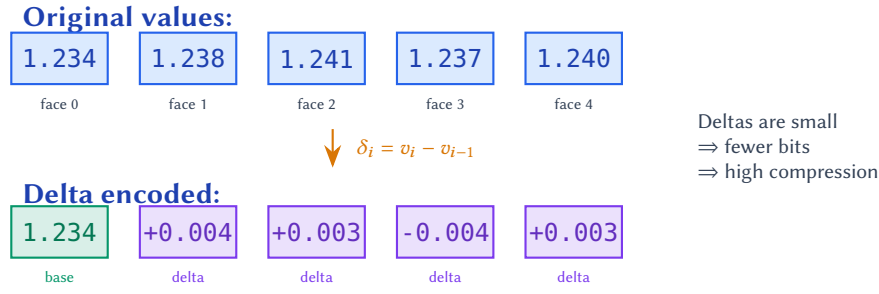| Compact variable-length bytes | Small δ = fewer bytes

Figure 15: DVZ encoding pipeline: data is reordered by component for better locality, then delta-encoded spatially. Quantization, zigzag encoding (for signed integers), and variable-length integer encoding produce compact output

Spatial Delta Encoding

Original values:

1.234	1.238	1.241	1.237	1.240
face 0	face 1	face 2	face 3	face 4

$\delta_i = v_i - v_{i-1}$

Deltas are small
$\Rightarrow$ fewer bits
$\Rightarrow$ high compression

Delta encoded:

1.234	+0.004	+0.003	-0.004	+0.003
base	delta	delta	delta	delta

Figure 16: Spatial delta encoding: instead of storing absolute values, DVZ stores the first value and differences between consecutive faces. Smooth CFD fields have small deltas, enabling high compression

> **i Note**
>
> Each DVZ timestep file is completely self-contained. Delta encoding is purely spatial (between consecutive faces in a single field), not temporal. Any timestep can be read independently without access to other timesteps.

7.2.2 DVZ Mathematical Formulation

Component-Major Reordering   For a vector field U with N faces, the raw data layout is face-major (eq. (13)):

$$\text{Raw} : [U_{x,0}, U_{y,0}, U_{z,0}, U_{x,1}, U_{y,1}, U_{z,1}, \dots, U_{x,N-1}, U_{y,N-1}, U_{z,N-1}] \tag{13}$$

DVZ reorders to component-major for better compression (eq. (14)):

$$\text{Reordered} : [\underbrace{U_{x,0}, U_{x,1}, \dots, U_{x,N-1}}_{\text{all } x}, \underbrace{U_{y,0}, \dots, U_{y,N-1}}_{\text{all } y}, \underbrace{U_{z,0}, \dots, U_{z,N-1}}_{\text{all } z}] \tag{14}$$

Spatial Delta Encoding   For each component sequence $\{v_0, v_1, \dots, v_{N-1}\}$, store deltas as shown in eq. (15):

$$\delta_0 = v_0, \quad \delta_i = v_i - v_{i-1} \quad \text{for } i = 1, \dots, N-1 \tag{15}$$

For smooth CFD fields, consecutive face values are similar, so $|\delta_i| \ll |v_i|$.

Quantization   Convert floating-point deltas to integers with configurable precision p (decimal digits) using eq. (16):

$$q_i = \text{round}(\delta_i \times 10^p) \tag{16}$$

The precision parameter controls the trade-off between compression ratio and accuracy. With $p = 6$ (default), values are accurate to $\sim 10^{-6}$ relative precision.

Zigzag Encoding   Convert signed integers to unsigned for efficient varint encoding (eq. (17)):

$$z_i = \begin{cases} 2q_i & \text{if } q_i \geq 0 \\ -2q_i - 1 & \text{if } q_i < 0 \end{cases} = (q_i \ll 1) \oplus (q_i \gg 31) \tag{17}$$

This maps small-magnitude signed integers to small unsigned integers: $0 \mapsto 0$, $-1 \mapsto 1$, $1 \mapsto 2$, $-2 \mapsto 3$, etc.

Variable-Length Integer Encoding   Encode unsigned integers using 7 bits per byte, with the high bit indicating continuation (eq. (18)):

$$\text{bytes}(z) = \left\lceil \frac{\lfloor \log_2(z) \rfloor + 1}{7} \right\rceil \tag{18}$$

Small values ($z < 128$) use 1 byte; larger values use more bytes. Since smooth CFD fields produce small deltas, most values compress to 1–2 bytes instead of 4–8 bytes for raw floats/doubles.

7.2.3 Delta-Varint-Temporal Codec (DVZT)

Enhanced codec that exploits both spatial and temporal correlation for better compression (see figs. 17 to 19):

1. **Keyframes** (every N timesteps): Self-contained, same as DVZ (fig. 17)

2. **Delta frames**: Hybrid spatial-temporal prediction (fig. 18)

   - Uses weighted prediction: $\hat{v} = 0.3 \cdot v_{\text{spatial}} + 0.7 \cdot v_{\text{temporal}}$
   - Encodes residuals (actual - predicted) instead of raw spatial deltas
   - Typically ~10% smaller than DVZ for delta frames
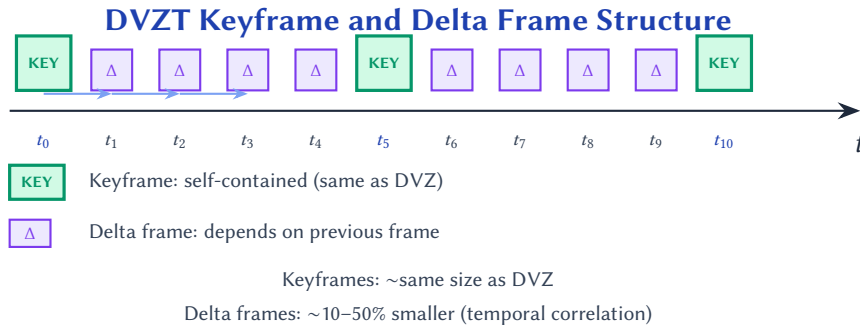
Figure 17: DVZT frame structure: keyframes are self-contained and appear every N timesteps (configurable). Delta frames between keyframes use temporal prediction for better compression

```
1  writeFormat          dvzt;
2  deltaVarintPrecision  6;        // ~1e-6 relative precision
3  dvztKeyframeInterval  20;       // Keyframe every 20 timesteps (default)
```

Listing 17: DVZT configuration

7.2.4 DVZT Mathematical Formulation

Frame Types   DVZT distinguishes between keyframes and delta frames based on the timestep index k (eq. (19)):

$$\text{Frame type}(k) = \begin{cases} \text{Keyframe} & \text{if } k \mod K = 0 \\ \text{Delta frame} & \text{otherwise} \end{cases} \tag{19}$$

where K is the keyframe interval (default $K = 20$).

DVZT Hybrid Prediction

Previous timestep $(t-1)$ Current timestep (t)

| 1.234 | 1.238 | 1.241 | | 1.235 | 1.240 | 1.243 |

face 0   face 1   face 2   face 0   face 1   face 2

Predicting face 1 at time t:

spatial: 1.235 $\hat{v} = 0.3 \times 1.235 + 0.7 \times 1.238$
temporal: 1.238 $\hat{v} = 1.2371$ (predicted)

Stored residual: +0.0029

actual − predicted = 1.240 − 1.2371

Small residuals $\Rightarrow$ high compression
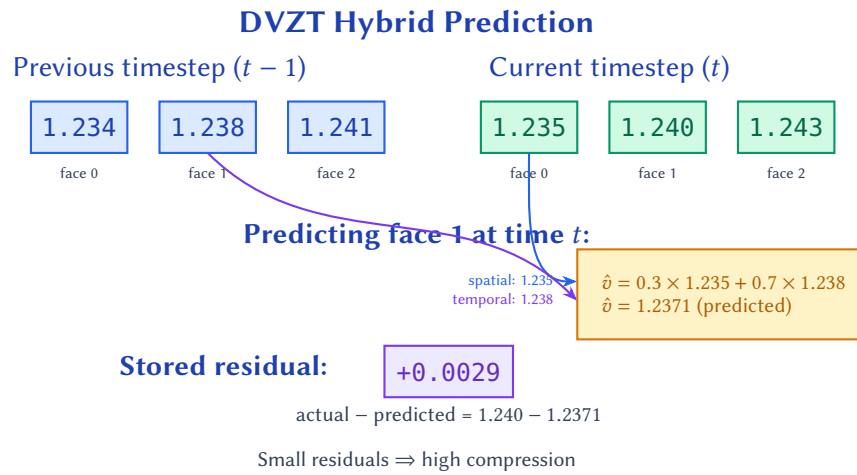
Figure 18: DVZT hybrid prediction: each value is predicted using 30% spatial neighbor (previous face at same timestep) and 70% temporal neighbor (same face at previous timestep). Only the small residual is stored

DVZT Workflow

| **Extraction** | → | **.dvzt** | **spaceTimeWindowInitCase** |
| writes .dvzt files | | compact storage | converts to .dvz |

| **Runtime BC** | ← | **.dvz** |
| random access | | self-contained timesteps |

Delta frames require sequential decoding
$\Rightarrow$ converted to DVZ before runtime
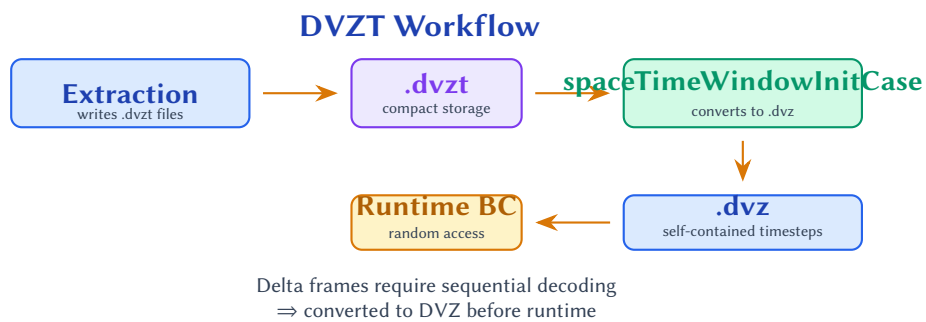
Figure 19: DVZT workflow: extraction writes compact .dvzt files. Before reconstruction, spaceTimeWindowInitCase converts them to .dvz format (required for random timestep access at runtime)

Keyframe Encoding Keyframes use pure DVZ encoding (spatial delta only), as shown in eq. (20):

$$\delta_i^{(k)} = v_i^{(k)} - v_{i-1}^{(k)} \quad \text{(spatial delta)} \tag{20}$$

Delta Frame Hybrid Prediction Delta frames use a weighted combination of spatial and temporal neighbors (eq. (21)):

$$\hat{v}_i^{(k)} = \alpha \cdot v_{i-1}^{(k)} + (1 - \alpha) \cdot v_i^{(k-1)} \tag{21}$$

where $\alpha = 0.3$ (30% spatial weight, 70% temporal weight).

The residual to be encoded is given by eq. (22):

$$r_i^{(k)} = v_i^{(k)} - \hat{v}_i^{(k)} \tag{22}$$

For slowly varying flows with small Δt, consecutive timesteps are nearly identical, so $v_i^{(k)} \approx v_i^{(k-1)}$, making the temporal prediction highly accurate and $|r_i^{(k)}| \ll |v_i^{(k)} - v_{i-1}^{(k)}|$.

Compression Ratio Analysis Let σ_s^2 be the variance of spatial deltas and σ_t^2 the variance of temporal deltas. The hybrid prediction residual variance is approximately (eq. (23)):

$$\sigma_r^2 \approx \alpha^2 \sigma_s^2 + (1 - \alpha)^2 \sigma_t^2 \tag{23}$$

For small timesteps where $\sigma_t^2 \ll \sigma_s^2$ (eq. (24)):

$$\frac{\sigma_r}{\sigma_s} \approx \alpha = 0.3 \tag{24}$$

This explains the ~70% reduction in residual magnitude, which translates to significant compression improvement through varint encoding.

Decoding Dependency Delta frames depend on the previous frame for reconstruction (eq. (25)):

$$v_i^{(k)} = r_i^{(k)} + \alpha \cdot v_{i-1}^{(k)} + (1 - \alpha) \cdot v_i^{(k-1)} \tag{25}$$

This creates a dependency chain from each keyframe (eq. (26)):

$$\text{Keyframe } k_0 \rightarrow \text{Frame } k_0 + 1 \rightarrow \cdots \rightarrow \text{Frame } k_0 + K - 1 \tag{26}$$

Random access requires decoding from the nearest preceding keyframe. For this reason, the initialization utility converts DVZT to DVZ before runtime.

DVZT Workflow:

During extraction, DVZT writes smaller `.dvzt` files. During case initialization, the utility automatically converts `.dvzt` to `.dvz` format (required because delta frames need sequential processing). The resulting `.dvz` files are read by the spaceTimeWindow BC at runtime.

Extraction $\rightarrow$ `.dvzt` files (~10% smaller) $\rightarrow$ `spaceTimeWindowInitCase` $\rightarrow$ `.dvz` files $\rightarrow$ Runtime

When to use DVZT:

- Long simulations with many timesteps (storage savings accumulate)

- Network/disk bandwidth constraints during extraction

- Small timesteps ($\Delta t = 10^{-5}$ or 10^{-6}) where temporal correlation is very strong

- DNS or acoustic simulations requiring fine temporal resolution

Compression vs Timestep Size:
DVZT benefits increase dramatically with smaller timesteps because consecutive values become nearly identical (see table 8):

Table 8: DVZT compression improvement by timestep size

Δt	Temporal Correlation	DVZT vs DVZ Savings
10^{-4}	Moderate	~10% smaller
10^{-5}	Strong	~20–30% smaller
10^{-6}	Very strong	~30–50% smaller

When to use DVZ:

- Simpler workflow (no conversion step)

- When random access to individual timesteps is needed during extraction

- Shorter simulations where DVZT overhead isn't worth it

- Large timesteps where temporal correlation is weak

7.2.5 External Compression Benchmark

DVZ and DVZT files can be further compressed using external tools for archival or transfer. The following benchmarks compare various compression algorithms on real boundary data files.

Test Environment:

- **CPU**: Intel Core i7-4790 @ 3.60 GHz (4 cores, 8 threads, Haswell microarchitecture)

- **L3 Cache**: 8 MB

- **RAM**: DDR3-1600

Test Data: 618 DVZ files totaling 13 MB (spatial delta-varint encoded), and 938 DVZT files totaling 30 MB (temporal delta-varint encoded).

The compression results are presented in table 9 for DVZ files and table 10 for DVZT files.
Key findings:

- **Best compression ratio**: 7z LZMA2 and xz achieve ~6% (94% reduction)

- **Best speed/ratio balance**: zstd -3 at 10–14% ratio with 300–400 MB/s throughput

- **zstd -3 is 40× faster than xz** with only 60% more space

- **zstd –ultra -22 provides no benefit** over zstd -19 for this data type

- **bzip2 and PPMd perform poorly** for CFD boundary data

Table 9: External compression results for DVZ files (13 MB original)

Method	Size	Ratio	Speed	Notes
7z lzma2 -mx9	769 KB	6.01%	11.2 MB/s	Best ratio
xz -6	769 KB	6.01%	10.2 MB/s	
zstd −ultra -22	964 KB	7.53%	4.7 MB/s	Very slow
zstd -19	965 KB	7.54%	15.3 MB/s	
rar -m5	1017 KB	7.95%	26.9 MB/s	
7z ppmd -mx9	1.4 MB	11.02%	10.7 MB/s	
zstd -9	1.7 MB	13.17%	109.5 MB/s	
zstd -3	1.8 MB	13.65%	309.0 MB/s	Best balance
zstd -1	1.9 MB	14.43%	533.7 MB/s	
bzip2 -9	2.0 MB	15.28%	13.5 MB/s	
gzip -6	2.1 MB	16.39%	94.2 MB/s	
lz4	2.3 MB	17.80%	635.2 MB/s	Fastest

Table 10: External compression results for DVZT files (30 MB original)

Method	Size	Ratio	Speed	Notes
7z lzma2 -mx9	1.9 MB	6.31%	10.1 MB/s	Best ratio
xz -6	1.9 MB	6.32%	10.5 MB/s	
zstd −ultra -22	2.6 MB	8.48%	2.4 MB/s	Very slow
zstd -19	2.6 MB	8.50%	10.4 MB/s	
rar -m5	2.8 MB	9.28%	28.0 MB/s	
zstd -9	2.8 MB	9.27%	120.6 MB/s	
7z ppmd -mx9	2.8 MB	9.37%	12.2 MB/s	
zstd -3	3.1 MB	10.10%	396.1 MB/s	Best balance
zstd -1	3.1 MB	10.25%	614.0 MB/s	
bzip2 -9	3.5 MB	11.52%	13.7 MB/s	
gzip -6	3.8 MB	12.71%	104.3 MB/s	
lz4	4.1 MB	13.56%	763.0 MB/s	Fastest

Recommendations:

- **Runtime/on-the-fly**: zstd -3 (~10% ratio, 300–400 MB/s)

- **Archive/transfer**: 7z lzma2 -mx9 or xz -6 (~6% ratio, 10 MB/s)

- **Real-time streaming**: lz4 (~14–18% ratio, 600–800 MB/s)

```
# Archive with best compression (7z)
cd subset-case/constant/boundaryData/oldInternalFaces
7z a -m0=lzma2 -mx=9 ../boundaryData.7z */U.dvz */U.dvzt

# Or with zstd for faster compression
tar -cf - */U.dvz */U.dvzt | zstd -3 > ../boundaryData.tar.zst
```

Listing 18: Archival compression example

7.3 Extraction Metadata

The `extractionMetadata` file contains:

```
{
    openfoamVersion    "v2512";
    openfoamApi        2512;
    solver             "pimpleFoam";
    deltaT             1e-04;
    adjustTimeStep     false;
    timePrecision      6;
    extractionStartTime 0.0001;
    boxMin             (0.05 -0.25 0.01);
    boxMax             (0.90 0.25 0.38);
    nGlobalFaces       12345;
    timesteps          (0.0001 0.0002 0.0003 ...);
}
```

Listing 19: extractionMetadata contents

8   Parallel Execution

Both the source simulation (extraction phase) and the reconstruction simulation can run in parallel. This enables efficient use of HPC resources for both phases of the workflow.

8.1 Parallel Extraction

The extraction function object fully supports parallel execution:

- Extraction box can span multiple processor domains

- Boundary data is gathered from all processors

- Master processor writes combined data files

- Processor boundary faces are handled automatically

```
1   # Decompose the case
2   decomposePar
3
4   # Run parallel extraction
5   mpirun -np 8 pimpleFoam -parallel
6
7   # Automatic field writes occur at:
8   #   t_0 - extraction start (for lookback)
9   #   t_1 - linear interpolation start
10  #   t_2 - cubic interpolation start
```

Listing 20: Parallel extraction

8.2 Field Reconstruction

After parallel extraction, reconstruct fields before case initialization:

```
1   # For cubic interpolation (recommended)
2   reconstructPar -time <t_2>
3
4   # For linear interpolation
5   reconstructPar -time <t_1>
```

Listing 21: Field reconstruction

△ **Warning**

The subset mesh created by `spaceTimeWindowInitCase` uses cell ordering from the reconstructed (serial) source mesh. Running `reconstructPar` before case initialization is mandatory for parallel extractions.

8.3 Parallel Reconstruction

The reconstruction simulation can also run in parallel, independently of how the extraction was performed:

```
1   cd subset-case
2   decomposePar
3   mpirun -np 4 pimpleFoam -parallel
4   reconstructPar
```

Listing 22: Parallel reconstruction

✓ **Tip**

The reconstruction case is typically much smaller than the source case, so fewer processors may be needed. The spaceTimeWindow boundary conditions work identically in serial and parallel modes.

9   Mass Conservation

9.1   The Mass Imbalance Problem

Face interpolation during extraction can introduce small mass flux imbalances:

$$\text{imbalance} = \sum_f \mathbf{U}_f \cdot \mathbf{S}_f \neq 0 \tag{27}$$

When all boundary patches have `fixesValue=true`, `adjustPhi()` cannot correct this imbalance, potentially causing pressure solver issues. Additionally, with all-Dirichlet BCs, the solver has no way to relieve pressure buildup.

9.2   Solutions

9.2.1   Use `-inletOutletBC` (Recommended)

The flux-based inlet-outlet BC naturally handles mass conservation:

- Outflow faces use zeroGradient, allowing natural outflow

- No artificial mass imbalance from prescribed outflow velocities

- Works without any special mass correction

```
spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC
```

Listing 23: Using inlet-outlet BC for mass conservation

9.2.2   Use `-correctMassFlux`

Applies least-squares correction to boundaryData to ensure exact mass conservation:

$$\mathbf{U}_{\text{corrected}} = \mathbf{U} - \frac{\text{imbalance}}{\sum_f |\mathbf{S}_f|} \cdot \hat{\mathbf{n}} \tag{28}$$

where $\hat{\mathbf{n}} = \mathbf{S}_f/|\mathbf{S}_f|$ is the face unit normal.
This minimizes $\|\mathbf{U}_{\text{corrected}} - \mathbf{U}\|^2$ subject to:

$$\sum_f \mathbf{U}_{\text{corrected}} \cdot \mathbf{S}_f = 0 \tag{29}$$

```
spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -correctMassFlux
```

Listing 24: Using mass flux correction

9.2.3   Use `-outletDirection` with `fixesValue true`

Creates an outlet patch where mass imbalance can escape:

- `oldInternalFaces` uses `fixesValue true` (values not modified by adjustPhi)

- `outlet` uses `inletOutlet` BC (allows adjustPhi correction)

9.3 The `fixesValue` Option

The `fixesValue` parameter controls `adjustPhi()` behavior:

- `fixesValue = true`: Patch excluded from flux correction (preserves exact values)

- `fixesValue = false`: Patch included in flux correction (allows modification)

9.4 Outlet Patch for Pressure Relief

The `-outletDirection` option creates an outlet patch (see fig. 20):

```
spaceTimeWindowInitCase -sourceCase ../source \
    -outletDirection "(1 0 0)" \
    -outletFraction 0.1
```

Listing 25: Creating outlet patch
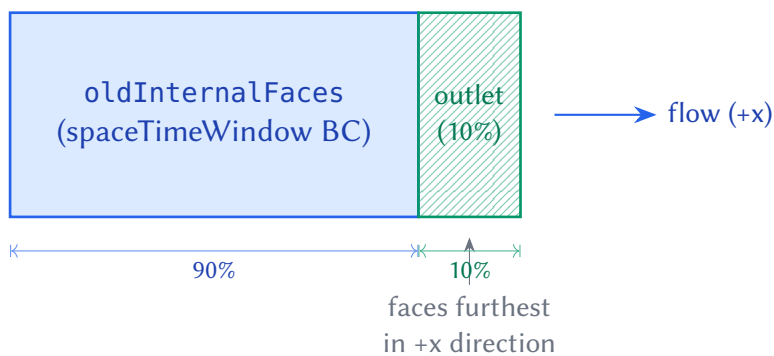
Figure 20: Outlet patch creation with `-outletDirection "(1 0 0)"`

Outlet faces are selected based on position (furthest along the outlet direction), not face orientation.

9.5 Recommended Configurations

The recommended mass conservation strategies are summarized in table 11.

Table 11: Mass conservation strategies

Configuration	Description
`-inletOutletBC`	**Recommended** for unsteady turbulent flows (vortex shedding, etc.). Natural mass balance through flux-based switching.
`-inletOutletBC -correctMassFlux`	Unsteady turbulent + extra safety. Ensures exact mass balance with inlet-outlet switching.
`-outletDirection "(1 0 0)"`	Steady-mean flow direction. Use when outlet location is known and flow direction is consistent.
`-correctMassFlux (no outlet)`	Maximum fidelity. All faces prescribed with exact mass balance.

10 Solver Settings and Relaxation

10.1 Time Stepping

For accurate reconstruction, use identical time stepping:

```
1  deltaT          1e-04;      // Must match extraction
2  adjustTimeStep  no;         // Fixed timestep recommended
3
4  // If adaptive timestep is required:
5  adjustTimeStep  yes;
6  maxCo           0.5;
7  maxDeltaT       1e-03;
```

Listing 26: Recommended controlDict settings

> ⚠ **Warning**
>
> The reconstruction must use identical `deltaT` and `adjustTimeStep` settings as the extraction. Mismatches cause fatal errors unless `allowTimeInterpolation=true`.

10.2 PIMPLE Settings

For incompressible flows:

```
1  PIMPLE
2  {
3      nOuterCorrectors    2;
4      nCorrectors         2;
5      nNonOrthogonalCorrectors 1;
6
7      // Pressure reference (set by spaceTimeWindowInitCase)
8      pRefPoint           (0.5 0 0.2);
9      pRefValue           0;
10  }
```

Listing 27: Recommended PIMPLE settings

10.3 Relaxation Factors

> ✓ **Tip**
>
> For reconstruction simulations, relaxation is typically **not needed** because:
>
> - Boundary conditions are prescribed (not coupled)
>
> - Initial conditions come from the source simulation
>
> - Flow field evolves smoothly from physical initial state

If stability issues occur, try:

```
1  relaxationFactors
2  {
3      fields
4      {
5          p                    0.7;
6      }
7      equations
8      {
9          U                    0.7;
10         "(k|epsilon|omega|nuTilda)"  0.7;
11     }
12 }
```

Listing 28: Optional relaxation

10.4 Linear Solver Settings

Standard settings work well:

```
1  solvers
2  {
3      p
4      {
5          solver          GAMG;
6          smoother        GaussSeidel;
7          tolerance       1e-06;
8          relTol          0.01;
9      }
10
11     U
12     {
13         solver          PBiCGStab;
14         preconditioner  DILU;
15         tolerance       1e-06;
16         relTol          0.1;
17     }
18 }
```

Listing 29: Linear solver settings

11   Time Interpolation

The boundary conditions support three time interpolation modes, summarized in Table 12 and illustrated in fig. 21. The comparison between linear and cubic interpolation quality is shown in fig. 22.

spaceTimeWindowInitCase automatically sets startTime and endTime to ensure sufficient buffer timesteps for the selected interpolation scheme (see fig. 23 for buffer requirements).

11.1 Exact Timestep Matching (Default)

By default, the boundary condition requires exact timestep matching:

Table 12: Time interpolation modes

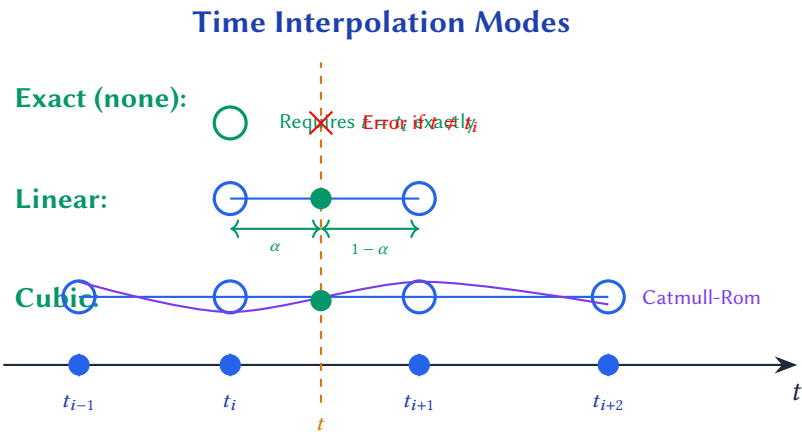| Mode	Start Time	Timesteps Used	Use Case
none (exact)	t_0	1 (exact match)	"Bit"-reproducible results
linear	t_1	2 (bracketing)	Simple, smoothly varying flows
cubic	t_2	4 (Catmull-Rom)	Unsteady turbulent flows (recommended)

Figure 21: Time interpolation modes: exact matching uses only one timestep, linear interpolation uses two bracketing timesteps, and cubic (Catmull-Rom) uses four timesteps for smooth C^1 continuous interpolation
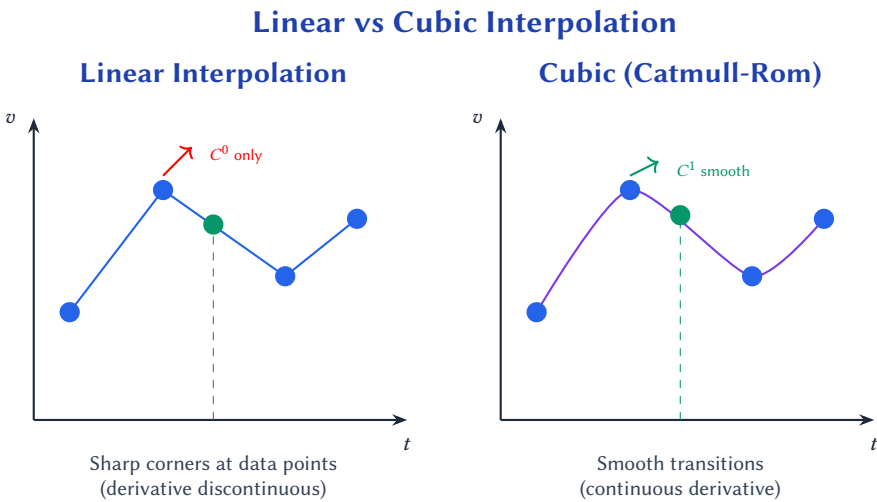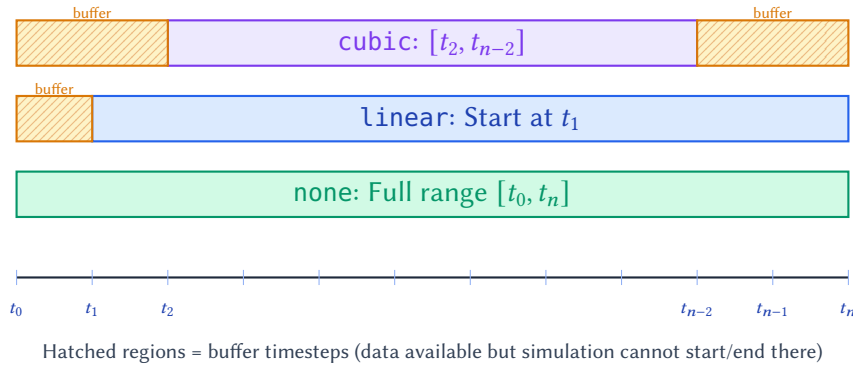

Figure 22: Comparison of linear and cubic interpolation: linear interpolation creates C^0 continuous curves with sharp corners at data points, while Catmull-Rom cubic splines provide C^1 continuity with smooth transitions

Time Buffer Requirements

Hatched regions = buffer timesteps (data available but simulation cannot start/end there)

Figure 23: Time buffer requirements for each interpolation mode: exact matching can use the full range, linear needs one buffer timestep at the start, and cubic needs two buffer timesteps at both start and end

- Simulation time must match available sample times (within 1% of `deltaT`)

- Fatal error if no matching timestep found

- Ensures "bit"-reproducible results (highest fidelity)

11.2 Linear Interpolation

For cases where exact matching is not possible:

```
oldInternalFaces
{
    type                  spaceTimeWindow;
    allowTimeInterpolation  true;
    timeInterpolationScheme linear;
    // ...
}
```

Listing 30: Linear interpolation

Uses two bracketing timesteps (eq. (30)):

$$\text{value} = (1 - \alpha) \cdot v_i + \alpha \cdot v_{i+1} \quad \text{where} \quad \alpha = \frac{t - t_i}{t_{i+1} - t_i} \tag{30}$$

The interpolation parameter $\alpha \in [0, 1]$ represents the normalized position between the two samples. This is equivalent to first-order polynomial interpolation (eq. (31)):

$$\phi(t) = \phi_i + \frac{\phi_{i+1} - \phi_i}{t_{i+1} - t_i}(t - t_i) \tag{31}$$

Linear interpolation provides C^0 continuity (continuous values but discontinuous derivatives at sample points).

11.3 Cubic Spline Interpolation

For smoother results with adaptive timestepping:

```
oldInternalFaces
{
    type                    spaceTimeWindow;
    allowTimeInterpolation  true;
    timeInterpolationScheme cubic;
    // ...
}
```

Listing 31: Cubic interpolation

Uses centripetal Catmull-Rom spline with four timesteps ($t_{i-1}, t_i, t_{i+1}, t_{i+2}$):

- Handles non-uniform time spacing correctly

- Provides C^1 continuity

- No overshoots or cusps

- Essential for `adjustTimeStep=yes`

11.3.1 Catmull-Rom Spline Formulation

The centripetal Catmull-Rom spline passes through all control points and provides C^1 continuity. Given four consecutive sample values $\phi_0, \phi_1, \phi_2, \phi_3$ at times t_0, t_1, t_2, t_3, the interpolated value for $t \in [t_1, t_2]$ is computed as follows.

First, compute the centripetal parameterization distances (eq. (32)):

$$d_j = |t_{j+1} - t_j|^{0.5}, \quad j = 0, 1, 2 \tag{32}$$

The normalized parameter within the segment $[t_1, t_2]$ is (eq. (33)):

$$u = \frac{t - t_1}{t_2 - t_1} \tag{33}$$

The spline is constructed using the Barry-Goldman algorithm. Define intermediate points (eq. (34)):

$$\begin{aligned}
A_1 &= \frac{t_2 - t}{t_2 - t_0}\phi_0 + \frac{t - t_0}{t_2 - t_0}\phi_1 \\
A_2 &= \frac{t_2 - t}{t_2 - t_1}\phi_1 + \frac{t - t_1}{t_2 - t_1}\phi_2 \\
A_3 &= \frac{t_3 - t}{t_3 - t_1}\phi_2 + \frac{t - t_1}{t_3 - t_1}\phi_3
\end{aligned} \tag{34}$$

Then compute (eq. (35)):

$$\begin{aligned}
B_1 &= \frac{t_2 - t}{t_2 - t_0}A_1 + \frac{t - t_0}{t_2 - t_0}A_2 \\
B_2 &= \frac{t_3 - t}{t_3 - t_1}A_2 + \frac{t - t_1}{t_3 - t_1}A_3
\end{aligned} \tag{35}$$

Finally, the interpolated value is (eq. (36)):

$$\phi(t) = \frac{t_2 - t}{t_2 - t_1}B_1 + \frac{t - t_1}{t_2 - t_1}B_2 \tag{36}$$

This formulation correctly handles non-uniform time spacing, which is essential when adaptive timestepping (`adjustTimeStep=yes`) produces variable timesteps.

11.4 Time Range Requirements

- **Linear**: Needs 2 buffer timesteps at start

- **Cubic**: Needs 2 buffer timesteps at start and end

- `spaceTimeWindowInitCase` automatically sets appropriate `startTime` and `endTime`

> **i Note**
>
> Extrapolation outside the extraction window is **never** allowed, regardless of interpolation settings.

12   Flux Reporting and Diagnostics

Enable flux reporting to monitor mass conservation:

```
oldInternalFaces
{
    type            spaceTimeWindow;
    reportFlux      true;
    // ...
}
```

Listing 32: Enabling flux reporting

Output format (fields explained in table 13):

```
spaceTimeWindow flux [oldInternalFaces] t=0.001 thisPatch=1.234e-06 (in=-0.0523 out=0.0523) | MESH TOTAL=5.678e-05 (fixed=-0.0523
    adjustable=0.0523) | adjustPhi will correct: -5.678e-05
```

Listing 33: Flux report output

Table 13: Flux report fields

Field	Description
thisPatch	Net flux through this spaceTimeWindow patch
in	Sum of inward fluxes
out	Sum of outward fluxes
MESH TOTAL	Total net flux across all boundary patches
fixed	Flux from patches with fixesValue=true
adjustable	Flux from patches with fixesValue=false
adjustPhi will correct	Correction to be distributed

13   Troubleshooting

13.1 Common Errors

13.1.1 Time Step Mismatch

```
1  FOAM FATAL ERROR:
2  Time step mismatch between extraction and reconstruction!
3     Extraction deltaT: 8.53e-04
4     Current deltaT:    1e-03
```

Listing 34: deltaT mismatch error

Solution: Set `deltaT` in `system/controlDict` to match extraction.

13.1.2 No Matching Timestep

```
1  FOAM FATAL ERROR:
2  No exact timestep match found for t = 0.00015
3  Available times: 0.0001, 0.0002, 0.0003
```

Listing 35: Missing timestep error

Solution: Enable time interpolation with `allowTimeInterpolation true`.

13.1.3 Pressure Solver Divergence

Symptoms: Pressure residuals increase, NaN values appear.

Solutions:

1. Use `-correctMassFlux` option

2. Add outlet patch with `-outletDirection`

3. Set `fixesValue false` on `oldInternalFaces`

4. Check `pRefPoint` is inside the domain

13.1.4 Encryption Errors

```
1  FOAM FATAL ERROR:
2  Failed to decrypt file: constant/boundaryData/.../U.dvz.enc
```

Listing 36: Decryption failure

Solutions:

1. Verify private key is correct

2. Ensure library was built with `FOAM_USE_SODIUM=1`

3. Check file is not corrupted

14 Acknowledgments

A   Example Case: ERCOFTAC UFR2-02 Square Cylinder

The library includes a complete example based on the ERCOFTAC UFR2-02 benchmark case [2, 3] (Case 043 in the ERCOFTAC database): turbulent flow around a square cylinder at Re = 21,400. This case demonstrates vortex shedding and is ideal for testing space-time window reconstruction.

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A.1   Reference Data and Validation Resources

The ERCOFTAC (European Research Community on Flow, Turbulence and Combustion) Classic Collection Database provides extensive reference data for this test case, including:

- Experimental measurements from Lyn et al. [3] (laser-Doppler velocimetry)

- Reference numerical simulations from various research groups

- Mesh generation scripts and case setup files

- Detailed flow statistics and validation data

The database is accessible at:

http://cfd.mace.manchester.ac.uk/ercoftac/

An OpenFOAM-specific implementation guide is available at:

https://openfoamwiki.net/index.php?title=Benchmark_ercoftac_ufr2-02

> **i Note**
>
> If HTTPS access fails for the ERCOFTAC database, use HTTP (`http://`) instead. The ERCOFTAC server may not support secure connections.

A.2   Physical Background: Von Kármán Vortex Street

When fluid flows past a bluff body (such as a square cylinder), the flow separates at the sharp edges, creating alternating vortices that are shed from each side of the body. This phenomenon, known as the **von Kármán vortex street**, is characterized by:

- **Periodic vortex shedding**: Vortices detach alternately from upper and lower surfaces

- **Strouhal number**: St = $fD/U_\infty \approx 0.13$ for square cylinders, where f is the shedding frequency, D is the cylinder side length, and U_∞ is the freestream velocity

- **Turbulent wake**: At Re = 21,400, the wake is fully turbulent with complex three-dimensional structures

- **Unsteady forces**: Fluctuating lift and drag on the cylinder

The vortex street extends far downstream, making it an excellent test case for space-time window extraction—the extraction region can capture the wake dynamics while excluding the cylinder and inlet regions.
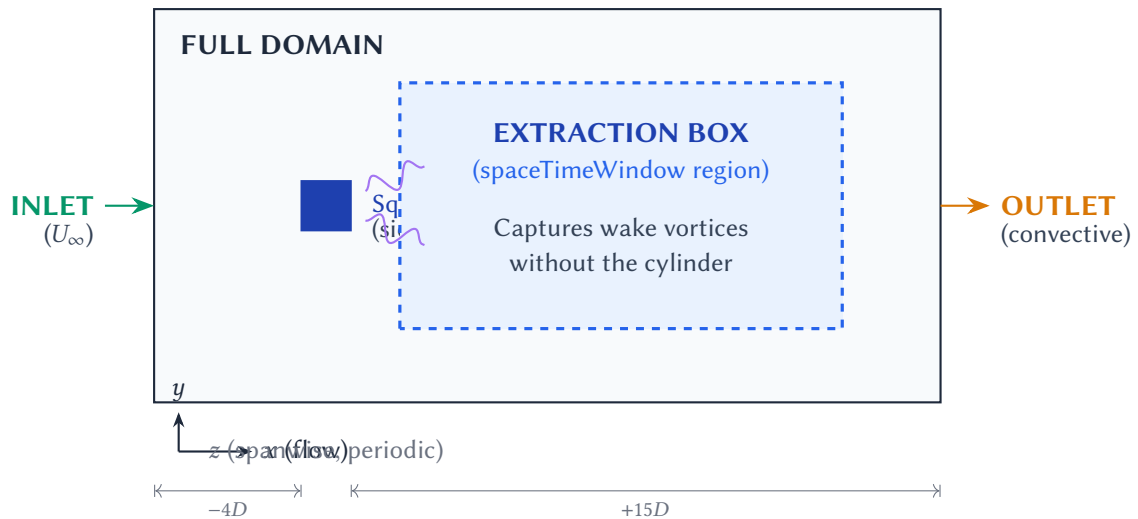
Figure 24: Computational domain for the square cylinder case showing the extraction box placement in the wake region

A.3 Domain and Mesh Configuration

The computational domain (fig. 24) extends from $-4D$ upstream to $+15D$ downstream of the cylinder, with lateral boundaries at $\pm 6.5D$. The spanwise extent is $4D$ with periodic boundary conditions.

A.4 Extraction Box Placement

The extraction box is positioned to capture the vortex street while avoiding:

- The cylinder itself (to avoid complex geometry in subset)

- The inlet region (where flow is uniform and uninteresting)

- Domain boundaries (box must be fully internal)

Example extraction configuration for this case:

```
extractSubset
{
    type            spaceTimeWindowExtract;
    libs            (spaceTimeWindow);

    // Box starts 0.5D downstream of cylinder, extends to 9D
    // Lateral extent captures the wake width
    // Full spanwise extent (periodic direction)
    box             ((0.05 -0.25 0.01) (0.90 0.25 0.38));

    outputDir       "../cylinder-subset";
    fields          (U p nut);
    writeFormat     deltaVarint;

    writeControl    timeStep;
    writeInterval   1;
```

```
17  }
```

Listing 37: Extraction configuration for square cylinder

A.5 Physical Parameters

The physical parameters for this case are listed in table 14.

Table 14: Square cylinder case parameters

Parameter	Value	Description
D	0.04 m	Cylinder side length
U_∞	8.25 m/s	Freestream velocity
ν	1.5×10^{-5} m^2/s	Kinematic viscosity
Re	21,400	Reynolds number
St	≈ 0.13	Strouhal number
T_{shed}	≈ 0.037 s	Vortex shedding period

A.6 Running the Example

```
1   cd examples/ufr2-02
2
3   # Generate mesh and run full simulation
4   ./Allrun
5
6   # The extraction creates ../ufr2-02-subset with:
7   #   - Subset mesh in constant/polyMesh
8   #   - Boundary data in constant/boundaryData
9   #   - Initial fields
10
11  # Initialize and run reconstruction (recommended: inlet-outlet BC)
12  cd ../ufr2-02-subset
13  spaceTimeWindowInitCase -sourceCase ../ufr2-02 -inletOutletBC
14
15  pimpleFoam
16
17  # Alternative: fixed outlet direction for steady-mean flows
18  # spaceTimeWindowInitCase -sourceCase ../ufr2-02 \
19  #     -outletDirection "(1 0 0)" \
20  #     -correctMassFlux
```

Listing 38: Running the example case

A.7 Validation

The reconstruction can be validated by comparing:

- Instantaneous velocity fields at matching timesteps

- Vortex shedding frequency (should match original)

- Mean velocity profiles in the wake

- Reynolds stress components

> **i Note**
>
> The reconstruction should exactly reproduce the original flow within the extraction region (to solver tolerance) when using exact timestep matching. Small differences may occur at the outlet boundary due to the different boundary condition type.

B Field Selection by Turbulence Model

When configuring the extraction, include all fields required by your turbulence model. Table 15 lists recommended fields for common models.

Table 15: Recommended fields by turbulence model

Turbulence Model	Recommended Fields
LES Smagorinsky	`(U p nut)`
LES dynamicKEqn	`(U p nut k)`
LES WALE	`(U p nut)`
RANS k-ε	`(U p nut k epsilon)`
RANS k-ω SST	`(U p nut k omega)`
Spalart-Allmaras	`(U p nut nuTilda)`

References

[1] Alin-Adrian Anton. *Space-Time Window Reconstruction in High-Performance Numeric Simulations: Application for CFD*. PhD thesis, Universitatea Politehnica Timişoara, Timişoara, Romania, November 2011. URL https://dspace.upt.ro/jspui/handle/123456789/643.

[2] ERCOFTAC. Classic collection database: Case 043 – flow around a square cylinder. http://cfd.mace.manchester.ac.uk/ercoftac/, 2024. Mesh generation script by Niklas Nordin.

[3] D. A. Lyn, S. Einav, W. Rodi, and J.-H. Park. A laser-Doppler velocimetry study of ensemble-averaged characteristics of the turbulent near wake of a square cylinder. *Journal of Fluid Mechanics*, 304:285–319, 1995. doi: 10.1017/S0022112095004435.