

spaceTimeWindow Library

Technical Manual

Version 1.0 (Draft) | OpenFOAM v2512

Boundary Data Extraction • Time Interpolation • Optional Encryption

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1 Introduction

The `spaceTimeWindow` library enables extraction and reconstruction of spatial subsets from Large Eddy Simulation (LES) and transient RANS simulations in OpenFOAM. This technique allows researchers to:

- Extract a region of interest from a full-domain simulation
- Store time-varying boundary conditions efficiently
- Reconstruct the flow within the subset using pre-computed boundary data
- Optionally encrypt boundary data for secure distribution

The library consists of four main components:

1. **`spaceTimeWindowExtract`** – Function object for boundary data extraction during simulation
2. **`spaceTimeWindowInitCase`** – Utility for reconstruction case initialization
3. **`spaceTimeWindow`** – Pure Dirichlet boundary condition for applying extracted data
4. **`spaceTimeWindowInletOutlet`** – Flux-based boundary condition (recommended for unsteady flows)

1.1 Requirements

- OpenFOAM v2512 (openfoam.com) or compatible ESI-OpenCFD version
- C++17 compatible compiler (GCC 7+ or Clang 5+)
- Optional: libsodium for encryption support
- Optional: MPI for parallel execution

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1.2 Building the Library

```

1 # Navigate to source directory
2 cd openfoam-spaceTimeWindow

3
4 # Build library and utilities
5 ./Allwmake

6
7 # Or with encryption support (requires libsodium)
8 ./Allwmake # Auto-detects libsodium if installed

```

Listing 1: Building spaceTimeWindow

For manual building with encryption:

```

1 cd src/spaceTimeWindow
2 export FOAM_USE_SODIUM=1 && wmake
3
4 cd applications/utilities/preProcessing/spaceTimeWindowInitCase
5 export FOAM_USE_SODIUM=1 && wmake
6
7 cd ../spaceTimeWindowKeygen
8 export FOAM_USE_SODIUM=1 && wmake

```

Listing 2: Manual build with encryption

2 Encryption of Boundary Data

The spaceTimeWindow library supports X25519 asymmetric encryption using libsodium sealed boxes. This allows secure distribution of simulation data where:

- Extraction uses only the **public key**
- Reconstruction requires the **private key**
- Data cannot be decrypted without the private key

2.1 Key Generation

Generate a keypair using the provided utility:

```

1 spaceTimeWindowKeygen
2 # Output:
3 # Public key: fqzYQ0U8j27tFEr5WzEMylbvXYP+9CAyk0JhwwZ2rwg=
4 # Private key: QgzxB5b+DGPQH8exbWDe18n4Kv0nu5gqljI2RPBCwl4=
5 #
6 # IMPORTANT: Store the private key securely!

```

Listing 3: Generating encryption keys

⚠ Warning

The private key must be stored securely and never committed to version control. Anyone with the private key can decrypt all boundary data encrypted with the corresponding public key.

2.2 Secure Key Storage

The private key should be stored using one of the following methods:

- **Hardware security keys:** YubiKey, Nitrokey, or similar FIDO2/PIV-capable devices provide the strongest protection. The private key never leaves the hardware token.
- **Secure password managers:** KeePassXC, 1Password, Bitwarden, or similar tools with strong master passwords and optional hardware key integration.
- **Encrypted vaults:** GPG-encrypted files or OS keychains (macOS Keychain, GNOME Keyring, Windows Credential Manager).

✓ Tip

For maximum security, generate the keypair on an air-gapped machine, store the private key on a hardware token, and only transfer the public key to the HPC system.

2.3 Encrypted Extraction

Add the public key to your extraction configuration in `system/controlDict`:

```

1  functions
2  {
3      extractSubset
4      {
5          type           spaceTimeWindowExtract;
6          libs           (spaceTimeWindow);
7
8          box            ((0.05 -0.25 0.01) (0.90 0.25 0.38));
9          outputDir     "../subset-case";
10         fields        (U p nut);
11
12         writeFormat    deltaVarint;
13
14         // Enable encryption with public key
15         publicKey      "fqzYQ0U8j27tFEr5WzEMlbvXYP+9CAyk0JhwwZ2rgw=";
16
17         writeControl    timeStep;
18         writeInterval   1;
19     }
20 }
```

Listing 4: Encrypted extraction configuration

Encrypted files have the `.enc` extension (e.g., `U.dvz.enc` for compressed and encrypted data).

2.4 Decryption During Case Initialization

When running `spaceTimeWindowInitCase` on encrypted data, you will be prompted for the private key:

```

1 cd subset-case
2 spaceTimeWindowInitCase -sourceCase ../source-case
3 # Enter private key (base64): [input not echoed]
```

Listing 5: Decrypting boundary data

The utility automatically:

1. Derives the public key from the private key
2. Decrypts all `.enc` files in `boundaryData`
3. Removes encrypted files after successful decryption

2.5 Security Properties

- **Sealed box encryption:** Anonymous sender, only recipient can decrypt
- **X25519 key exchange:** 128-bit security level
- **XSalsa20-Poly1305:** Authenticated encryption
- **No plaintext on disk:** Encryption occurs before writing

2.5.1 Cryptographic Foundations

The encryption uses elliptic curve Diffie-Hellman on Curve25519. Key generation produces a private scalar s and public point (eq. (1)):

$$P_{\text{pub}} = s \cdot G \quad (1)$$

where G is the curve's base point. The discrete logarithm problem makes recovering s from P_{pub} computationally infeasible.

Sealed Box Construction For each encryption, a sealed box generates an ephemeral keypair $(e, e \cdot G)$ and computes a shared secret:

$$K = \text{BLAKE2b}(e \cdot P_{\text{recv}}) = \text{BLAKE2b}(e \cdot s_{\text{recv}} \cdot G) \quad (2)$$

The ciphertext is constructed as shown in eq. (3):

$$C = (e \cdot G) \| \text{XSalsa20-Poly1305}_K(M) \quad (3)$$

where M is the plaintext boundary data and $\|$ denotes concatenation. The ephemeral public key $(e \cdot G)$ is prepended to allow decryption.

Decryption The recipient computes the same shared secret using their private key (eq. (4)):

$$K = \text{BLAKE2b}(s_{\text{recv}} \cdot (e \cdot G)) \quad (4)$$

By the associativity of scalar multiplication on elliptic curves (eq. (5)):

$$s_{\text{recv}} \cdot (e \cdot G) = e \cdot (s_{\text{recv}} \cdot G) = e \cdot P_{\text{recv}} \quad (5)$$

This ensures both parties derive the same key K without ever transmitting it.

Security Level X25519 provides approximately 128 bits of security. Breaking the encryption requires either:

- Solving the elliptic curve discrete logarithm problem (ECDLP): $O(2^{128})$ operations
- Brute-forcing the symmetric key: $O(2^{256})$ operations for XSalsa20

2.6 Ethical Considerations and HPC Transparency

Most high-performance computing (HPC) centers require full transparency regarding the simulations performed on their infrastructure. For this reason, **encryption support is an optional compile-time feature** controlled by the `FOAM_USE_SODIUM` flag. Centers may choose not to enable this functionality.

It is important to understand what encryption does and does not protect:

- **What is protected:** The time-varying boundary field data in `constant/boundaryData`. When downloaded, this data is sealed and cannot be read without the private key.
- **What is NOT protected:** The test case setup (mesh, dictionaries, initial conditions) remains unencrypted. Anyone can re-run the global simulation to regenerate the boundary data—encryption does not prevent this.

The practical security model relies on the following observations:

1. Re-running the global simulation to obtain internal fields is **computationally expensive** and requires HPC resources. Such jobs are recorded in the scheduler logs, providing an audit trail.
2. Offline recalculation on a personal workstation is typically infeasible due to computational cost.
3. If file permissions on HPC scratch directories are misconfigured and the user chooses not to write timestep data from the global simulation, other users can only copy the unencrypted test case setup—not the valuable boundary data.

i Note

The encryption feature is designed for protecting intellectual property during data distribution, not for hiding simulations from HPC administrators. Always comply with your computing center's acceptable use policies.

2.7 Protection Against Malware and Ransomware

The spaceTimeWindow approach offers an additional security benefit: by storing only the minimal data required for reconstruction, the valuable simulation results can be protected against malware and ransomware attacks.

2.7.1 Secure Archival Strategy

The reconstruction case contains only:

- The subset mesh (`constant/polyMesh`)
- Encrypted boundary data (`constant/boundaryData/*.enc`)
- Initial fields for one timestep
- Configuration dictionaries

This minimal dataset (typically a few gigabytes) can be stored on:

- **Write-Once Read-Many (WORM) media:** Optical discs (M-DISC), tape archives with WORM capability, or cloud storage with object lock/immutability settings (AWS S3 Object Lock, Azure Immutable Blob Storage).
- **Secure vaults:** Hardware-encrypted drives kept offline, or institutional secure storage with access controls and audit logging.
- **Air-gapped backups:** Disconnected storage that cannot be reached by network-based malware.

2.7.2 Security Model

1. **Encrypted boundary data is immutable:** Once written to WORM storage, the encrypted files cannot be modified or deleted by malware.
2. **Private key stored separately:** The decryption key resides on a hardware token or secure password manager, not on the same system as the data.
3. **Reconstruction is always possible:** Even if the HPC system or workstation is compromised, the archived data remains intact and can be decrypted on a clean system.
4. **Minimal attack surface:** The small archive size makes backup and verification practical, unlike terabyte-scale full simulation outputs.

 Tip

For critical simulations, archive the encrypted reconstruction case to WORM storage immediately after extraction completes. The full simulation data can then be deleted from HPC scratch space, eliminating the risk of data loss from ransomware or accidental deletion.

3 Boundary Condition Approaches

The library provides two approaches for applying boundary conditions on the extraction boundary (`oldInternalFaces`):

3.1 Inlet-Outlet BC (-inletOutletBC) – Recommended for Unsteady Flows

Uses `spaceTimeWindowInletOutlet BC` which applies:

- **Velocity (U):** Flux-based switching – Dirichlet (prescribed value) at inflow faces, zero-Gradient at outflow faces
- **All scalar fields (p, nut, k, epsilon, omega):** zeroGradient

This approach is **physically correct** for unsteady turbulent flows because:

- Turbulent flows have instantaneous velocity fluctuations that can reverse direction locally
- Vortex shedding, recirculation zones, and turbulent eddies cause portions of the boundary to alternate between inflow and outflow

- Prescribing fixed values at outflow faces is non-physical (information should leave the domain freely)
- The flux-based switching automatically adapts to the instantaneous flow direction at each face

```
1 spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
```

Listing 6: Using inlet-outlet BC

3.2 Fixed Outlet Direction (-outletDirection)

Creates a separate outlet patch from faces at one edge of the extraction box:

- **oldInternalFaces:** Pure Dirichlet BC (spaceTimeWindow) on all remaining faces
- **outlet:** Pressure relief patch with `inletOutlet` for U and `zeroGradient` for p

Use when the mean flow direction is well-defined and outflow always occurs at a known location.

```
1 spaceTimeWindowInitCase -sourceCase ../source-case -outletDirection "(1 0 0)"
```

Listing 7: Using fixed outlet direction

⚠ Warning

These options are mutually exclusive. Using both `-inletOutletBC` and `-outletDirection` together produces an error with guidance.

3.3 Boundary Condition Assignment Logic

For each field in the initial time directory, `spaceTimeWindowInitCase` assigns BCs according to Table 1.

Table 1: Boundary condition assignment logic

In boundaryData?	-inletOutletBC?	Field Type	BC Applied
Yes	Yes	vector (U)	<code>spaceTimeWindowInletOutlet</code>
Yes	Yes	scalar	<code>zeroGradient</code>
Yes	No	any	<code>spaceTimeWindow</code> (Dirichlet)
No	any	any	<code>zeroGradient</code>

This ensures fields without time-varying data automatically get appropriate BCs.

4 Workflow Overview

The space-time window reconstruction workflow is strictly sequential, as shown in fig. 1.

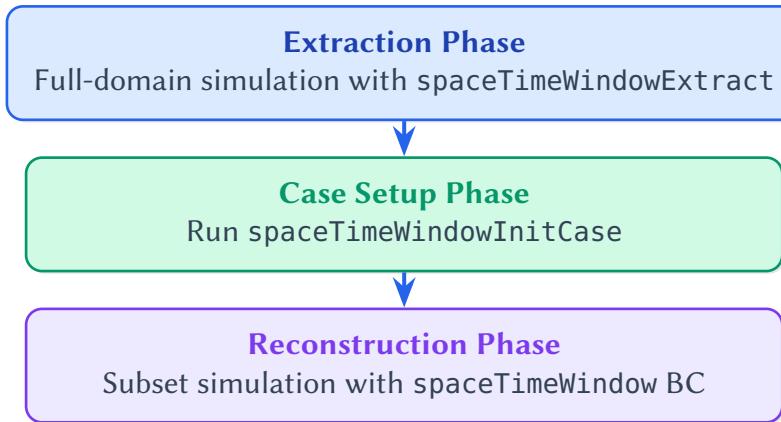


Figure 1: Space-time window reconstruction workflow

4.1 Serial Workflow

```

1 # 1. Run extraction during simulation
2 cd source-case
3 pimpleFoam # With spaceTimeWindowExtract function object
4
5 # 2. Initialize reconstruction case (recommended: inlet-outlet BC)
6 cd ../subset-case
7 spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
8
9 # 3. Run reconstruction
10 pimpleFoam
  
```

Listing 8: Complete serial workflow

In serial mode:

- Mesh and initial fields are written directly to the output directory
- Boundary data is written at every timestep
- The extractor forces field writes at t_1 and t_2 (for interpolation buffers)

i Note

In serial mode, the extractor writes internal fields only at t_0 (extraction start). The t_1 and t_2 internal fields are **not** automatically saved. If you need linear interpolation starting at t_1 , ensure your `writeInterval` captures t_1 , or use parallel mode which forces writes at t_0 , t_1 , and t_2 .

4.2 Parallel Workflow

1. Run the original simulation in parallel with extraction enabled
2. Run `reconstructPar` for the desired start timestep (t_2 for cubic interpolation)
3. Run `spaceTimeWindowInitCase -sourceCase <path> -inletOutletBC`
4. Run the solver on the subset case (serial or parallel)

```

1 # Step 1: Run parallel extraction
2 cd source-case
3 mpirun -np 4 pimpleFoam -parallel
4 # Extraction automatically forces writes at t_0, t_1, t_2
5
6 # Step 2: Reconstruct fields at cubic-safe start time (t_2)
7 reconstructPar -time 0.0002
8
9 # Step 3: Initialize subset case (recommended: inlet-outlet BC)
10 cd ../subset-case
11 spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
12
13 # Step 4: Run reconstruction
14 pimpleFoam

```

Listing 9: Complete parallel workflow

In parallel mode:

- Boundary data from all processors is gathered to master and written as single files
- The extractor forces field writes at t_0 , t_1 , and t_2 for interpolation buffers (t_0 only in parallel)
- Only extraction box parameters are written (not mesh) — `spaceTimeWindowInitCase` creates the mesh
- `reconstructPar` must be run at the reconstruction start time (t_2) to provide source fields

5 Configuration Reference

5.1 Extraction Configuration

The extraction function object is configured in `system/controlDict` within the `functions` sub-dictionary. The available parameters are listed in table 2.

```

1 functions
2 {
3     extractSubset
4     {
5         type          spaceTimeWindowExtract;
6         libs          (spaceTimeWindow);
7
8         // Bounding box: ((minX minY minZ) (maxX maxY maxZ))
9         // Must be fully internal to domain
10        box           ((0.05 -0.25 0.01) (0.90 0.25 0.38));
11
12        outputDir      "../subset-case";
13
14        // Fields for time-varying boundary data (written every timestep)
15        fields         (U);           // Typically just velocity
16

```

```

17   // Fields for initial conditions (optional, defaults to 'fields')
18   initialFields  (Upнут);           // More fields for IC
19
20   // Write format: ascii, binary, deltaVarint, or dvzt
21   writeFormat    dvzt;             // Recommended: best compression
22
23   // Precision for deltaVarint/dvzt (default: 6)
24   deltaVarintPrecision 6;
25
26   // Keyframe interval for dvzt (default: 20)
27   dvztKeyframeInterval 20;
28
29   // Gzip compression (ignored for deltaVarint/dvzt)
30   writeCompression off;
31
32   // Optional encryption
33   // publicKey      "base64-encoded-public-key";
34
35   // Time window (optional)
36   // timeStart      0.0;
37   // timeEnd        1.0;
38
39   writeControl    timeStep;
40   writeInterval   1;
41 }
42 }
```

Listing 10: Complete extraction configuration**Table 2:** Extraction parameters

Parameter	Type	Required	Description
box	pointPair	Yes	Extraction bounding box
outputDir	fileName	Yes	Output case directory
fields	wordList	Yes	Fields for time-varying BC (boundary-Data)
initialFields	wordList	No	Fields for initial conditions (default: same as fields)
writeFormat	word	No	ascii, binary, deltaVarint, or dvzt
deltaVarintPrecision	label	No	Decimal digits (default: 6)
dvztKeyframeInterval	label	No	Keyframe interval for dvzt (default: 20)
writeCompression	switch	No	Gzip compression (ignored for deltaVarint/dvzt)
publicKey	string	No	Base64 public key for encryption
timeStart	scalar	No	Extraction start time
timeEnd	scalar	No	Extraction end time

5.2 Initial Fields vs Boundary Data Fields

The extraction can separate which fields are used for:

- **Initial conditions (initialFields):** Fields written to the start time directory for solver initialization
- **Time-varying boundary data (fields):** Fields written to boundaryData/ for time-varying BCs

This allows extracting more fields for initial conditions (e.g., `U p nut k omega`) while only storing time-varying data for velocity:

```

1 // In extraction function object
2 fields          (U);           // Only U for time-varying BC (saves
3               storage)
4 initialFields  (U p nut);    // More fields for initial conditions

```

Listing 11: Field selection strategy

Fields NOT in boundaryData automatically get zeroGradient BC on oldInternalFaces.

✓ Tip

For unsteady turbulent flows with `-inletOutletBC`, the recommended approach is to extract only velocity (`U`) for boundary data while including all turbulence fields for initial conditions. This works because pressure and turbulence quantities use zeroGradient (no BC data needed), reducing storage by approximately 66%.

5.3 Boundary Condition Configuration

5.3.1 spaceTimeWindowInletOutlet (Recommended)

Flux-based boundary condition that reads pre-computed velocity values and applies them only at inflow faces. The parameters are listed in table 3.

```

1 boundaryField
2 {
3     oldInternalFaces
4     {
5         type                  spaceTimeWindowInletOutlet;
6         dataDir              "constant/boundaryData";
7         phi                  phi;           // Flux field name
8         allowTimeInterpolation true;
9         timeInterpolationScheme cubic;        // or "linear" or "none"
10        value                uniform (0 0 0);
11    }
12 }

```

Listing 12: spaceTimeWindowInletOutlet configuration

How it works:

1. At each timestep, reads velocity values from boundaryData (with optional time interpolation)
2. Computes flux through each face: $\phi_f = \mathbf{U}_f \cdot \mathbf{S}_f$

3. For inflow faces ($\phi < 0$): applies prescribed velocity from boundaryData
4. For outflow faces ($\phi \geq 0$): applies zeroGradient (extrapolates from interior)

Table 3: spaceTimeWindowInletOutlet parameters

Parameter	Type	Default	Description
dataDir	fileName	constant/boundaryData	Path to boundary data
phi	word	phi	Name of flux field
allowTimeInterpolation	bool	false	Permit interpolation for missing timesteps
timeInterpolationScheme	word	linear	none, linear, or cubic

5.3.2 spaceTimeWindow (Pure Dirichlet)

Pure Dirichlet boundary condition that prescribes values on all faces regardless of flow direction. The parameters are listed in table 4.

```

1  boundaryField
2  {
3      oldInternalFaces
4      {
5          type                  spaceTimeWindow;
6          dataDir              "constant/boundaryData";
7          fixesValue           true;           // Tells adjustPhi these values
8          are fixed
9          allowTimeInterpolation  true;
10         timeInterpolationScheme  cubic;
11         reportFlux            true;
12         value                 uniform (0 0 0);
13     }
14 }
```

Listing 13: spaceTimeWindow configuration

Use this for:

- Scalar fields when not using -inletOutletBC
- Situations where fixed values are explicitly desired on all faces

5.4 Case Initialization Options

The spaceTimeWindowInitCase utility accepts command-line options (see table 5):

```

1  # Recommended: inlet-outlet BC for unsteady turbulent flows
2  spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
3
4  # Alternative: fixed outlet direction for steady-mean flows
5  spaceTimeWindowInitCase -sourceCase ../source-case -outletDirection "(1 0 0)"
```

Table 4: spaceTimeWindow parameters

Parameter	Type	Default	Description
dataDir	fileName	constant/boundaryData	Path to boundary data
fixesValue	bool	true	Report to <code>adjustPhi</code> that values are fixed
allowTimeInterpolation	bool	false	Enable time interpolation
timeInterpolationScheme	word	linear	none, linear, or cubic
reportFlux	bool	false	Print net flux through patch (velocity only)
setAverage	bool	false	Adjust field average
offset	Type	Zero	Offset value

```

6
7 # With mass flux correction (optional, ensures exact mass conservation)
8 spaceTimeWindowInitCase -sourceCase ../source-case -inletOutletBC
   -correctMassFlux

```

Listing 14: spaceTimeWindowInitCase usage**Table 5:** spaceTimeWindowInitCase options

Option	Type	Description
-sourceCase	directory	Source case where extraction ran (required)
-extractDir	directory	Directory with extracted data (default: cwd)
-inletOutletBC	flag	Recommended. Use flux-based inlet-outlet BC for U, zero-Gradient for scalars
-outletDirection	vector	Create fixed outlet patch in given direction (e.g., "(1 0 0)")
-outletFraction	scalar	Fraction of box extent for outlet region (default: 0.1)
-correctMassFlux	flag	Apply least-squares mass flux correction to boundaryData
-initialFields	list	Override initial fields list (e.g., "(U p nut k)")
-refineLevel	label	Refine mesh N times (spatial interpolation at runtime)
-coarsenLevel	label	Coarsen mesh N times (spatial interpolation at runtime)
-overwrite	flag	Overwrite existing files

 **Warning**

-inletOutletBC and -outletDirection are mutually exclusive. Using both together produces an error with guidance on which option to choose.

5.5 Mesh Coarsening and Refinement

The reconstruction mesh can be coarsened or refined relative to the extraction mesh (table 6). This enables running reconstructions at different resolutions than the original simulation.

```

1 # Refine mesh (finer than extraction)
2 spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -refineLevel 1
3
4 # Coarsen mesh (coarser than extraction)
5 spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -coarsenLevel 1
6
7 # Multiple levels
8 spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -refineLevel 2

```

Listing 15: Mesh resolution options**Table 6:** Mesh resolution options

Option	Type	Description
-refineLevel	label	Refine mesh N times (each level splits cells $\times 8$)
-coarsenLevel	label	Coarsen mesh N times (each level merges cells)

 **Warning**

-refineLevel and -coarsenLevel are mutually exclusive. Use only one at a time.

5.5.1 Spatial Interpolation Algorithms

When the reconstruction mesh differs from the extraction mesh, spatial interpolation is required for boundary data. The spaceTimeWindow boundary conditions handle this automatically at runtime using different algorithms depending on the resolution change.

Refinement: Barycentric Interpolation with 2D Delaunay Triangulation When the target mesh has more faces than the source (refinement), the algorithm triangulates source face centers using the Bowyer-Watson algorithm, as illustrated in fig. 2. For each target face center, the enclosing triangle is found and barycentric weights are computed. If the target point lies outside all triangles (which can happen because the extracted submesh uses original cells from the source case and may have irregular boundaries), the algorithm finds the nearest triangle by centroid distance and uses clamped barycentric coordinates. This provides smooth C^0 continuous interpolation.

Given a target point \mathbf{p} inside a triangle with vertices $\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$, the barycentric coordinates $(\lambda_1, \lambda_2, \lambda_3)$ satisfy eq. (6):

$$\mathbf{p} = \lambda_1 \mathbf{v}_1 + \lambda_2 \mathbf{v}_2 + \lambda_3 \mathbf{v}_3, \quad \text{where } \lambda_1 + \lambda_2 + \lambda_3 = 1 \quad (6)$$

The weights are computed from signed triangle areas (eq. (7)):

$$\lambda_1 = \frac{A(\mathbf{p}, \mathbf{v}_2, \mathbf{v}_3)}{A(\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3)}, \quad \lambda_2 = \frac{A(\mathbf{v}_1, \mathbf{p}, \mathbf{v}_3)}{A(\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3)}, \quad \lambda_3 = \frac{A(\mathbf{v}_1, \mathbf{v}_2, \mathbf{p})}{A(\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3)} \quad (7)$$

where the signed area of a 2D triangle is given by eq. (8):

$$A(\mathbf{a}, \mathbf{b}, \mathbf{c}) = \frac{1}{2} [(b_x - a_x)(c_y - a_y) - (c_x - a_x)(b_y - a_y)] \quad (8)$$

The interpolated field value at the target point is then (eq. (9)):

$$\phi(\mathbf{p}) = \lambda_1 \phi_1 + \lambda_2 \phi_2 + \lambda_3 \phi_3 \quad (9)$$

Barycentric Interpolation (Refinement)

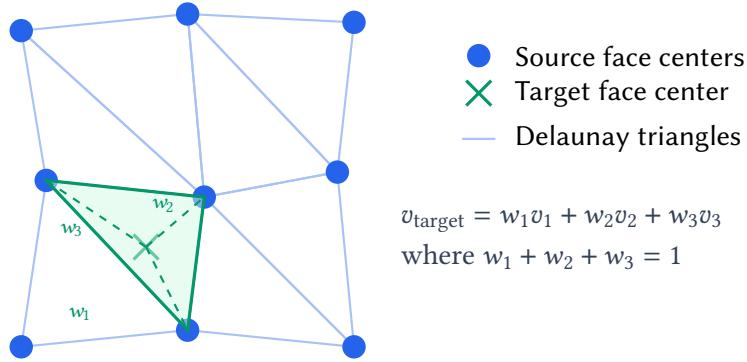


Figure 2: Barycentric interpolation for mesh refinement: source face centers (blue) are triangulated, and each target point (green) is interpolated using barycentric weights from the enclosing triangle

Coarsening: Area-Weighted Averaging When the target mesh has fewer faces than the source (coarsening), an octree is built from source points for efficient spatial lookup, as shown in fig. 3. For each target face, all source points within a search radius are found and averaged with equal weights. If no points are found, the search radius is progressively expanded. This ensures conservation of integral quantities.

For a target point \mathbf{p} with search radius r , define the set of contributing source points (eq. (10)):

$$\mathcal{S}(\mathbf{p}, r) = \{i : \|\mathbf{x}_i - \mathbf{p}\| \leq r\} \quad (10)$$

The interpolated value is the arithmetic mean of all contributing sources (eq. (11)):

$$\phi(\mathbf{p}) = \frac{1}{|\mathcal{S}|} \sum_{i \in \mathcal{S}} \phi_i \quad (11)$$

If $|\mathcal{S}| = 0$, the search radius is expanded by a factor $\alpha > 1$ (typically $\alpha = 1.5$) and the search is repeated (eq. (12)):

$$r \leftarrow \alpha \cdot r \quad \text{until} \quad |\mathcal{S}(\mathbf{p}, r)| > 0 \quad (12)$$

The octree provides $O(\log N)$ lookup complexity for finding points within the search radius, making the algorithm efficient even for large meshes.

2D Projection by Box Face The interpolation is performed on 2D point clouds, as illustrated in fig. 4. Points are grouped by which face of the extraction bounding box they belong to (6 planar surfaces: $\pm X$, $\pm Y$, $\pm Z$), then projected to 2D by dropping the constant coordinate. This exploits the box geometry while handling the irregular face distribution that arises from extracting a submesh with original cell shapes.

5.5.2 Initial Field Interpolation

Initial fields are also interpolated when mesh resolution changes (see figs. 5 and 6):

- **Refinement:** Uses `mapFields` with cell-center interpolation (fig. 5)
- **Coarsening:** Uses volume-weighted averaging of source cells (fig. 6)

Area-Weighted Averaging (Coarsening)

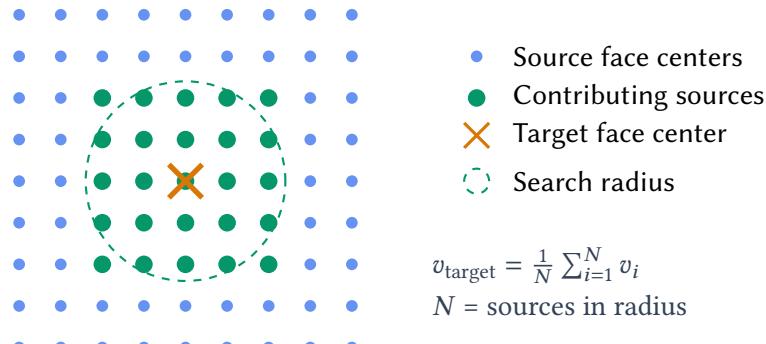


Figure 3: Area-weighted averaging for mesh coarsening: all source face centers (blue) within the search radius of each target point (orange) are averaged with equal weights

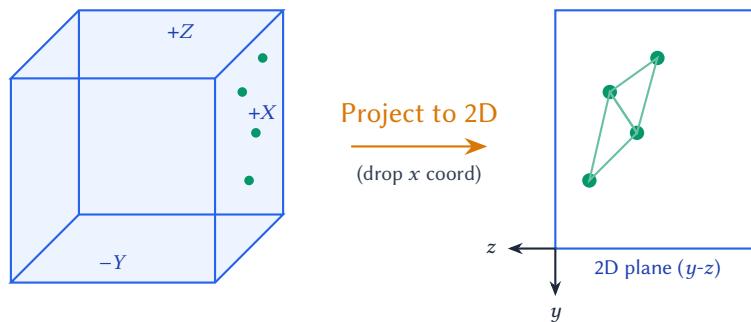


Figure 4: Points on each box face are projected to 2D for triangulation. The constant coordinate (perpendicular to the face) is dropped, enabling efficient 2D algorithms

mapFields Cell-Center Interpolation (Refinement)

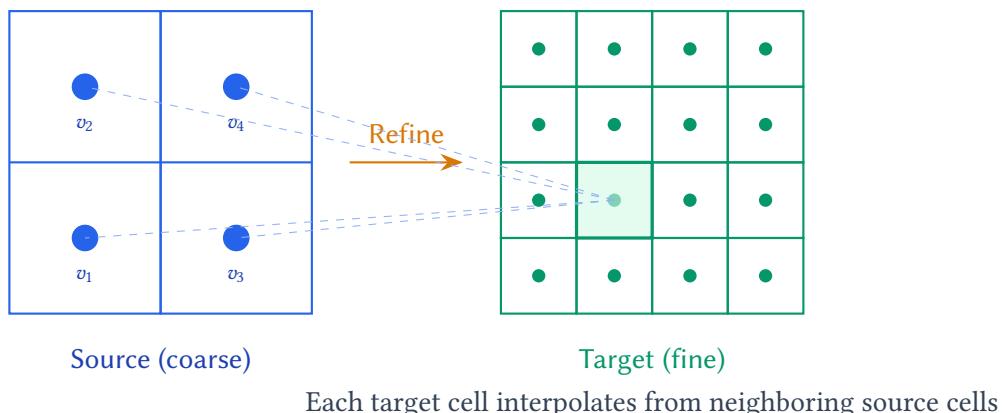


Figure 5: Initial field refinement using mapFields: target cell values are interpolated from surrounding source cell centers using distance-weighted averaging

Volume-Weighted Averaging (Coarsening)

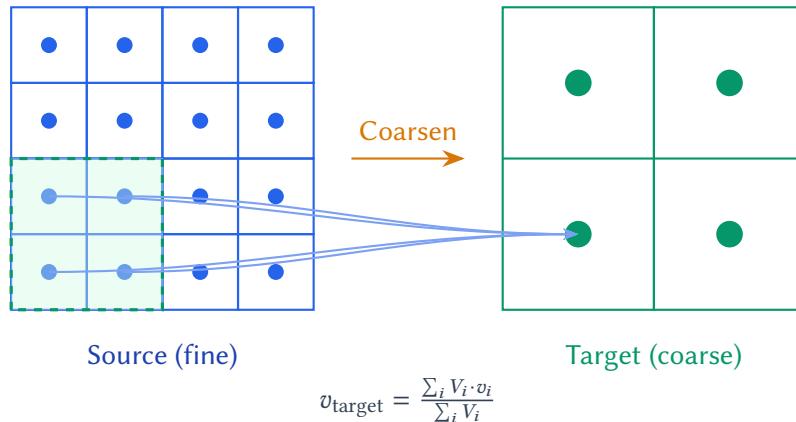


Figure 6: Initial field coarsening using volume-weighted averaging: source cell values within each target cell region are averaged weighted by their volumes

i Note

Spatial interpolation introduces smoothing, particularly for coarsening. For turbulent flows, this may affect small-scale structures. Consider the trade-off between computational cost and resolution fidelity.

What spaceTimeWindowInitCase creates:

1. system/controlDict – With matching solver, deltaT, adjustTimeStep from extraction
 - startTime set to t_2 (third timestep) for cubic interpolation buffer
 - endTime set to t_{n-2} (third-to-last) for cubic interpolation buffer
2. system/fvSchemes, system/fvSolution – Copied from source case (with pRefPoint added)
3. constant/ files – All physics properties copied (mandatory for fidelity)
4. Initial field files with appropriate BCs based on options and boundaryData availability

6 Data Storage Format

6.1 Directory Structure

The extraction creates the following directory structure:

```

1 outputDir/
2   constant/
3     polyMesh/           # Subset mesh
4       points
5       faces
6       owner
7       neighbour
  
```

```

8      boundary
9      extractionBox      # (parallel only)
10     boundaryData/
11     oldInternalFaces/
12     points            # Face centres
13     extractionMetadata # Settings and timestep list
14     0.0001/
15     U                  # or U.dvz or U.dvz.enc
16     p
17     nut
18     0.0002/
19     ...
20     0.0001/           # Initial fields (serial only)
21     U
22     p
23     nut

```

Listing 16: Extracted data structure

6.2 Boundary Data Compression

The `writeFormat` parameter controls how boundary data files are written, with compression ratios summarized in table 7.

Table 7: Compression comparison

Format	Extension	Typical Size	Notes
ASCII	(none)	100%	Human-readable
Binary	(none)	~50%	OpenFOAM native
ASCII + gzip	.gz	~10%	Compressed
Binary + gzip	.gz	~8%	Compressed
deltaVarint	.dvz	~2.7%	High compression, self-contained
dvzt	.dvzt	~2.4%	Best compression, recommended

6.2.1 Delta-Varint Codec (DVZ)

Specialized codec optimized for CFD boundary data (see figs. 7 and 8):

1. **Component-major ordering:** Groups similar values (all U_x , then U_y , then U_z)
2. **Spatial delta encoding:** Stores differences between consecutive face values within the same timestep
3. **Quantization:** Rounds to configurable precision
4. **Varint encoding:** Variable-length integer encoding
5. **Zigzag encoding:** Efficient signed integer representation

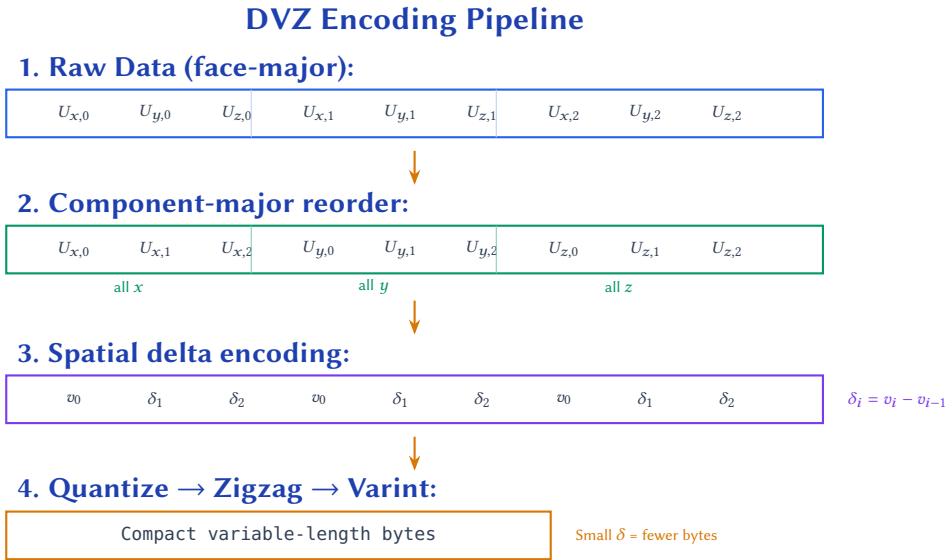


Figure 7: DVZ encoding pipeline: data is reordered by component for better locality, then delta-encoded spatially. Quantization, zigzag encoding (for signed integers), and variable-length integer encoding produce compact output

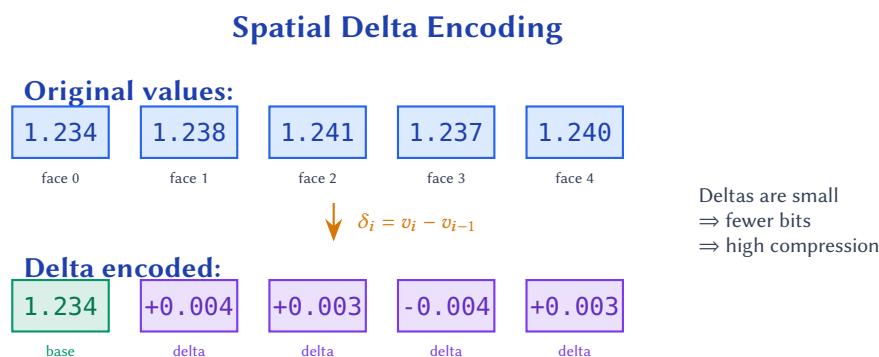


Figure 8: Spatial delta encoding: instead of storing absolute values, DVZ stores the first value and differences between consecutive faces. Smooth CFD fields have small deltas, enabling high compression

i Note

Each DVZ timestep file is completely self-contained. Delta encoding is purely spatial (between consecutive faces in a single field), not temporal. Any timestep can be read independently without access to other timesteps.

6.2.2 DVZ Mathematical Formulation

Component-Major Reordering For a vector field \mathbf{U} with N faces, the raw data layout is face-major (eq. (13)):

$$\text{Raw : } [U_{x,0}, U_{y,0}, U_{z,0}, U_{x,1}, U_{y,1}, U_{z,1}, \dots, U_{x,N-1}, U_{y,N-1}, U_{z,N-1}] \quad (13)$$

DVZ reorders to component-major for better compression (eq. (14)):

$$\text{Reordered : } \underbrace{[U_{x,0}, U_{x,1}, \dots, U_{x,N-1}]}_{\text{all } x}, \underbrace{[U_{y,0}, \dots, U_{y,N-1}]}_{\text{all } y}, \underbrace{[U_{z,0}, \dots, U_{z,N-1}]}_{\text{all } z} \quad (14)$$

Spatial Delta Encoding For each component sequence $\{v_0, v_1, \dots, v_{N-1}\}$, store deltas as shown in eq. (15):

$$\delta_0 = v_0, \quad \delta_i = v_i - v_{i-1} \quad \text{for } i = 1, \dots, N-1 \quad (15)$$

For smooth CFD fields, consecutive face values are similar, so $|\delta_i| \ll |v_i|$.

Quantization Convert floating-point deltas to integers with configurable precision p (decimal digits) using eq. (16):

$$q_i = \text{round}(\delta_i \times 10^p) \quad (16)$$

The precision parameter controls the trade-off between compression ratio and accuracy. With $p = 6$ (default), values are accurate to $\sim 10^{-6}$ relative precision.

Zigzag Encoding Convert signed integers to unsigned for efficient varint encoding (eq. (17)):

$$z_i = \begin{cases} 2q_i & \text{if } q_i \geq 0 \\ -2q_i - 1 & \text{if } q_i < 0 \end{cases} = (q_i \ll 1) \oplus (q_i \gg 31) \quad (17)$$

This maps small-magnitude signed integers to small unsigned integers: $0 \mapsto 0$, $-1 \mapsto 1$, $1 \mapsto 2$, $-2 \mapsto 3$, etc.

Variable-Length Integer Encoding Encode unsigned integers using 7 bits per byte, with the high bit indicating continuation (eq. (18)):

$$\text{bytes}(z) = \left\lceil \frac{\lfloor \log_2(z) \rfloor + 1}{7} \right\rceil \quad (18)$$

Small values ($z < 128$) use 1 byte; larger values use more bytes. Since smooth CFD fields produce small deltas, most values compress to 1–2 bytes instead of 4–8 bytes for raw floats/doubles.

6.2.3 Delta-Varint-Temporal Codec (DVZT)

Enhanced codec that exploits both spatial and temporal correlation for better compression (see figs. 9 to 11):

1. **Keyframes** (every N timesteps): Self-contained, same as DVZ (fig. 9)
2. **Delta frames**: Hybrid spatial-temporal prediction (fig. 10)
 - Uses weighted prediction: $\hat{v} = 0.3 \cdot v_{\text{spatial}} + 0.7 \cdot v_{\text{temporal}}$
 - Encodes residuals (actual - predicted) instead of raw spatial deltas
 - Typically ~10% smaller than DVZ for delta frames

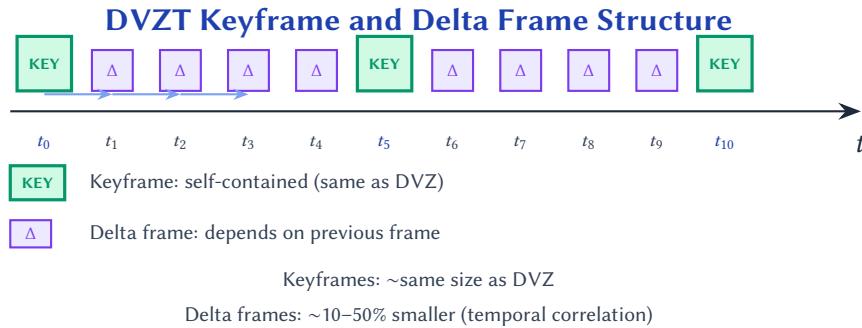


Figure 9: DVZT frame structure: keyframes are self-contained and appear every N timesteps (configurable). Delta frames between keyframes use temporal prediction for better compression

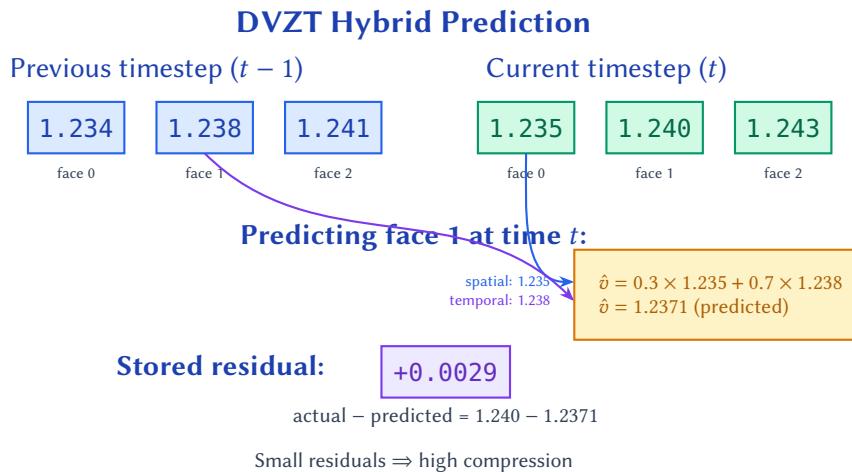


Figure 10: DVZT hybrid prediction: each value is predicted using 30% spatial neighbor (previous face at same timestep) and 70% temporal neighbor (same face at previous timestep). Only the small residual is stored

```

1 writeFormat          dvzt;
2 deltaVarintPrecision 6;           // ~1e-6 relative precision
3 dvztKeyframeInterval 20;         // Keyframe every 20 timesteps (default)

```

Listing 17: DVZT configuration

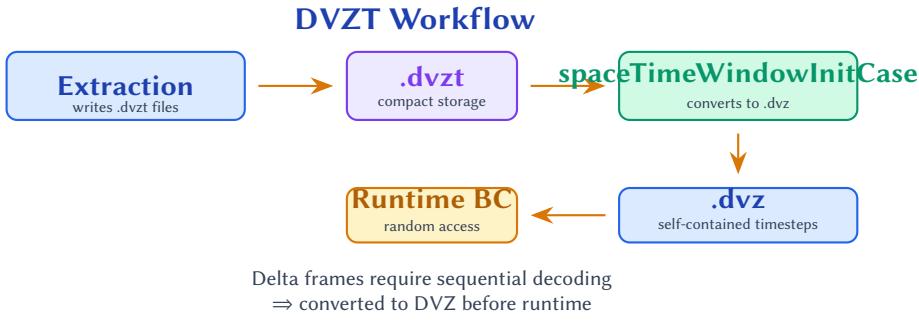


Figure 11: DVZT workflow: extraction writes compact .dvzt files. Before reconstruction, spaceTimeWindowInitCase converts them to .dvz format (required for random timestep access at runtime)

6.2.4 DVZT Mathematical Formulation

Frame Types DVZT distinguishes between keyframes and delta frames based on the timestep index k (eq. (19)):

$$\text{Frame type}(k) = \begin{cases} \text{Keyframe} & \text{if } k \bmod K = 0 \\ \text{Delta frame} & \text{otherwise} \end{cases} \quad (19)$$

where K is the keyframe interval (default $K = 20$).

Keyframe Encoding Keyframes use pure DVZ encoding (spatial delta only), as shown in eq. (20):

$$\delta_i^{(k)} = v_i^{(k)} - v_{i-1}^{(k)} \quad (\text{spatial delta}) \quad (20)$$

Delta Frame Hybrid Prediction Delta frames use a weighted combination of spatial and temporal neighbors (eq. (21)):

$$\hat{v}_i^{(k)} = \alpha \cdot v_{i-1}^{(k)} + (1 - \alpha) \cdot v_i^{(k-1)} \quad (21)$$

where $\alpha = 0.3$ (30% spatial weight, 70% temporal weight).

The residual to be encoded is given by eq. (22):

$$r_i^{(k)} = v_i^{(k)} - \hat{v}_i^{(k)} \quad (22)$$

For slowly varying flows with small Δt , consecutive timesteps are nearly identical, so $v_i^{(k)} \approx v_i^{(k-1)}$, making the temporal prediction highly accurate and $|r_i^{(k)}| \ll |v_i^{(k)} - v_{i-1}^{(k)}|$.

Compression Ratio Analysis Let σ_s^2 be the variance of spatial deltas and σ_t^2 the variance of temporal deltas. The hybrid prediction residual variance is approximately (eq. (23)):

$$\sigma_r^2 \approx \alpha^2 \sigma_s^2 + (1 - \alpha)^2 \sigma_t^2 \quad (23)$$

For small timesteps where $\sigma_t^2 \ll \sigma_s^2$ (eq. (24)):

$$\frac{\sigma_r}{\sigma_s} \approx \alpha = 0.3 \quad (24)$$

This explains the ~70% reduction in residual magnitude, which translates to significant compression improvement through varint encoding.

Decoding Dependency Delta frames depend on the previous frame for reconstruction (eq. (25)):

$$v_i^{(k)} = r_i^{(k)} + \alpha \cdot v_{i-1}^{(k)} + (1 - \alpha) \cdot v_i^{(k-1)} \quad (25)$$

This creates a dependency chain from each keyframe (eq. (26)):

$$\text{Keyframe } k_0 \rightarrow \text{Frame } k_0 + 1 \rightarrow \dots \rightarrow \text{Frame } k_0 + K - 1 \quad (26)$$

Random access requires decoding from the nearest preceding keyframe. For this reason, the initialization utility converts DVZT to DVZ before runtime.

DVZT Workflow:

During extraction, DVZT writes smaller .dvzt files. During case initialization, the utility automatically converts .dvzt to .dvz format (required because delta frames need sequential processing). The resulting .dvz files are read by the spaceTimeWindow BC at runtime.

Extraction → .dvzt files (~10% smaller) → spaceTimeWindowInitCase → .dvz files → Runtime

When to use DVZT:

- Long simulations with many timesteps (storage savings accumulate)
- Network/disk bandwidth constraints during extraction
- Small timesteps ($\Delta t = 10^{-5}$ or 10^{-6}) where temporal correlation is very strong
- DNS or acoustic simulations requiring fine temporal resolution

Compression vs Timestep Size:

DVZT benefits increase dramatically with smaller timesteps because consecutive values become nearly identical (see table 8):

Table 8: DVZT compression improvement by timestep size

Δt	Temporal Correlation	DVZT vs DVZ Savings
10^{-4}	Moderate	~10% smaller
10^{-5}	Strong	~20–30% smaller
10^{-6}	Very strong	~30–50% smaller

When to use DVZ:

- Simpler workflow (no conversion step)
- When random access to individual timesteps is needed during extraction
- Shorter simulations where DVZT overhead isn't worth it
- Large timesteps where temporal correlation is weak

Table 9: External compression results for DVZ files (13 MB original)

Method	Size	Ratio	Speed	Notes
7z lzma2 -mx9	769 KB	6.01%	11.2 MB/s	Best ratio
xz -6	769 KB	6.01%	10.2 MB/s	
zstd -ultra -22	964 KB	7.53%	4.7 MB/s	Very slow
zstd -19	965 KB	7.54%	15.3 MB/s	
rar -m5	1017 KB	7.95%	26.9 MB/s	
7z ppmd -mx9	1.4 MB	11.02%	10.7 MB/s	
zstd -9	1.7 MB	13.17%	109.5 MB/s	
zstd -3	1.8 MB	13.65%	309.0 MB/s	Best balance
zstd -1	1.9 MB	14.43%	533.7 MB/s	
bzip2 -9	2.0 MB	15.28%	13.5 MB/s	
gzip -6	2.1 MB	16.39%	94.2 MB/s	
lz4	2.3 MB	17.80%	635.2 MB/s	Fastest

Table 10: External compression results for DVZT files (30 MB original)

Method	Size	Ratio	Speed	Notes
7z lzma2 -mx9	1.9 MB	6.31%	10.1 MB/s	Best ratio
xz -6	1.9 MB	6.32%	10.5 MB/s	
zstd -ultra -22	2.6 MB	8.48%	2.4 MB/s	Very slow
zstd -19	2.6 MB	8.50%	10.4 MB/s	
rar -m5	2.8 MB	9.28%	28.0 MB/s	
zstd -9	2.8 MB	9.27%	120.6 MB/s	
7z ppmd -mx9	2.8 MB	9.37%	12.2 MB/s	
zstd -3	3.1 MB	10.10%	396.1 MB/s	Best balance
zstd -1	3.1 MB	10.25%	614.0 MB/s	
bzip2 -9	3.5 MB	11.52%	13.7 MB/s	
gzip -6	3.8 MB	12.71%	104.3 MB/s	
lz4	4.1 MB	13.56%	763.0 MB/s	Fastest

6.2.5 External Compression Benchmark

DVZ and DVZT files can be further compressed using external tools for archival or transfer. Tables 9 and 10 present benchmark results comparing various compression algorithms on real boundary data files (618 DVZ files totaling 13 MB, and 938 DVZT files totaling 30 MB).

Key findings:

- **Best compression ratio:** 7z LZMA2 and xz achieve ~6% (94% reduction)
- **Best speed/ratio balance:** zstd -3 at 10–14% ratio with 300–400 MB/s throughput
- **zstd -3 is 40× faster than xz** with only 60% more space
- **zstd –ultra -22 provides no benefit** over zstd -19 for this data type
- **bzip2 and PPMd perform poorly** for CFD boundary data

Recommendations:

- **Runtime/on-the-fly:** zstd -3 (~10% ratio, 300–400 MB/s)
- **Archive/transfer:** 7z lzma2 -mx9 or xz -6 (~6% ratio, 10 MB/s)
- **Real-time streaming:** lz4 (~14–18% ratio, 600–800 MB/s)

```

1 # Archive with best compression (7z)
2 cd subset-case/constant/boundaryData/oldInternalFaces
3 7z a -m0=lzma2 -mx=9 ./boundaryData.7z */U.dvz */U.dvzt
4
5 # Or with zstd for faster compression
6 tar -cf - */U.dvz */U.dvzt | zstd -3 > ./boundaryData.tar.zst

```

Listing 18: Archival compression example

6.3 Extraction Metadata

The extractionMetadata file contains:

```

1 {
2     openfoamVersion      "v2512";
3     openfoamApi          2512;
4     solver                "pimpleFoam";
5     deltaT               1e-04;
6     adjustTimeStep        false;
7     timePrecision         6;
8     extractionStartTime   0.0001;
9     boxMin                (0.05 -0.25 0.01);
10    boxMax                (0.90 0.25 0.38);
11    nGlobalFaces          12345;
12    timesteps              (0.0001 0.0002 0.0003 ...);
13 }

```

Listing 19: extractionMetadata contents

7 Parallel Execution

Both the source simulation (extraction phase) and the reconstruction simulation can run in parallel. This enables efficient use of HPC resources for both phases of the workflow.

7.1 Parallel Extraction

The extraction function object fully supports parallel execution:

- Extraction box can span multiple processor domains
- Boundary data is gathered from all processors
- Master processor writes combined data files
- Processor boundary faces are handled automatically

```

1 # Decompose the case
2 decomposePar
3
4 # Run parallel extraction
5 mpirun -np 8 pimpleFoam -parallel
6
7 # Automatic field writes occur at:
8 #   t_0 - extraction start (for lookback)
9 #   t_1 - linear interpolation start
10 #  t_2 - cubic interpolation start

```

Listing 20: Parallel extraction

7.2 Field Reconstruction

After parallel extraction, reconstruct fields before case initialization:

```

1 # For cubic interpolation (recommended)
2 reconstructPar -time <t_2>
3
4 # For linear interpolation
5 reconstructPar -time <t_1>

```

Listing 21: Field reconstruction

⚠ Warning

The subset mesh created by `spaceTimeWindowInitCase` uses cell ordering from the reconstructed (serial) source mesh. Running `reconstructPar` before case initialization is mandatory for parallel extractions.

7.3 Parallel Reconstruction

The reconstruction simulation can also run in parallel, independently of how the extraction was performed:

```

1 cd subset-case
2 decomposePar
3 mpirun -np 4 pimpleFoam -parallel
4 reconstructPar

```

Listing 22: Parallel reconstruction

✓ Tip

The reconstruction case is typically much smaller than the source case, so fewer processors may be needed. The spaceTimeWindow boundary conditions work identically in serial and parallel modes.

8 Mass Conservation

8.1 The Mass Imbalance Problem

Face interpolation during extraction can introduce small mass flux imbalances:

$$\text{imbalance} = \sum_f \mathbf{U}_f \cdot \mathbf{S}_f \neq 0 \quad (27)$$

When all boundary patches have `fixesValue=true`, `adjustPhi()` cannot correct this imbalance, potentially causing pressure solver issues. Additionally, with all-Dirichlet BCs, the solver has no way to relieve pressure buildup.

8.2 Solutions

8.2.1 Use `-inletOutletBC` (Recommended)

The flux-based inlet-outlet BC naturally handles mass conservation:

- Outflow faces use zeroGradient, allowing natural outflow
- No artificial mass imbalance from prescribed outflow velocities
- Works without any special mass correction

```

1 spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC

```

Listing 23: Using inlet-outlet BC for mass conservation

8.2.2 Use -correctMassFlux

Applies least-squares correction to boundaryData to ensure exact mass conservation:

$$\mathbf{U}_{\text{corrected}} = \mathbf{U} - \frac{\text{imbalance}}{\sum_f |\mathbf{S}_f|} \cdot \hat{\mathbf{n}} \quad (28)$$

where $\hat{\mathbf{n}} = \mathbf{S}_f / |\mathbf{S}_f|$ is the face unit normal.

This minimizes $\|\mathbf{U}_{\text{corrected}} - \mathbf{U}\|^2$ subject to:

$$\sum_f \mathbf{U}_{\text{corrected}} \cdot \mathbf{S}_f = 0 \quad (29)$$

```
1 spaceTimeWindowInitCase -sourceCase ../source -inletOutletBC -correctMassFlux
```

Listing 24: Using mass flux correction

8.2.3 Use -outletDirection with fixesValue true

Creates an outlet patch where mass imbalance can escape:

- oldInternalFaces uses fixesValue true (values not modified by adjustPhi)
- outlet uses inletOutlet BC (allows adjustPhi correction)

8.3 The fixesValue Option

The fixesValue parameter controls `adjustPhi()` behavior:

- `fixesValue = true`: Patch excluded from flux correction (preserves exact values)
- `fixesValue = false`: Patch included in flux correction (allows modification)

8.4 Outlet Patch for Pressure Relief

The -outletDirection option creates an outlet patch (see fig. 12):

```
1 spaceTimeWindowInitCase -sourceCase ../source \
2   -outletDirection "(1 0 0)" \
3   -outletFraction 0.1
```

Listing 25: Creating outlet patch

Outlet faces are selected based on position (furthest along the outlet direction), not face orientation.

8.5 Recommended Configurations

The recommended mass conservation strategies are summarized in table 11.

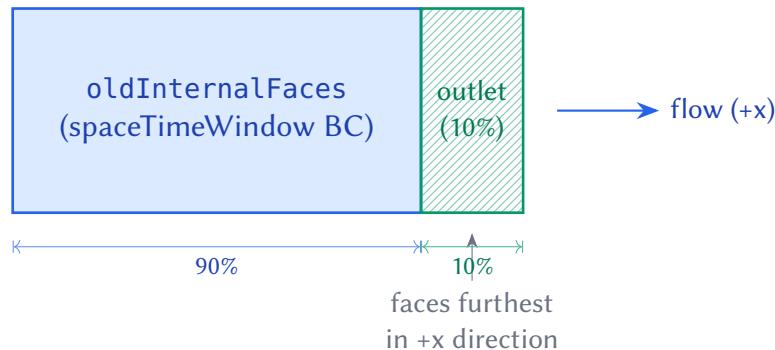


Figure 12: Outlet patch creation with `-outletDirection "(1 0 0)"`

Table 11: Mass conservation strategies

Configuration	Description
<code>-inletOutletBC</code>	Recommended for unsteady turbulent flows (vortex shedding, etc.). Natural mass balance through flux-based switching.
<code>-inletOutletBC -correctMassFlux</code>	Unsteady turbulent + extra safety. Ensures exact mass balance with inlet-outlet switching.
<code>-outletDirection "(1 0 0)"</code>	Steady-mean flow direction. Use when outlet location is known and flow direction is consistent.
<code>-correctMassFlux (no outlet)</code>	Maximum fidelity. All faces prescribed with exact mass balance.

9 Solver Settings and Relaxation

9.1 Time Stepping

For accurate reconstruction, use identical time stepping:

```

1  deltaT           1e-04;      // Must match extraction
2  adjustTimeStep  no;        // Fixed timestep recommended
3
4  // If adaptive timestep is required:
5  adjustTimeStep yes;
6  maxCo          0.5;
7  maxDeltaT      1e-03;
```

Listing 26: Recommended controlDict settings

⚠ Warning

The reconstruction must use identical `deltaT` and `adjustTimeStep` settings as the extraction. Mismatches cause fatal errors unless `allowTimeInterpolation=true`.

9.2 PIMPLE Settings

For incompressible flows:

```

1  PIMPLE
2  {
3      nOuterCorrectors    2;
4      nCorrectors         2;
5      nNonOrthogonalCorrectors 1;
6
7      // Pressure reference (set by spaceTimeWindowInitCase)
8      pRefPoint           (0.5 0 0.2);
9      pRefValue            0;
10 }
```

Listing 27: Recommended PIMPLE settings

9.3 Relaxation Factors

✓ Tip

For reconstruction simulations, relaxation is typically **not needed** because:

- Boundary conditions are prescribed (not coupled)
- Initial conditions come from the source simulation
- Flow field evolves smoothly from physical initial state

If stability issues occur, try:

```

1  relaxationFactors
2  {
3      fields
4      {
5          p           0.7;
6      }
7      equations
8      {
9          U           0.7;
10         "(k|epsilon|omega|nuTilda)"  0.7;
11     }
12 }
```

Listing 28: Optional relaxation

9.4 Linear Solver Settings

Standard settings work well:

```

1  solvers
2  {
3      p
4      {
5          solver      GAMG;
6          smoother   GaussSeidel;
7          tolerance   1e-06;
8          relTol     0.01;
9      }
10
11     U
12     {
13         solver      PBiCGStab;
14         preconditioner DILU;
15         tolerance   1e-06;
16         relTol     0.1;
17     }
18 }
```

Listing 29: Linear solver settings

10 Time Interpolation

The boundary conditions support three time interpolation modes, summarized in Table 12 and illustrated in fig. 13. The comparison between linear and cubic interpolation quality is shown in fig. 14.

`spaceTimeWindowInitCase` automatically sets `startTime` and `endTime` to ensure sufficient buffer timesteps for the selected interpolation scheme (see fig. 15 for buffer requirements).

10.1 Exact Timestep Matching (Default)

By default, the boundary condition requires exact timestep matching:

Table 12: Time interpolation modes

Mode	Start Time	Timesteps Used	Use Case
none (exact)	t_0	1 (exact match)	“Bit”-reproducible results
linear	t_1	2 (bracketing)	Simple, smoothly varying flows
cubic	t_2	4 (Catmull-Rom)	Unsteady turbulent flows (recommended)

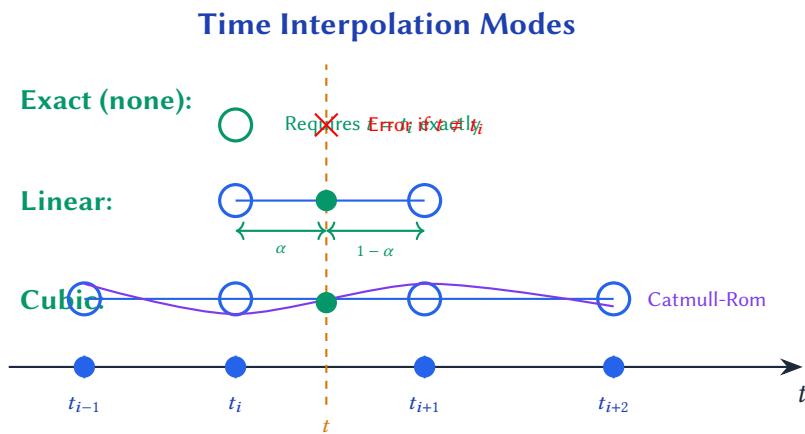


Figure 13: Time interpolation modes: exact matching uses only one timestep, linear interpolation uses two bracketing timesteps, and cubic (Catmull-Rom) uses four timesteps for smooth C^1 continuous interpolation

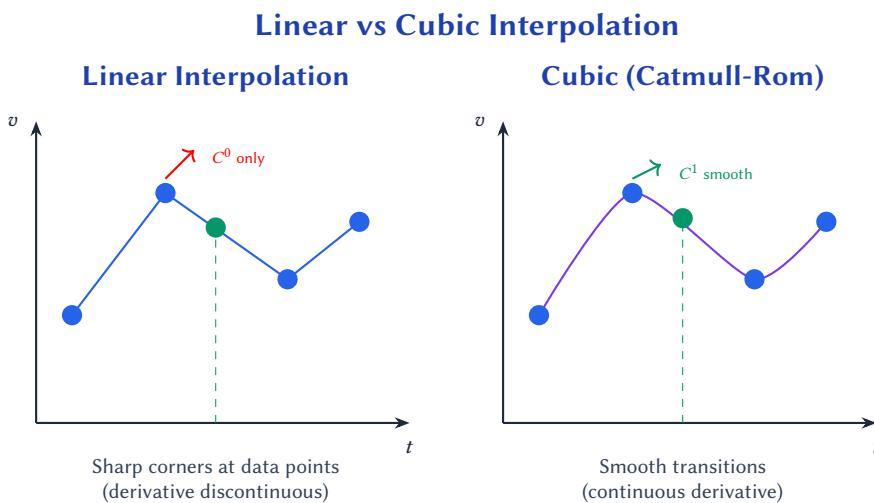


Figure 14: Comparison of linear and cubic interpolation: linear interpolation creates C^0 continuous curves with sharp corners at data points, while Catmull-Rom cubic splines provide C^1 continuity with smooth transitions

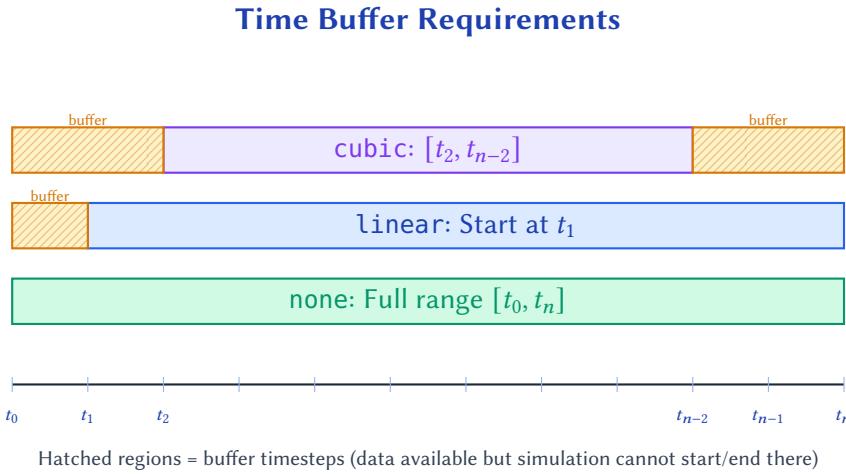


Figure 15: Time buffer requirements for each interpolation mode: exact matching can use the full range, linear needs one buffer timestep at the start, and cubic needs two buffer timesteps at both start and end

- Simulation time must match available sample times (within 1% of `deltaT`)
- Fatal error if no matching timestep found
- Ensures “bit”-reproducible results (highest fidelity)

10.2 Linear Interpolation

For cases where exact matching is not possible:

```

1 oldInternalFaces
2 {
3     type spaceTimeWindow;
4     allowTimeInterpolation true;
5     timeInterpolationScheme linear;
6     // ...
7 }
```

Listing 30: Linear interpolation

Uses two bracketing timesteps (eq. (30)):

$$\text{value} = (1 - \alpha) \cdot v_i + \alpha \cdot v_{i+1} \quad \text{where} \quad \alpha = \frac{t - t_i}{t_{i+1} - t_i} \quad (30)$$

The interpolation parameter $\alpha \in [0, 1]$ represents the normalized position between the two samples. This is equivalent to first-order polynomial interpolation (eq. (31)):

$$\phi(t) = \phi_i + \frac{\phi_{i+1} - \phi_i}{t_{i+1} - t_i} (t - t_i) \quad (31)$$

Linear interpolation provides C^0 continuity (continuous values but discontinuous derivatives at sample points).

10.3 Cubic Spline Interpolation

For smoother results with adaptive timestepping:

```

1 oldInternalFaces
2 {
3     type spaceTimeWindow;
4     allowTimeInterpolation true;
5     timeInterpolationScheme cubic;
6     // ...
7 }
```

Listing 31: Cubic interpolation

Uses centripetal Catmull-Rom spline with four timesteps ($t_{i-1}, t_i, t_{i+1}, t_{i+2}$):

- Handles non-uniform time spacing correctly
- Provides C^1 continuity
- No overshoots or cusps
- Essential for `adjustTimeStep=yes`

10.3.1 Catmull-Rom Spline Formulation

The centripetal Catmull-Rom spline passes through all control points and provides C^1 continuity. Given four consecutive sample values $\phi_0, \phi_1, \phi_2, \phi_3$ at times t_0, t_1, t_2, t_3 , the interpolated value for $t \in [t_1, t_2]$ is computed as follows.

First, compute the centripetal parameterization distances (eq. (32)):

$$d_j = |t_{j+1} - t_j|^{0.5}, \quad j = 0, 1, 2 \quad (32)$$

The normalized parameter within the segment $[t_1, t_2]$ is (eq. (33)):

$$u = \frac{t - t_1}{t_2 - t_1} \quad (33)$$

The spline is constructed using the Barry-Goldman algorithm. Define intermediate points (eq. (34)):

$$\begin{aligned} A_1 &= \frac{t_2 - t}{t_2 - t_0} \phi_0 + \frac{t - t_0}{t_2 - t_0} \phi_1 \\ A_2 &= \frac{t_2 - t}{t_2 - t_1} \phi_1 + \frac{t - t_1}{t_2 - t_1} \phi_2 \\ A_3 &= \frac{t_3 - t}{t_3 - t_1} \phi_2 + \frac{t - t_1}{t_3 - t_1} \phi_3 \end{aligned} \quad (34)$$

Then compute (eq. (35)):

$$\begin{aligned} B_1 &= \frac{t_2 - t}{t_2 - t_0} A_1 + \frac{t - t_0}{t_2 - t_0} A_2 \\ B_2 &= \frac{t_3 - t}{t_3 - t_1} A_2 + \frac{t - t_1}{t_3 - t_1} A_3 \end{aligned} \quad (35)$$

Finally, the interpolated value is (eq. (36)):

$$\phi(t) = \frac{t_2 - t}{t_2 - t_1} B_1 + \frac{t - t_1}{t_2 - t_1} B_2 \quad (36)$$

This formulation correctly handles non-uniform time spacing, which is essential when adaptive timestepping (`adjustTimeStep=yes`) produces variable timesteps.

10.4 Time Range Requirements

- **Linear**: Needs 2 buffer timesteps at start
- **Cubic**: Needs 2 buffer timesteps at start and end
- `spaceTimeWindowInitCase` automatically sets appropriate `startTime` and `endTime`

i Note

Extrapolation outside the extraction window is **never** allowed, regardless of interpolation settings.

11 Flux Reporting and Diagnostics

Enable flux reporting to monitor mass conservation:

```

1 oldInternalFaces
2 {
3     type          spaceTimeWindow;
4     reportFlux   true;
5     // ...
6 }
```

Listing 32: Enabling flux reporting

Output format (fields explained in table 13):

```

1 spaceTimeWindow flux [oldInternalFaces] t=0.001 thisPatch=1.234e-06 (in=-0.0523 out=0.0523) | MESH TOTAL=5.678e-05 (fixed=-0.0523
adjustable=0.0523) | adjustPhi will correct: -5.678e-05
```

Listing 33: Flux report output

Table 13: Flux report fields

Field	Description
thisPatch	Net flux through this spaceTimeWindow patch
in	Sum of inward fluxes
out	Sum of outward fluxes
MESH TOTAL	Total net flux across all boundary patches
fixed	Flux from patches with <code>fixesValue=true</code>
adjustable	Flux from patches with <code>fixesValue=false</code>
adjustPhi will correct	Correction to be distributed

12 Troubleshooting

12.1 Common Errors

12.1.1 Time Step Mismatch

```

1 FOAM FATAL ERROR:
2 Time step mismatch between extraction and reconstruction!
3 Extraction deltaT: 8.53e-04
4 Current deltaT: 1e-03

```

Listing 34: deltaT mismatch error**Solution:** Set deltaT in system/controlDict to match extraction.

12.1.2 No Matching Timestep

```

1 FOAM FATAL ERROR:
2 No exact timestep match found for t = 0.00015
3 Available times: 0.0001, 0.0002, 0.0003

```

Listing 35: Missing timestep error**Solution:** Enable time interpolation with allowTimeInterpolation true.

12.1.3 Pressure Solver Divergence

Symptoms: Pressure residuals increase, NaN values appear.

Solutions:

1. Use -correctMassFlux option
2. Add outlet patch with -outletDirection
3. Set fixesValue false on oldInternalFaces
4. Check pRefPoint is inside the domain

12.1.4 Encryption Errors

```

1 FOAM FATAL ERROR:
2 Failed to decrypt file: constant/boundaryData/.../U.dvz.enc

```

Listing 36: Decryption failure**Solutions:**

1. Verify private key is correct
2. Ensure library was built with FOAM_USE_SODIUM=1
3. Check file is not corrupted

13 Acknowledgments

This library implements the space-time window reconstruction method developed in [1]. The example case uses mesh generation from the ERCOFTAC Classic Collection Database [2].

A Example Case: ERCOFTAC UFR2-02 Square Cylinder

The library includes a complete example based on the ERCOFTAC UFR2-02 benchmark case [2, 3] (Case 043 in the ERCOFTAC database): turbulent flow around a square cylinder at $Re = 21,400$. This case demonstrates vortex shedding and is ideal for testing space-time window reconstruction.

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A.1 Reference Data and Validation Resources

The ERCOFTAC (European Research Community on Flow, Turbulence and Combustion) Classic Collection Database provides extensive reference data for this test case, including:

- Experimental measurements from Lyn et al. [3] (laser-Doppler velocimetry)
- Reference numerical simulations from various research groups
- Mesh generation scripts and case setup files
- Detailed flow statistics and validation data

The database is accessible at:

<http://cfd.mace.manchester.ac.uk/ercoftac/>

An OpenFOAM-specific implementation guide is available at:

https://openfoamwiki.net/index.php?title=Benchmark_ercftac_ufr2-02

i Note

If HTTPS access fails for the ERCOFTAC database, use HTTP (<http://>) instead. The ERCOFTAC server may not support secure connections.

A.2 Physical Background: Von Kármán Vortex Street

When fluid flows past a bluff body (such as a square cylinder), the flow separates at the sharp edges, creating alternating vortices that are shed from each side of the body. This phenomenon, known as the **von Kármán vortex street**, is characterized by:

- **Periodic vortex shedding:** Vortices detach alternately from upper and lower surfaces
- **Strouhal number:** $St = fD/U_\infty \approx 0.13$ for square cylinders, where f is the shedding frequency, D is the cylinder side length, and U_∞ is the freestream velocity
- **Turbulent wake:** At $Re = 21,400$, the wake is fully turbulent with complex three-dimensional structures
- **Unsteady forces:** Fluctuating lift and drag on the cylinder

The vortex street extends far downstream, making it an excellent test case for space-time window extraction—the extraction region can capture the wake dynamics while excluding the cylinder and inlet regions.

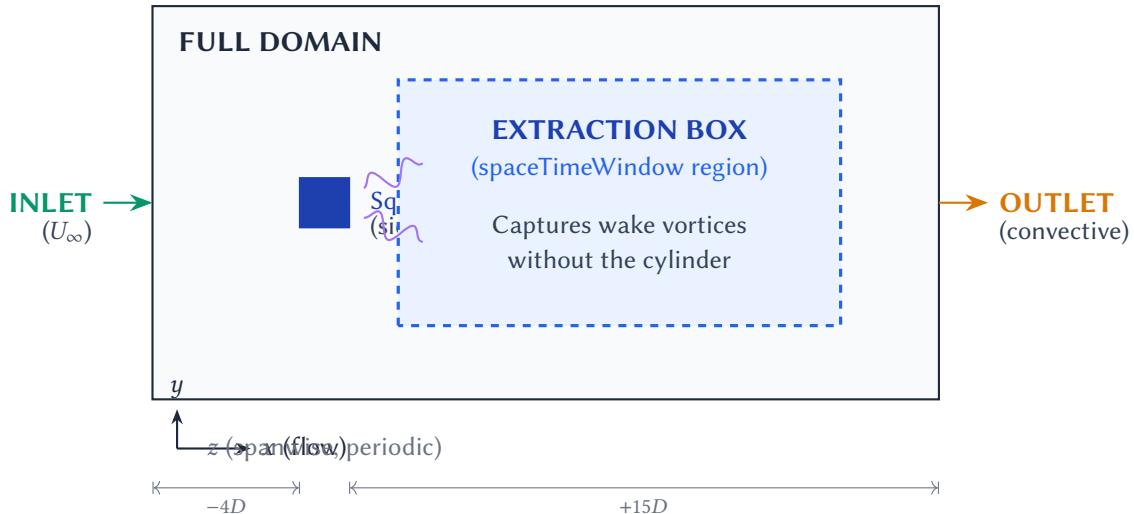


Figure 16: Computational domain for the square cylinder case showing the extraction box placement in the wake region

A.3 Domain and Mesh Configuration

The computational domain (fig. 16) extends from $-4D$ upstream to $+15D$ downstream of the cylinder, with lateral boundaries at $\pm 6.5D$. The spanwise extent is $4D$ with periodic boundary conditions.

A.4 Extraction Box Placement

The extraction box is positioned to capture the vortex street while avoiding:

- The cylinder itself (to avoid complex geometry in subset)
- The inlet region (where flow is uniform and uninteresting)
- Domain boundaries (box must be fully internal)

Example extraction configuration for this case:

```

1 extractSubset
2 {
3     type          spaceTimeWindowExtract;
4     libs          (spaceTimeWindow);
5
6     // Box starts 0.5D downstream of cylinder, extends to 9D
7     // Lateral extent captures the wake width
8     // Full spanwise extent (periodic direction)
9     box           ((0.05 -0.25 0.01) (0.90 0.25 0.38));
10
11    outputDir    ".../cylinder-subset";
12    fields        (U p nut);
13    writeFormat   deltaVarint;
14
15    writeControl  timeStep;
16    writeInterval 1;

```

17 }

Listing 37: Extraction configuration for square cylinder

A.5 Physical Parameters

The physical parameters for this case are listed in table 14.

Table 14: Square cylinder case parameters

Parameter	Value	Description
D	0.04 m	Cylinder side length
U_∞	8.25 m/s	Freestream velocity
ν	1.5×10^{-5} m ² /s	Kinematic viscosity
Re	21,400	Reynolds number
St	≈ 0.13	Strouhal number
T_{shed}	≈ 0.037 s	Vortex shedding period

A.6 Running the Example

```

1 cd examples/ufr2-02
2
3 # Generate mesh and run full simulation
4 ./Allrun
5
6 # The extraction creates ../ufr2-02-subset with:
7 #   - Subset mesh in constant/polyMesh
8 #   - Boundary data in constant/boundaryData
9 #   - Initial fields
10
11 # Initialize and run reconstruction (recommended: inlet-outlet BC)
12 cd ../ufr2-02-subset
13 spaceTimeWindowInitCase -sourceCase ../ufr2-02 -inletOutletBC
14
15 pimpleFoam
16
17 # Alternative: fixed outlet direction for steady-mean flows
18 # spaceTimeWindowInitCase -sourceCase ../ufr2-02 \
19 #   -outletDirection "(1 0 0)" \
20 #   -correctMassFlux

```

Listing 38: Running the example case

A.7 Validation

The reconstruction can be validated by comparing:

- Instantaneous velocity fields at matching timesteps
- Vortex shedding frequency (should match original)

- Mean velocity profiles in the wake
- Reynolds stress components

i Note

The reconstruction should exactly reproduce the original flow within the extraction region (to solver tolerance) when using exact timestep matching. Small differences may occur at the outlet boundary due to the different boundary condition type.

B Field Selection by Turbulence Model

When configuring the extraction, include all fields required by your turbulence model. Table 15 lists recommended fields for common models.

Table 15: Recommended fields by turbulence model

Turbulence Model	Recommended Fields
LES Smagorinsky	(U p nut)
LES dynamicKEqn	(U p nut k)
LES WALE	(U p nut)
RANS k- ε	(U p nut k epsilon)
RANS k- ω SST	(U p nut k omega)
Spalart-Allmaras	(U p nut nuTilda)

References

- [1] Alin-Adrian Anton. *Space-Time Window Reconstruction in High-Performance Numeric Simulations: Application for CFD*. PhD thesis, Universitatea Politehnica Timișoara, Timișoara, Romania, November 2011. URL <https://dspace.upt.ro/jspui/handle/123456789/643>.
- [2] ERCOFTAC. Classic collection database: Case 043 – flow around a square cylinder. <http://cfd.mace.manchester.ac.uk/ercoftac/>, 2024. Mesh generation script by Niklas Nordin.
- [3] D. A. Lyn, S. Einav, W. Rodi, and J.-H. Park. A laser-Doppler velocimetry study of ensemble-averaged characteristics of the turbulent near wake of a square cylinder. *Journal of Fluid Mechanics*, 304:285–319, 1995. doi: 10.1017/S0022112095004435.