



UDAAN



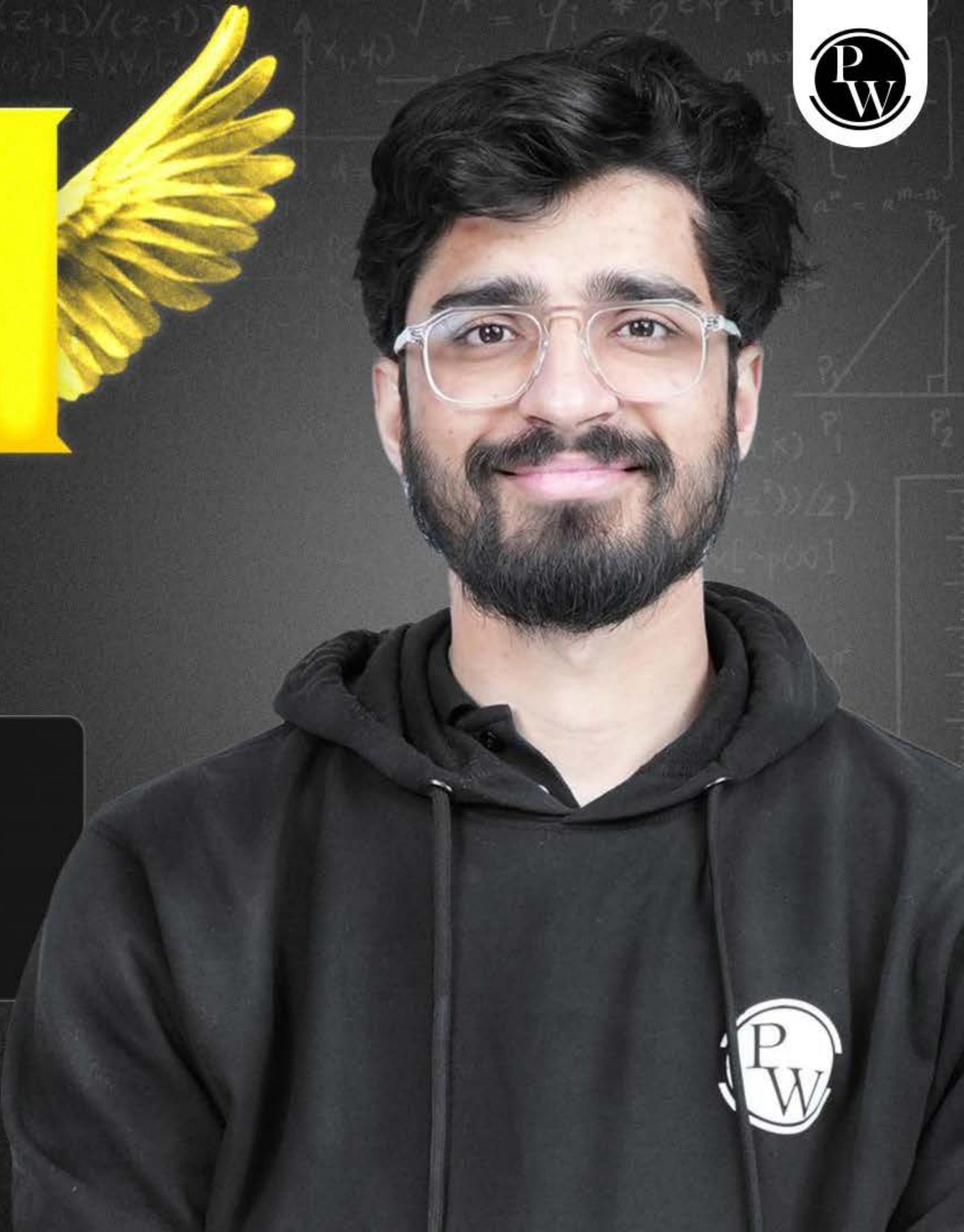
2026

Pair of Linear Equation in
Two Variables

MATHS

LECTURE-1

BY-RITIK SIR



Topics *to be covered*

- A Basics
 - B Linear Equation in one variable
 - C Linear Equation in two variable
 - D Pair of linear equation in two variable
 - E Graphical Representation
- 
- A white line-art illustration of a crown or scepter lying diagonally across the bottom of the slide.



RITIK SIR

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Linear Equation in One Variable

$a \neq 1$

$$\begin{aligned}x - 1 &= 0 \\2x + 1 &= 0 \\3x + 5 &= 0 \\-2x + 0 &= 0\end{aligned}$$

General form

$$ax + b = 0$$

$a, b \in \mathbb{R}$

$a \neq 0$

Solution

Variable x value

eqn satisfy

$$L.H.S = R.H.S$$

$$(i) x + 1 = 0$$

$$x = -1$$

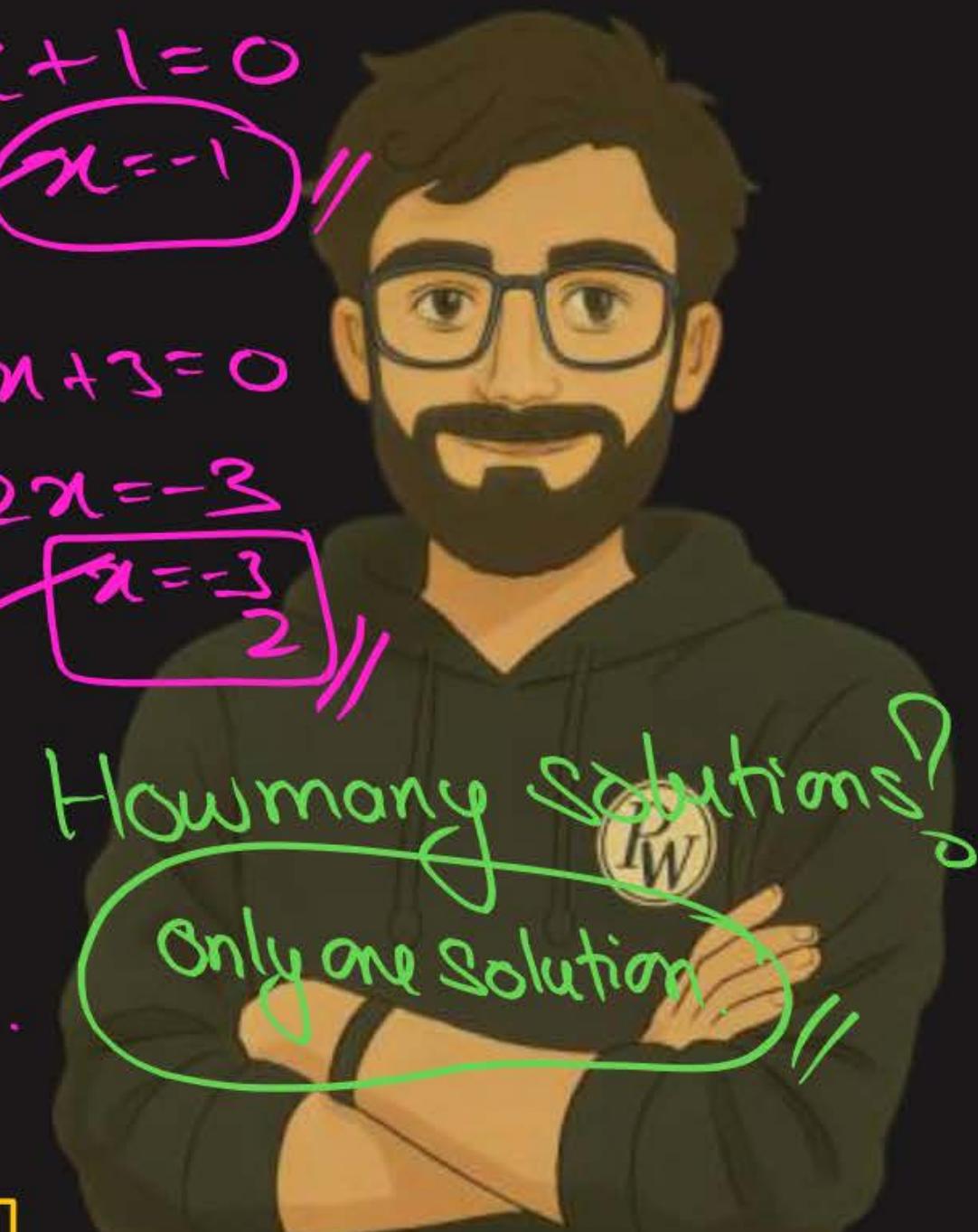
$$(ii) 2x + 3 = 0$$

$$2x = -3$$

$$x = -\frac{3}{2}$$

How many solutions?

Only one solution





Linear Equation in Two Variable



$$x + y = 1$$

$$2x - 3y + 2 = 0$$

$$5x + 4y + 3 = 0$$

$$9x - 8y + 2 = 0$$

General Form

$$ax + by + c = 0$$

$a, b, c \in \mathbb{R}$

'a' and 'b' both cannot
be zero at the same time.



Solution:

$$x + y = 2$$

- ✓ (1, 1)
- ✓ (2, 0)
- ✓ (0, 2)
- ✓ (100, -98)
- ✓ (5, -3)
- ✓ (200, -198)

How many Solutions?

Infinite

$$y = \frac{2-x}{3} \rightarrow x = ?$$

$$2x - 2\left(\frac{2-x}{3}\right) = 2$$

$$2x - 2 = 2$$

$$2x = 2 + 2$$

$$2x = 4$$

$$x = 2$$

x	0	1	2	?
y	-2	0	2	?

$$\text{② } 2x - 3y = 2 \rightarrow I$$



System.

Pair of Linear Equation in Two Variable

Solution

$$\begin{aligned}x + y + 5 &= 0 \\2x - 3y + 2 &= 0\end{aligned}$$

General form

$$\begin{aligned}a_1x + b_1y + c_1 &= 0 \\a_2x + b_2y + c_2 &= 0\end{aligned}$$

How many solutions?



#Q. Show that $x = 2, y = 1$ is a solution of the system of simultaneous linear equation:

$$3x - 2y = 4$$

$$2x + 4y = 5$$

$$a_1 = 3$$

$$b_1 = -2$$

$$c_1 = -4$$

$$a_2 = 2$$

$$b_2 = 4$$

$$c_2 = -5$$

$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

$$3(2) - 2(1) = 4$$

$$6 - 2 = 4$$

$$\boxed{4=4}$$

$$2(2) + 4(1) = 5$$

$$4 + 4 = 5$$

$$\boxed{8 \neq 5}$$

Not a solution

I

Consistent
system

II

Unique solution.

Infinite many
solution.

III

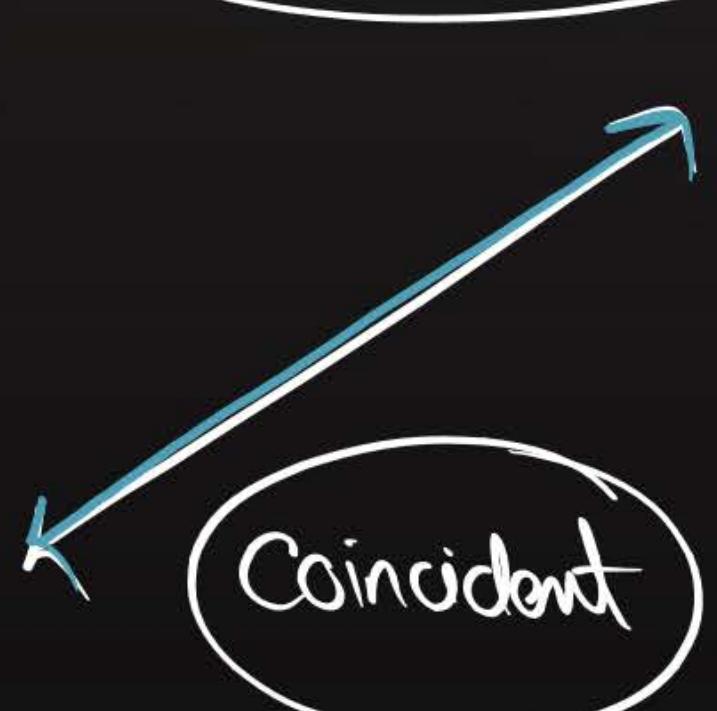
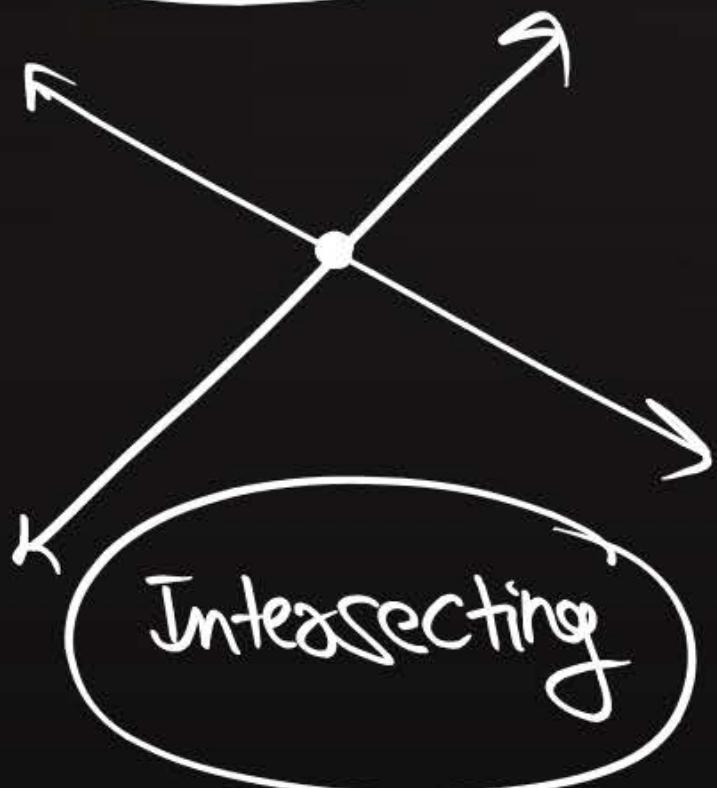
Inconsist
ent
system

No solution

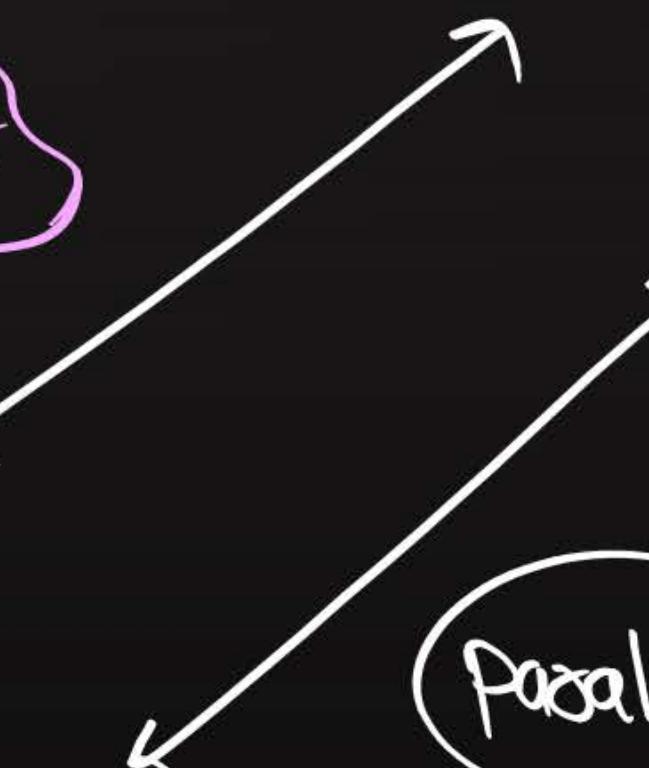
$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$



dependent



Intersecting

Coincident

Parallel

$$\text{Q: } \begin{aligned} 2x - 3y + 4 &= 0 \\ 5x + 4y - 2 &= 0 \end{aligned}$$

$$\begin{aligned} a_1 &= 2 & a_2 &= 5 \\ b_1 &= -3 & b_2 &= 4 \\ c_1 &= 4 & c_2 &= -2 \end{aligned}$$

$$\frac{2}{5} \neq \frac{-3}{4}$$

$$\frac{4}{-2}$$

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

Unique solution (Intersecting) (consistent)

$$\text{Q: } \begin{aligned} 2x + 4y + 3 &= 0 \\ 6x + 12y + 9 &= 0 \end{aligned}$$

$$\frac{2}{6}, \quad \frac{4}{12}, \quad \frac{3}{9}$$

$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

Coincident.
Infinite solution.

Consistent.
dependent.

$$Q: 2x - 4y - 9 = 0$$

$$12x - 24y - 3 = 0$$

$$\begin{array}{r} \cancel{2} \\ | \cancel{12} \\ 6 \end{array} \quad \begin{array}{r} \cancel{4} \\ | \cancel{-24} \\ 6 \end{array} \quad \begin{array}{r} \cancel{9}^3 \\ | \cancel{-3} \\ 1 \end{array}$$

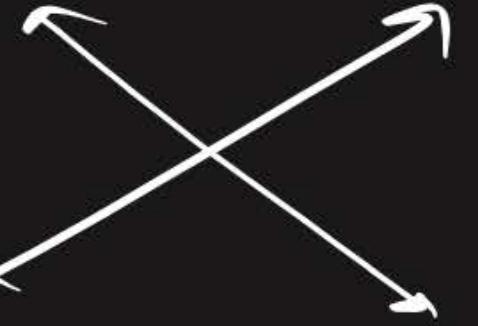
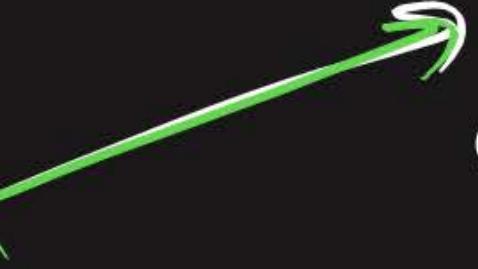
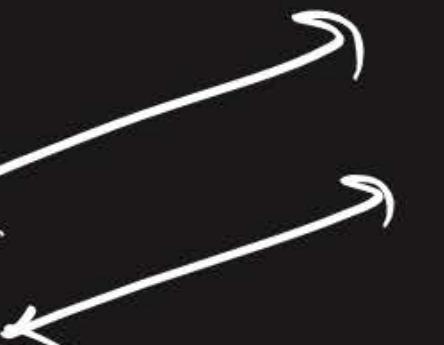
$$\frac{1}{6} \quad \frac{1}{6} \quad \frac{3}{1}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

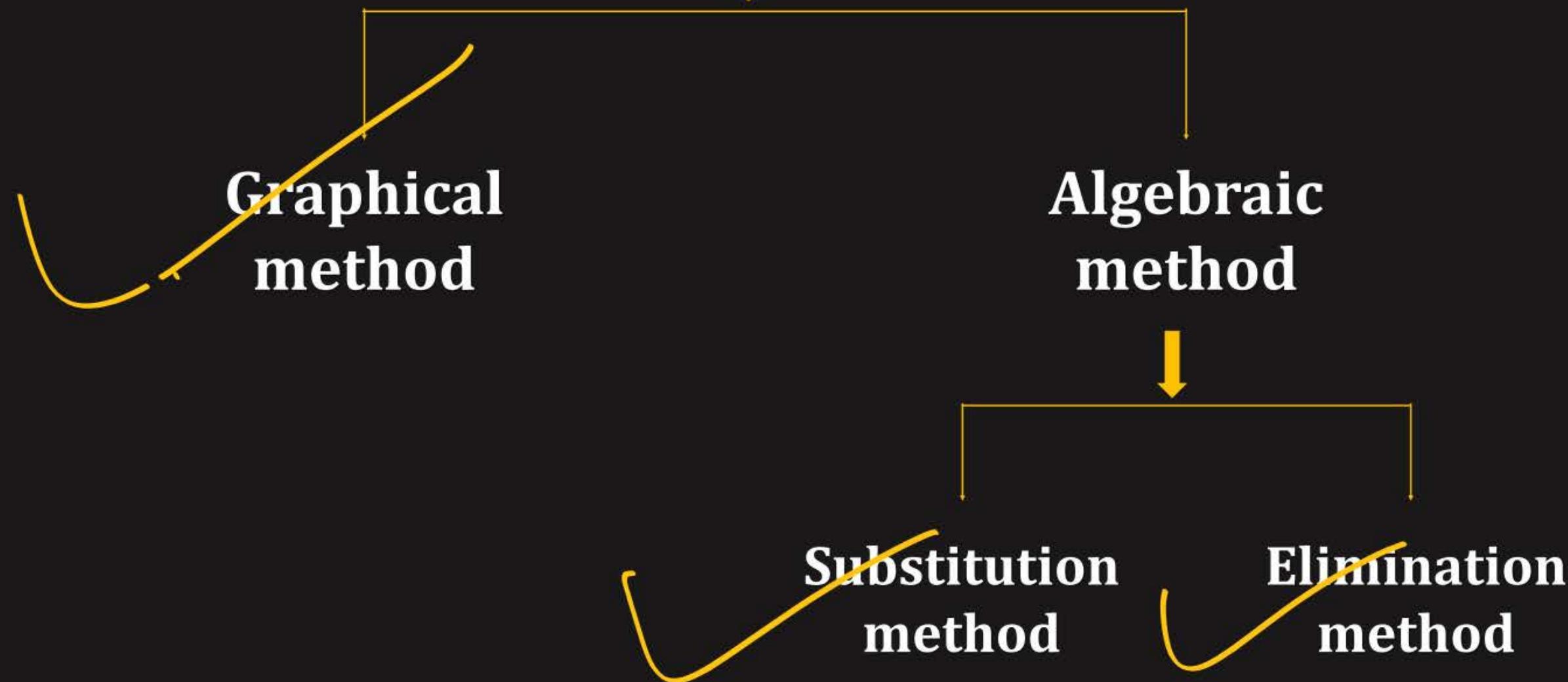
No solution.

Inconsistent.

Parallel lines.

S. No.	Pair of Lines	$\frac{a_1}{a_2}$	$\frac{b_1}{b_2}$	$\frac{c_1}{c_2}$	Compare the Ratios	Graphical representation	Algebraic Interpretation
1.	$x - 2y = 0$ $3x + 4y - 20 = 0$	$\frac{1}{3}$	$\frac{-2}{4}$	$\frac{0}{-20}$	$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$	 intersecting.	Exactly one solution consistent (Unique)
2.	$2x + 3y - 9 = 0$ $4x + 6y - 18 = 0$	$\frac{2}{4}$	$\frac{3}{6}$	$\frac{-9}{-18}$	$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$	 Coincident.	Infinitely many solutions consistent (Dependent)
3.	$x + 2y - 4 = 0$ $2x + 4y - 12 = 0$	$\frac{1}{2}$	$\frac{2}{4}$	$\frac{-4}{-12}$	$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$	 Parallel lines.	No solutions Inconsistent

How to Solve?? (Solving System of Equations)



#Q. Graphically, the pair of equations $\begin{aligned} 6x - 3y + 10 &= 0 \\ 2x - y + 9 &= 0 \end{aligned}$ represents two lines which are

A

Intersecting at exactly one point

B

Intersecting at exactly two points

C

Coincident

D

Parallel

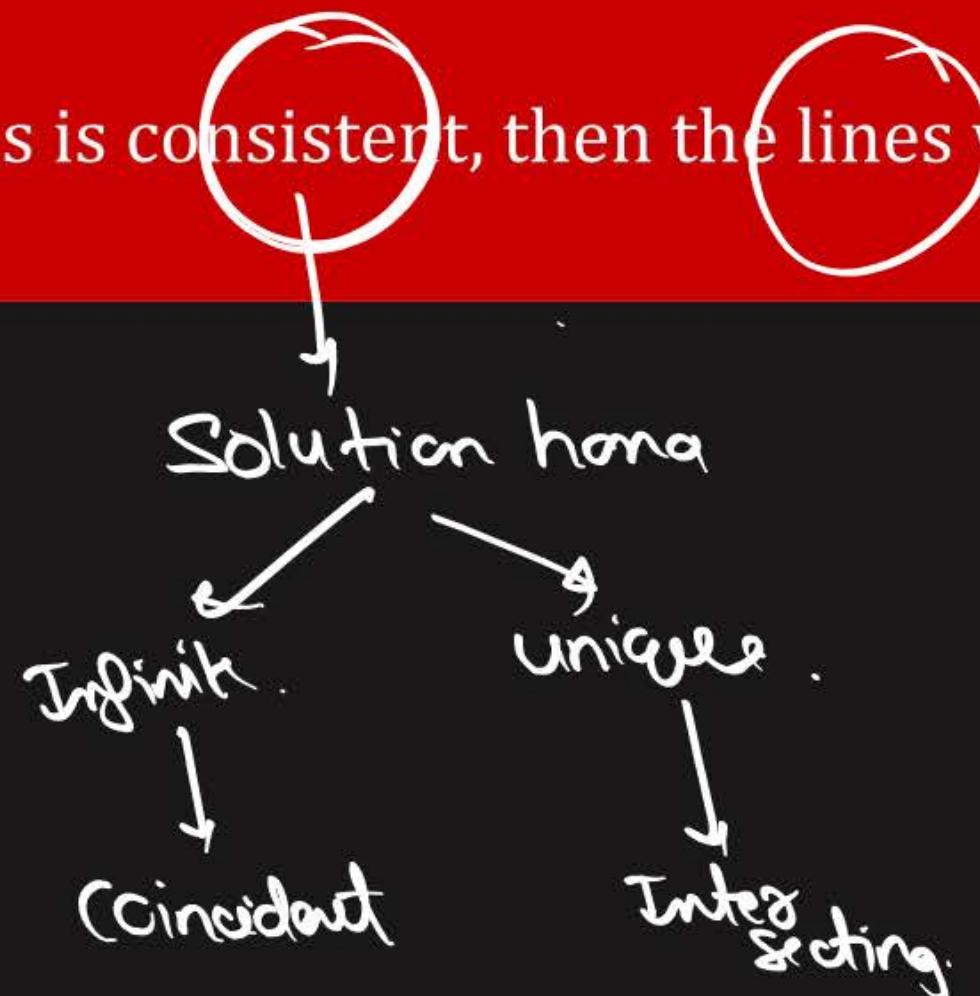
$$\frac{3}{2} \neq \frac{3}{1} \neq \frac{10}{9}$$

$$\frac{3}{1} = \frac{3}{1} \neq \frac{10}{9}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

#Q. If a pair of linear equations is consistent, then the lines will be

- A Parallel
- B Always coincident
- C Intersecting or coincident
- D Always intersecting



#Q. Show graphically that the system of equations $\begin{aligned} 2x + 4y &= 10 \\ 3x + 6y &= 12 \end{aligned}$ has no solution.

$$2x + 4y = 10$$

x	5	1
y	0	2
x	0	4

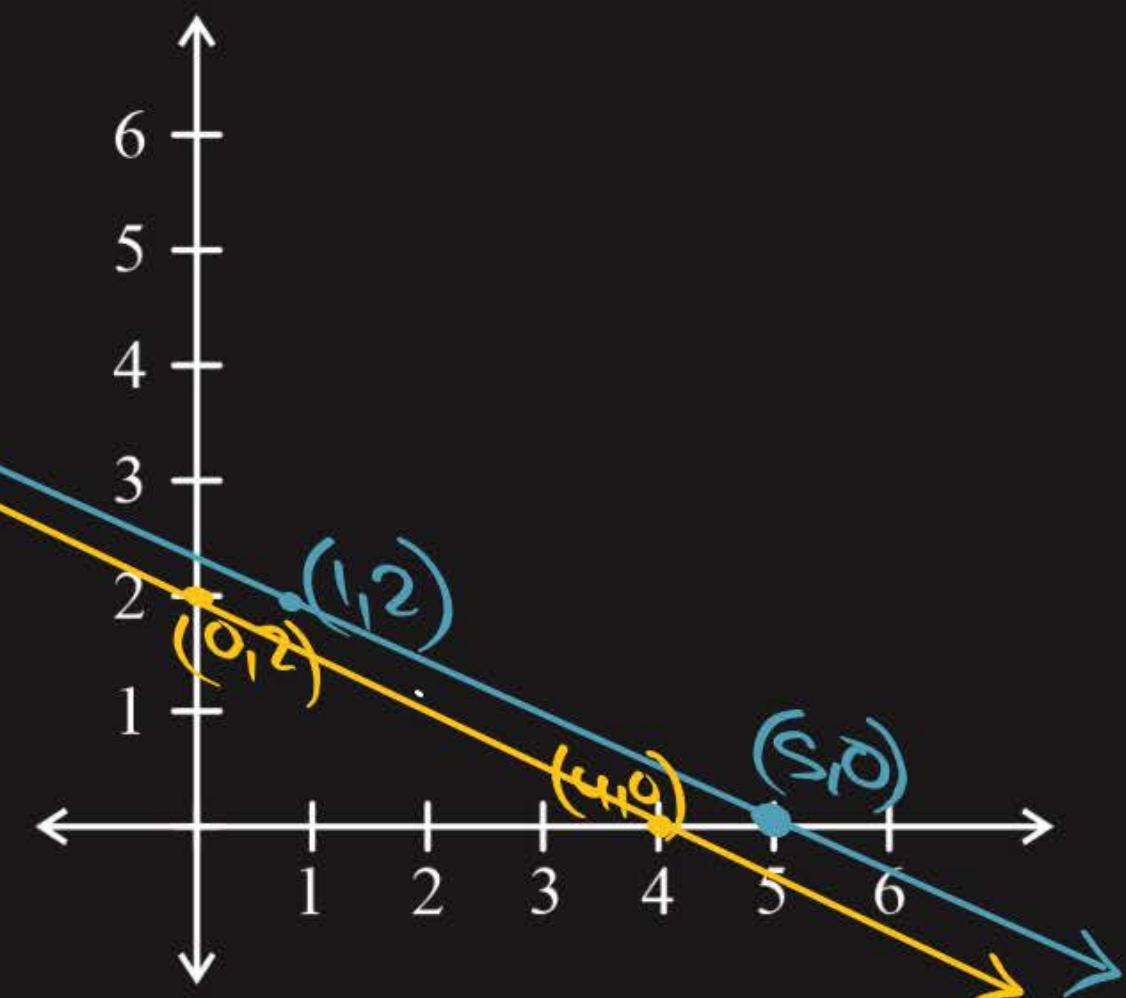
$(5, 0)$
 $(1, 2)$

$$3x + 6y = 12$$

x	0	4
y	2	0
x	0	4

$(0, 2)$
 $(4, 0)$

Since, lines are parallel.
 \therefore the system will no solution.



#Q. Solve graphically the system of equations:

$$x + y = 3$$

$$3x - 2y = 4$$

$$x + y = 3$$

x	0	3
y	3	0

$(0, 3)$
 $(3, 0)$

$$3x - 2y = 4$$

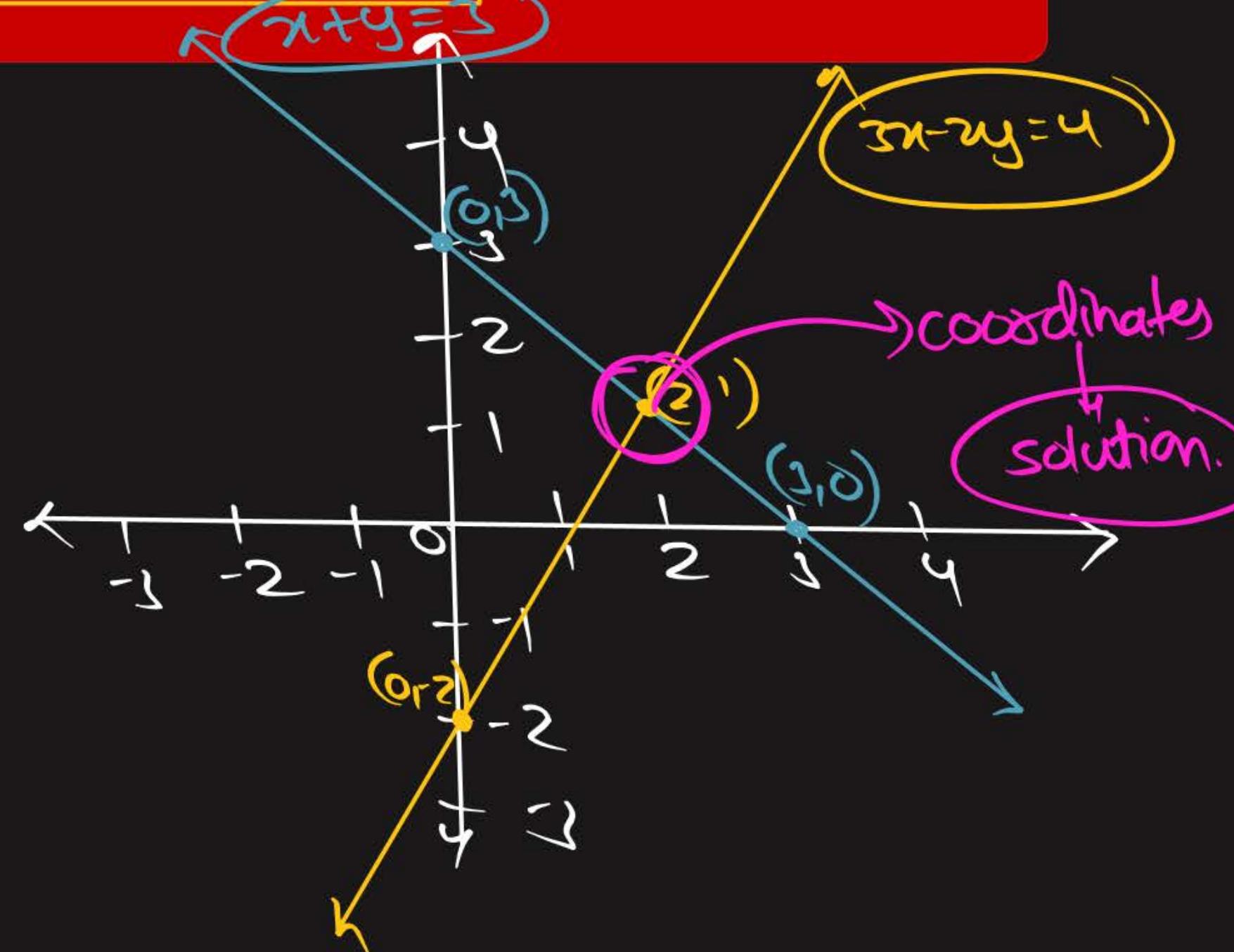
x	0	2
y	-2	1

$(0, -2)$
 $(2, 1)$

$\rightarrow \because$ lines are intersecting.

\therefore unique solution.

Ans: $(2, 1)$

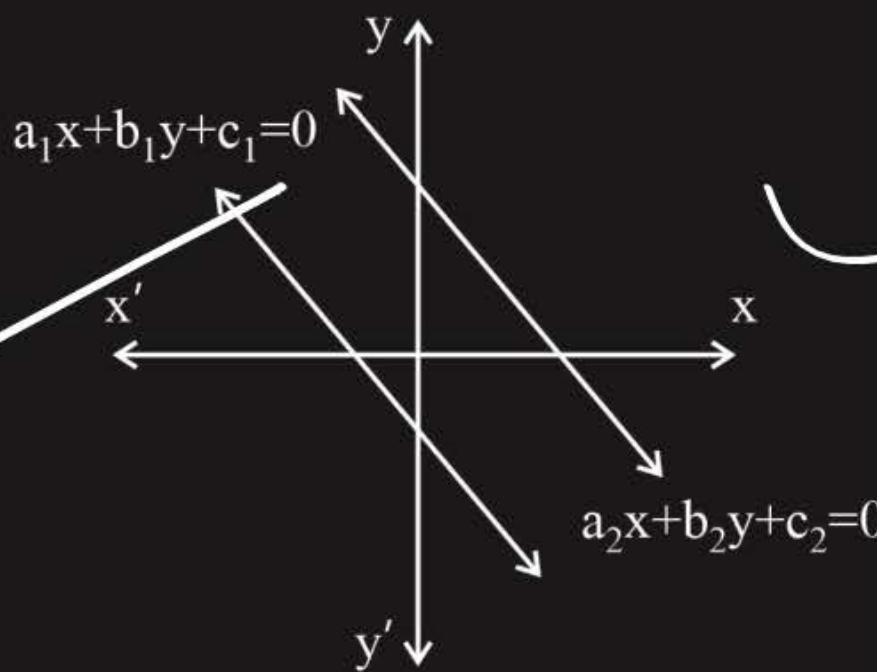


CONSISTENT SYSTEM : A system of simultaneous linear equations is said to be consistent, if it has at least one solution.

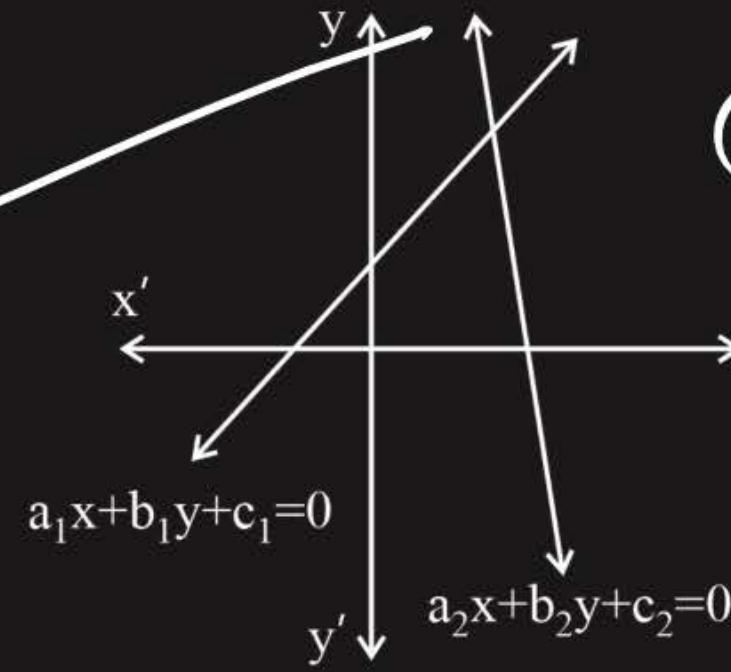
IN-CONSISTENT SYSTEM : A system of simultaneous linear equations is said to be inconsistent, if it has no solution.

Graphical Representation of Linear Equations

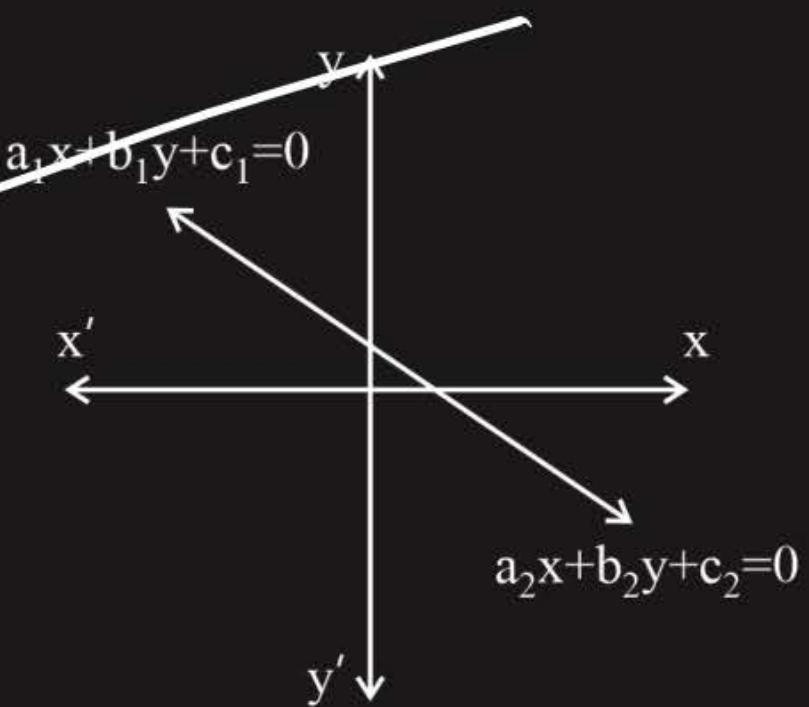
- (i) The two lines intersect at one point.
- (ii) The two lines are parallel i.e. they do not intersect however far they are extended.
- (iii) The two lines are coincident lines i.e. one line overlaps the other line.



Parallel lines



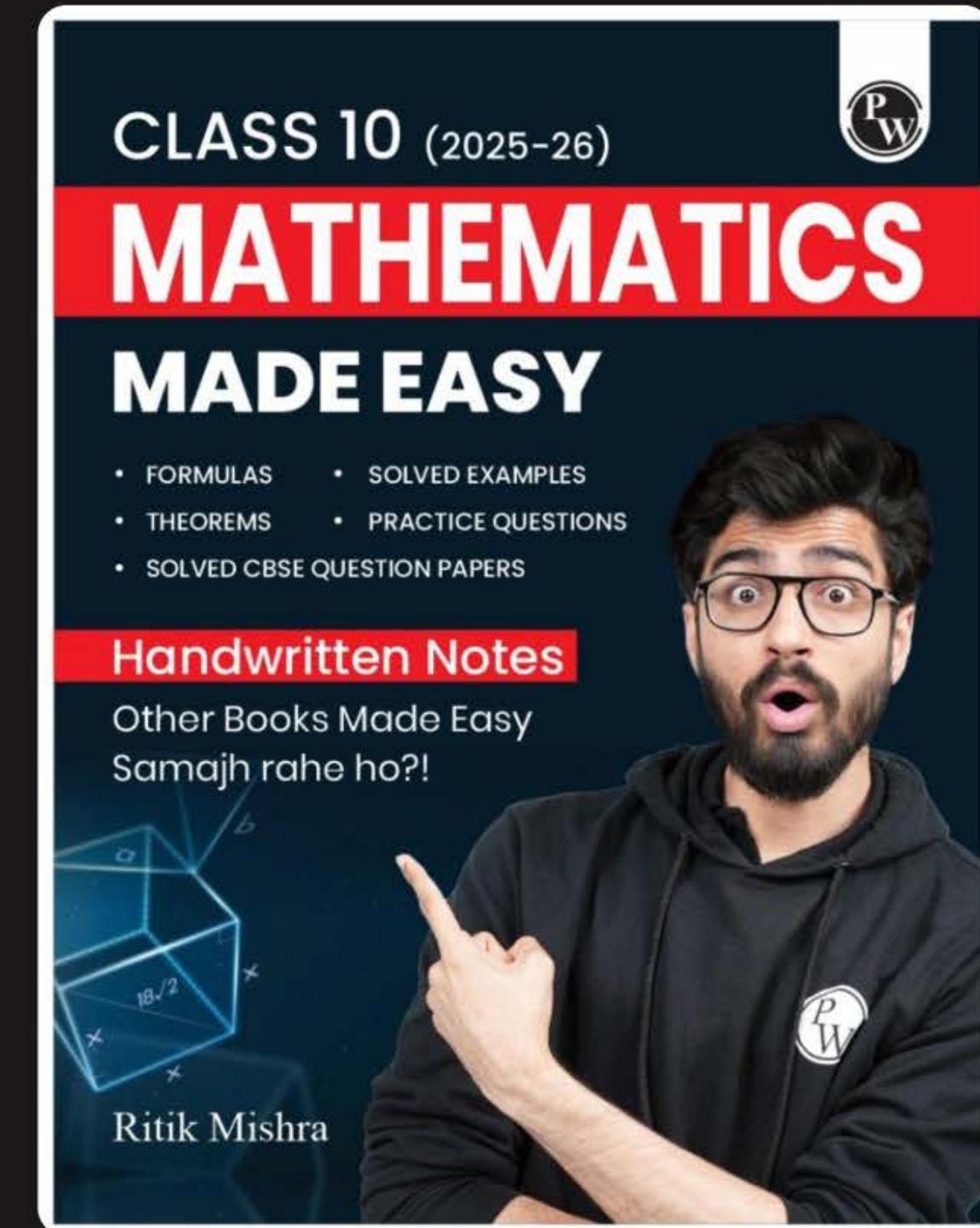
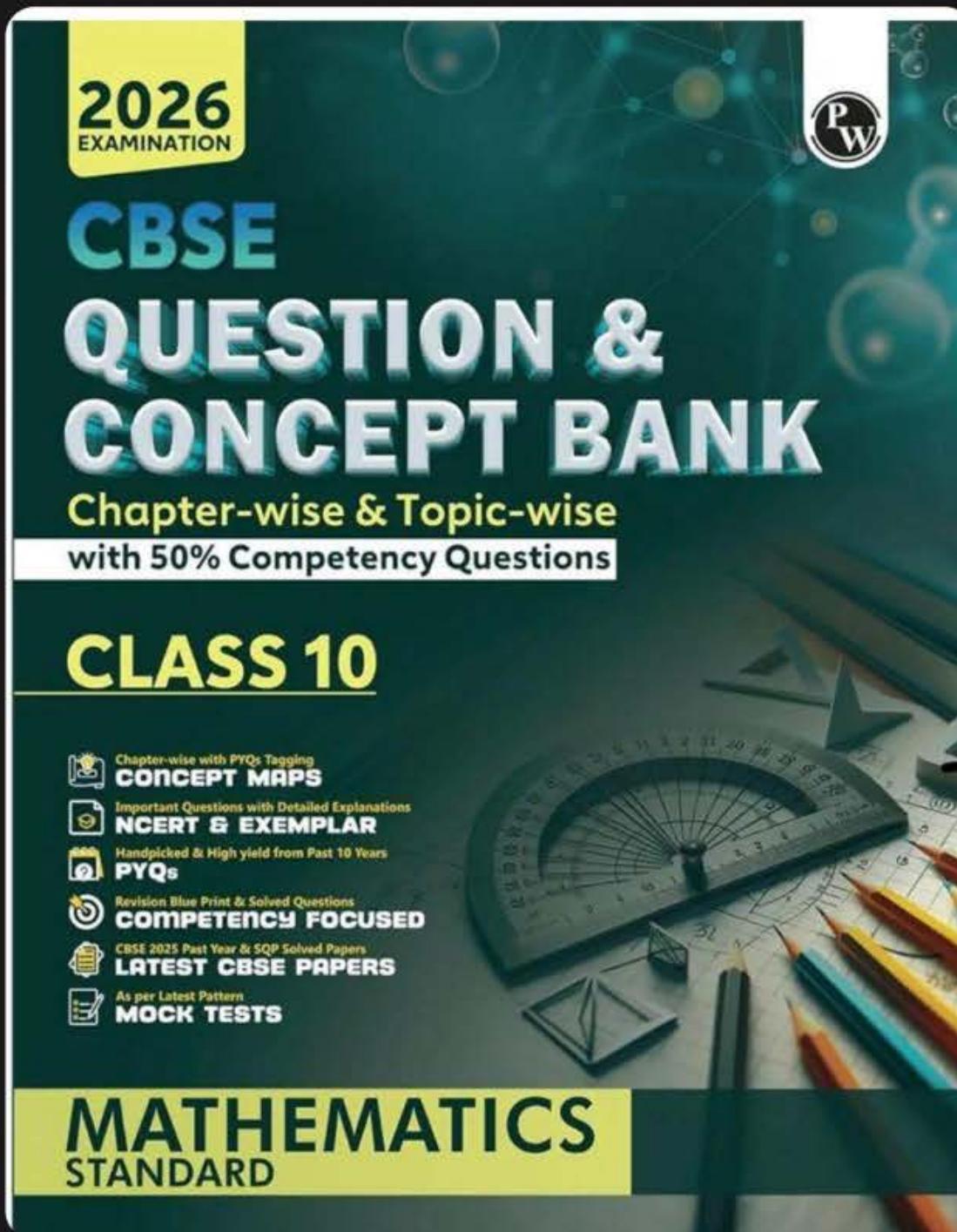
Intersecting lines



Coincident lines

#Q. Show graphically that the system of equations $\begin{aligned} 3x - y &= 2 \\ 9x - 3y &= 6 \end{aligned}$ has infinitely many solutions.





CLASS 10 (2025-26)

PW

MATHEMATICS MADE EASY

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Handwritten Notes

Other Books Made Easy
Samajh rahe ho?!

Ritik Mishra

A portrait of a man with glasses and a beard, pointing upwards with his right hand. A geometric diagram of a cube is visible in the background.



**WORK HARD
DREAM BIG
NEVER GIVE UP**



Thank
You