

Udaan



2026

Coordinate Geometry

MATHS

LECTURE-1

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Topics *to be covered*



A Basics of class 9th

B Distance formula.

Basics

abscissa

x -coordinate \rightarrow y -axis \perp dist.

y -coordinate \rightarrow x -axis \perp dist.

ordinate

$(x, 0)$

Cartesian system

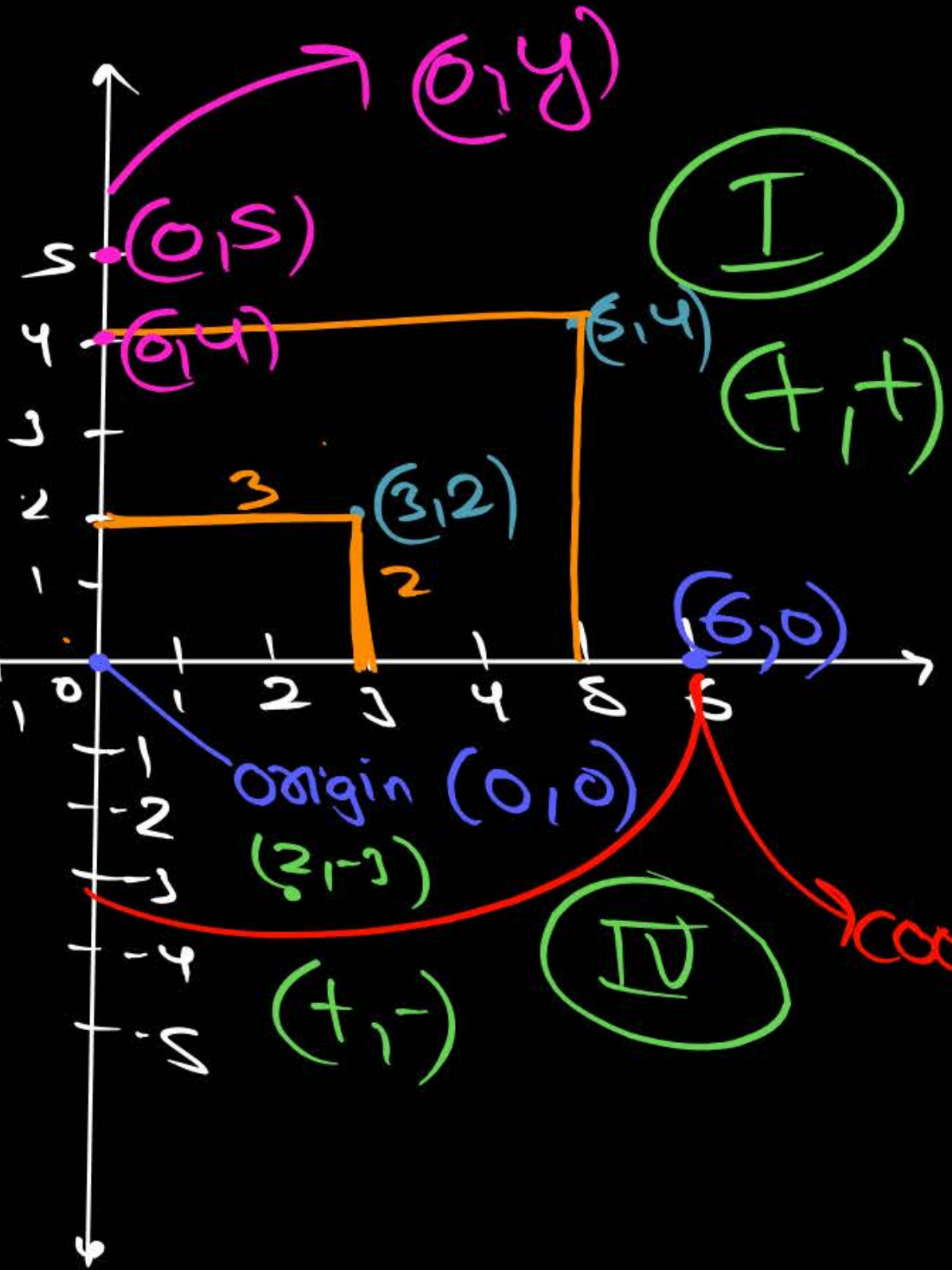
x - y -plane

Cartesian plane



II

III
 $(-3, -5)$

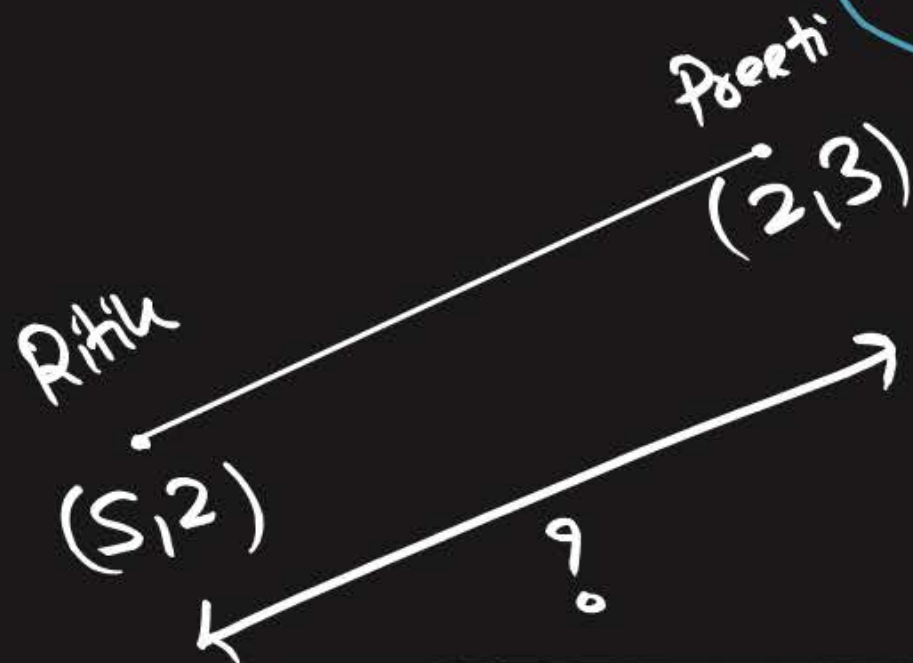


coordinate axes

DISTANCE BETWEEN TWO POINTS



$$\sqrt{(\text{Difference of abscissae})^2 + (\text{Difference of ordinates})^2}$$



$$\begin{aligned} RP &= \sqrt{(3-2)^2 + (2-5)^2} \\ &= \sqrt{1+9} = \boxed{\sqrt{10} \text{ units}} \end{aligned}$$

Q $A(5, -2)$

$B(-7, 3)$

$$\begin{aligned} AB &= \sqrt{(-3 - -2)^2 + (-7 - 5)^2} \\ &= \sqrt{1 + 144} \\ &= \boxed{\sqrt{145} \text{ units}} \end{aligned}$$

A (x_1, y_1) ————— B (x_2, y_2)

$$AB = \sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$$

distance
formula

#Q. Find the distance between the points

(i) $P(-6, 7)$ and $Q(-1, -5)$

$$PQ = \sqrt{(-1 - (-6))^2 + (-5 - 7)^2}$$

$$= \sqrt{25 + 144}$$

$$= \sqrt{169}$$

$$AB = 13 \text{ units}$$

(ii) $R(a + b, a - b)$ and $S(a - b, -a - b)$

$$RS = \sqrt{[(-a - b) - (a - b)]^2 + [(a - b) - (a + b)]^2}$$

$$= \sqrt{(-a - b - a + b)^2 + (a - b - a - b)^2}$$

$$= \sqrt{(-2a)^2 + (-2b)^2}$$

$$= \sqrt{4a^2 + 4b^2}$$

$$= \sqrt{4(a^2 + b^2)} = \sqrt{4} \sqrt{a^2 + b^2}$$

$$= \boxed{2\sqrt{a^2 + b^2}}$$



$$\sqrt{a^2 \cdot b^2} = \sqrt{a^2} \cdot \sqrt{b^2} = \textcircled{ab}$$

$$\cancel{\sqrt{(a+b)^2}} = a+b$$

$$\sqrt{a^2 + b^2} \neq \sqrt{a^2} + \sqrt{b^2}$$

$$\cancel{\sqrt{a^2 + b^2}} \quad \text{XXX}$$

Mistakes to avoid

#Q. Find the value of x , if the distance between the points $(x, -1)$ and $(3, 2)$ is 5.

$$AB = 5$$

$$\sqrt{(2 - (-1))^2 + (3 - x)^2} = (5)^2$$

$$\underline{S \cdot B \cdot S}$$

$$9 + (3 - x)^2 = 25$$

$$(3 - x)^2 = 16$$

$$3 - x = \pm \sqrt{16}$$

$$3 - x = \pm 4$$

$$3 - x = 4, \quad 3 - x = -4$$

$$3 - 4 = x$$

$$\boxed{-1 = x}$$

$$3 + 4 = x$$

$$\boxed{7 = x}$$

$$\underline{\underline{\text{Ans: } -1, 7}}$$

$$PQ = \sqrt{a}$$

$$\underline{S \cdot B \cdot S}$$

$$\boxed{PQ^2 = a}$$

#Q. If the points A (4, 3) and B (x, 5) are on the circle with centre O(2, 3), find the value of x.

OA = OB (radius of same circle)

$$\sqrt{(3-3)^2 + (4-2)^2} = \sqrt{(5-3)^2 + (x-2)^2}$$

SOS

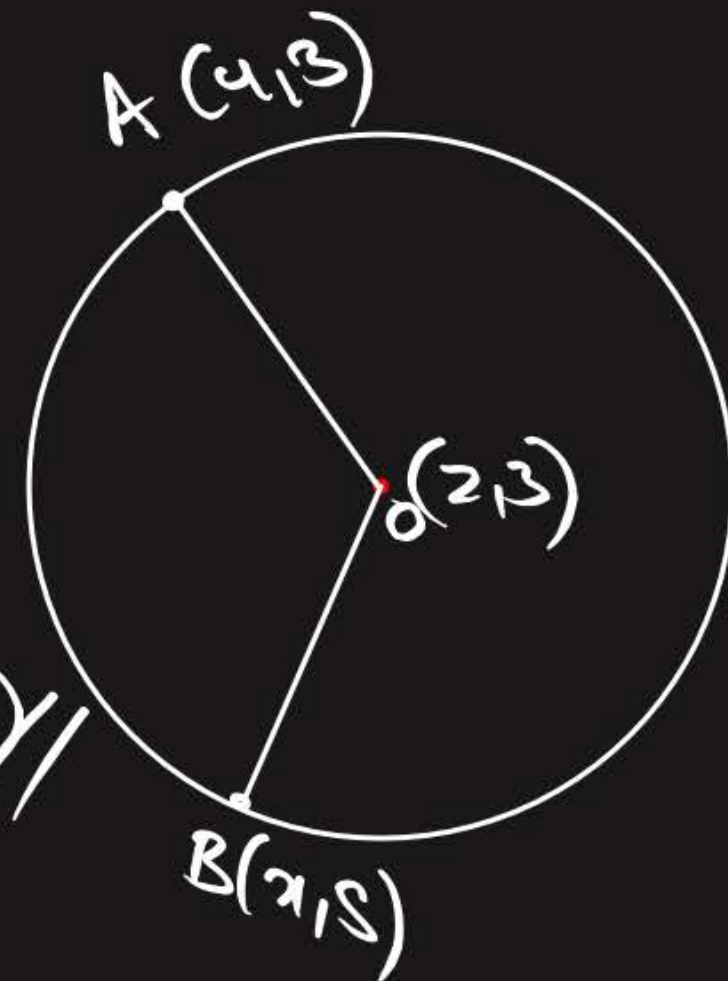
$$0 + 4 = 4 + (x-2)^2$$

$$0 = (x-2)^2$$

$$\pm \sqrt{0} = x-2$$

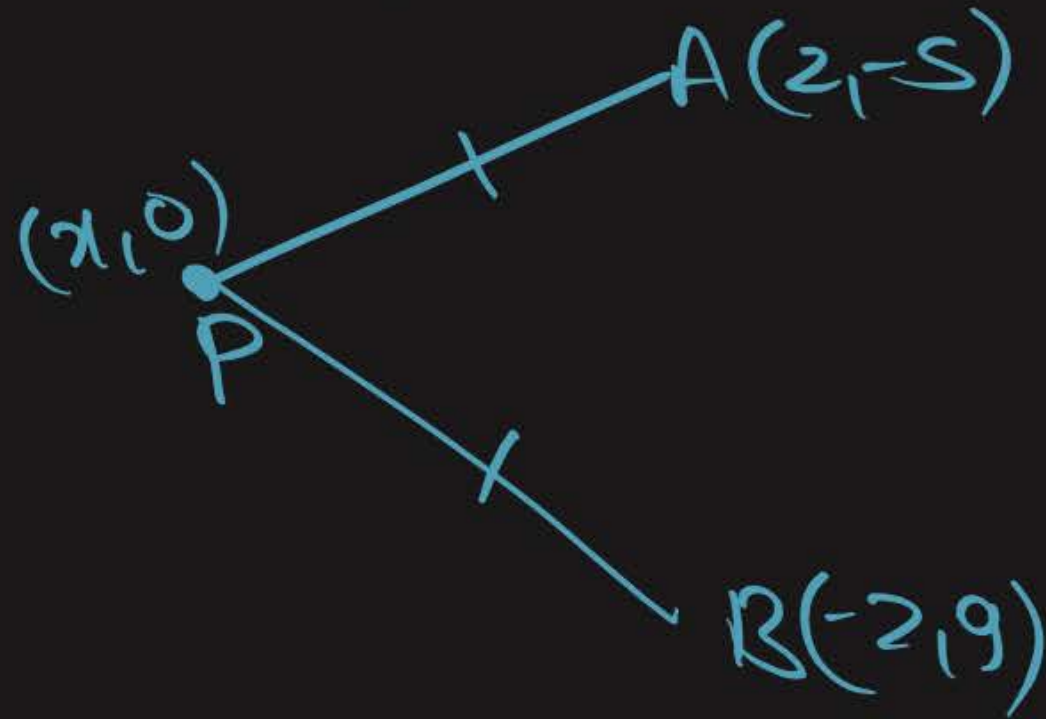
$$0 = x-2$$

$$2 = x$$



#Q. Find a point on x-axis which is equidistant from A(2, -5) and B(-2, 9). point key coordinates (x, y) → equal distance.

let the point on x-axis be P(x, 0)



$$PA = PB \\ \Rightarrow \boxed{PA^2 = PB^2}$$

$$(0 - (-5))^2 + (x - 2)^2 = (0 - 9)^2 + (x - (-2))^2 \\ 25 + x^2 + 4 - 4x = 81 + x^2 + 4 + 4x$$

$$25 - 4x = 81 + 4x$$

$$25 - 81 = 4x + 4x$$

$$-56 = 8x$$

$$\boxed{-7 = x} //$$

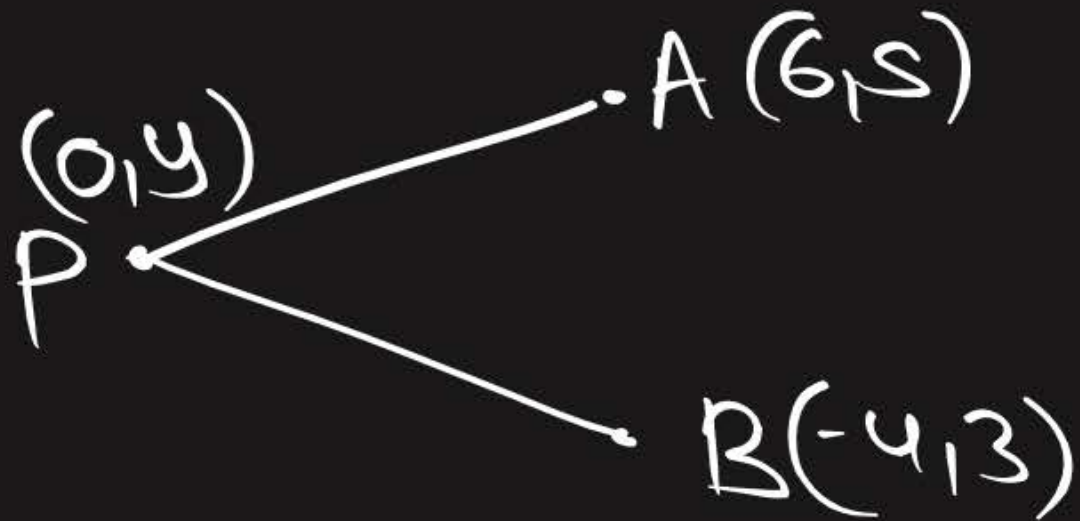
Ans: P(-7, 0)

#Q. Find a point on the y-axis which is equidistant from the point A(6, 5) and B(-4, 3).

y-axis $\rightarrow P(0, y)$

$$PA = PB$$

$$= \boxed{PA^2 = PB^2}$$



$$(5 - y)^2 + (6 - 0)^2 = (3 - y)^2 + (-4 - 0)^2$$

$$25 + \cancel{y^2} - 10y + 36 = 9 + \cancel{y^2} - 6y + 16$$

$$36 = 4y$$

$$\boxed{9 = y}$$

Ans: $P(0, 9)$

$$25 - 10y + 36 = 9 - 6y + 16$$

$$25 + 36 - 9 - 16 = -6y + 10y$$

$$61 - 25 = 4y$$

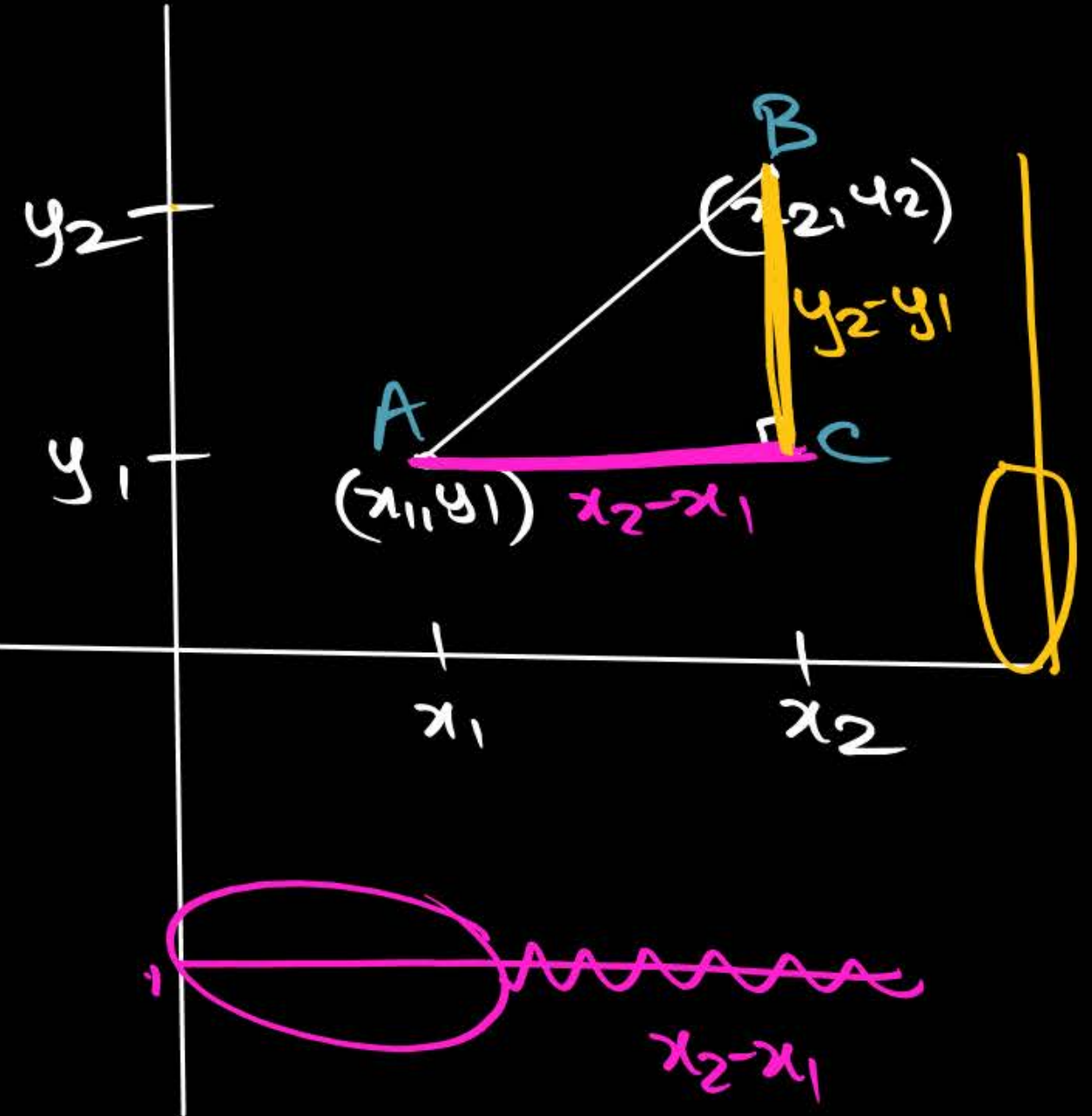
Proof of distance formula.

P.T

$$H^2 = P^2 + B^2$$

$$AB^2 = (y_2 - y_1)^2 + (x_2 - x_1)^2$$

$$AB = \sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$$



#Q. The x-coordinate of a point P is twice its y-coordinate. If P is equidistant from Q(2, -5) and R(-3, 6), then find the coordinates of P.

#Graph



WORK HARD

DREAM BIG

NEVER GIVE UP



RITIK SIR

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Thank
You