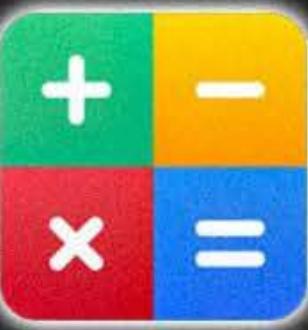




UDAAN



2026

REAL NUMBERS

MATHS

LECTURE-2

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Topics

to be covered

A

Questions on HCF, LCM, Prime numbers, Composite numbers

B

Relation between HCF and LCM of two numbers

C

Coprime numbers

Next class

QUESTION

#Q. Find the HCF and LCM of 144, 180 and 192 by the prime factorization

method.

$$144 = 2^4 \times 3^2 \times 5^0$$

$$180 = 2^2 \times 3^2 \times 5^1$$

$$192 = 2^6 \times 3^1 \times 5^0$$

$$HCF = 2^2 \times 3^1 \times 5^0$$

$$= 12$$

$$LCM = 2^6 \times 3^2 \times 5^1$$

$$= 2880$$

A 12, 280

B 12, 2880

C 14, 2880

D NOTA

2	144	2	180	2	192
2	72	2	90	2	96
2	36	2	45	2	48
2	18	3	27	2	24
3	9	3	9	3	12
3	3	3	3	2	6
1	1	1	1	2	3
					1

Prime Numbers

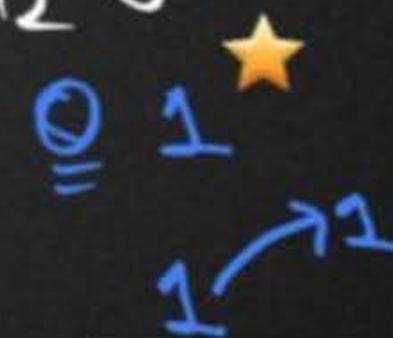
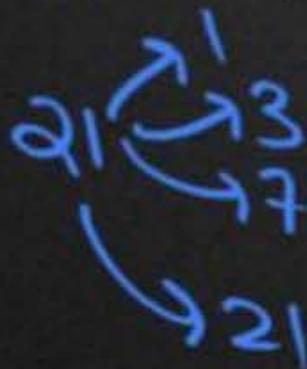


only two factors.

Composite Numbers



0 21 → composite no.



neither prime nor composite

#Q. If $a = 2^2 \times 3^x$, $b = 2^2 \times 3 \times 5$, $c = 2^2 \times 3 \times 7$, and $\text{LCM}(a, b, c) = 3780$, then $x =$

$$a = 2^2 \times 3^x \times 5^0 \times 7^0$$

$$b = 2^2 \times 3^1 \times 5^1 \times 7^0$$

$$c = 2^2 \times 3^1 \times 7^1 \times 5^0$$

$$\text{LCM}(a, b, c) = 3780$$

A 0

B 1

C 2

D 3

$$\text{LCM} = 2^2 \times 3^x \times 5^1 \times 7^1$$

$$3780 = 2^2 \times 3^x \times 5^1 \times 7^1$$

$$3780 = 2^2 \times 3^3 \times 5^1 \times 7^1$$

$$\begin{array}{r|l}
 2 & 3780 \\
 \hline
 2 & 1890 \\
 3 & 945 \\
 3 & 315 \\
 3 & 105 \\
 3 & 35 \\
 7 & 5
 \end{array}$$

#Q. If the HCF of 85 and 153 is expressible in the form $85n - 153$ then the value of n is

A

3

B

2

C

4

D

1

$$\begin{array}{r}
 5 \mid 85 \\
 \hline
 17 \mid 17 \\
 \hline
 1
 \end{array}
 \quad
 \begin{array}{r}
 3 \mid 153 \\
 \hline
 3 \mid 51 \\
 \hline
 17
 \end{array}$$

$$\text{HCF} = 85n - 153$$

$$17 = 85n - 153$$

$$17 + 153 = 85n$$

$$170 = 85n$$

$$\frac{170}{85} = n$$

$2 = n$

$$85 = 5^1 \times 17^1 \times 2^0$$

$$153 = 3^2 \times 17^1 \times 5^0$$

$$\text{HCF} = 3^0 \times 17^1 \times 5^0$$

$$= 1 \times 17 \times 1 \times 17$$

#Q. The HCF of [smallest prime number] and [the smallest composite number] is:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, ...

Smallest prime no.

Composite no.

A 2

B 4

C 6

D 8

$$\text{HCF}(2, 4) = 2^1$$

$$2 = 2^1$$

$$4 = 2^2$$

$$\begin{array}{r} 2 \\ \hline 2 \end{array} \quad \begin{array}{r} 2 \\ \hline 4 \end{array}$$

#Q. The LCM of the smallest two digit composite number and the smallest composite number is:

- A 12
- B 20
- C 4
- D 44

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, ...
Smallest two digit composite no.

$$\text{LCM}(4, 10) = 2^2 \times 5^1 = 20$$

$$4 = 2^2 \times 5^0$$

$$10 = 2^1 \times 5^1$$

#Q. The least number that is divisible by all the numbers from 1 to 10 (both inclusive)

A

10

B

100

C

504

D

2520

1 = 1
 2 = 2¹
 3 = 3¹
 4 = 2²
 5 = 5¹
 6 = 2¹ x 3¹

LCM = $2^3 \times 3^2 \times 5^1 \times 7^1$

2520

2	1, 2, 3, 4, 5, 6, 7, 8, 9, 10
2	1, 3, 5, 7, 9, 11
2	1, 3, 5, 7, 11, 13
3	1, 3, 5, 7, 9, 11
3	1, 3, 5, 7, 9, 11, 13
5	1, 5, 7, 11, 13
7	1, 7, 11, 13

$$\text{HCF} = 5^0 \times 7^0 = 1$$

$$5 = 5^1 \times 7^0$$

$$7 = 7^1 \times 5^0$$

$$\text{LCM} = 5^1 \times 7^1 = 35$$

a, b
Primno

$$\text{HCF}(a, b) = 1$$

$$\text{LCM}(a, b) = a \times b$$

#Q. If p and q are two distinct prime numbers, then their HCF is

- A** 2
- B** 0
- C** Either 1 or 2
- D** 1

#Q. If p and q are two distinct numbers, then their LCM (p, q) is

A 1

B p

C q

D pq

#Q. Let n be a natural number. Then, the LCM ($n, n + 1$) is

A

n

B

$n + 1$

C

$n(n + 1)$

D

1

$$n = 2^0 \times 3^0 \times 5^0$$

$$n + 1 = 2^1 \times 3^1 \times 5^0$$

$$\text{LCM} = 2^1 \times 3^1 \times 5^1$$

$$= 6 \times 5 = 30$$

$$(6, 6+1) \rightarrow (6, 7)$$

$$(6, 6)$$

#Q. Let p be a prime number. The sum of its factors is:

- A p
- B 1
- C $p + 1$
- D $p - 1$

$$\begin{array}{ccc} 5 & & 7 \\ \swarrow & \uparrow & \swarrow \\ & 1 & \\ \uparrow & & \uparrow \\ p & & p \end{array}$$

$1 + p$

$$\begin{array}{ccc} 8 & & 1 + 2 + 4 + 8 \\ \swarrow & \uparrow & \\ & 4 & \\ \uparrow & & \uparrow \\ 8 & & \end{array}$$

Sum of its factors = 15

#Q. The LCM of two prime numbers p and q ($p > q$) is 221. Find the value of $3p - q$.

$$\text{LCM}(p, q) = p \times q$$

$$p > q$$

A

4

B

28

C

38

D

48

$$221 = p \times q$$

$$17 \times 13 = p \times q$$

$$\begin{aligned} &= 3p - q \\ &= 3(17) - 13 \\ &= 51 - 13 \\ &= 38 \end{aligned}$$

$$\begin{array}{r} 13 \\ \hline 221 \\ 13 \\ \hline 17 \\ 17 \\ \hline 1 \end{array}$$

#Q. Find the greatest number which divides 85 and 72 leaving remainder 1 and 2 respectively.

$$\begin{array}{l}
 \text{?} \div 85 \rightarrow R=1 \\
 \text{?} \div 72 \rightarrow R=2
 \end{array}$$

$$\begin{array}{r}
 2 \overline{)84} \\
 2 \overline{)42} \\
 3 \overline{)21} \\
 7 \overline{)7} \\
 \end{array}
 \quad
 \begin{array}{r}
 2 \overline{)70} \\
 2 \overline{)35} \\
 5 \overline{)7} \\
 \end{array}$$

$$\begin{array}{l}
 \text{?} \div 84 \rightarrow R=0 \\
 \text{?} \div 70 \rightarrow R=0
 \end{array}$$

$$84 = 2^2 \times 3^1 \times 7^1 \times 5^0$$

$$70 = 2^1 \times 5^1 \times 7^1 \times 10^0$$

$$\text{HCF} = 2^1 \times 3^0 \times 5^0 \times 7^1$$

$$= 14$$

#Q. Find the largest number which on dividing 1251, 9377 and 15628 leaves remainders 1, 2 and 3 respectively

A

620

B

625

C

600

D

5

$$\begin{aligned} &\div 1251 \rightarrow R=1 \\ &\div 9377 \rightarrow R=2 \\ &\div 15628 \rightarrow R=3 \end{aligned}$$

HK.F

$$\begin{array}{r}
 & 15625 \\
 \hline
 & 3125 \\
 & 625 \\
 & 125 \\
 & 25 \\
 & 5 \\
 & 1
 \end{array}$$

$$\begin{array}{l}
 \div 1250 \\
 \div 9375 \\
 \div 15625
 \end{array}
 \left. \begin{array}{l}
 R=0
 \end{array} \right\}$$

$$4680 - 17 = 4663$$



#Q. Find the smallest number which increased by 17 is exactly divisible by both 520 and 468.

A 4663

B 4720

C 4680

D None of the above

$$520 = 5^1 \times 2^3 \times 13^1 \times 10^0$$

$$468 = 2^2 \times 3^2 \times 13^1 \times 5^0$$

$$\text{LCM}(520, 468) = 2^3 \times 5^1 \times 13^1 \times 3^2$$

$$= 8 \times 5 \times 13 \times 9$$

$$= 360 \times 13$$

$$= 4680$$

$$\begin{array}{r|rr}
 5 & 520 & 2 & 468 \\
 \hline
 2 & 104 & 2 & 234 \\
 2 & 52 & 3 & 117 \\
 2 & 26 & 3 & 39 \\
 13 & 13 & 13 & 13 \\
 & & & 1
 \end{array}$$

#Q. If 'p' and 'q' are natural numbers and 'p' is the multiple of 'q', then what is the HCF of 'p' and 'q'?

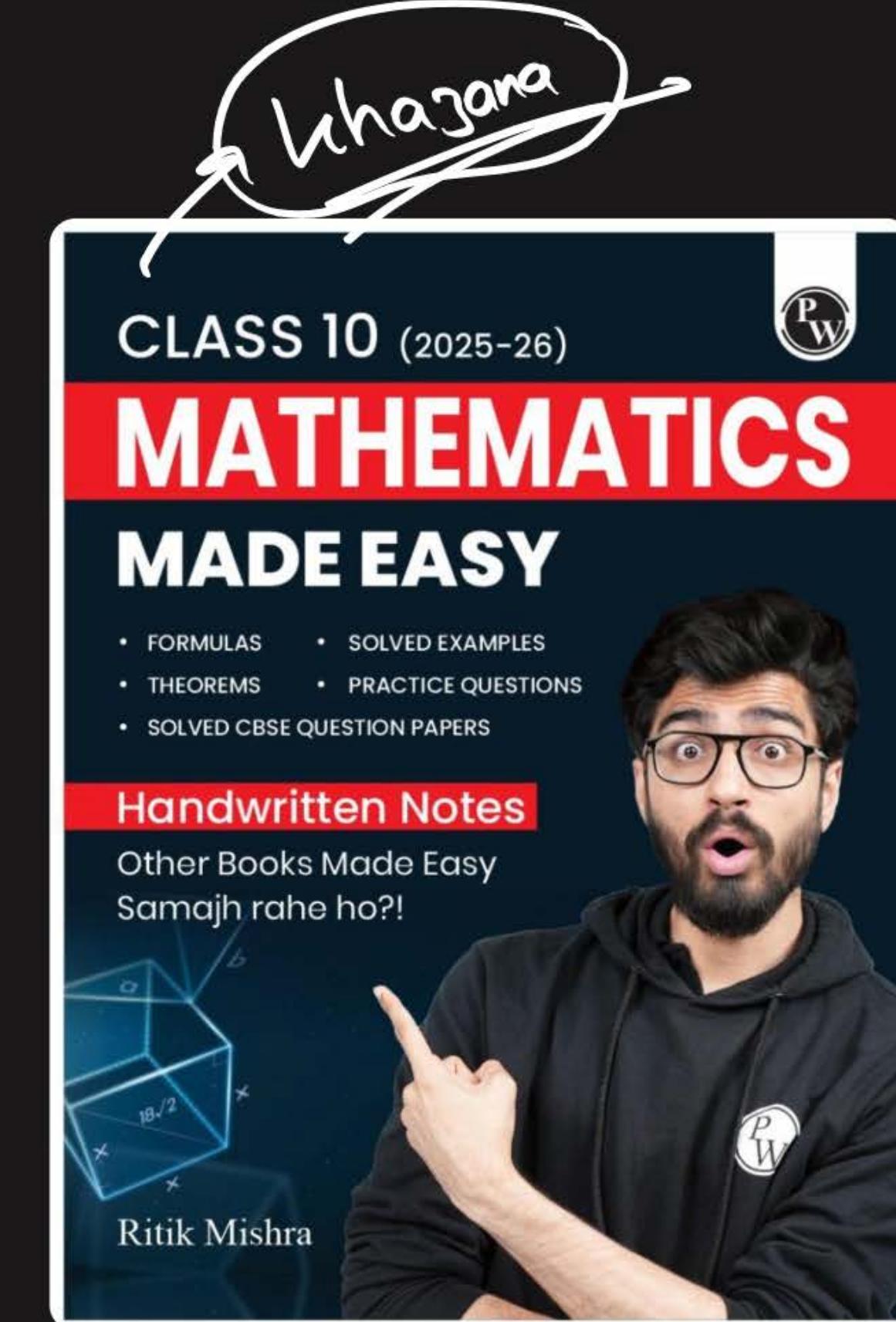
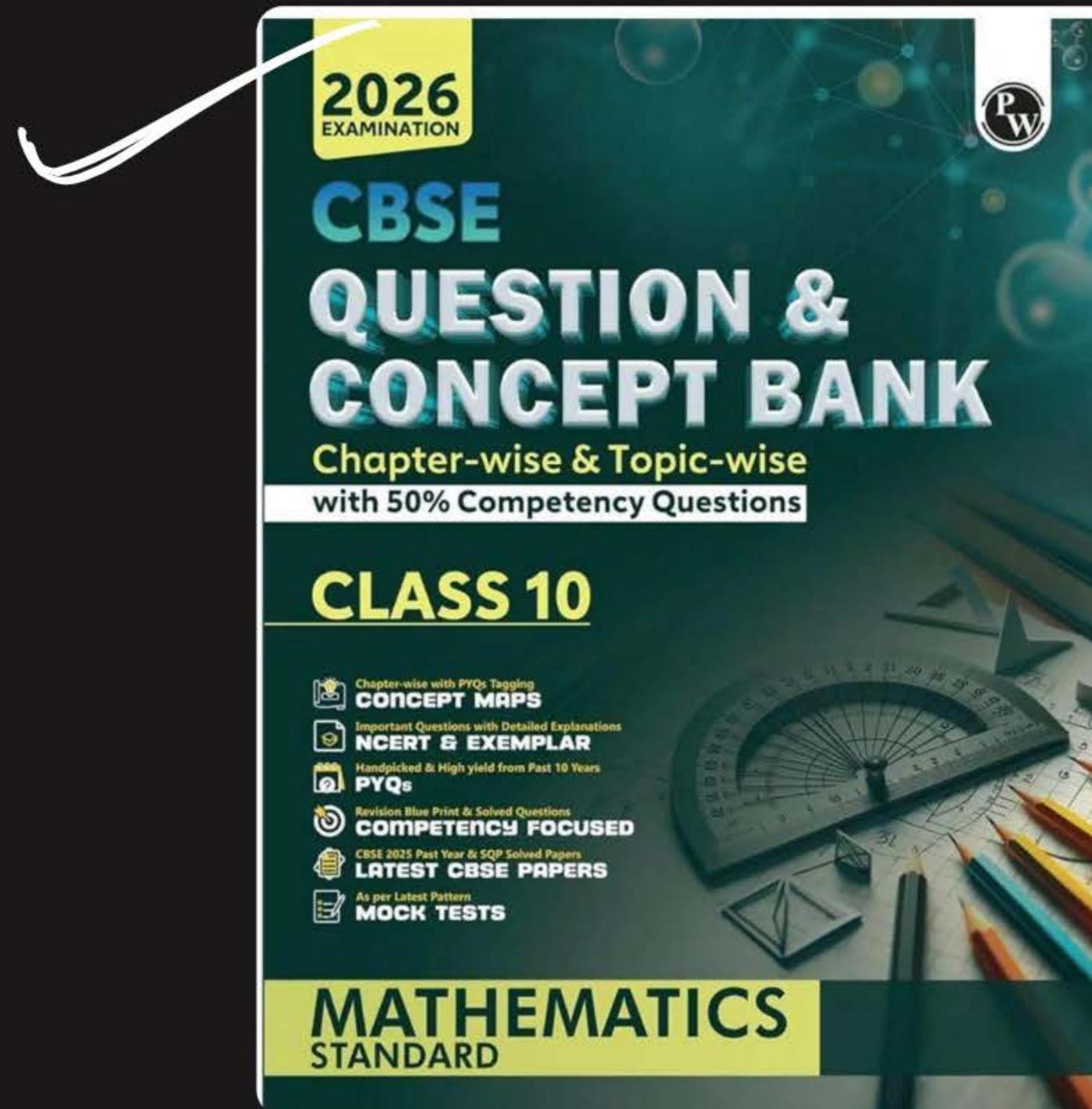
A pq

B p

C q

D $p + q$

#GPH



**WORK HARD
DREAM BIG
NEVER GIVE UP**



Thank
You