



UDAAN



2026

Circles

MATHS

LECTURE-5

BY-RITIK SIR



Topics

to be covered

Important Questions (Part 4)

A

Remaining Questions and Important One Markers



#Q. Assertion (A) : If a chord AB subtends an angle of 60° at the centre of a circle,
then the angle between the tangents at A and B is also 60° .

Reason (R): The length of the tangent from an external point P on a circle with centre O is always less than OP.

#Gpu

1, 20

- A** Both Assertion (A) and Reason (R) are true and Reason (R) is correct explanation of Assertion (A).
- B** Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).
- C** Assertion (A) is true but Reason (R) is false.
- D** Assertion (A) is false but Reason (R) is true.

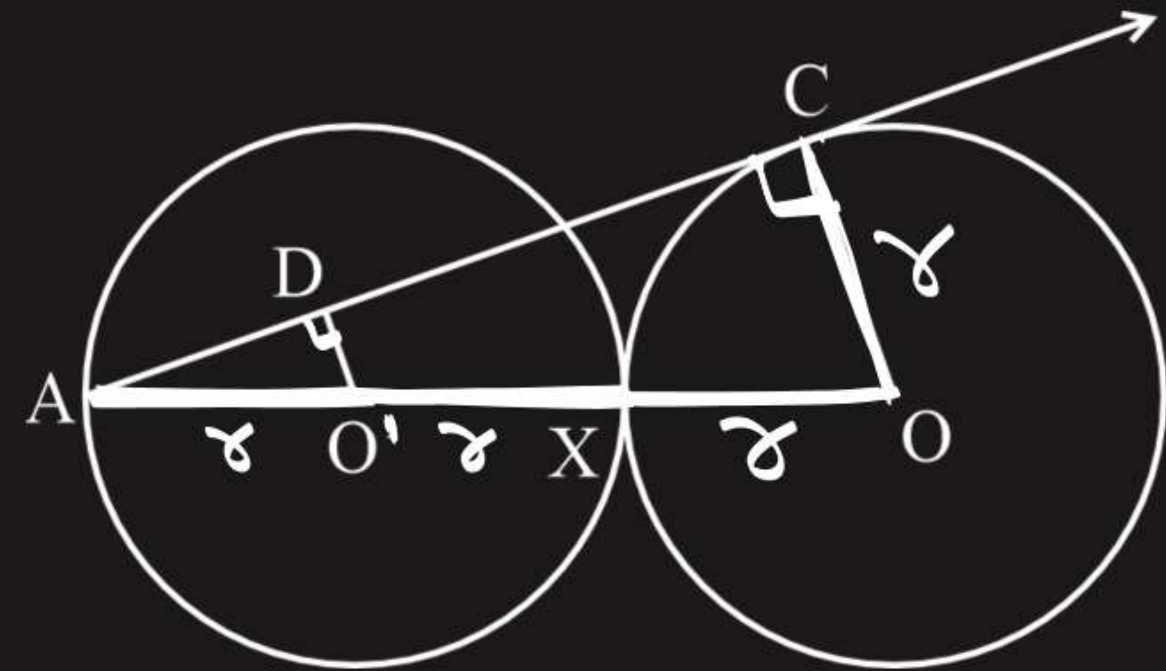
#Q. In figure below, equal circles with centres O and O' touch each other at X. OO' produced to meet a circle O', at A. AC is a tangent to the circle whose centre is O. O'D is perpendicular to AC. Find the value of $\frac{DO'}{CO}$.

AA

$$\triangle ADO' \sim \triangle ACO$$

By CPST, $\frac{AD}{AC} = \frac{DO'}{CO} = \frac{AO'}{AO}$

$$\frac{DO'}{CO} = \frac{r}{3r} = \frac{1}{3}$$



#Q. A round balloon of radius r subtends an angle α at the eye of the observer while the angle of elevation of its centre is β . Prove that the height of the centre of the balloon is $r \sin \beta \operatorname{cosec} \alpha/2$.

to p: $OC = r \sin \beta \operatorname{cosec} \frac{\alpha}{2}$

PROOF:

In $\triangle ODC$

$$\sin \beta = \frac{OC}{OD}$$

$$\sin \beta = \frac{OC}{OD} \quad (1)$$

In $\triangle ODB$

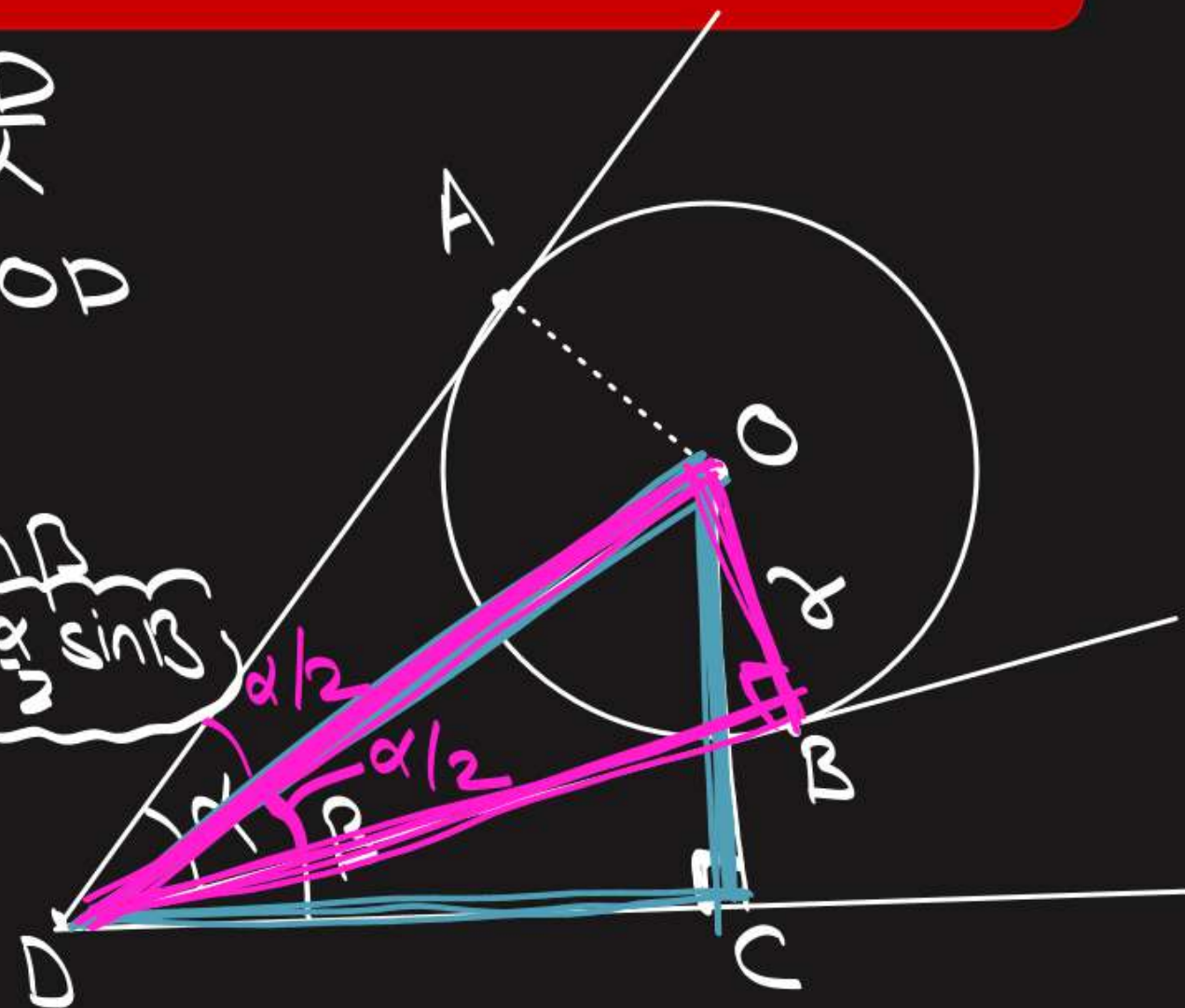
$$\operatorname{cosec} \frac{\alpha}{2} = \frac{1}{\sin \frac{\alpha}{2}} = \frac{OD}{OB}$$

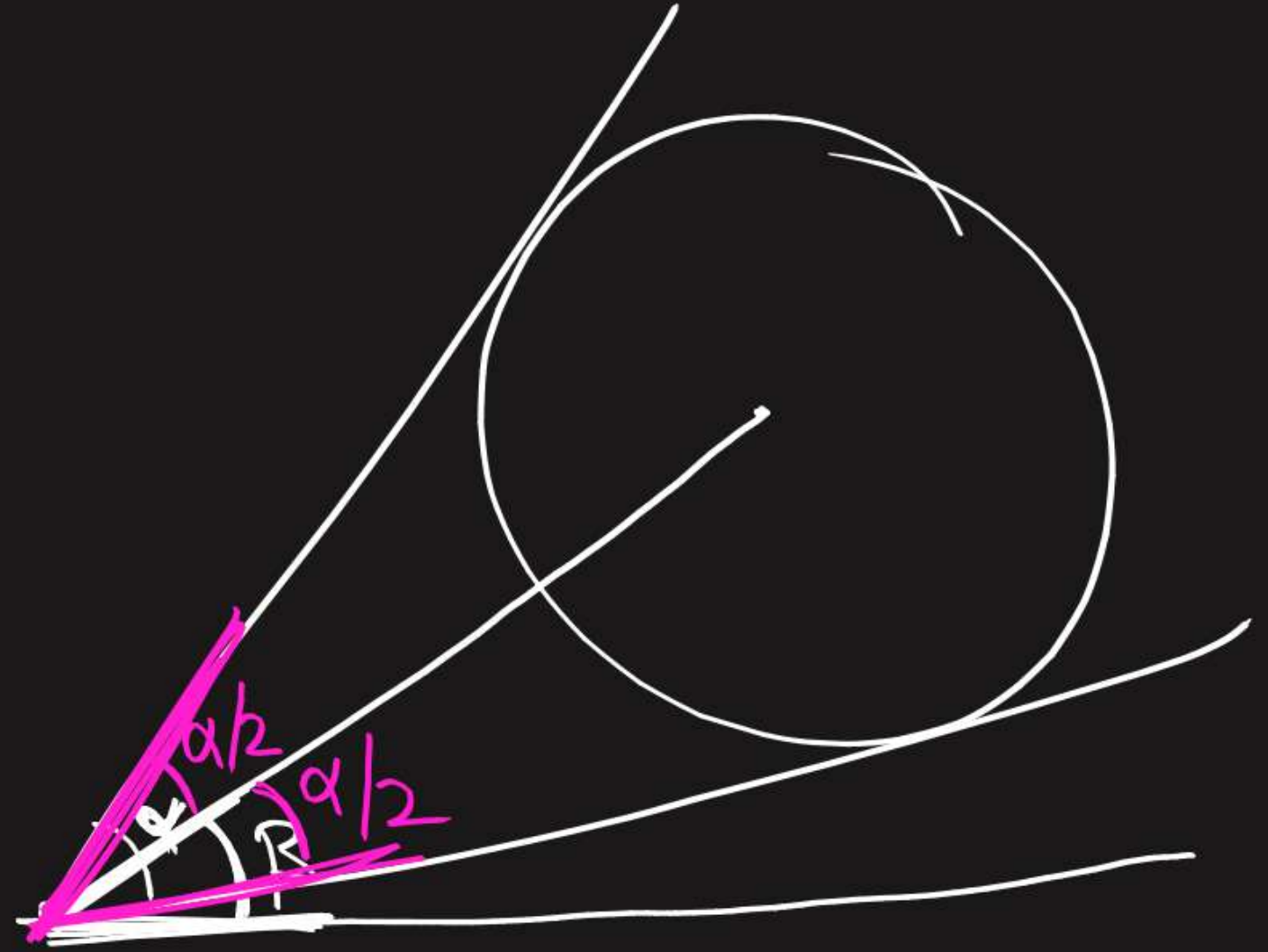
$$r \operatorname{cosec} \frac{\alpha}{2} = \frac{OD}{2}$$

$$r \operatorname{cosec} \frac{\alpha}{2} = OD$$

$$OC = OD \sin \beta$$

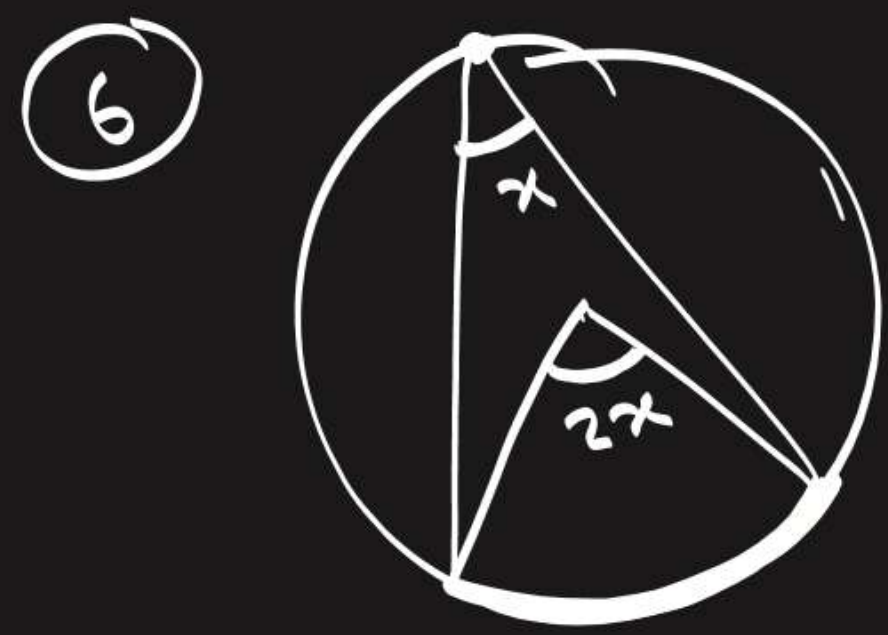
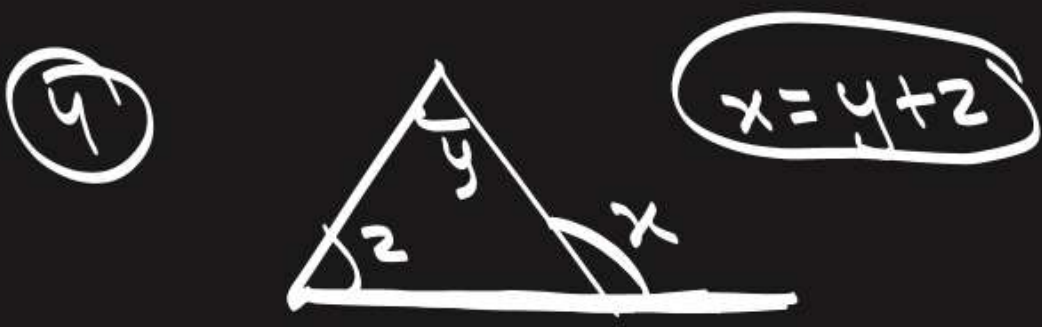
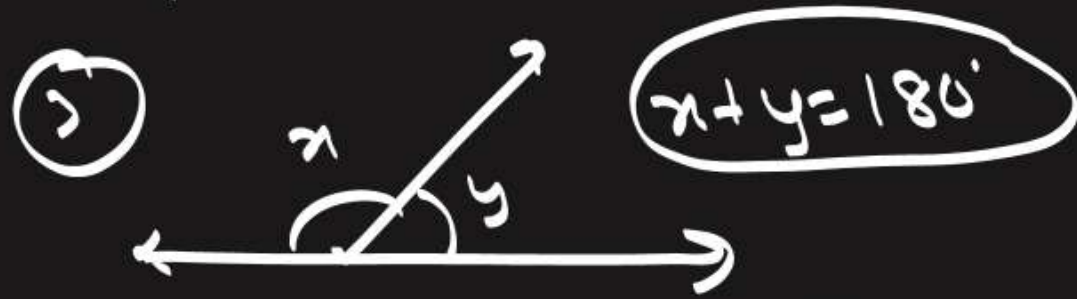
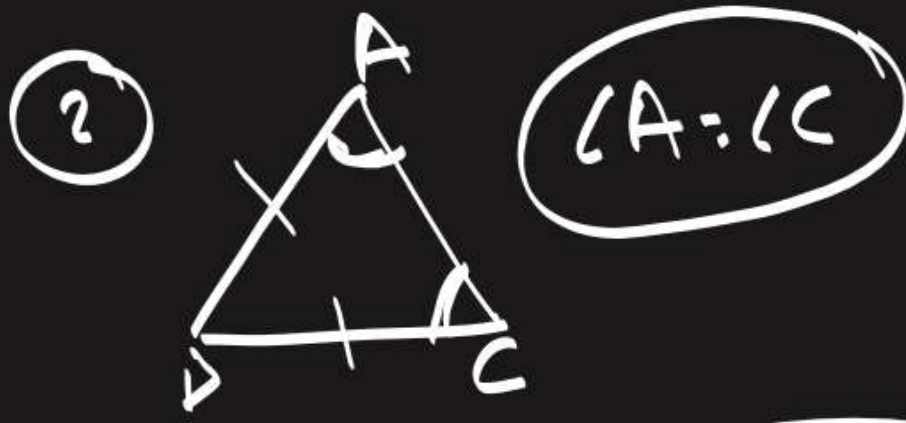
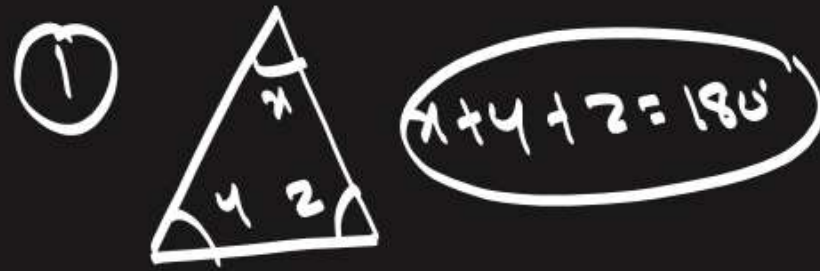
$$OC = r \operatorname{cosec} \frac{\alpha}{2} \sin \beta$$



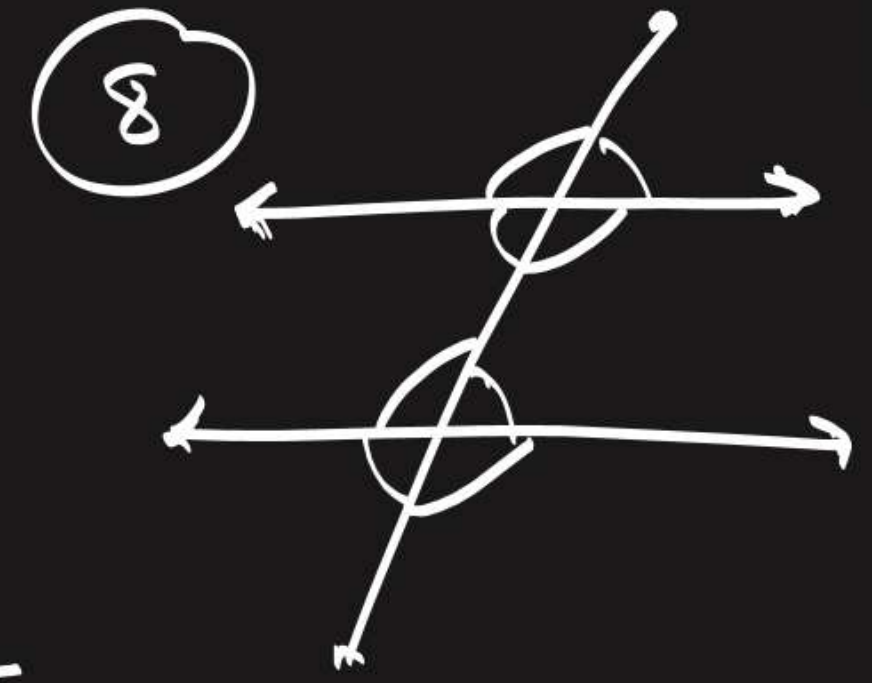
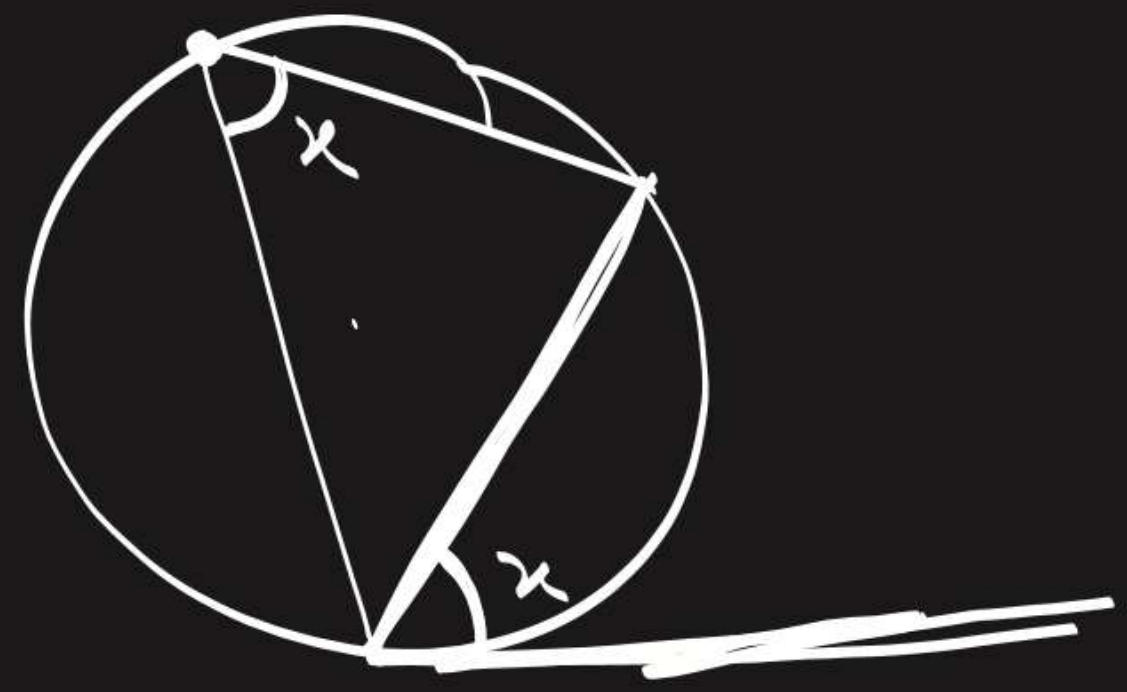


#Q. A spherical balloon of radius r subtends an angle of 60° at the eye of an observer. if the angle of elevation of its centre is 45° from the same point, then prove that height of the centre of the balloon is $\sqrt{2}$ times its radius.





⑦ Alternate Segment theorem [chord-tangent theorem]



#Q. In figure below, PQ is a tangent to the circle with centre O. If $\angle OPQ = x$, $\angle POQ = y$, then $x + y$ is :

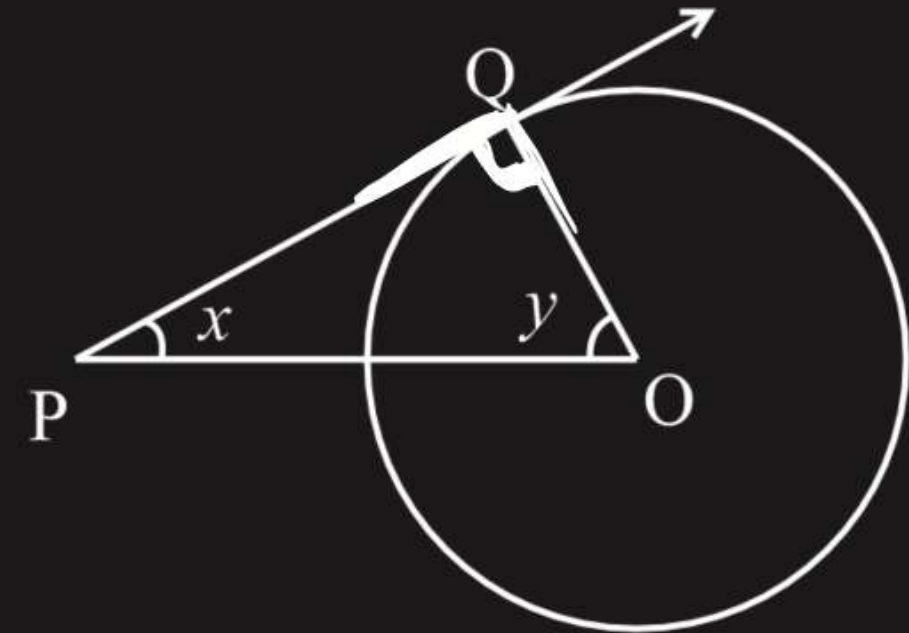
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A 45°

B 90°

C 60°

D 180°



#Q. In figure below, TA is a tangent to the circle with centre O such that $OT = 4$ cm, $\angle OTA = 30^\circ$, then length of TA is:

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A $2\sqrt{3}$ cm

B 2 cm

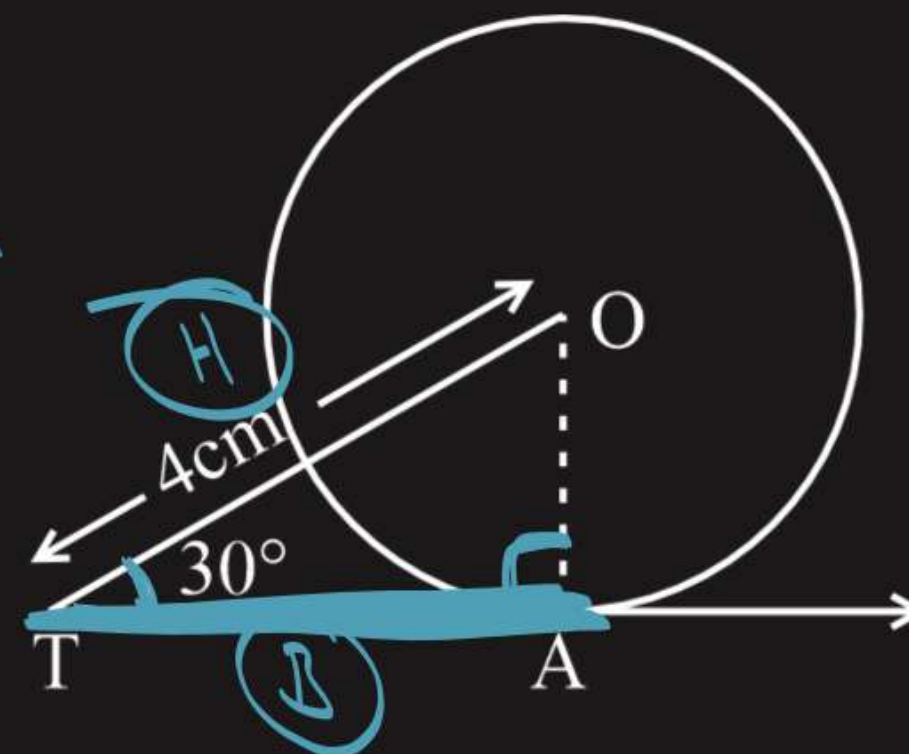
C $2\sqrt{2}$ cm

D $\sqrt{3}$ cm

$$\cos 30^\circ = \frac{TA}{OT}$$

$$\frac{\sqrt{3}}{2} = \frac{TA}{4}$$

$$2\sqrt{3} = TA$$



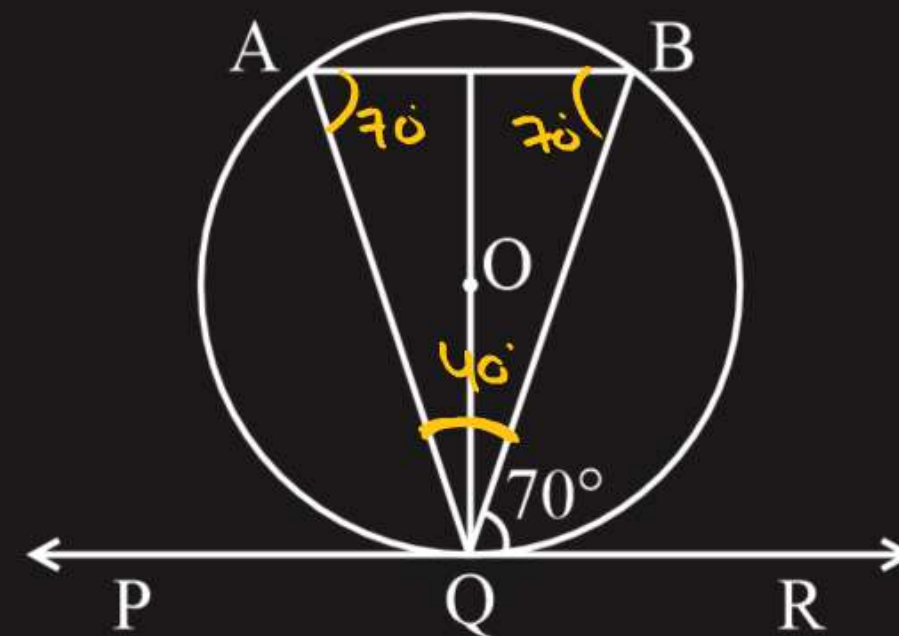
#Q. In figure below, if PQR is the tangent to a circle at Q whose centre is O, AB is a chord parallel to PR and $\angle BQR = 70^\circ$, then $\angle AQB$ is equal to:

A 20°

B 40°

C 35°

D 45°



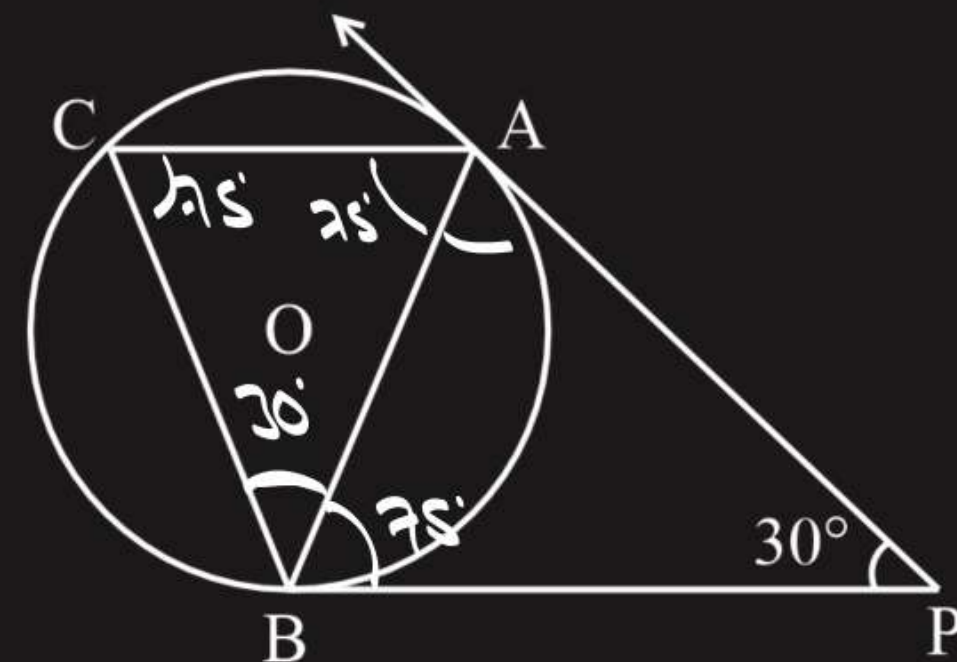
#Q. In figure below, if tangents PA and PB are drawn to a circle such that $\angle APB = 30^\circ$ and chord AC is drawn parallel to the tangent PB, then $\angle ABC =$

A 60°

B 90°

C 30°

D None of these



Based on given information, answer the following questions.

(i) In given figure, the measure of $\angle ROQ$ is:

- (a) 60° (b) 100° ~~(c) 150°~~ (d) 90°

(ii) In given figure, the measure of $\angle RQP$ is:

- ~~(a) 75°~~ (b) 60° (c) 30° (d) 90°

(iii) In given figure, the measure of $\angle RSQ$ is:

- (a) 60° ~~(b) 75°~~ (c) 100° (d) 30°

(iv) In given figure, the measure of $\angle ORP$ is:

- ~~(a) 90°~~ (b) 70° (c) 100° (d) 60°

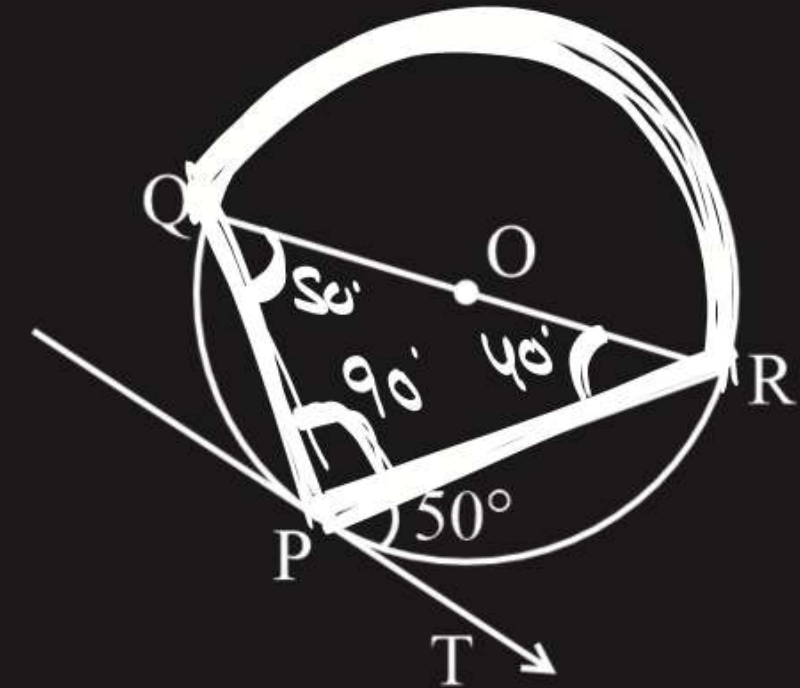
#Q. In figure below, PT is a tangent to the circle at P and QR is a diameter of the circle, if $\angle RPT = 50^\circ$, then $\angle QRP =$

A 50°

B 90°

C 60°

D 40°



#Q. In figure below, PA and PB are tangents from external point P to a circle with centre C and Q is only opint on the circle. Then the measure of $\angle AQB$ is:

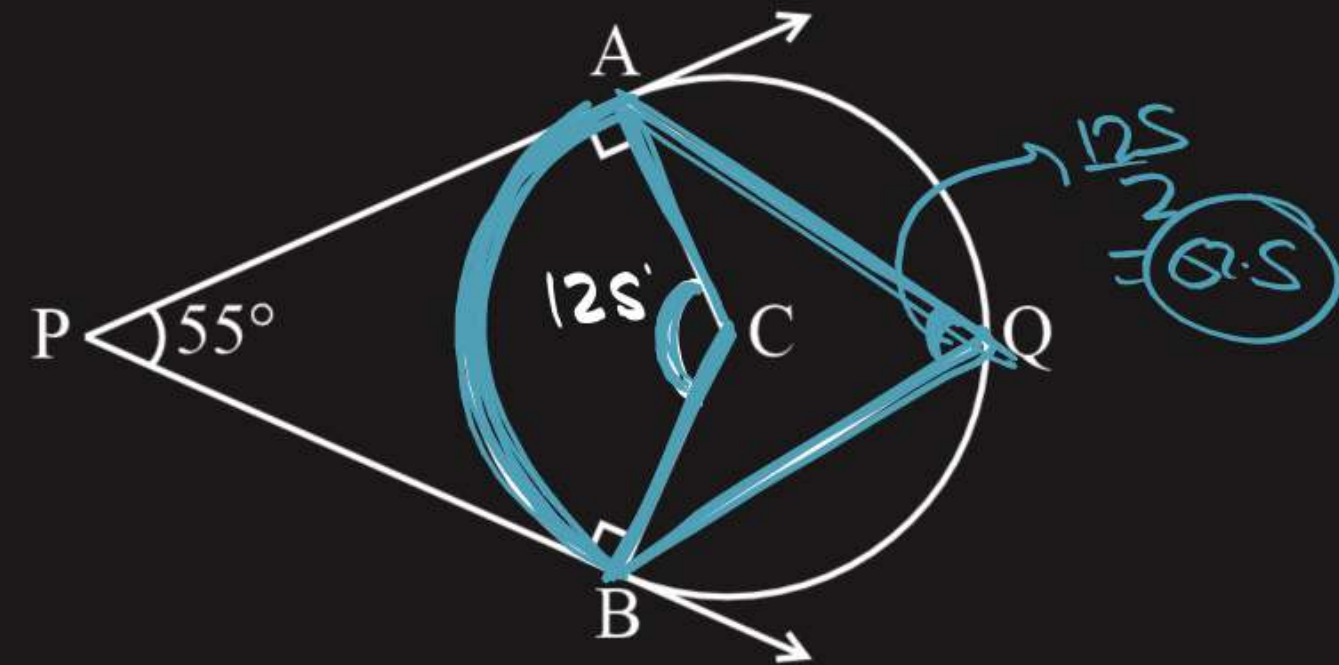
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A 62.5°

B 125°

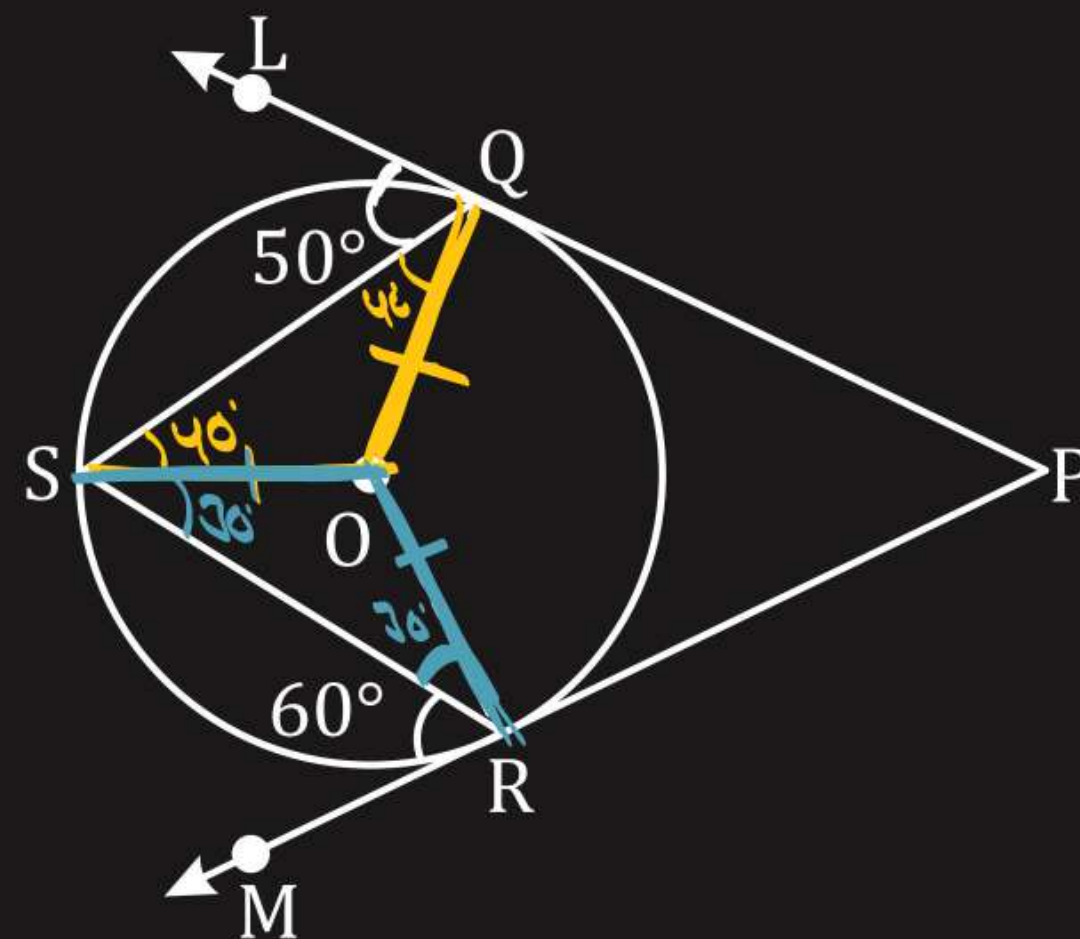
C 55°

D 90°

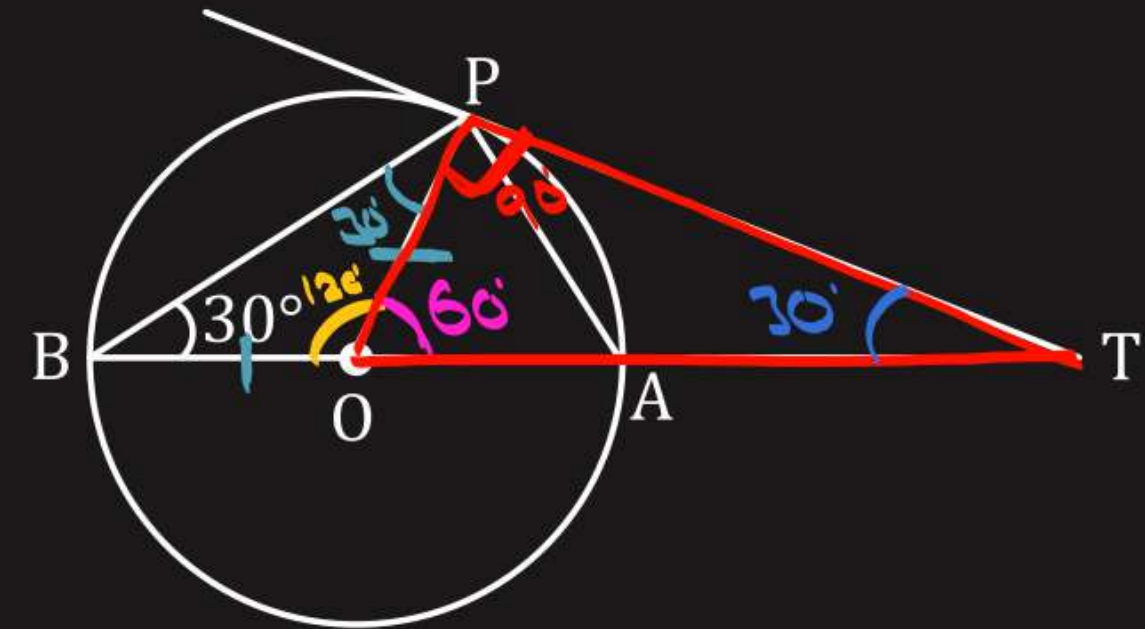


#Q. In fig. PQL and PRM are tangents to the circle with centre O at the points Q and R respectively and S is the point on the circle such that $\angle SQL = 50^\circ$, $\angle SRM = 60^\circ$. Then find $\angle QSR$.

70



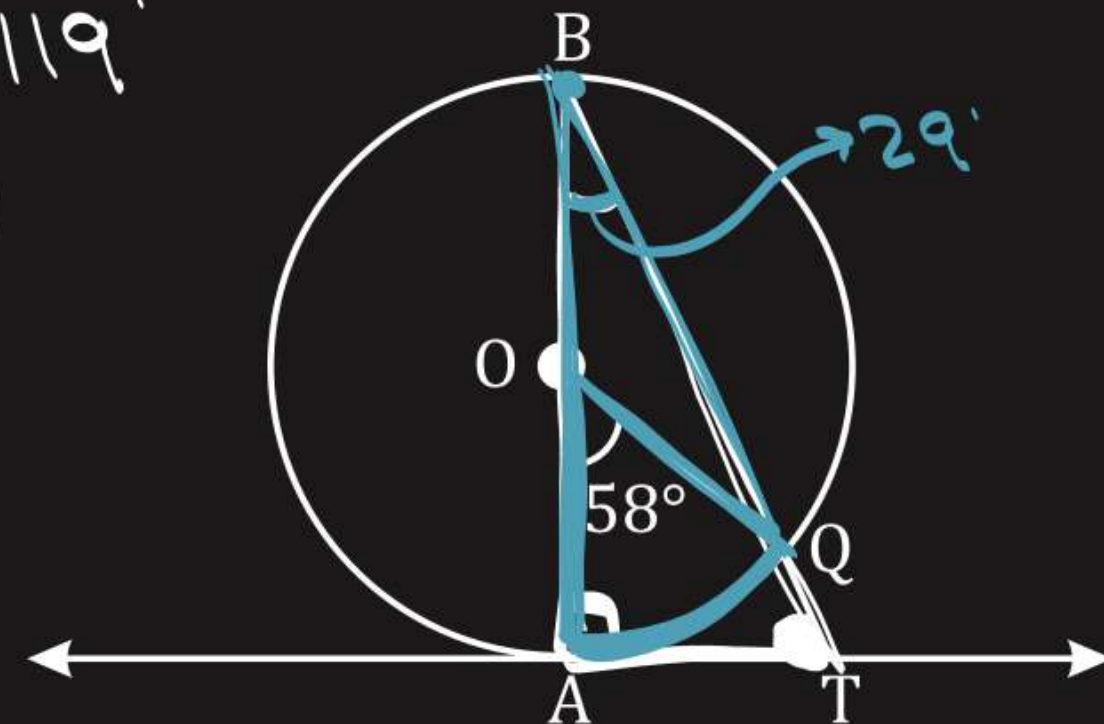
#Q. In fig. BOA is a diameter of a circle and the tangent at a point P meets BA produced at T. If $\angle PBO = 30^\circ$, then find $\angle PTA$.



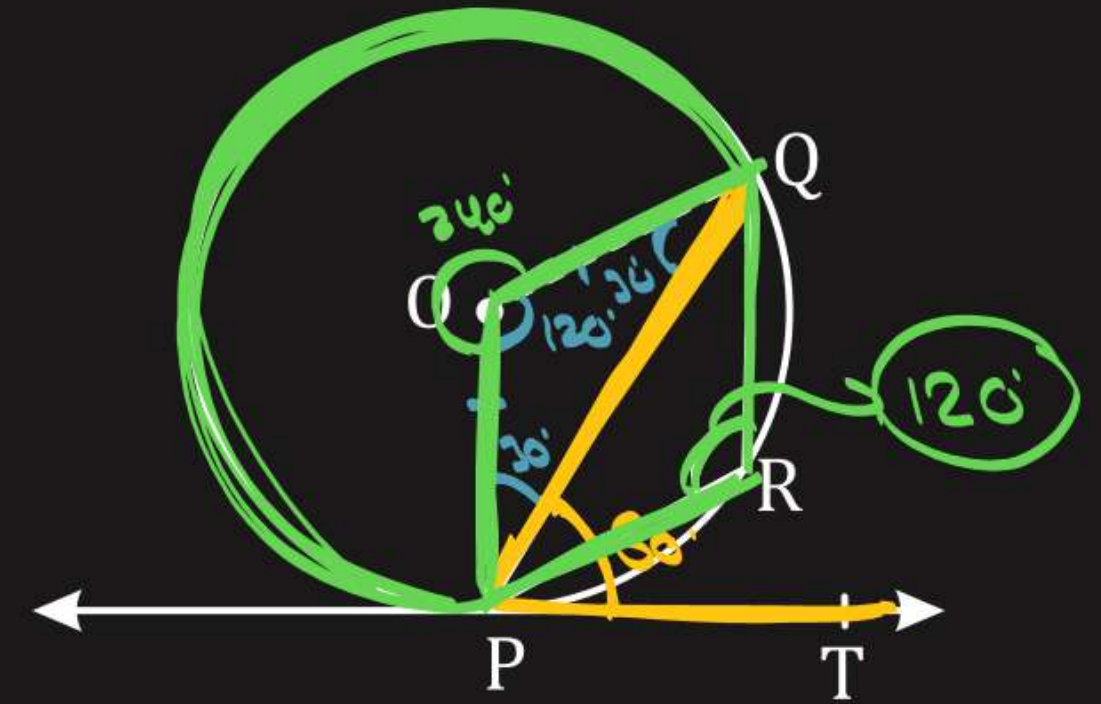
#Q. In fig. AB is a diameter of a circle with centre O and AT is a tangent. If $\angle AOQ = 58^\circ$, find $\angle ATQ$.

CBSE 2015

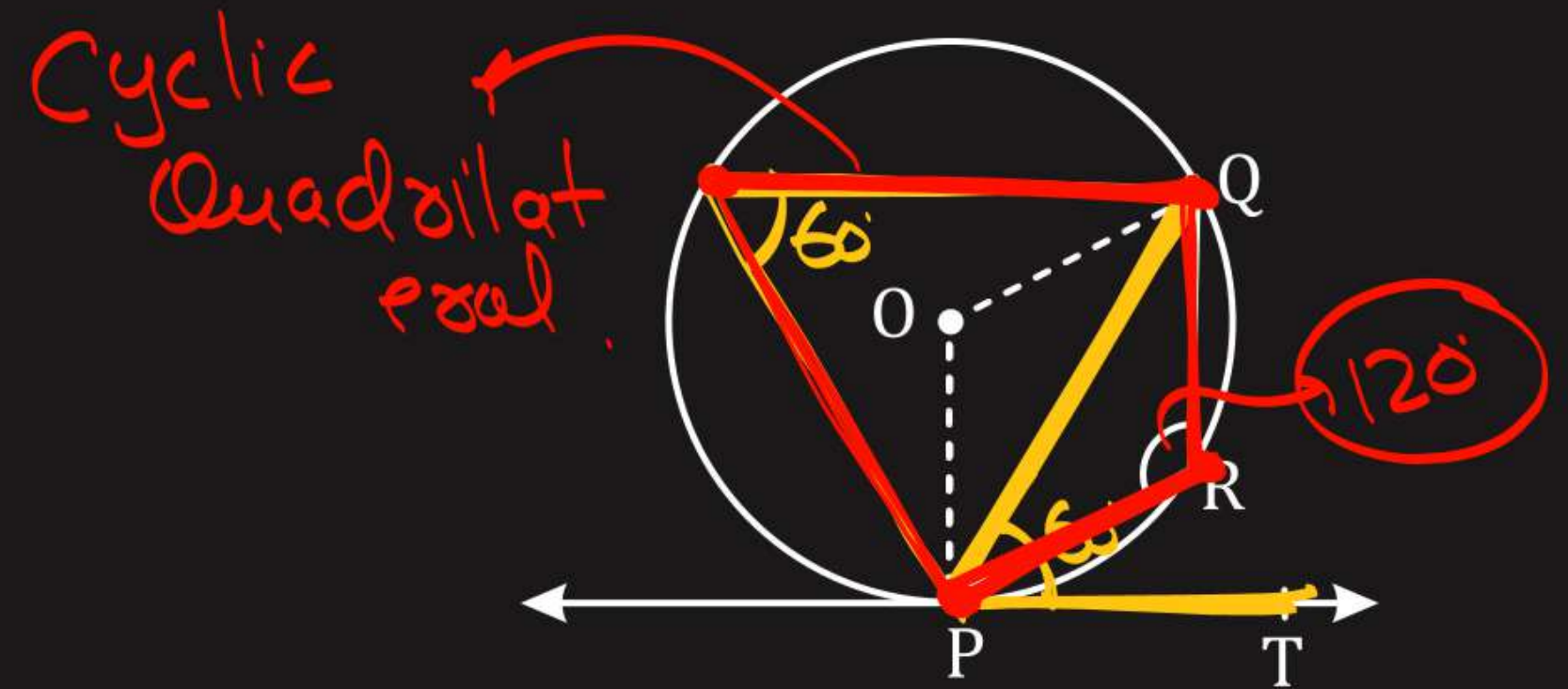
$$\begin{aligned}\angle ATQ + 90^\circ + 29^\circ &= 180^\circ \\ \angle ATQ &= 180^\circ - 119^\circ \\ &= \boxed{61^\circ}\end{aligned}$$



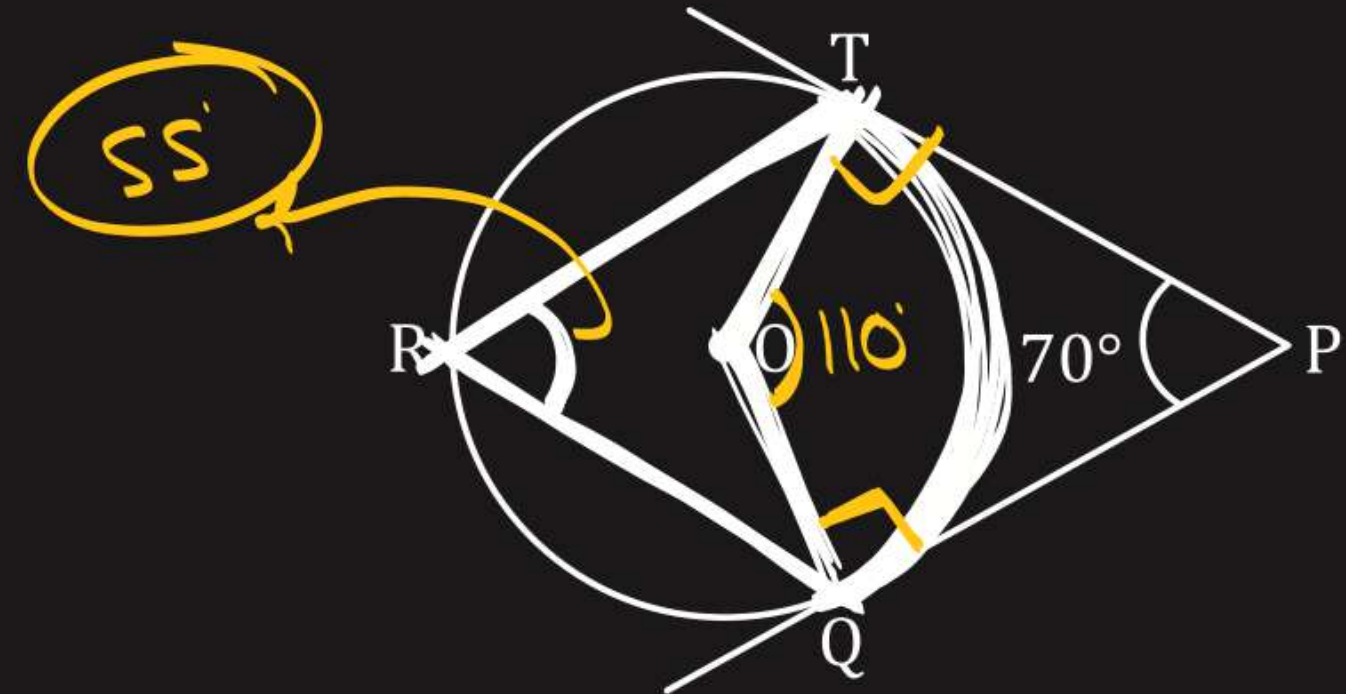
#Q. In fig. PQ is a chord of a circle centre O and PT is a tangent. If $\angle QPT = 60^\circ$, find $\angle PRQ$.



#Q. In fig. PQ is a chord of a circle centre O and PT is a tangent. If $\angle QPT = 60^\circ$, find $\angle PRQ$.

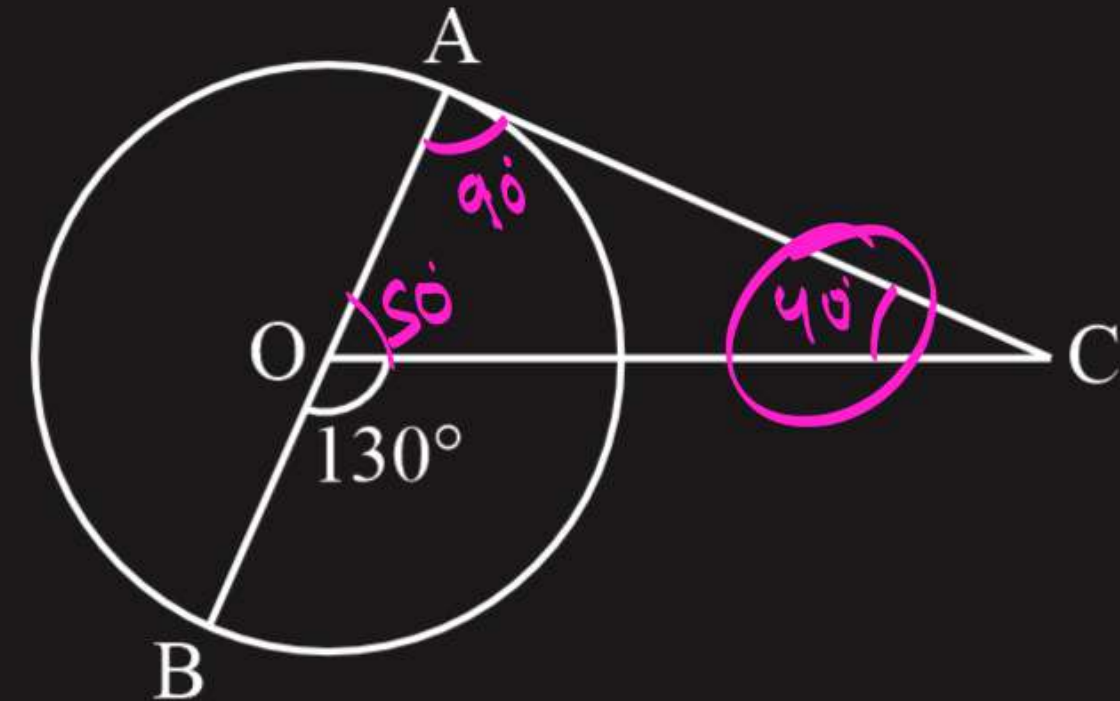


#Q. In fig., O is the centre of a circle. PT and PQ are tangents to the circle from an external point P. If $\angle TPQ = 70^\circ$, find $\angle TRQ$.



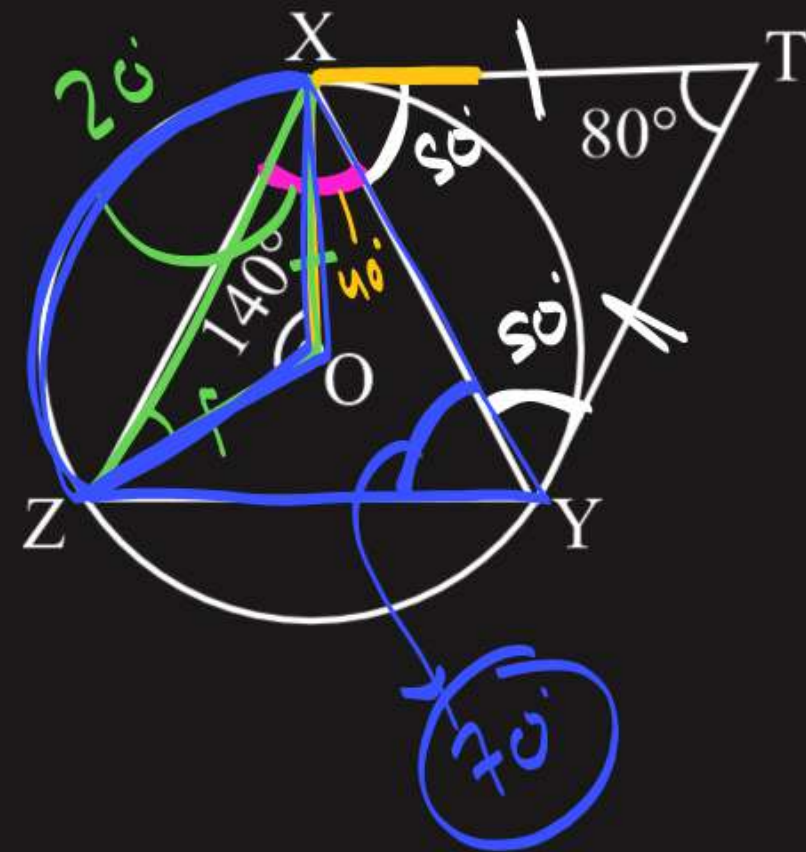
The diagram shows a triangle PAB with a circle passing through points A and B . The circle is tangent to the extensions of sides PA and PB at points C and D respectively. The angle at vertex P is 90° . The angle at vertex A between the extension of PA and the chord AB is 135° . The angle at vertex B between the extension of PB and the chord AB is 45° . The angle at vertex A between the chord AB and the tangent line AC is 45° . The angle at vertex B between the chord AB and the tangent line BD is 45° . The radius of the circle is 4 cm .

#Q. In the given figure, AOB is a diameter of a circle with center O and AC is a tangent to the circle at A. If $\angle BOC = 130^\circ$, then find $\angle ACO$.



#Q. In the given figure, O is the centre of the circumcircle of triangle XYZ. Tangents at X and Y intersect at T. Given $\angle XTY = 80^\circ$ and $\angle XOZ = 140^\circ$. Find the value of $\angle ZXY$.

60



#Q. In the given figure, O is the centre of the circle and QPR is a tangent to it at P.
Prove that, $\angle QAP + \angle APR = 90^\circ$

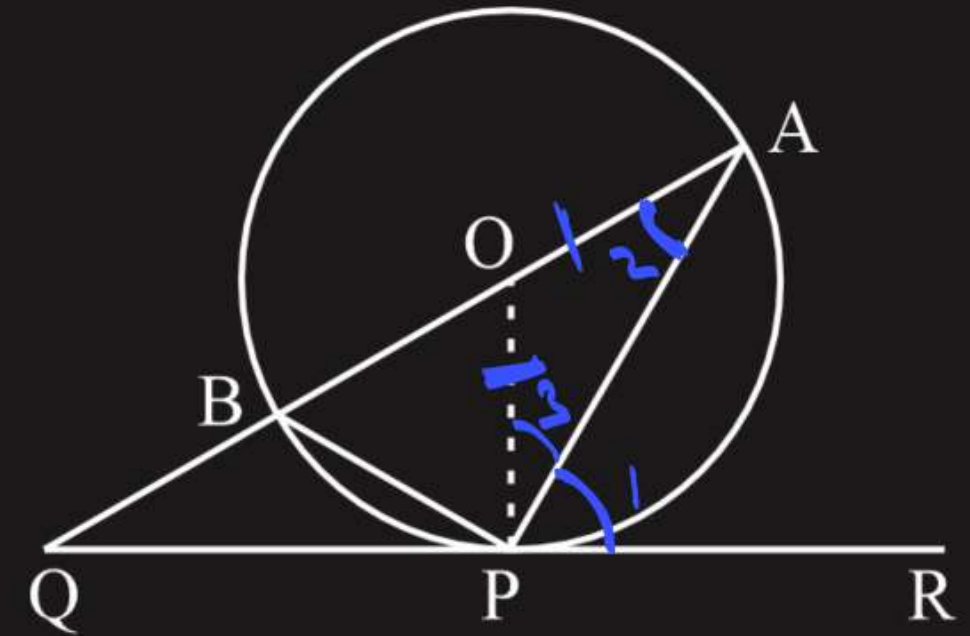
Given:

To prove: $\angle 1 + \angle 2 = 90^\circ$

Proof: $\angle 1 + \angle 3 = 90^\circ$

$\angle 2 = \angle 3$

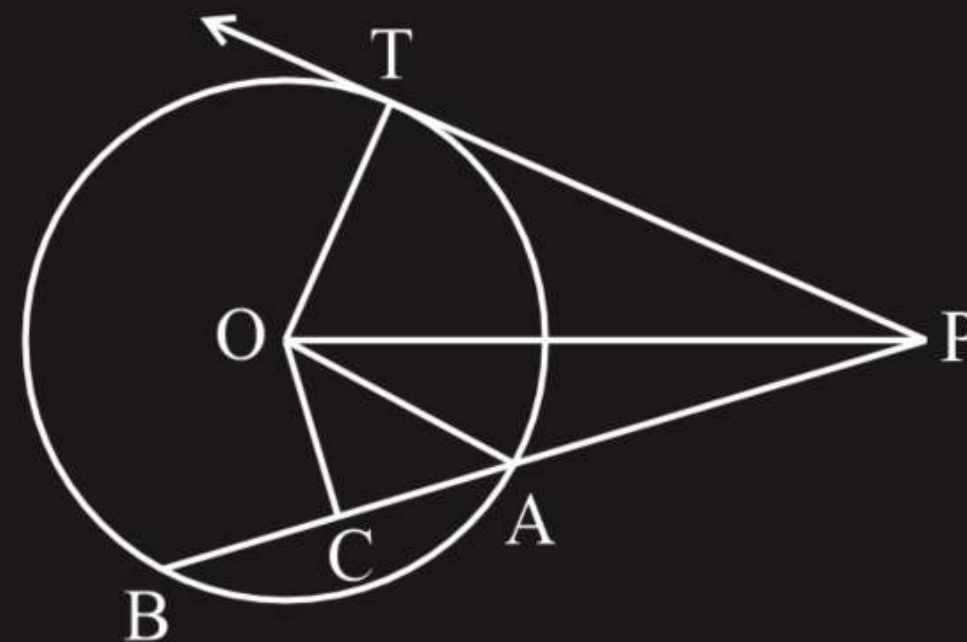
$\angle 1 + \angle 2 = 90^\circ //$

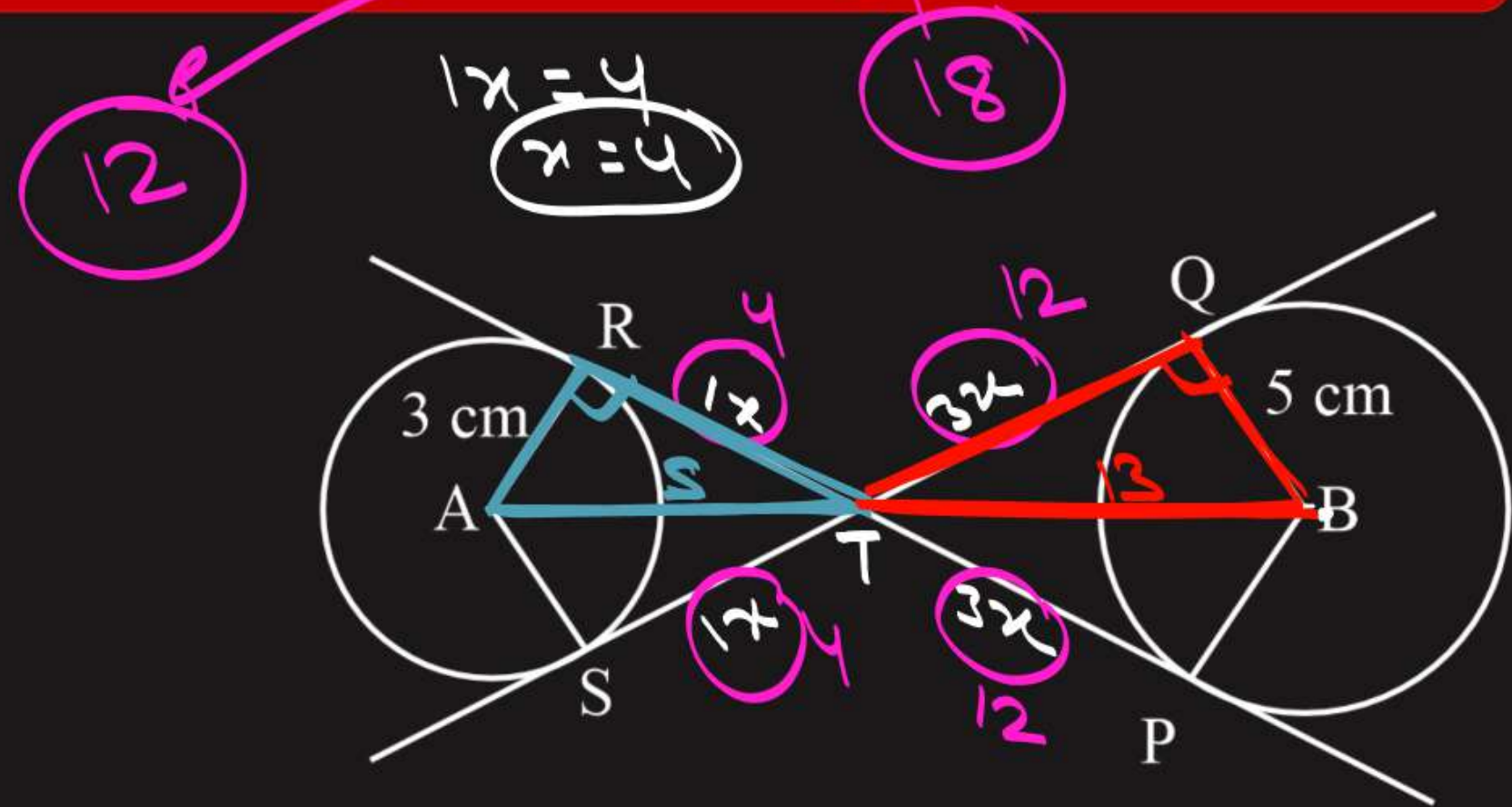


#Q. In the given figure, PT is a tangent to the circle centered at O. OC is perpendicular to chord AB. Prove that $PA \cdot PB = PC^2 - AC^2$.

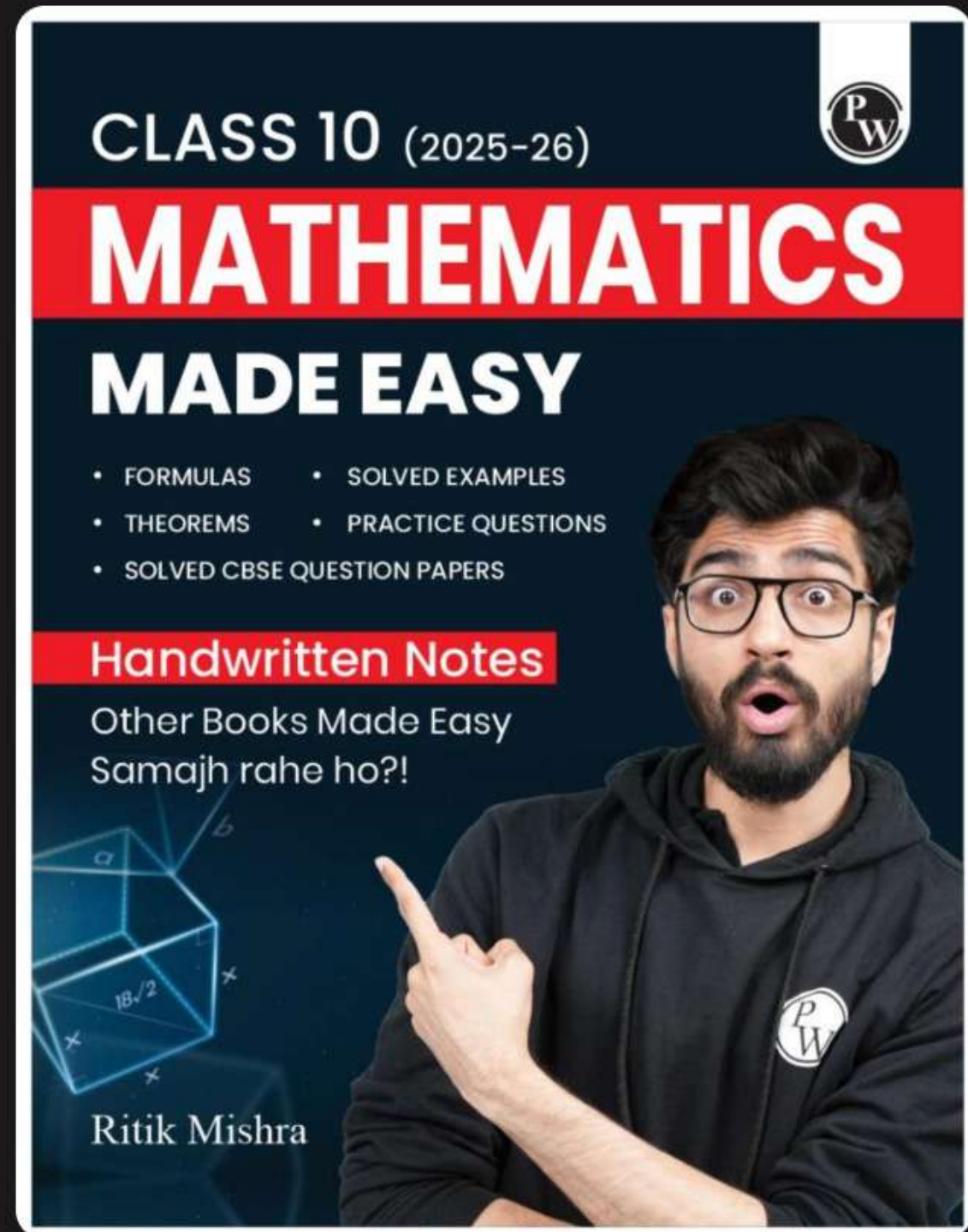
#Gp4

Hint:
 $PA = PC - CA$
 $PB = PC + BC$

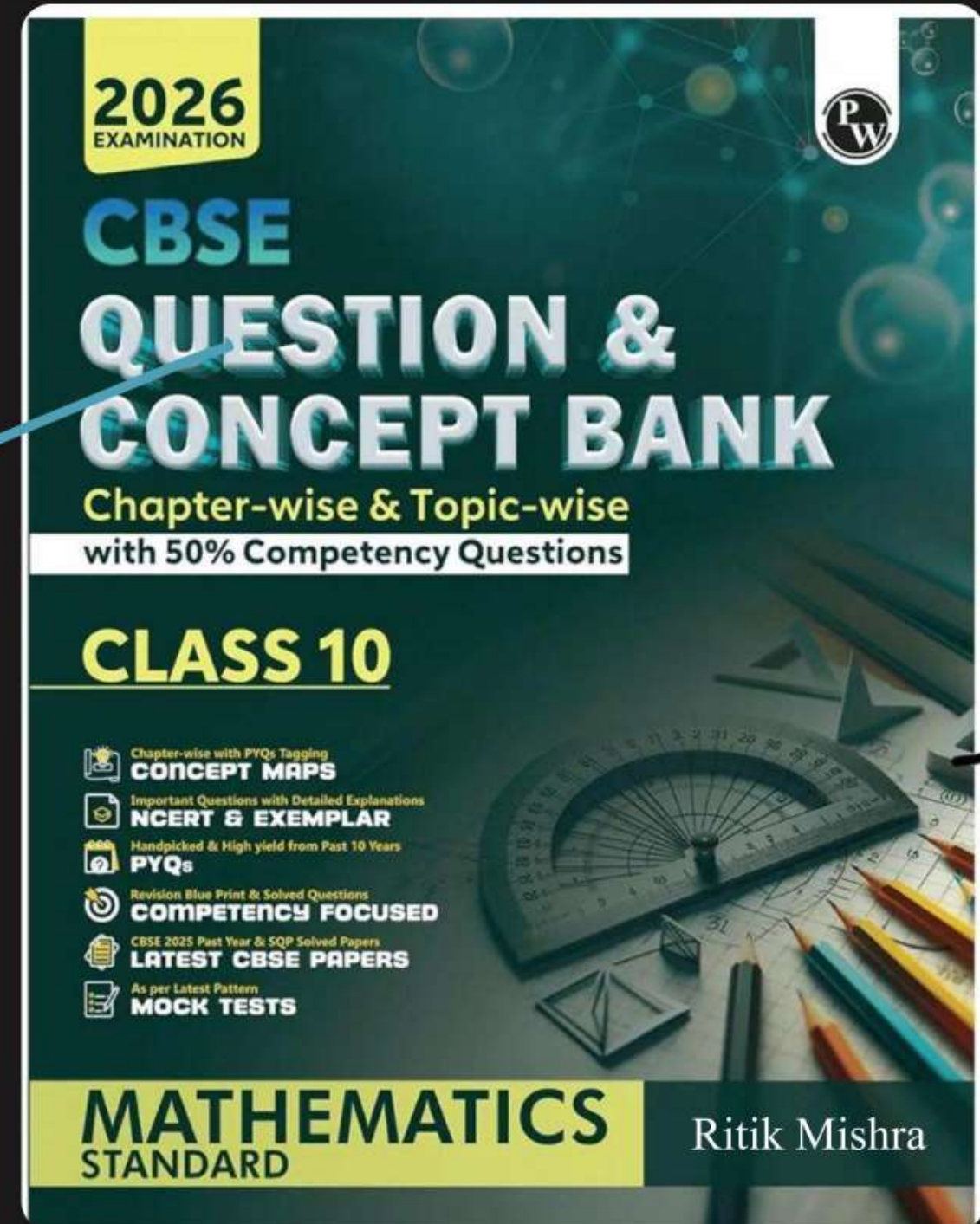




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