



# UDAAN



2026

Circles

MATHS

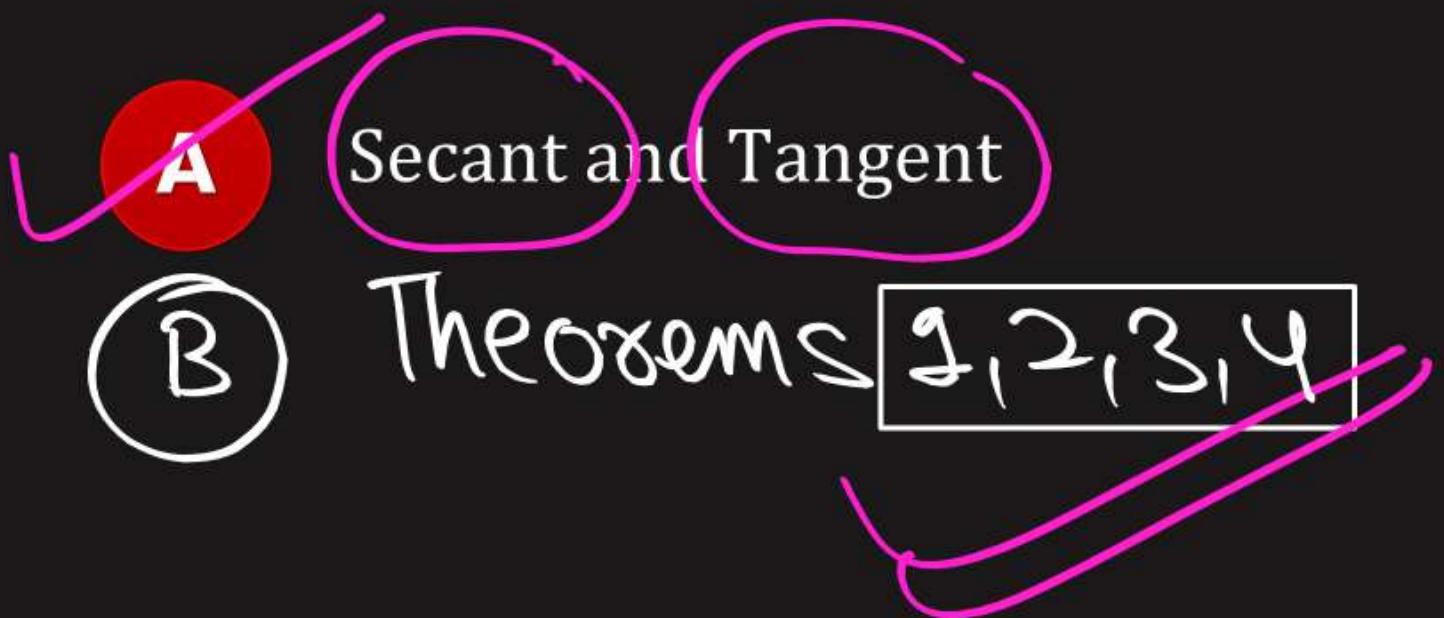
LECTURE-1

BY-RITIK SIR



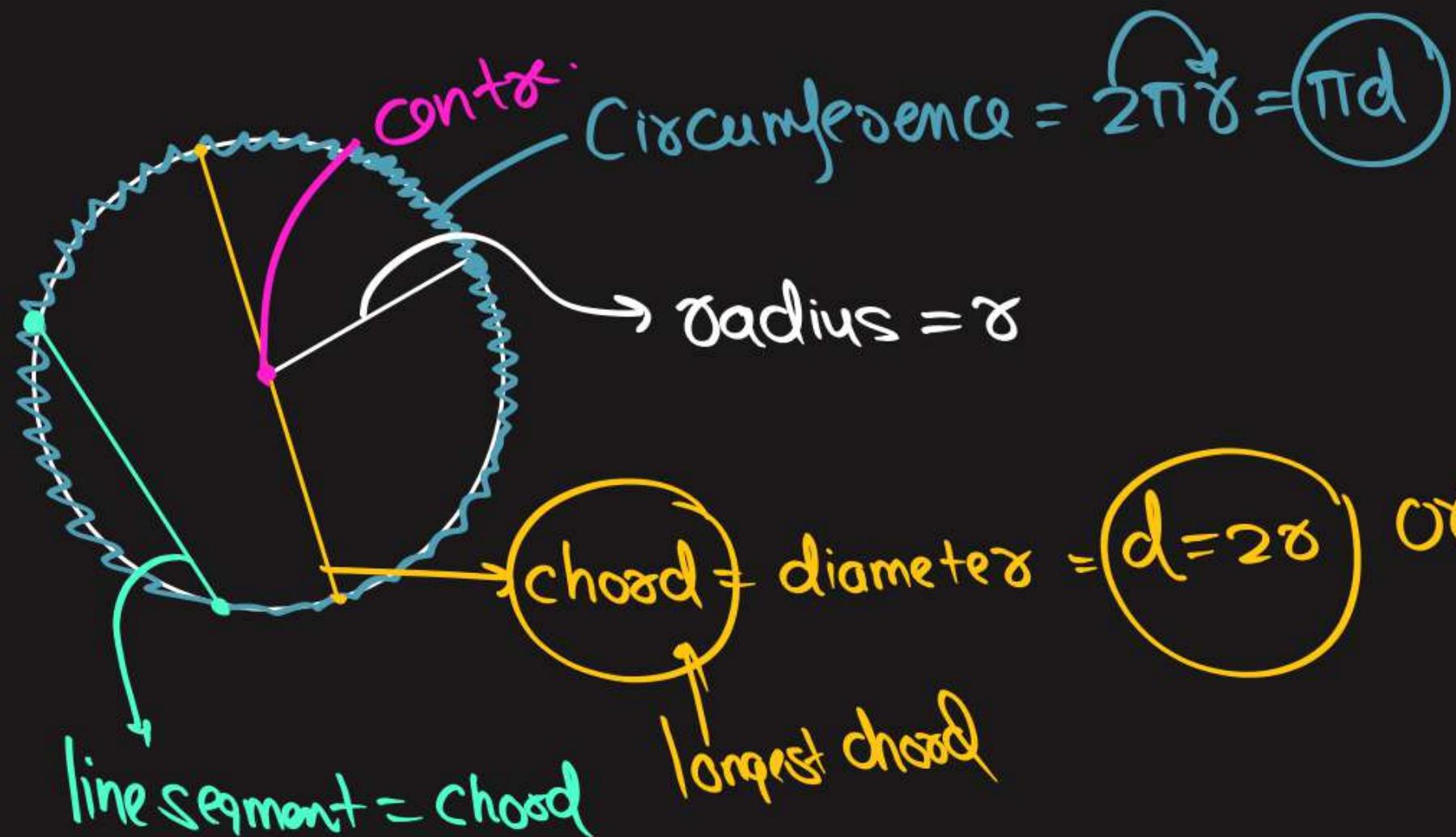
# Topics

to be covered



#SochnaSeeWho

NCERT //



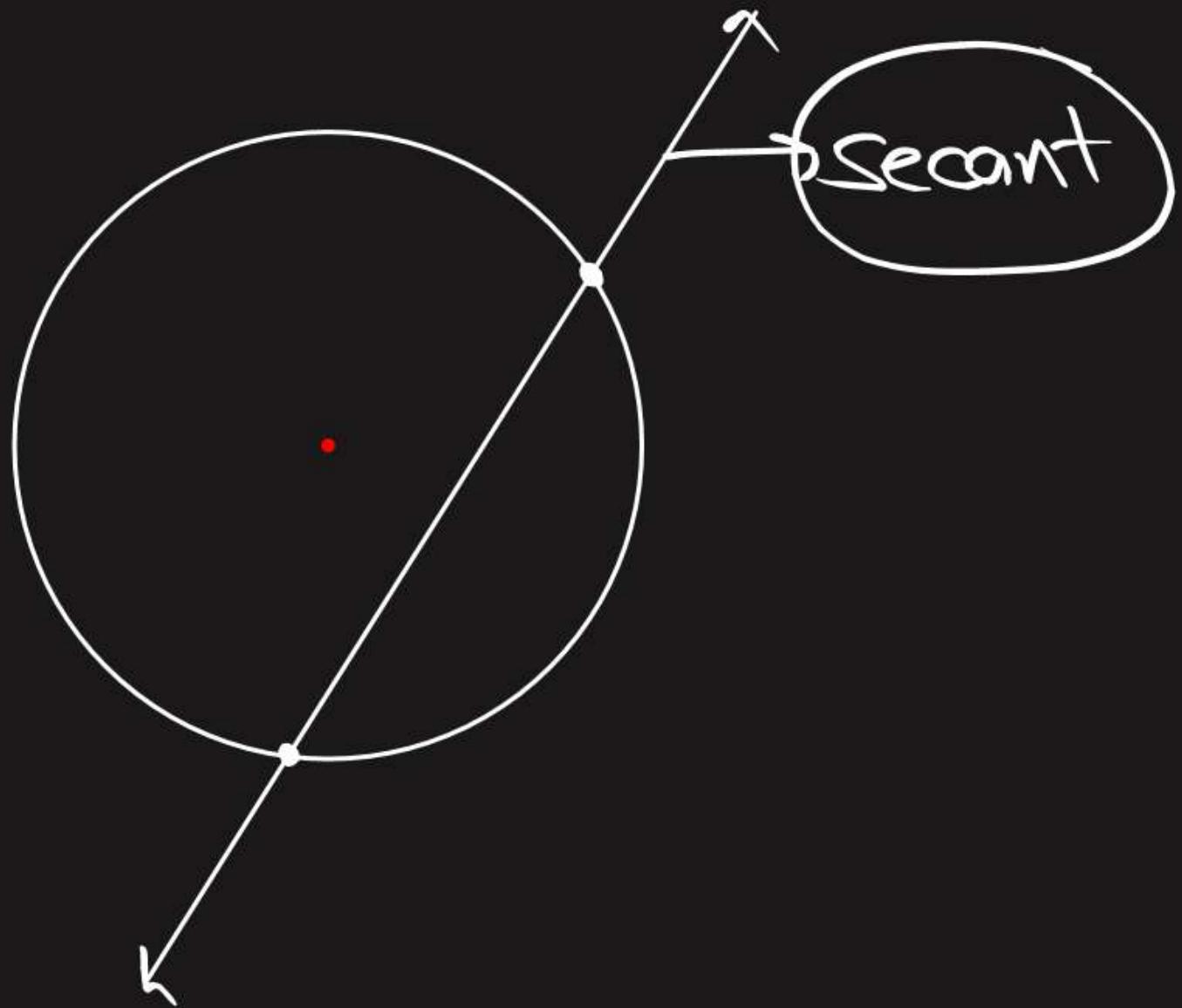
$$d = 2r \quad \text{or} \quad r = \frac{d}{2}$$



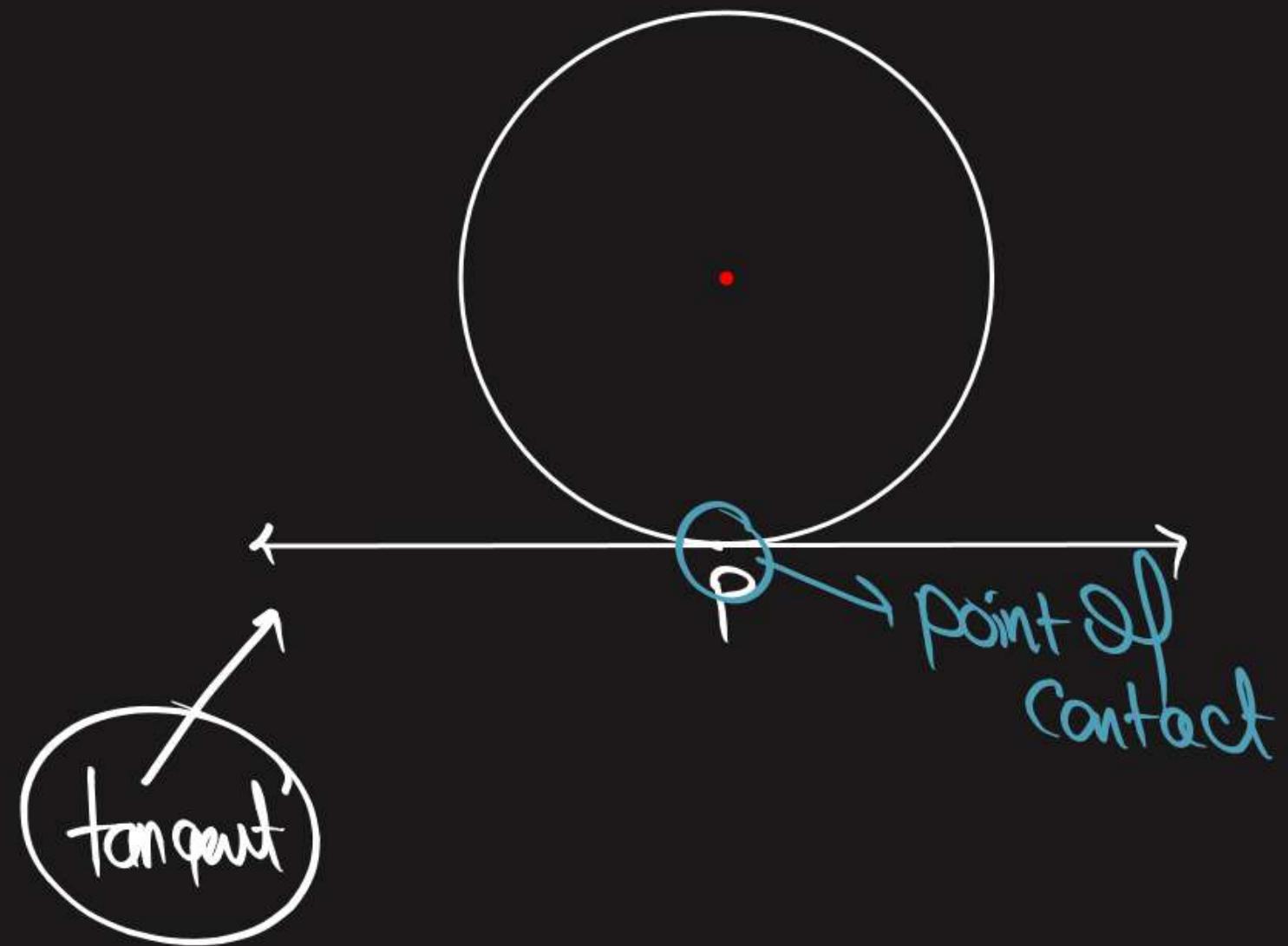
**Definition:** A circle is a collection of all those points in a plane which are at **fixed distance** from a **fixed point**.

↓  
radius  
Centre.

Secant



Tangent





## SECANT AND TANGENT



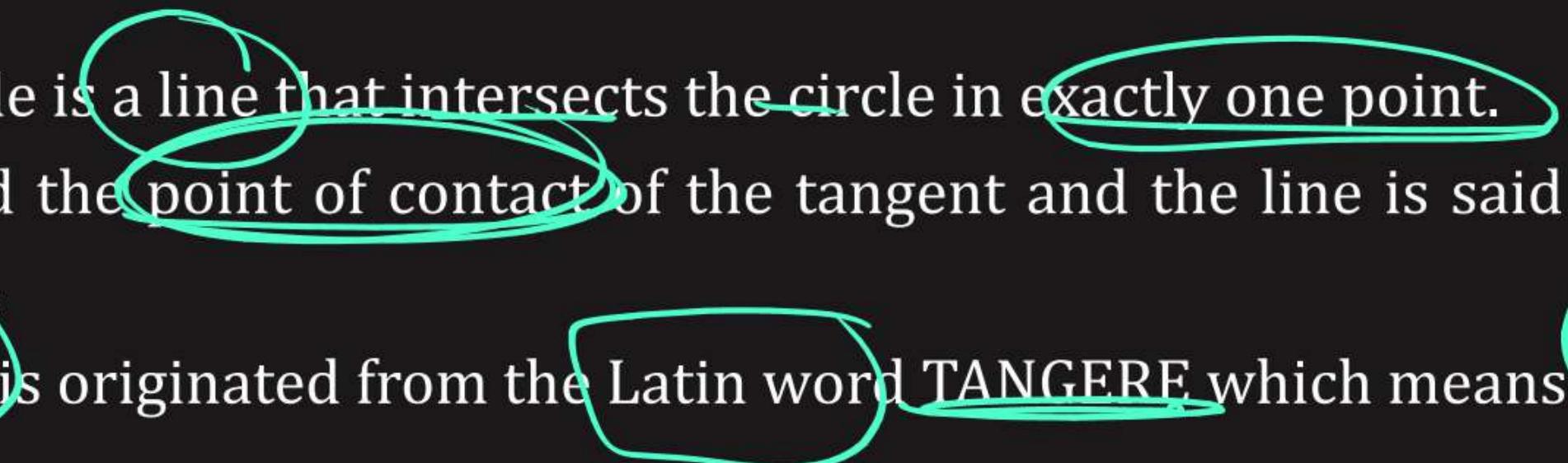
### SECANT:

- A line which intersects a circle in two distinct points is called a secant of the circle.



### TANGENT:

- A tangent to a circle is a line that intersects the circle in exactly one point.
- The point is called the point of contact of the tangent and the line is said to touch the circle at this point.
- The word tangent is originated from the Latin word TANGERE which means 'to touch'.

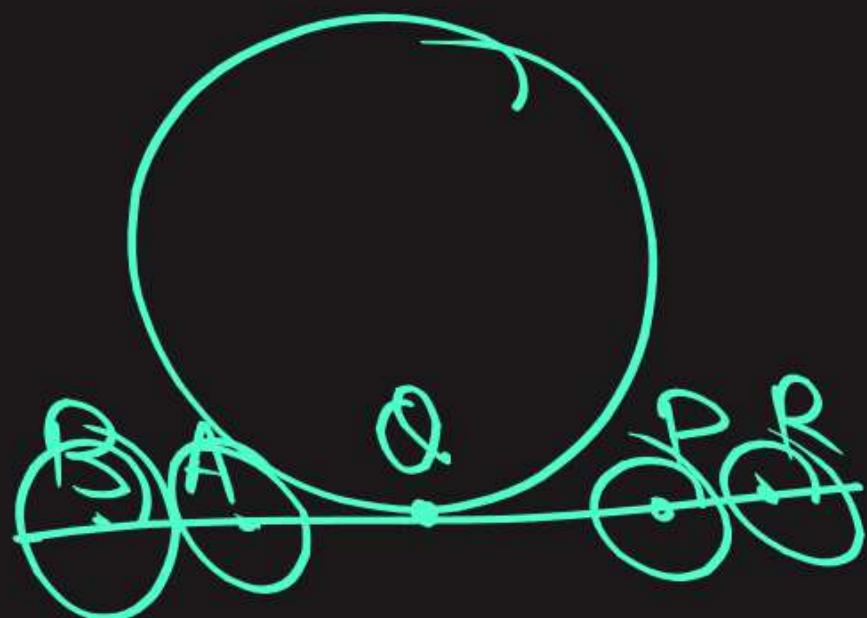




## SECANT AND TANGENT

### NOTE:

- The point of contact is the only point which is common to the tangent and the circle and every other point on the tangent lies outside the circle. Thus, of all the points on a tangent to a circle, the point of contact is nearest to the center of the circle.





## THEOREM 1

A tangent to a circle is perpendicular to the radius through the point of contact.

Given: A circle  $C(O, r)$  and a tangent  $AB$ , point of contact  $P$ .

**CBSE 2009, 12, 14, 15, 16**

To Prove:  $OP \perp AB$

Proof:  $OQ > OR$  ( $Q$  lies outside the circle)

$$OR = OP$$

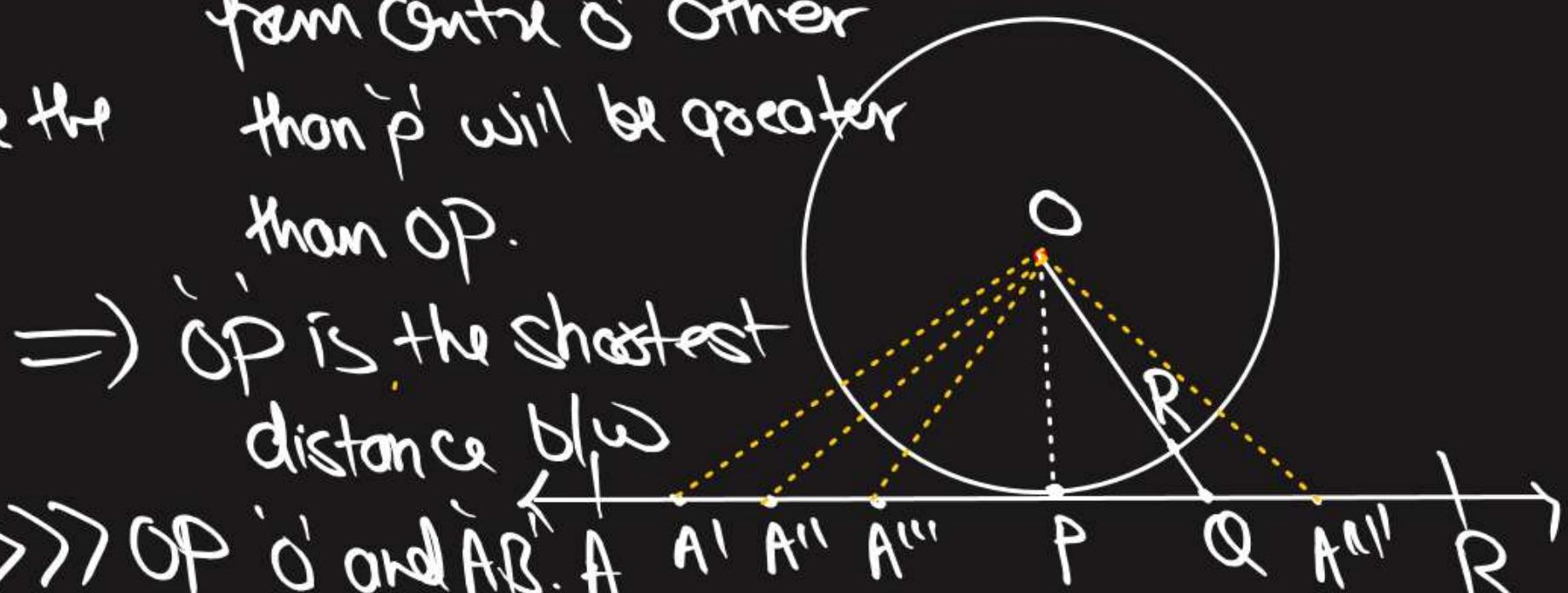
$$\Rightarrow OQ > OP$$

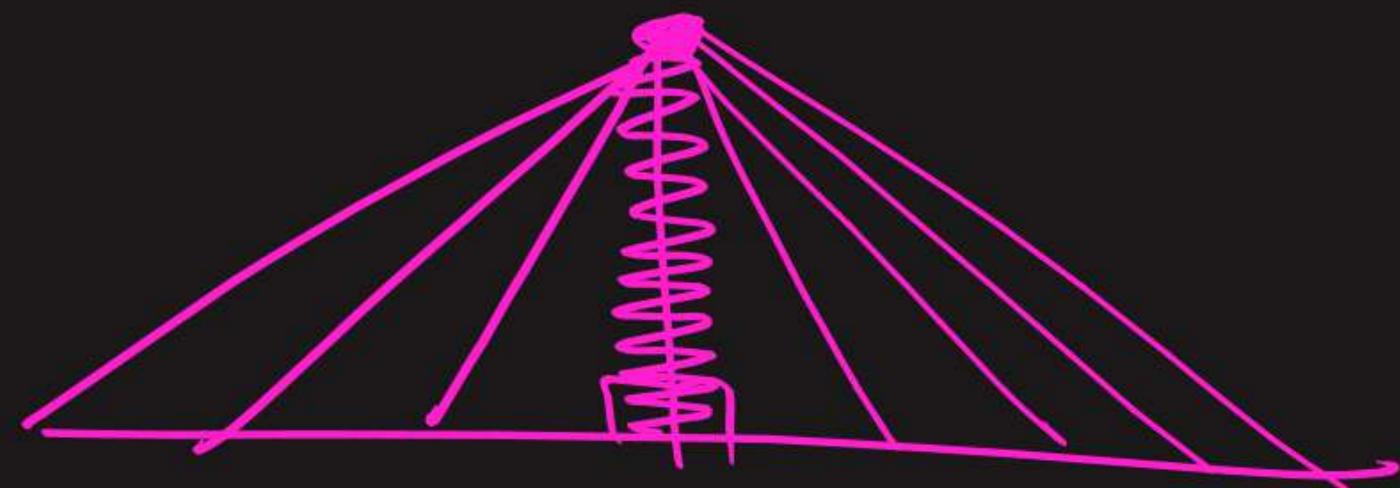
Similarly,  $OA', OA'', OA''', OA'''' >>> OP$  'd' and  $AB$ . A

Any point other than  $P$  will be greater than  $OP$ .

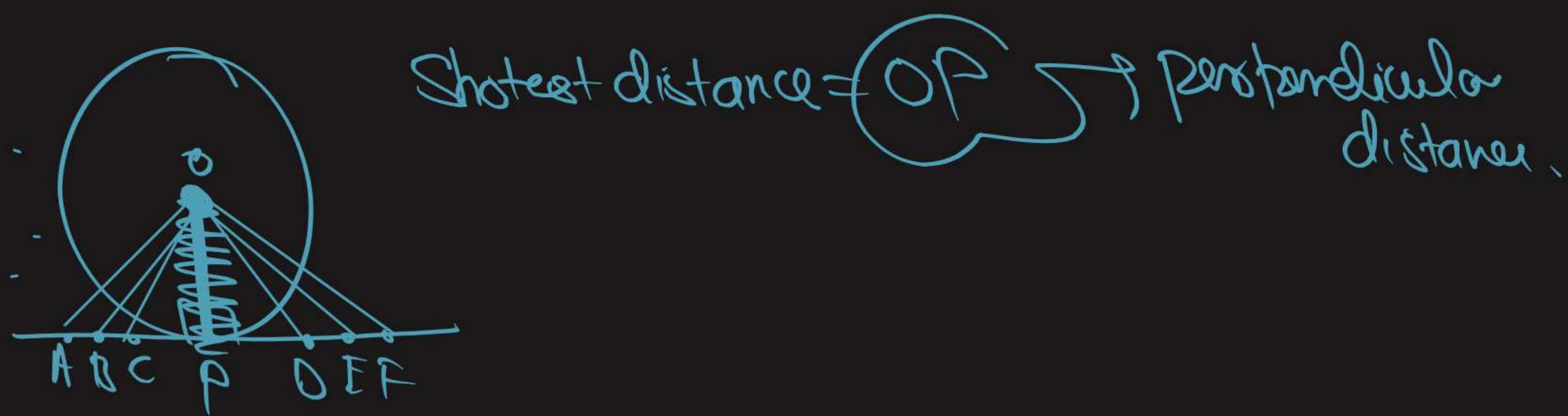
$\Rightarrow OP$  is the shortest distance b/w

also, shortest distance is  $\perp$  distance,  $\therefore OP \perp AB$





Shortest distance is always Perpendicular.





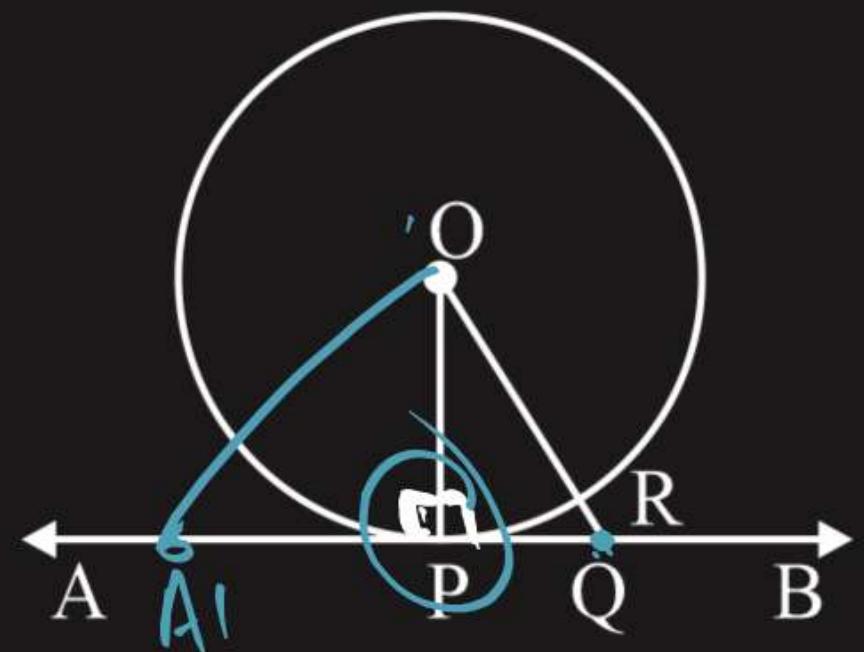
## THEOREM 2

A line drawn through the end point of a radius and perpendicular to it is a tangent to the circle.

Line  $\rightarrow$  tangent poore karna hai.

akhi point par touch.

CBSE 2012, 13



- ① Shortest distance = OP (because  $\rightarrow$  1st distance).
- ② OP  $\cong$  radius hai.

Given: A radius OP of a circle C (O, r) and a line APB, perpendicular to OP.

To Prove: AB is a tangent to the circle at the point P.

PROOF: Take a point Q, different from P, on the line AB.

Now,  $OP \perp AB$ .

$\Rightarrow$  Among all the line segments joining O to a point on AB  $OP$  is the shortest.

$\Rightarrow$   $OQ > OP$  and ' $OP$ ' is radius.

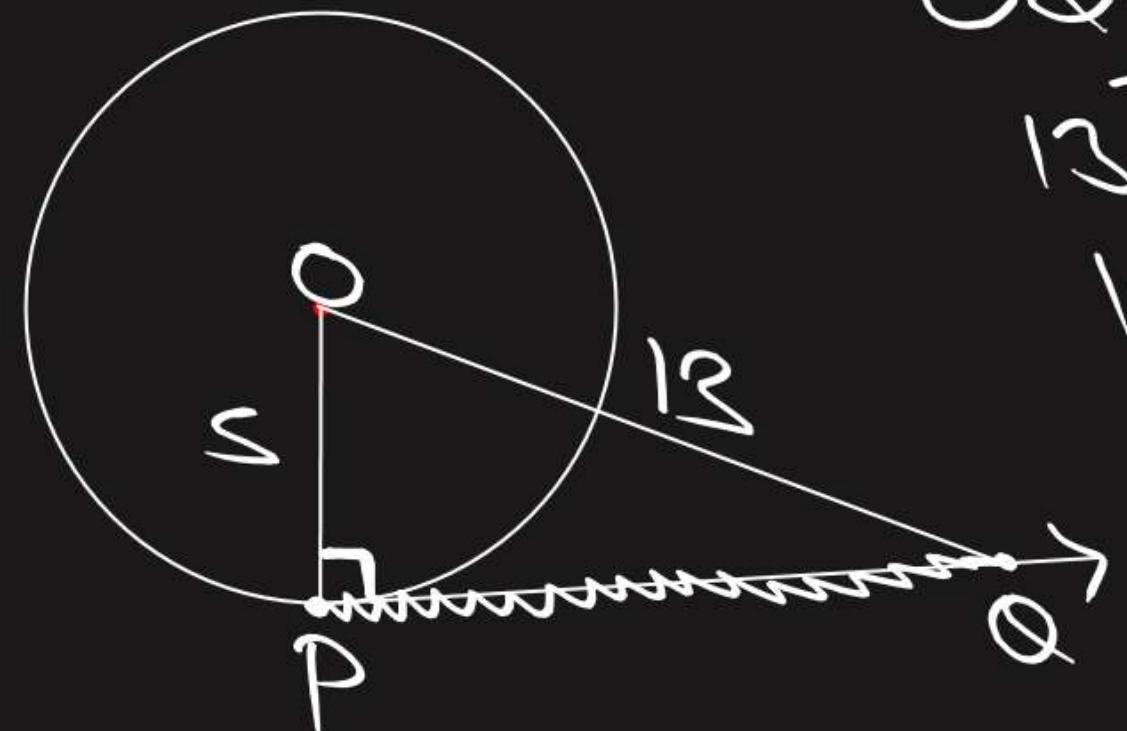
$\Rightarrow$  Q lies outside the circle.

Thus, every point on AB, other than P, lies outside the circle. This shows that AB meets the circle only at the point P.

Hence AB is a tangent to the circle at P.

*Point of control*

#Q. A tangent PQ at a point P of a circle of radius 5 cm meets a line through the centre O at a point Q so that  $OQ = 13 \text{ cm}$ . Find the length of PQ.



$$OQ^2 = OP^2 + PQ^2$$

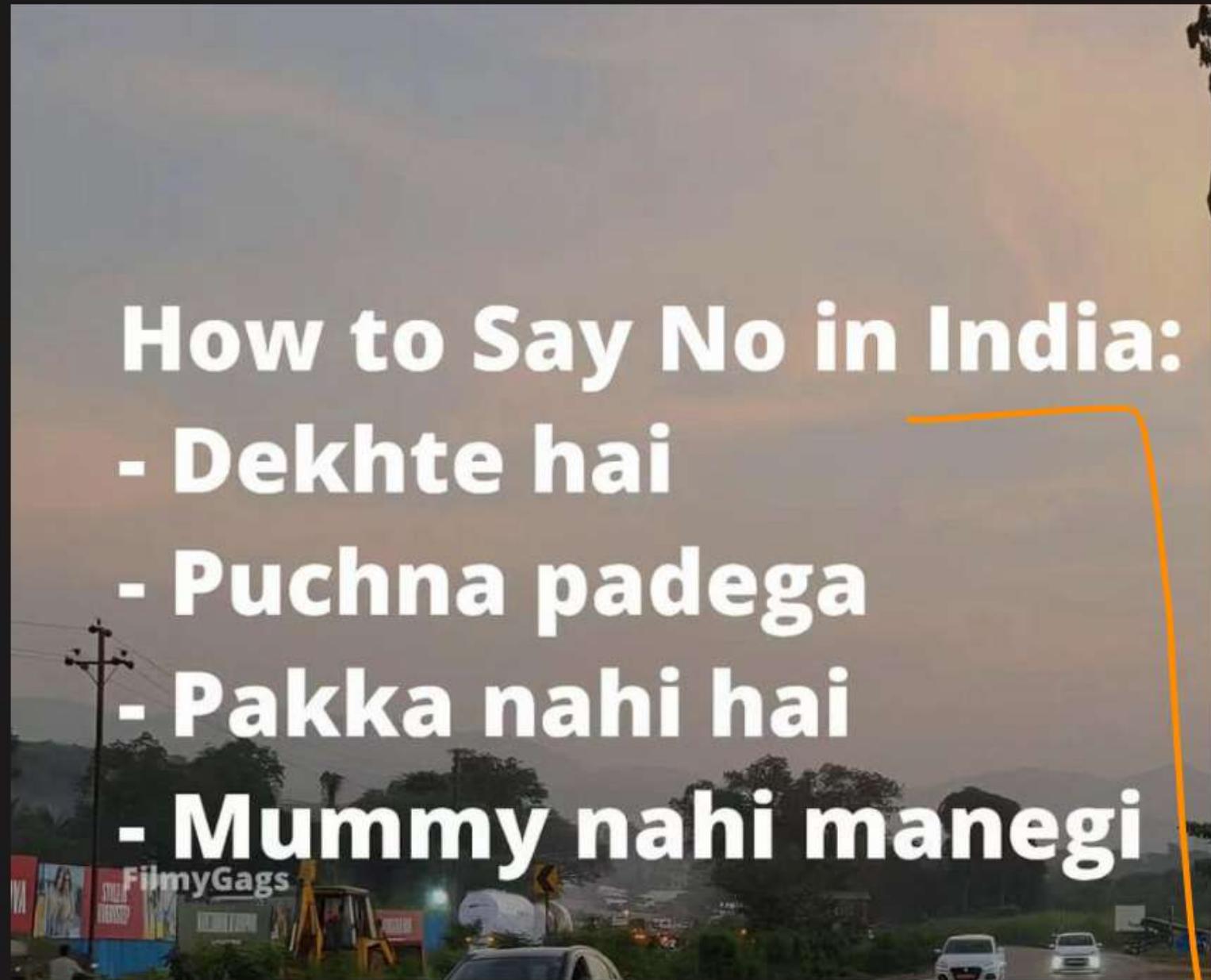
$$13^2 = 5^2 + PQ^2$$

$$169 - 25 = PQ^2$$

$$144 = PQ^2$$

$$\pm \sqrt{144} = PQ$$

$\pm 12 = PQ$   
 $12 \text{ cm} = PQ$



Naa

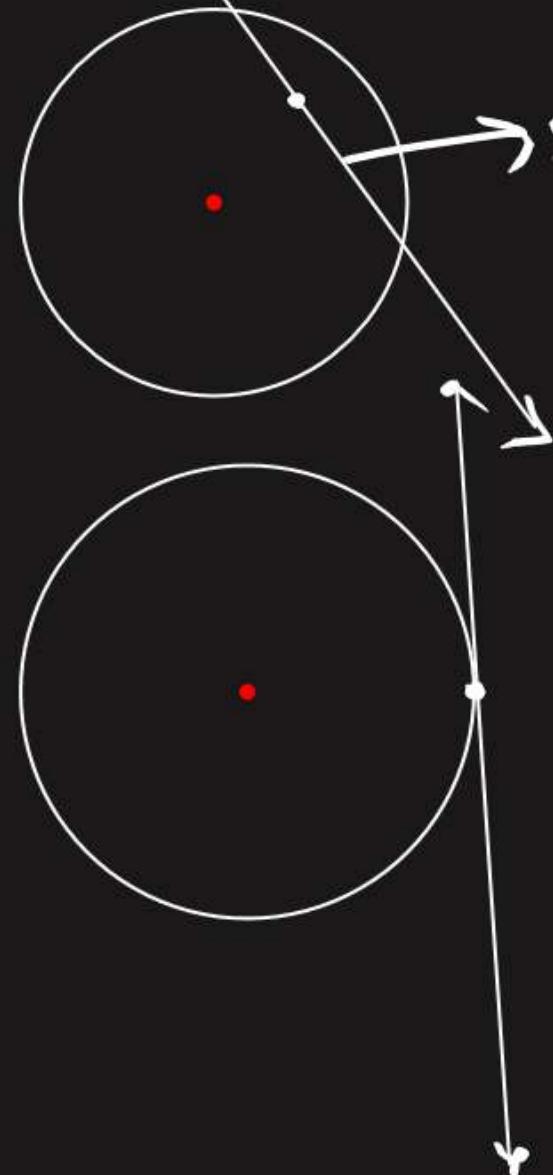
#Q. Show that tangent lies at the end points of a diameter of a circle are parallel.

**CBSE 2014, 17**

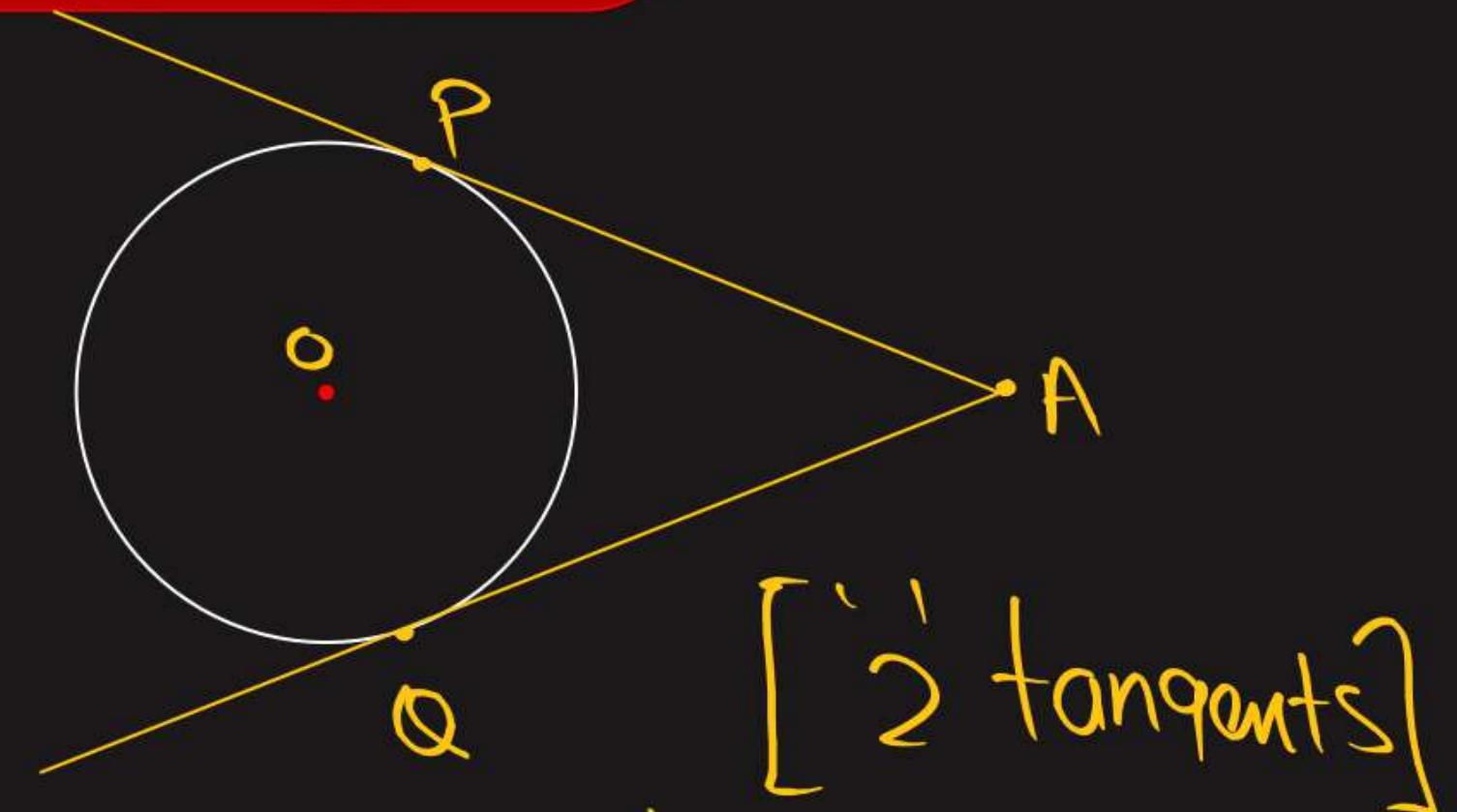


## TANGENTS FROM A POINT TO A CIRCLE

#OT<sup>10</sup>



secant [ '0' tangents ]  
[ '1' tangent ]



[ '2' tangents ]

These facts can be summarized as follows:

- (i) No tangent can be drawn to a circle from a point lying inside it.
- (ii) One and only one tangent can be drawn to a circle at a point on the circle.
- (iii) Two tangents can be drawn to a circle from a point lying outside it.



## THEOREM 3

The lengths of two tangents drawn from an external point to a circle are equal.

G: AP and AB are tangents to a circle.

**CBSE 2008, 09, 10, 13, 14, 15, 16, 17, 18**

To Prove:  $AP = AB$

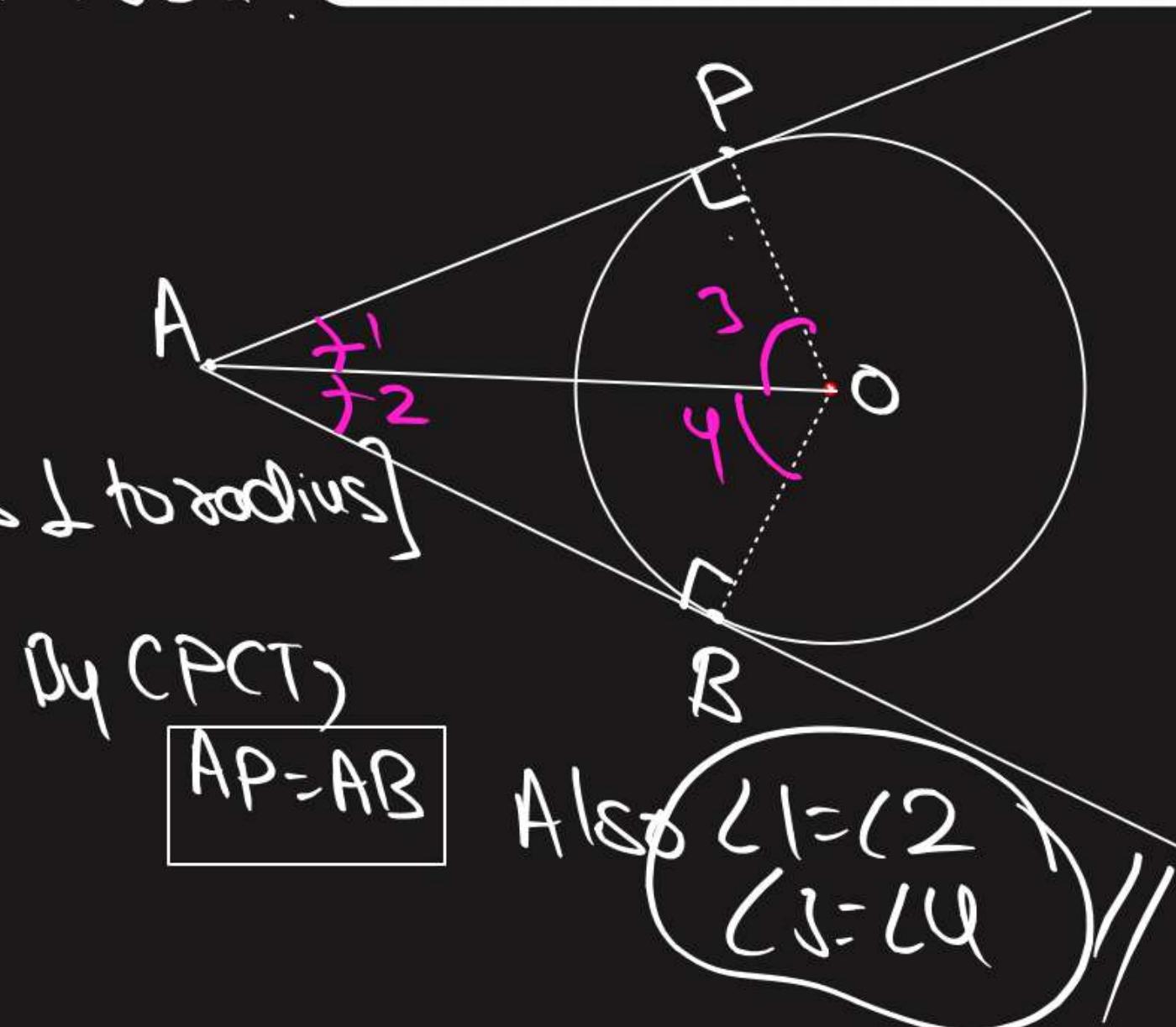
Proof: In  $\triangle APO$  and  $\triangle ABO$

$OB = OP$  (radius)

$\angle OPA = \angle OBA$  ( $90^\circ$ ) [tangent is  $\perp$  to radius]

$OA = AO$  (common)

By RHS,  $\triangle APO \cong \triangle ABO$





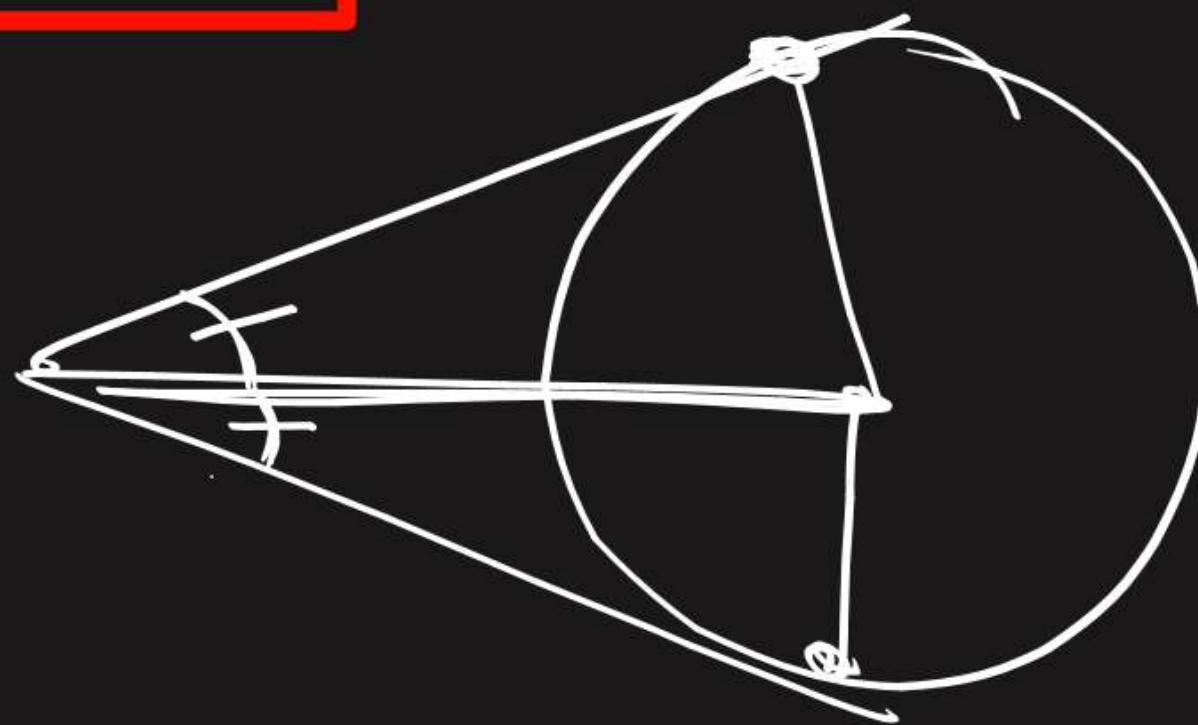
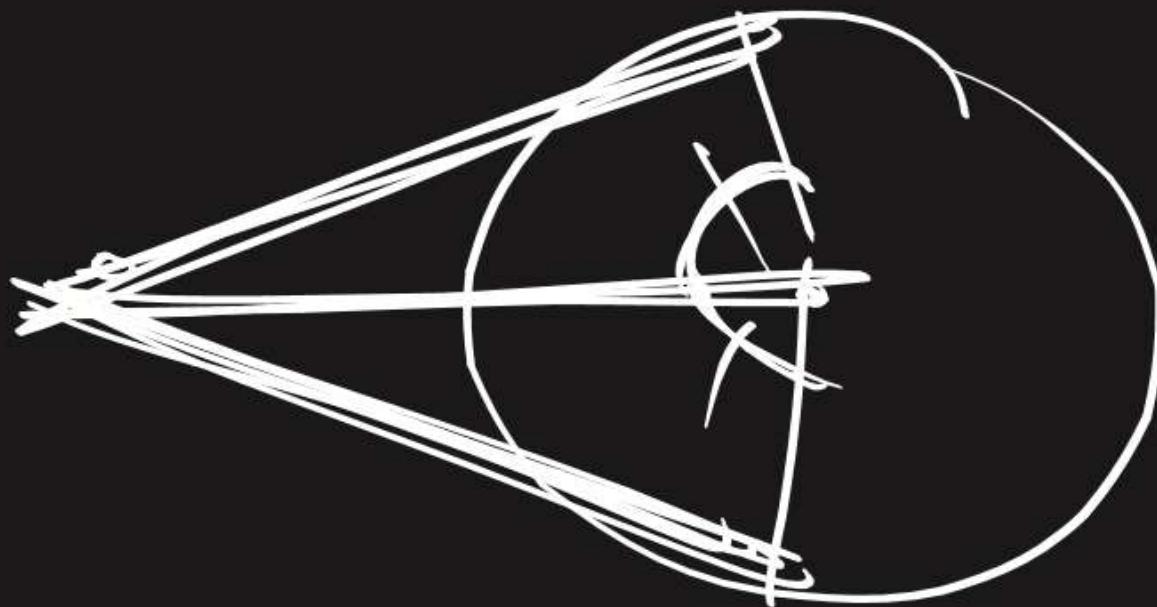
## THEOREM 4

*Tangent*

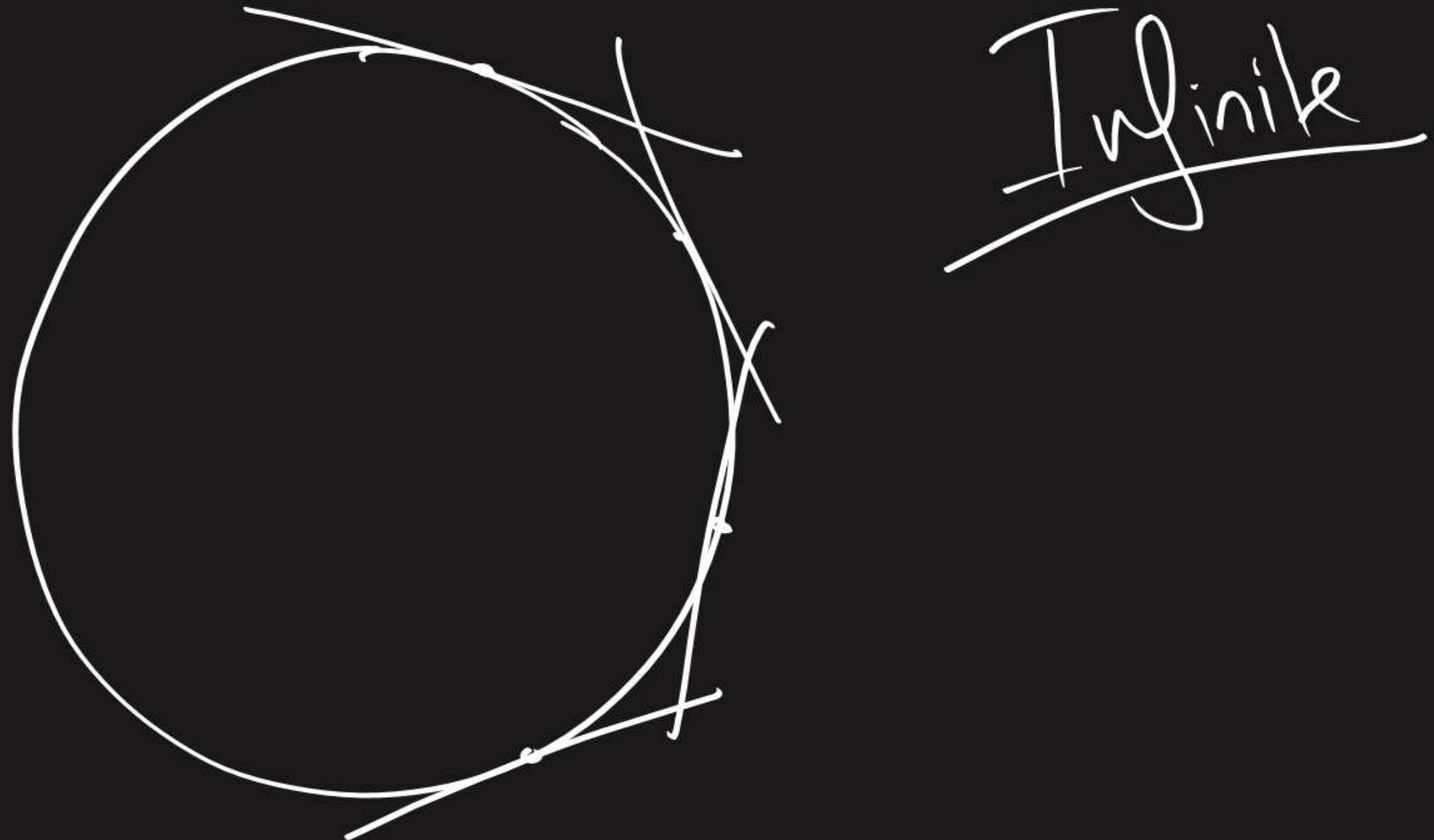
If two tangents are drawn to a circle from an external point, then:

(i) they subtend equal angles at the centre.

(ii) they are equally inclined to the segment joining the centre to that point i.e. the centre lies on the bisector of the angle between the tangents.

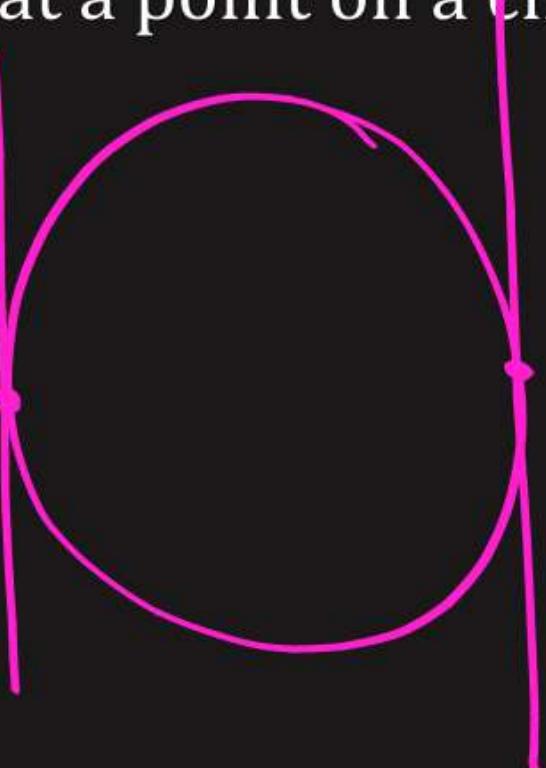


#Q. How many tangents can a circle have?



#Q. Fill in the blanks :

- (i) The common point of a tangent and the circle is called Point of Contact.
- (ii) A circle may have 2 parallel tangents.
- (iii) A tangent to a circle intersects it in 1 point(s).
- (iv) A line intersecting a circle in two points is called a Secant.
- (v) The angle between tangent at a point on a circle and the radius through the point is 90°.



वो तो लड़कियों का  
बस नहीं चलता वरना  
**instagram** का नाम भी  
**instu** रख लेती !



 Attention: 10th Class Students

# PHYSICS FUN WORKSHOP - OPTICS



## THE ULTIMATE SCIENCE COMBO

- Mirror Magic: Reflection & Refraction
- Sunset Mystery: Why the Sun Turns Red
- DIY Electroscope: Make Your Own Electroscope



## Interactive Learning Experience

WORKSHOP DATE: 1st NOVEMBER 2025

TIME: 04:00 PM - 07:00 PM

VENUE: At Your Nearest Vidyapeeth  
( PAN India )



Limited Seats Available!

Hurry! Register Before Seats Fill Up

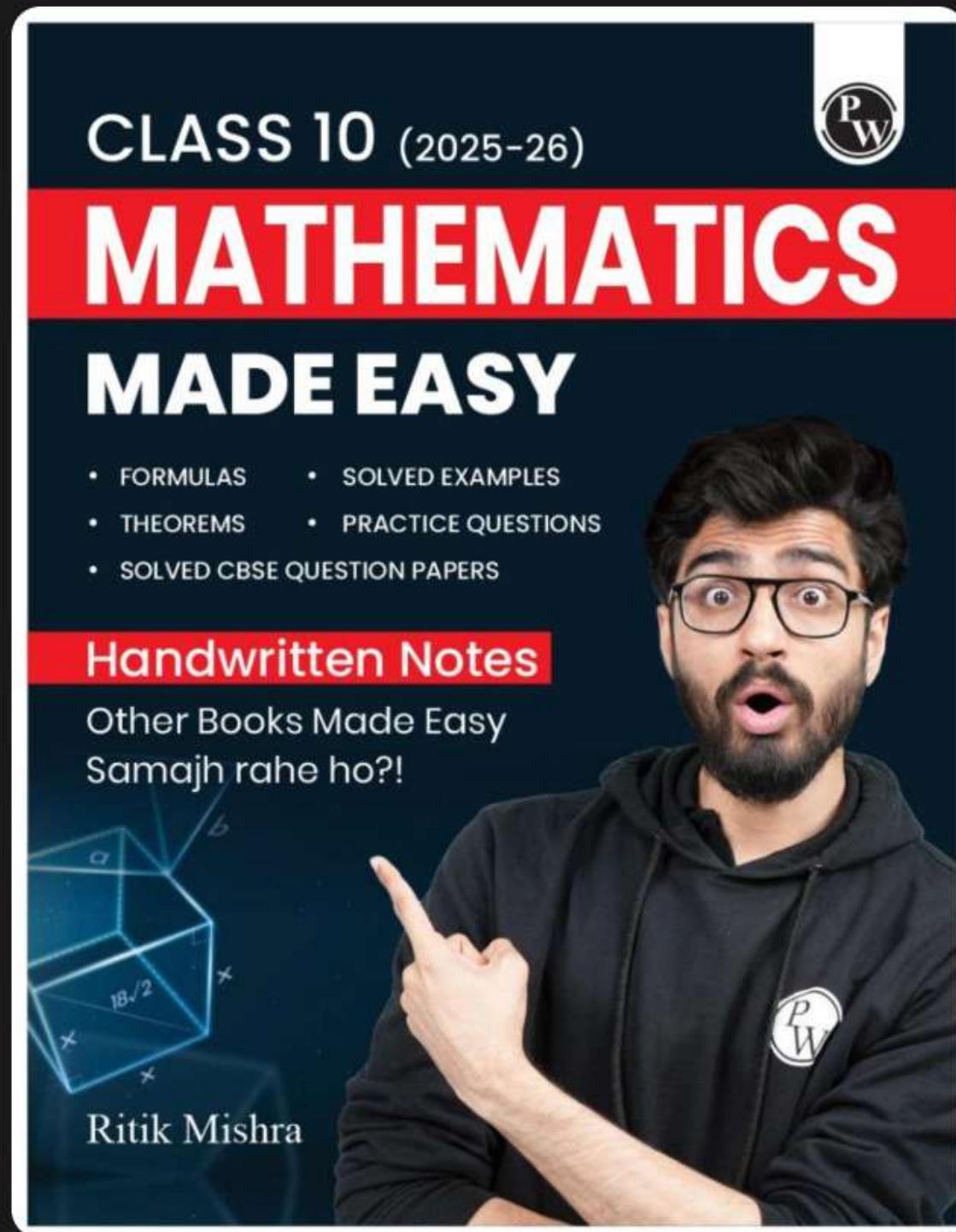
For Registration & Details:

Call: 9513369828

Scan to Register

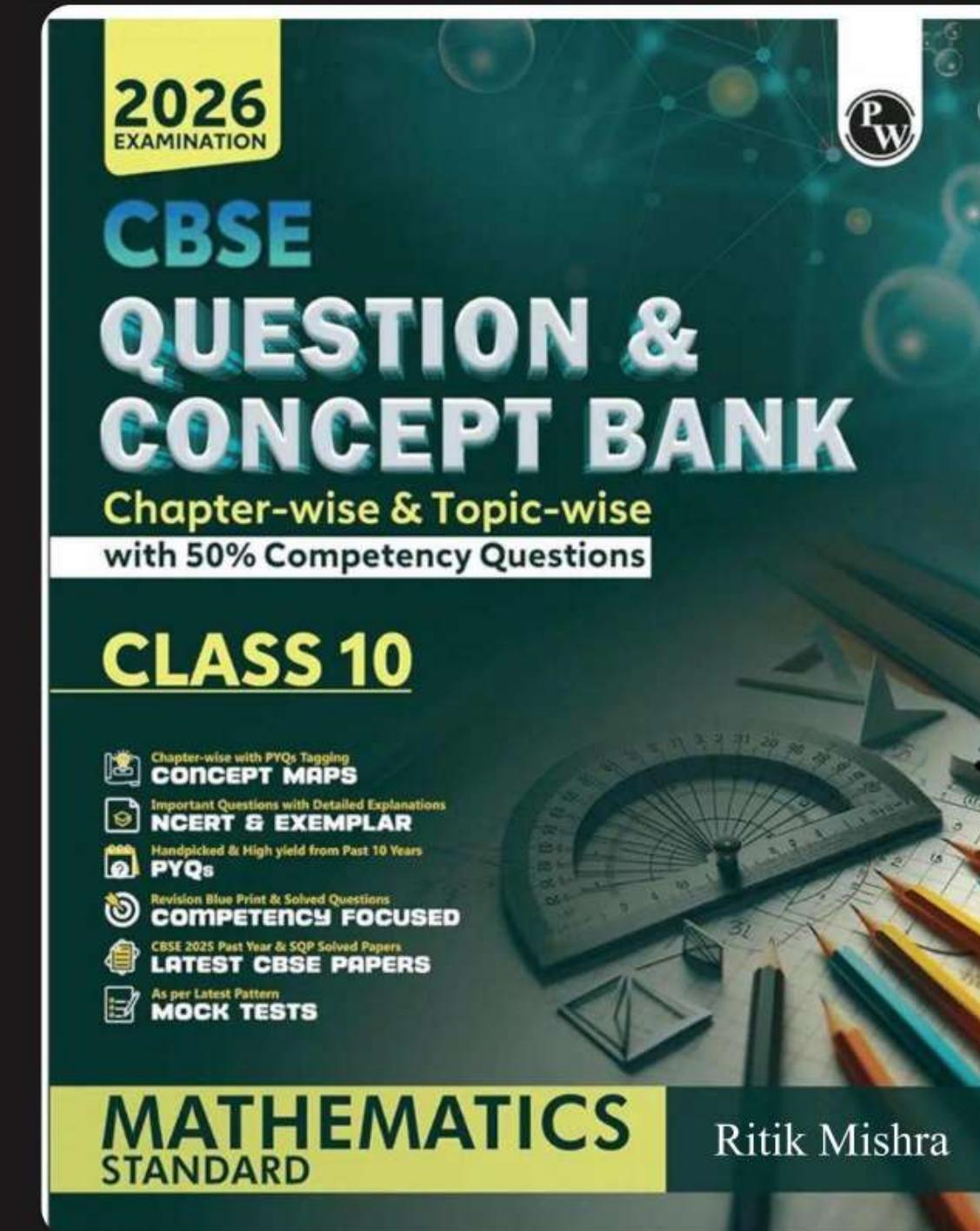


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49 → MCQs



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# RITIK SIR

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Thank  
*You*