



UDAAN



2026

REAL NUMBERS

MATHS

LECTURE-2

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Topics

to be covered



#Gpu

A Questions on HCF, LCM, Prime numbers, Composite numbers

B Relation between HCF and LCM of two numbers

C Coprime numbers

Next class

QUESTION

#Q. Find the HCF and LCM of 144, 180 and 192 by the prime factorization method.

$$144 = 2^4 \times 3^2 \times 5^0$$

$$180 = 2^2 \times 3^2 \times 5^1$$

$$192 = 2^6 \times 3^1 \times 5^0$$

$$\text{HCF} = 2^2 \times 3^1 \times 5^0$$

$$= 12$$

$$\text{LCM} = 2^6 \times 3^2 \times 5^1$$

$$= 2880$$

$$\begin{array}{r|l} 2 & 144 \\ \hline 2 & 72 \\ 2 & 36 \\ 2 & 18 \\ 2 & 9 \\ 3 & 3 \\ 3 & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 180 \\ \hline 2 & 90 \\ 2 & 45 \\ 3 & 15 \\ 3 & 5 \\ 5 & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 192 \\ \hline 2 & 96 \\ 2 & 48 \\ 2 & 24 \\ 2 & 12 \\ 2 & 6 \\ 3 & 2 \\ 2 & 1 \end{array}$$

A 12, 280

☒ B 12, 2880

C 14, 2880

D NOTA

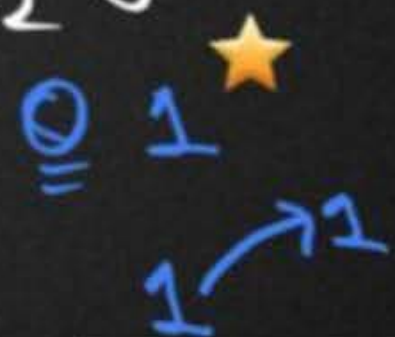
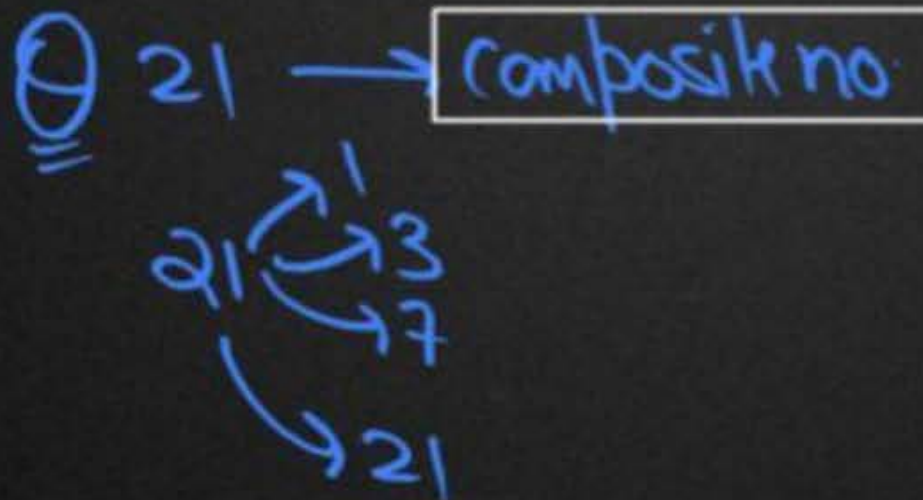
Prime Numbers



only two factors.

Composite Numbers

more than 2 factors



neither prime nor composite

#Graph



#Q. If $a = 2^2 \times 3^x$, $b = 2^2 \times 3 \times 5$, $c = 2^2 \times 3 \times 7$, and $\text{LCM}(a, b, c) = 3780$, then $x =$

$$\text{LCM}(a, b, c) = 3780$$

$$a = 2^2 \times 3^x \times 5^0 \times 7^0$$

$$b = 2^2 \times 3^1 \times 5^1 \times 7^0$$

$$c = 2^2 \times 3^1 \times 7^1 \times 5^0$$

$$\text{LCM} = 2^2 \times 3^x \times 5^1 \times 7^1$$

$$3780 = 2^2 \times 3^x \times 5^1 \times 7^1$$

$$2^2 \times 3^3 \times 5^1 \times 7^1 = 2^2 \times 3^x \times 5^1 \times 7^1$$

$$\begin{array}{r} 2 \overline{) 3780} \\ 2 \\ \hline 2 \\ 2 \\ \hline 2 \\ 2 \\ \hline 2 \\ 2 \\ \hline 0 \end{array}$$

A

0

B

1

C

2

D

3

#Q. If the HCF of 85 and 153 is expressible in the form $85n - 153$ then the value of n is

A 3

☒ B 2

C 4

D 1

$$\begin{array}{r|l} 5 & 85 \\ \hline 17 & 17 \\ & 1 \end{array} \quad \begin{array}{r|l} 3 & 153 \\ \hline 3 & 51 \\ 17 & 17 \\ & 1 \end{array}$$

$$85 = 5^1 \times 17^1 \times 2^0$$

$$153 = 3^2 \times 17^1 \times 5^0$$

$$\text{HCF} = 3^0 \times 17^1 \times 5^0$$

$$= 1 \times 17 \times 1 = 17$$

$$\text{HCF} = 85n - 153$$

$$17 = 85n - 153$$

$$17 + 153 = 85n$$

$$170 = 85n$$

$$\frac{170}{85} = n$$

$$2 = n$$

#Q. The HCF of smallest prime number and the smallest composite number is:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, ...

Smallest
prime
no.

composite
no.

$$\begin{array}{r} 2 \overline{) 2} \\ 1 \end{array} \quad \begin{array}{r} 2 \overline{) 4} \\ 2 \\ 2 \end{array}$$

$$\text{HCF}(2, 4) = 2$$

$$2 = 2^1$$

$$4 = 2^2$$

☒ A 2

☐ B 4

☐ C 6

☐ D 8

#Q. The LCM of the smallest two digit composite number and the smallest composite number is:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, ...

Smallest two digit composite no.

$$\text{LCM}(4, 10) = 2^2 \times 5^1 = 20$$

$$4 = 2^2 \times 5^0$$

$$10 = 2^1 \times 5^1$$

A 12

☒ B 20

C 4

D 44

The least inclusive

- 

2520

| | |
|---|------------------------------------|
| 2 | 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 |
| 2 | 1, 1, 3, 2, 5, 3, 7, 4, 9, 5 |
| 2 | 1, 1, 3, 1, 5, 3, 7, 2, 9, 5 |
| 3 | 1, 1, 3, 1, 5, 3, 7, 1, 9, 5 |
| 3 | 1, 1, 1, 1, 5, 1, 7, 1, 3, 2 |
| 5 | 1, 1, 1, 1, 5, 1, 7, 1, 1, 2 |
| 7 | 1, 1, 1, 1, 1, 1, 1, 7, 1, 1, 1 |
| | 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1 |

$$\text{HCF} = 5^0 \times 7^0 = \textcircled{1}$$

$$5 = 5^1 \times 7^0$$

$$\text{LCM} = 5^1 \times 7^1 = \textcircled{35}$$

$$7 = 7^1 \times 5^0$$



$$\text{HCF}(a, b) = 1$$

$$\text{LCM}(a, b) = \textcircled{a \times b}$$

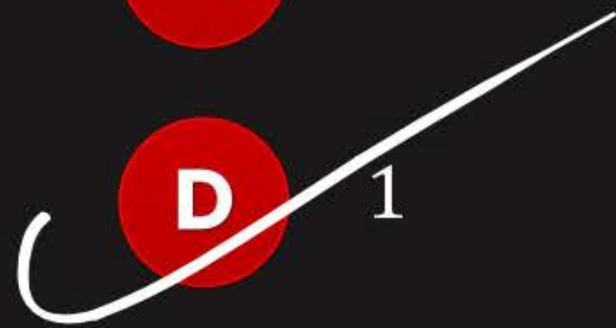
#Q. If p and q are two distinct prime numbers, then their HCF is

A 2

B 0

C Either 1 or 2

D 1



alg-alg.

#Q. If p and q are two distinct numbers, then their $\text{LCM}(p, q)$ is

A 1

B p

C q

D pq

#Q. Let n be a natural number. Then, the LCM ($n, n + 1$) is

A n

B $n + 1$

C $n(n + 1)$

D 1

$$S = 5^1 \times 2^0 \times 3^0$$

$$6 = 2^1 \times 3^1 \times 5^0$$

$$\text{LCM} = 2^1 \times 3^1 \times 5^1$$

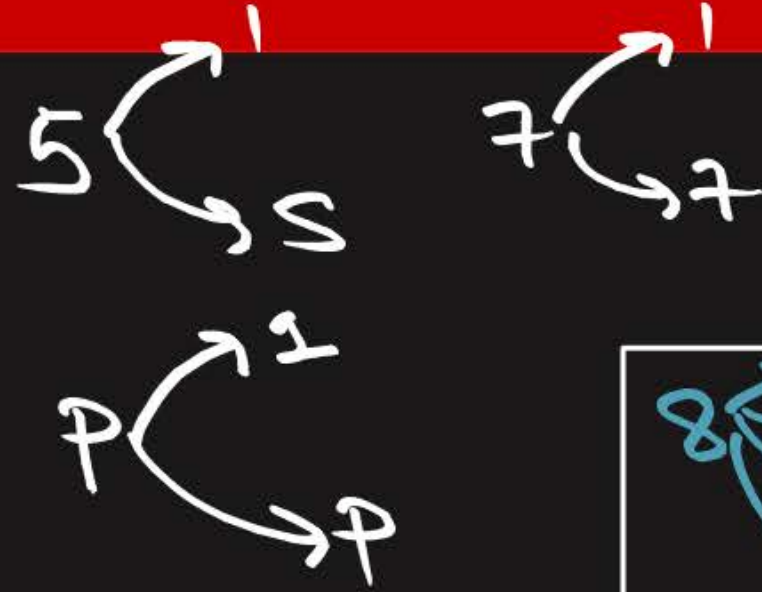
$$= 6 \times 5 = 30$$

$$(6, 6+1) \rightarrow (6, 7)$$

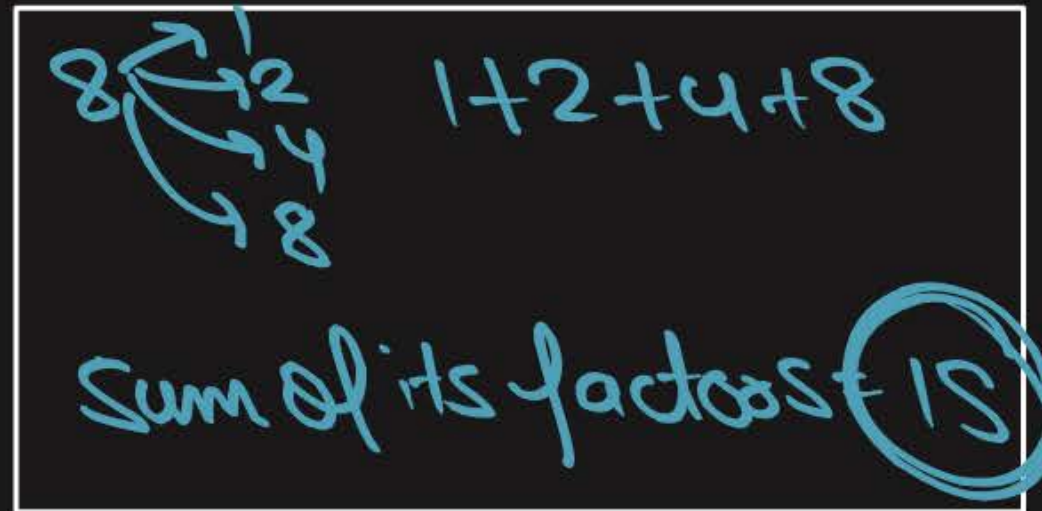
$$(5, 6)$$

#Q. Let p be a prime number. The sum of its factors is:

- A** p
- B** 1
- ☒ **C** $p + 1$
- D** $p - 1$



$$1 + p$$



$1 + 2 + 4 + 8$
 sum of its factors is 15

#Q. The LCM of two prime numbers p and q ($p > q$) is 221. Find the value of

$$3p - q.$$

$$\text{LCM}(p, q) = p \times q$$

$$p > q$$

$$221 = p \times q$$

$$17 \times 13 = p \times q$$

$$\begin{aligned} &= 3p - q \\ &= 3(17) - 13 \\ &= 51 - 13 \\ &= 38 \end{aligned}$$

$$\begin{array}{r} 13 \overline{) 221} \\ 17 \\ \hline 17 \\ \hline 1 \end{array}$$

A 4

B 28

C 38

D 48

#Q. Find the greatest number which divides 85 and 72 leaving remainder 1 and 2 respectively.

$$\begin{array}{l} \bigcirc \div 85 \longrightarrow R=1 \\ \bigcirc \div 72 \longrightarrow R=2 \end{array}$$

$$\begin{array}{r} 2 \overline{)84} \\ 2 \overline{)42} \\ 3 \overline{)21} \\ 7 \overline{)7} \\ 1 \end{array} \quad \begin{array}{r} 2 \overline{)70} \\ 5 \overline{)35} \\ 7 \overline{)7} \\ 1 \end{array}$$

$$\begin{array}{l} \bigcirc \div 84 \longrightarrow R=0 \\ \bigcirc \div 70 \longrightarrow R=0 \end{array}$$

$$\begin{aligned} 84 &= 2^2 \times 3^1 \times 7^1 \times 5^0 \\ 70 &= 2^1 \times 5^1 \times 7^1 \times 10^1 \end{aligned}$$

$$\begin{aligned} \text{HCF} &= 2^1 \times 3^0 \times 5^0 \times 7^1 \\ &= 14 \end{aligned}$$

#Q. Find the largest number which on dividing 1251, 9377 and 15628 leaves remainders 1, 2 and 3 respectively

A 620

☒ B 625

C 600

D 5

$$\begin{aligned} \div 1251 &\rightarrow R=1 \\ \div 9377 &\rightarrow R=2 \\ \div 15628 &\rightarrow R=3 \end{aligned}$$

H.C.F

$$\begin{array}{r} 15628 \\ 3125 \times 4 \\ \hline 12500 \\ 3128 \\ 625 \times 2 \\ \hline 1250 \\ 28 \\ 25 \times 1 \\ \hline 25 \\ 3 \end{array}$$

$$\begin{array}{r} \div 1250 \\ \div 9375 \\ \div 15625 \end{array} \quad R=0$$

$$4680 - 17 = 4663 \quad \bigcirc + 17$$

#Q. Find the smallest number which increased by 17 is exactly divisible by both 520 and 468.

A 4663

B 4720

C 4680

D None of the above

$$520 = 2^3 \times 5 \times 13$$

$$468 = 2^2 \times 3^2 \times 13$$

$$\text{LCM}(520, 468) = 2^3 \times 5 \times 13 \times 3^2$$

$$= 8 \times 5 \times 13 \times 9$$

$$= 360 \times 13$$

$$= 4680$$

$$\begin{array}{r|l} 5 & 520 \\ \hline 2 & 104 \\ 2 & 52 \\ 2 & 26 \\ 13 & 13 \\ & 1 \end{array}$$

$$\begin{array}{r|l} 2 & 468 \\ \hline 2 & 234 \\ 3 & 117 \\ 3 & 39 \\ 13 & 13 \\ & 1 \end{array}$$

#Q. If 'p' and 'q' are natural numbers and 'p' is the multiple of 'q', then what is the HCF of 'p' and 'q'?

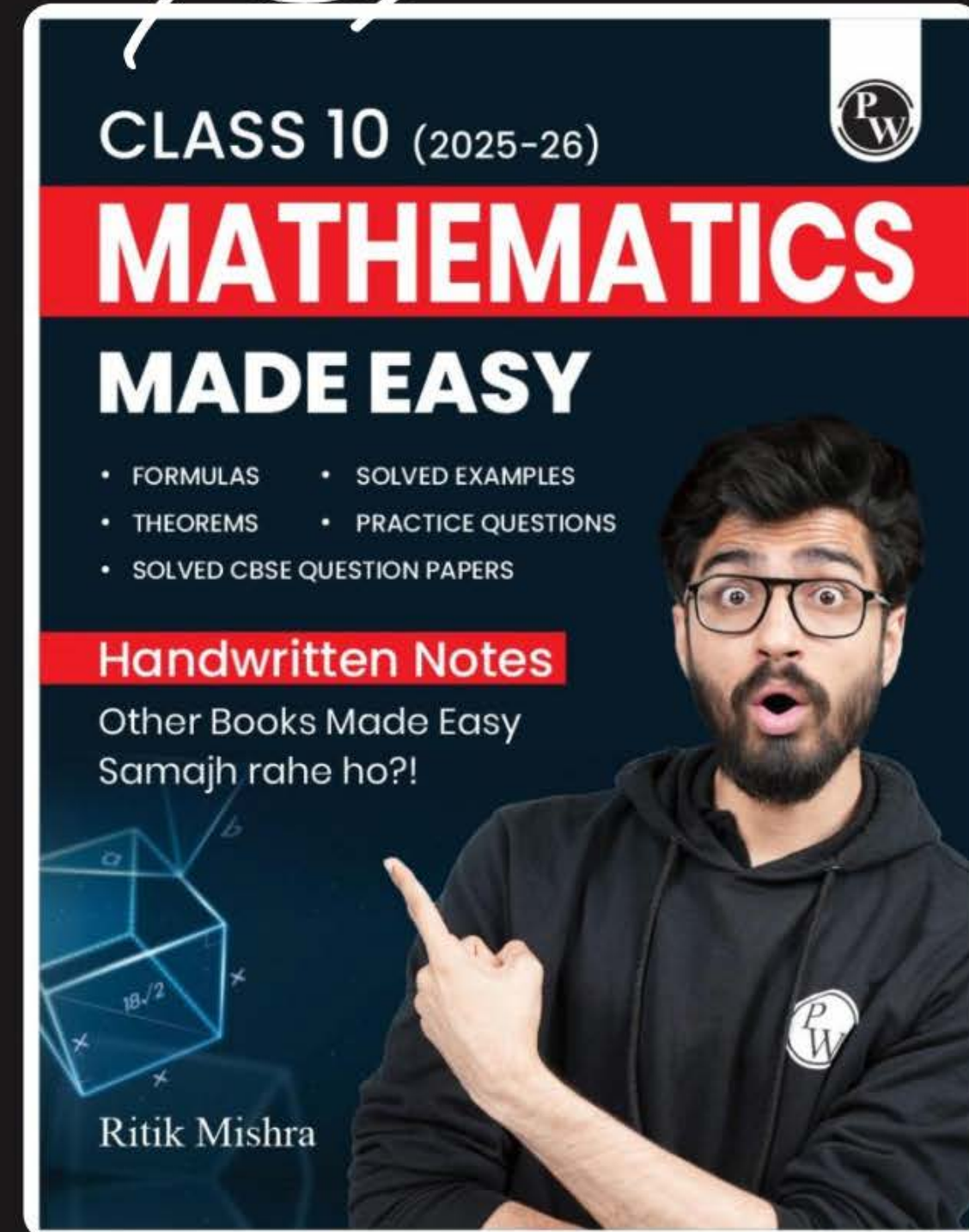
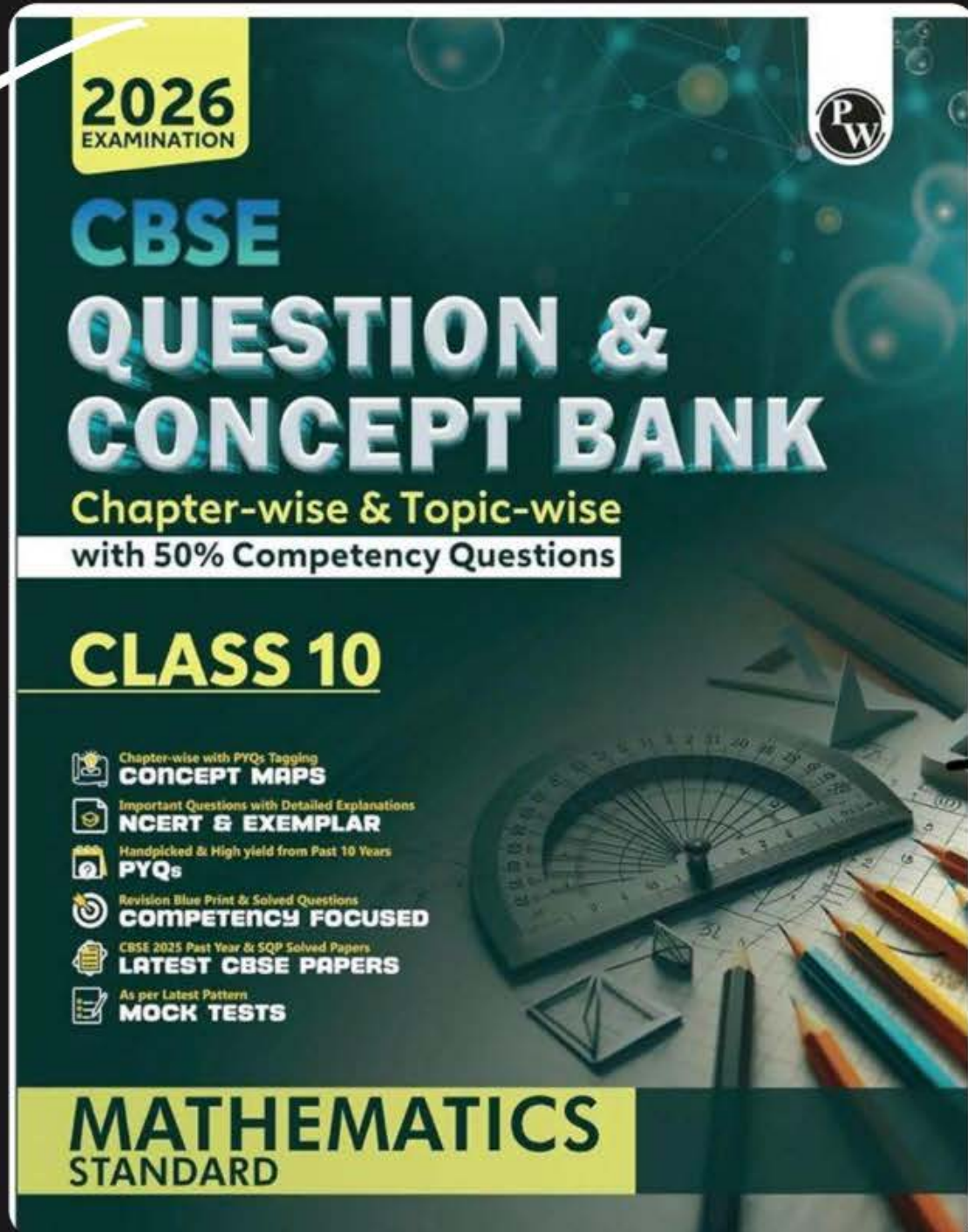
HCF

A pq

B p

C q

D $p + q$



Whazana



WORK HARD

DREAM BIG

NEVER GIVE UP



Thank
You