



# UDAAN



**2026**

**Pair of Linear Equation in  
Two Variables**

**MATHS**

**LECTURE-1**

**BY-RITIK SIR**





# Topics *to be covered*



**A**

Basics

**B**

Linear Equation in one variable

**C**

Linear Equation in two variable

**D**

Pair of linear equation in two variable

**E**

Graphical Representation







# RITIK SIR

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# Linear Equation in One Variable



$$x - 1 = 0$$

$$2x + 1 = 0$$

$$3x + 5 = 0$$

$$-2x + 0 = 0$$

General form

$$ax + b = 0$$

$$a, b \in \mathbb{R}$$

$$a \neq 0$$

Solution

Variable ki value

eqn satisfy

$$L.H.S = R.H.S$$

$$(i) \quad x + 1 = 0$$

$$x = -1 //$$

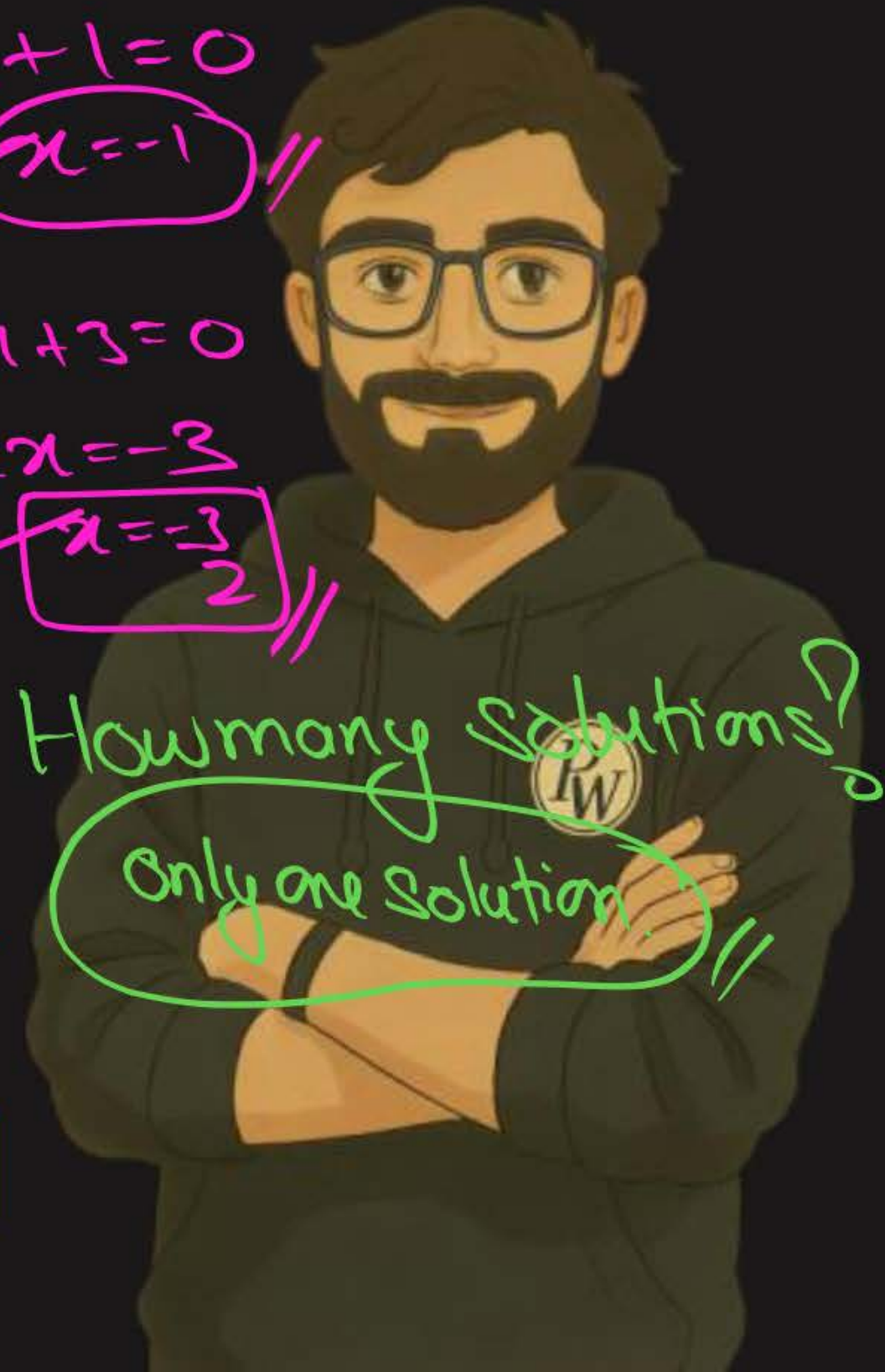
$$(ii) \quad 2x + 3 = 0$$

$$2x = -3$$

$$x = -\frac{3}{2} //$$

How many solutions?

Only one solution //







# Linear Equation in Two Variable



General form

$$ax + by + c = 0$$

$$a, b, c \in \mathbb{R}$$

'a' and 'b' both cannot  
be zero at the same time.

$$x + y = 1$$

$$2x - 3y + 2 = 0$$

$$5x + 4y + 3 = 0$$

$$9x - 9y + 2 = 0$$



Solution:

$$x + y = 2$$

- ✓ (1, 1)
- ✓ (2, 0)
- ✓ (0, 2)
- ✓ (100, -98)
- ✓ (5, -3)
- ✓ (999, -998)

How many solutions?

Infinite

②  $2x - 3y = 2$  I

x	0	1	2	7/2
y	-2/3	0	2/3	5/3

$$y = \frac{5}{3} \rightarrow x = ?$$

$$2x - 3\left(\frac{5}{3}\right) = 2$$

$$2x - 5 = 2$$

$$2x = 2 + 5$$

$$2x = 7$$

$$x = 7/2$$





System.

## Pair of Linear Equation in Two Variable

Solution

$$x + y + 5 = 0$$

$$2x - 3y + 2 = 0$$

General form

$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

How many Solutions?

#Q. <sup>IS</sup> ~~Show that~~  $x = 2, y = 1$  is a solution of the system of simultaneous linear equation:

$$3x - 2y = 4$$

$$2x + 4y = 5$$

$$a_1 = 3$$

$$b_1 = -2$$

$$c_1 = -4$$

$$a_2 = 2$$

$$b_2 = 4$$

$$c_2 = -5$$

$$a_1x + b_1y + c_1 = 0$$

$$a_2x + b_2y + c_2 = 0$$

Not a solution

$$3(2) - 2(1) = 4$$

$$6 - 2 = 4$$

$$\checkmark \boxed{4 = 4}$$

$$2(2) + 4(1) = 5$$

$$4 + 4 = 5$$

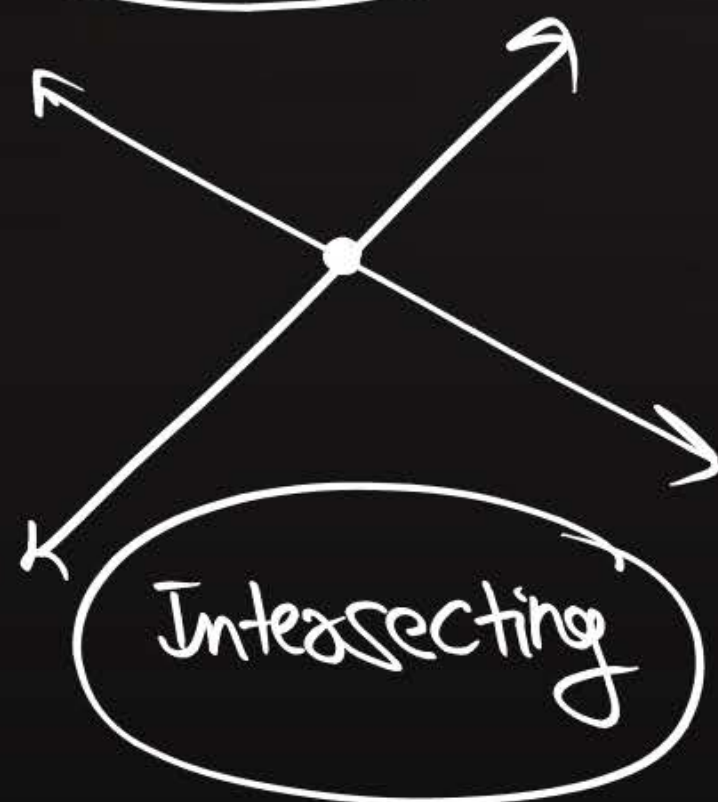
$$\boxed{8 \neq 5}^X$$



I

Unique solution

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

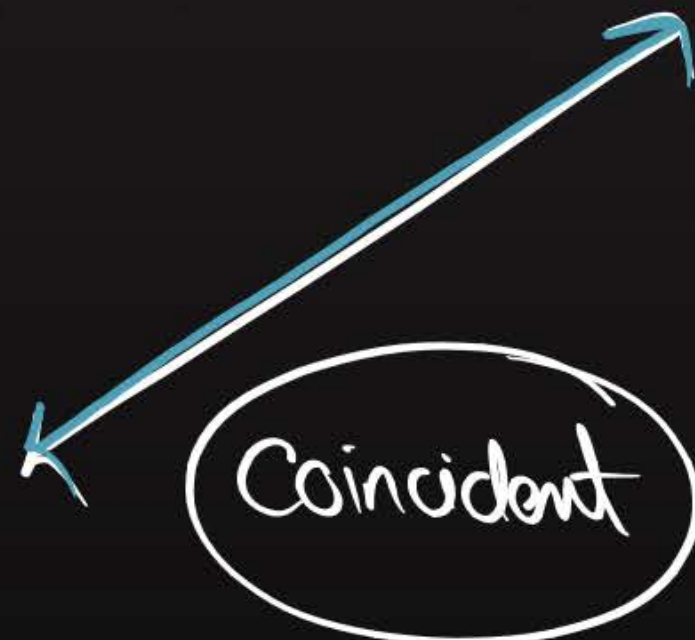


Consistent system

II

Infinite many solution

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$



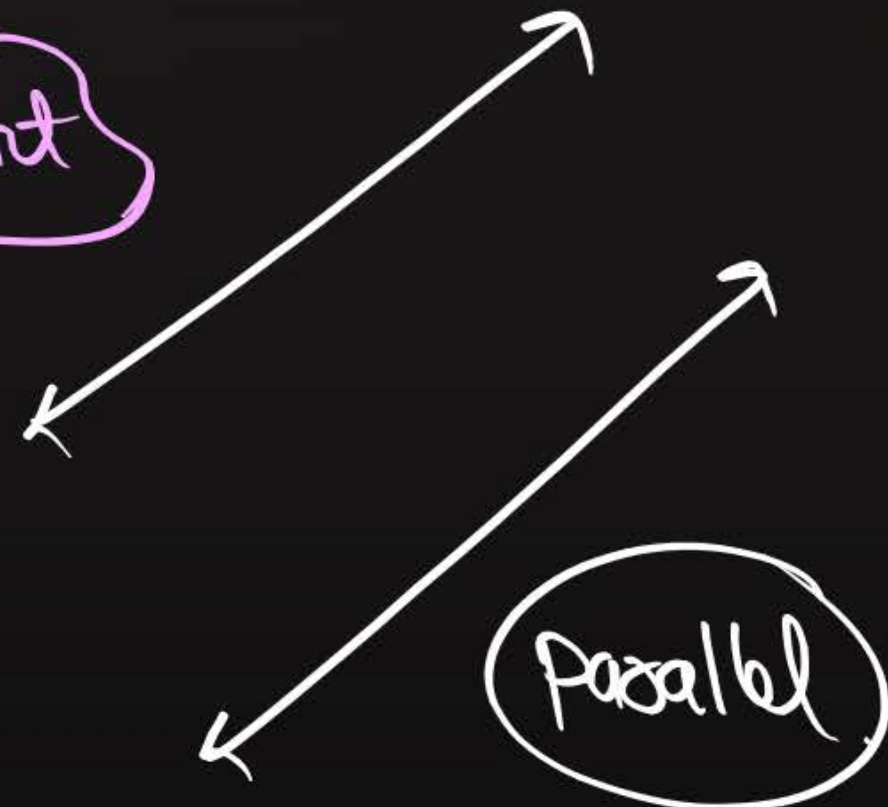
dependent

Inconsistent system

III

No solution

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$





$$\textcircled{Q} \quad 2x - 3y + 4 = 0$$

$$5x + 4y - 2 = 0$$

$$a_1 = 2 \quad a_2 = 5$$

$$b_1 = -3 \quad b_2 = 4$$

$$c_1 = 4 \quad c_2 = -2$$

$$\frac{2}{5} \neq \frac{-3}{4}$$

$$\frac{4}{-2}$$

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

Unique solution (Intersecting) (consistent)

$$\textcircled{Q} \quad 2x + 4y + 3 = 0$$

$$6x + 12y + 9 = 0$$

$$\frac{2}{6} = \frac{4}{12} = \frac{3}{9}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

Coincident.  
Infinite solution.  
Consistent.  
dependent.



Q  $2x - 4y - 9 = 0$

$$12x - 24y - 3 = 0$$

$$\begin{array}{ccc} \cancel{1}x & \cancel{+4}y & \cancel{+9} \\ \cancel{12}x & \cancel{-24}y & \cancel{-3} \\ 6 & & 6 \end{array}$$

$$\frac{1}{6}$$

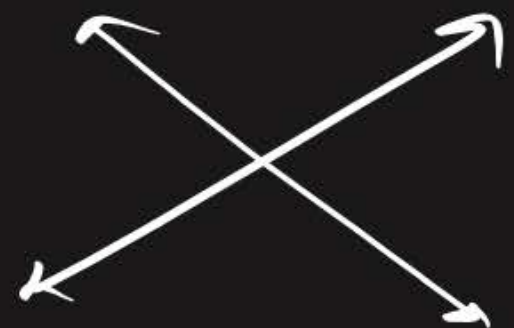

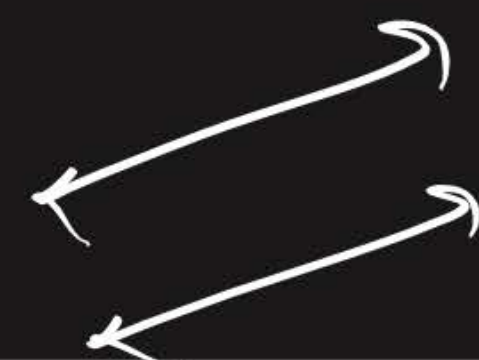
$$\frac{1}{6}$$

$$\frac{3}{1}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

No solution.  
Inconsistent.  
Parallel lines.



S. No.	Pair of Lines	$\frac{a_1}{a_2}$	$\frac{b_1}{b_2}$	$\frac{c_1}{c_2}$	Compare the Ratios	Graphical representation	Algebraic Interpretation
1.	$\begin{aligned} x - 2y &= 0 \\ 3x + 4y - 20 &= 0 \end{aligned}$	$\frac{1}{3}$	$\frac{-2}{4}$	$\frac{0}{-20}$	$\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$	 <i>intersecting.</i>	Exactly one solution consistent (Unique)
2.	$\begin{aligned} 2x + 3y - 9 &= 0 \\ 4x + 6y - 18 &= 0 \end{aligned}$	$\frac{2}{4}$	$\frac{3}{6}$	$\frac{-9}{-18}$	$\begin{aligned} \frac{a_1}{a_2} &= \frac{b_1}{b_2} \\ &= \frac{c_1}{c_2} \end{aligned}$	 <i>Coincident.</i>	Infinitely many solutions consistent (Dependent)
3.	$\begin{aligned} x + 2y - 4 &= 0 \\ 2x + 4y - 12 &= 0 \end{aligned}$	$\frac{1}{2}$	$\frac{2}{4}$	$\frac{-4}{-12}$	$\begin{aligned} \frac{a_1}{a_2} &= \frac{b_1}{b_2} \\ &\neq \frac{c_1}{c_2} \end{aligned}$	 <i>parallel lines.</i>	No solutions Inconsistent



# How to Solve?? (Solving System of Equations)

**Graphical  
method**

**Algebraic  
method**

**Substitution  
method**

**Elimination  
method**



#Q. Graphically, the pair of equations  $6x - 3y + 10 = 0$   
 $2x - y + 9 = 0$  represents two lines which  
 are

$$\frac{6}{2} \quad \frac{-3}{-1} \quad \frac{10}{9}$$

$$\frac{3}{1} = \frac{3}{1} \neq \frac{10}{9}$$

$$\boxed{\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}}$$

**A** Intersecting at exactly one point

**B** Intersecting at exactly two point

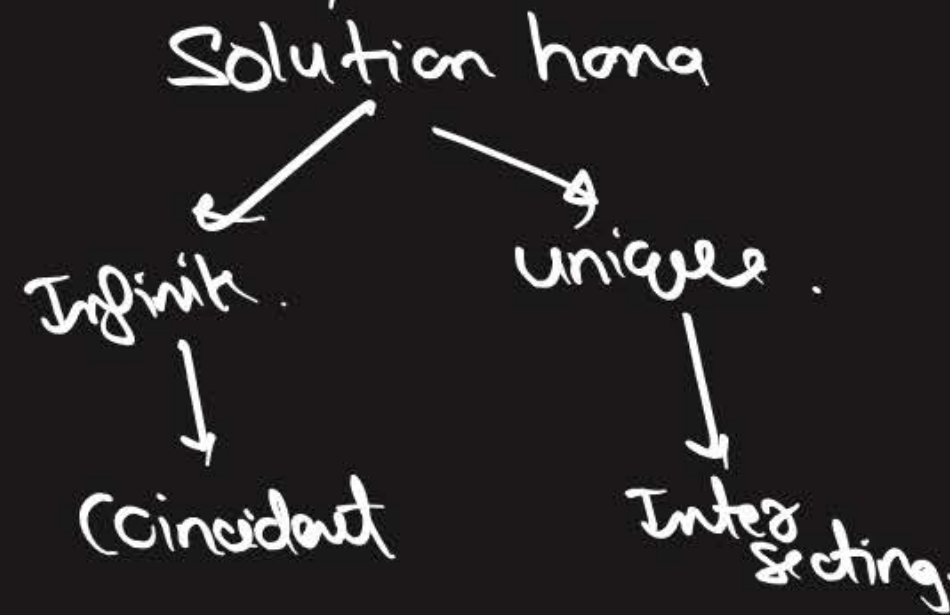
**C** Coincident

**D** Parallel





#Q. If a pair of linear equations is consistent, then the lines will be



- A** Parallel
- B** Always coincident
- C** Intersecting or coincident
- D** Always intersecting



#Q. Show graphically that the system of equations  $2x + 4y = 10$   
 $3x + 6y = 12$  has no solution.

$$2x + 4y = 10$$

x	5	1
y	0	2

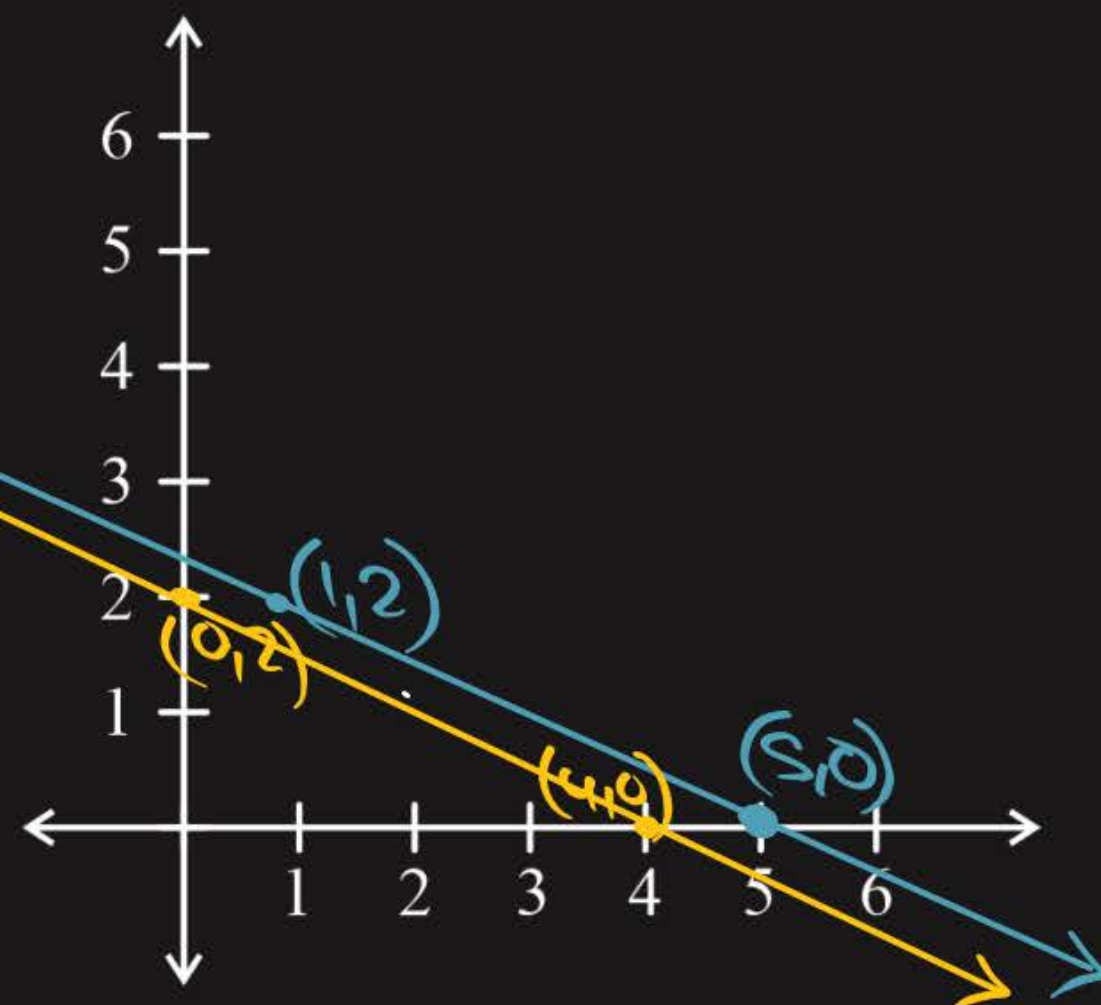
✓ (5, 0)  
 ✓ (1, 2)

$$3x + 6y = 12$$

x	0	4
y	2	0

✓ (0, 2)  
 ✓ (4, 0)

Since, lines are parallel.  
 $\therefore$  the system will have no solution.





#Q. Solve graphically the system of equations:

$$x + y = 3$$

$$3x - 2y = 4$$

$$x + y = 3$$

x	0	3
y	3	0

$$3x - 2y = 4$$

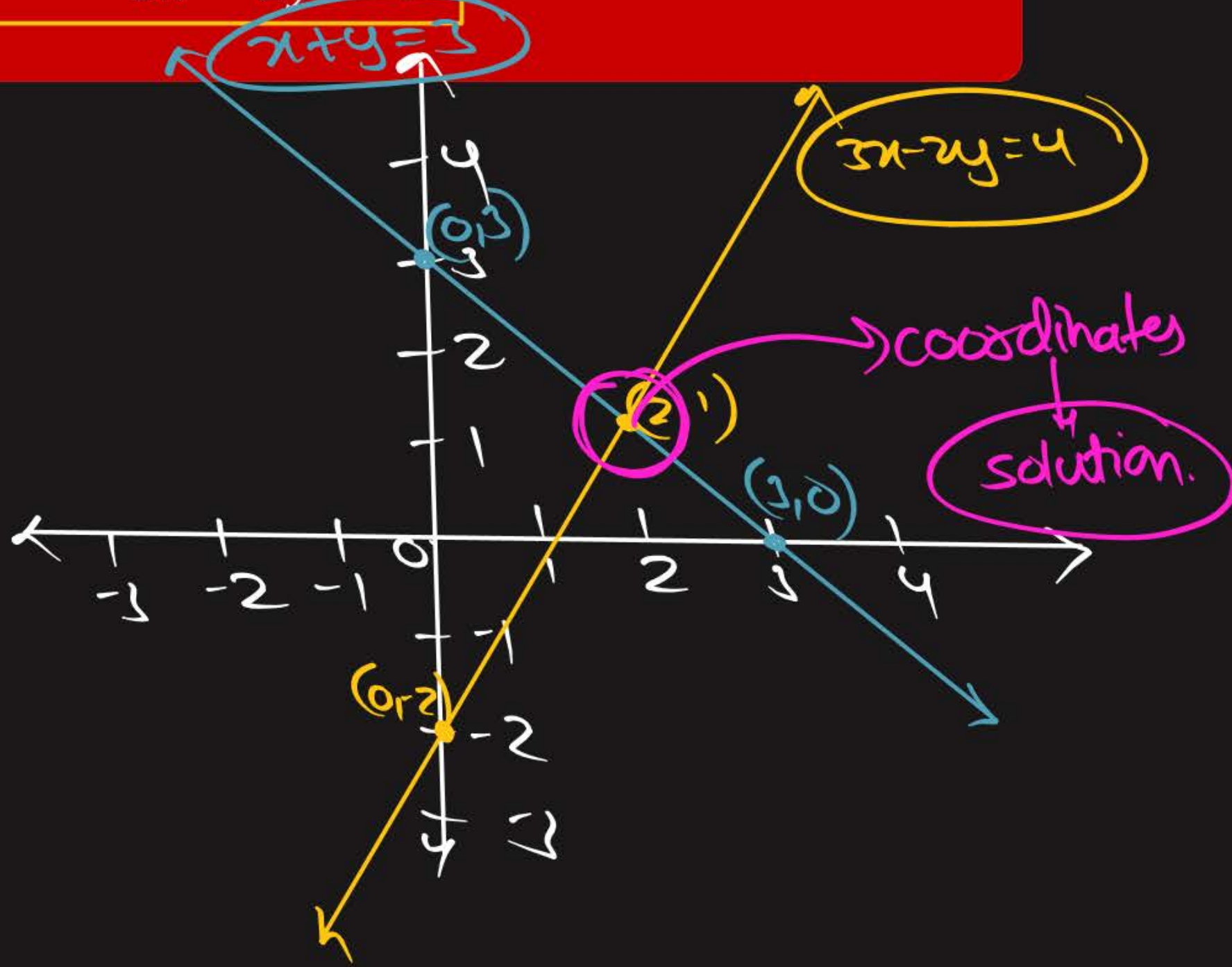
x	0	2
y	-2	1

✓ (0, 3)  
✓ (3, 0)

✓ (0, -2)  
✓ (2, 1)

→ ∴ lines are intersecting.  
∴ unique solution.

Ams: (2, 1)



**CONSISTENT SYSTEM** : A system of simultaneous linear equations is said to be consistent, if it has at least one solution.

**IN-CONSISTENT SYSTEM** : A system of simultaneous linear equations is said to be inconsistent, if it has no solution.

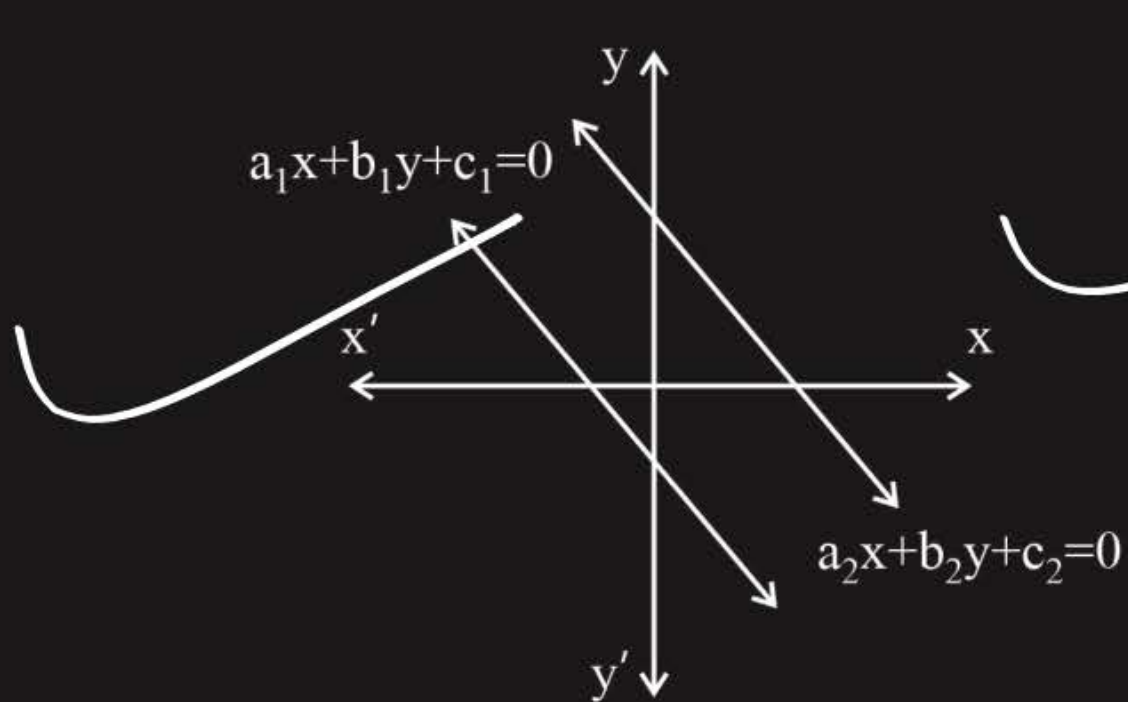
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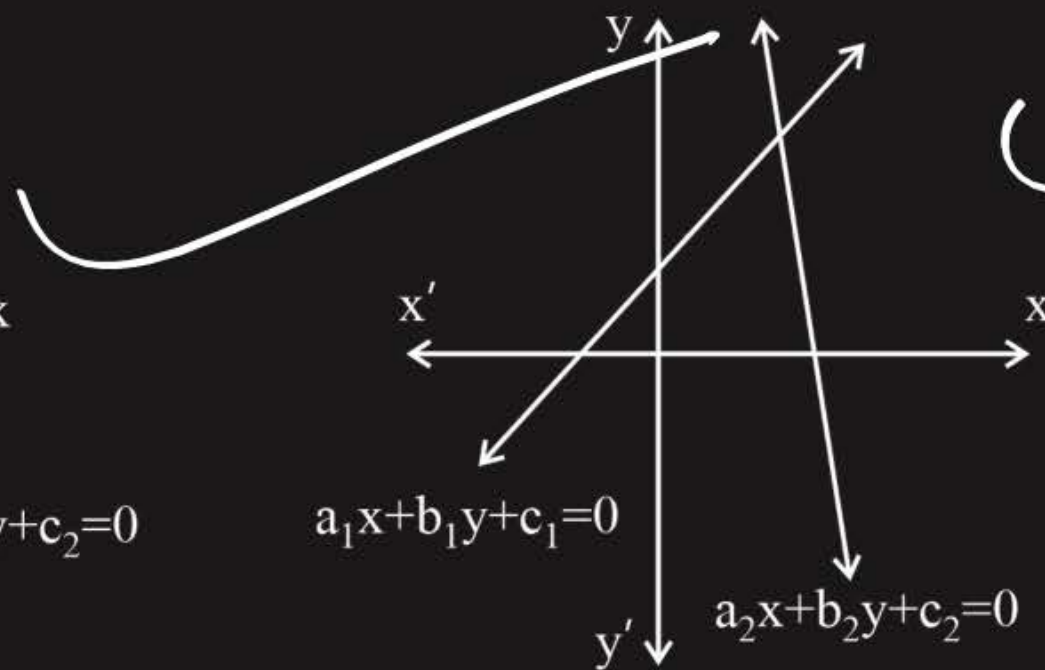


## Graphical Representation of Linear Equations

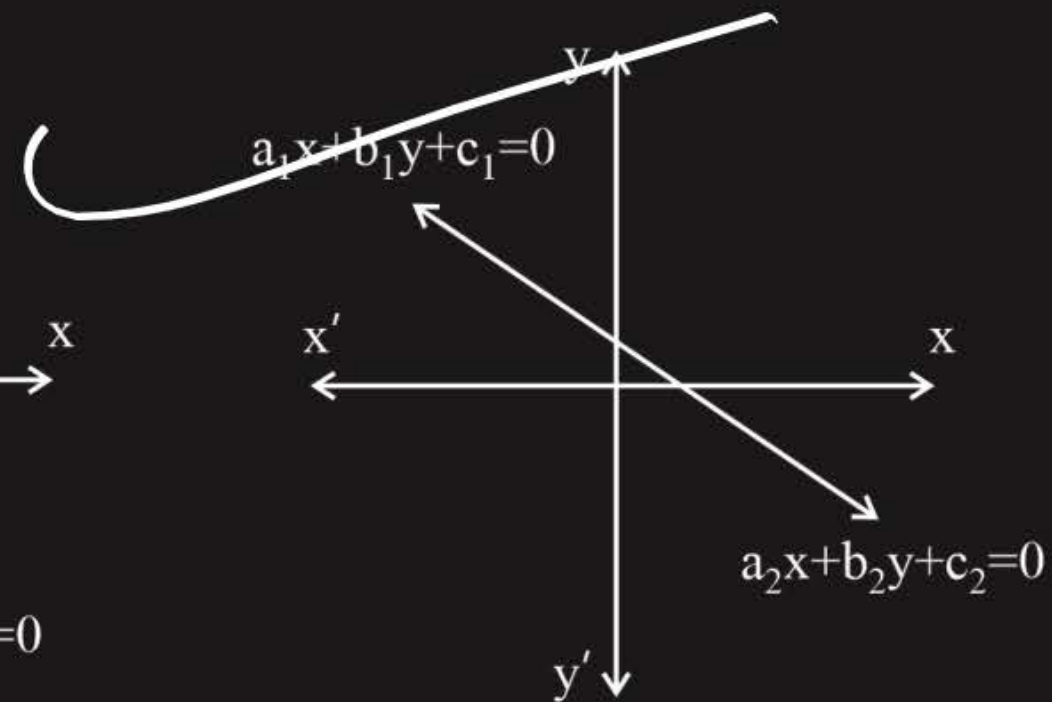
- (i) The two lines intersect at one point.
- (ii) The two lines are parallel i.e. they do not intersect however far they are extended.
- (iii) The two lines are coincident lines i.e. one line overlaps the other line.



Parallel lines



Intersecting lines

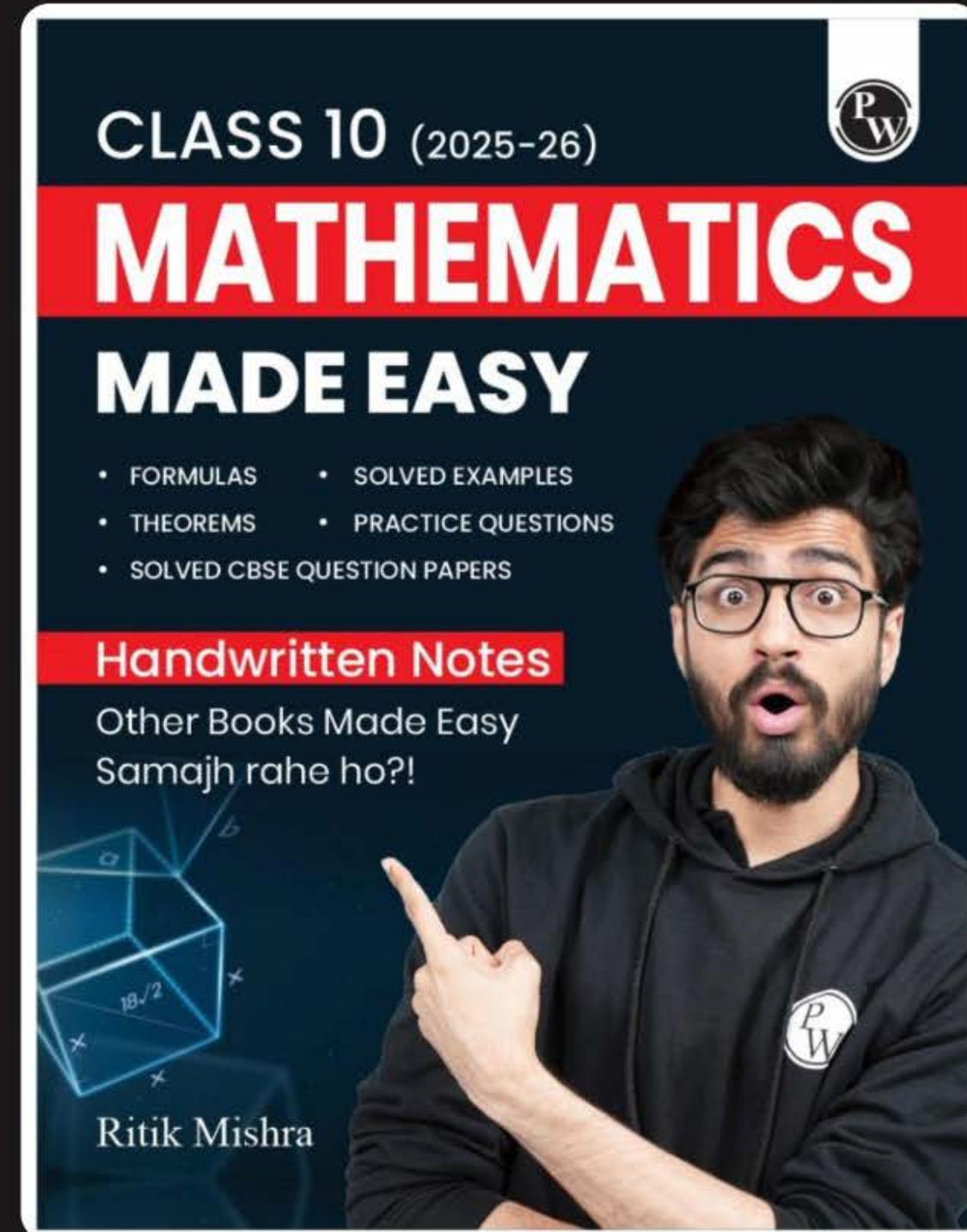
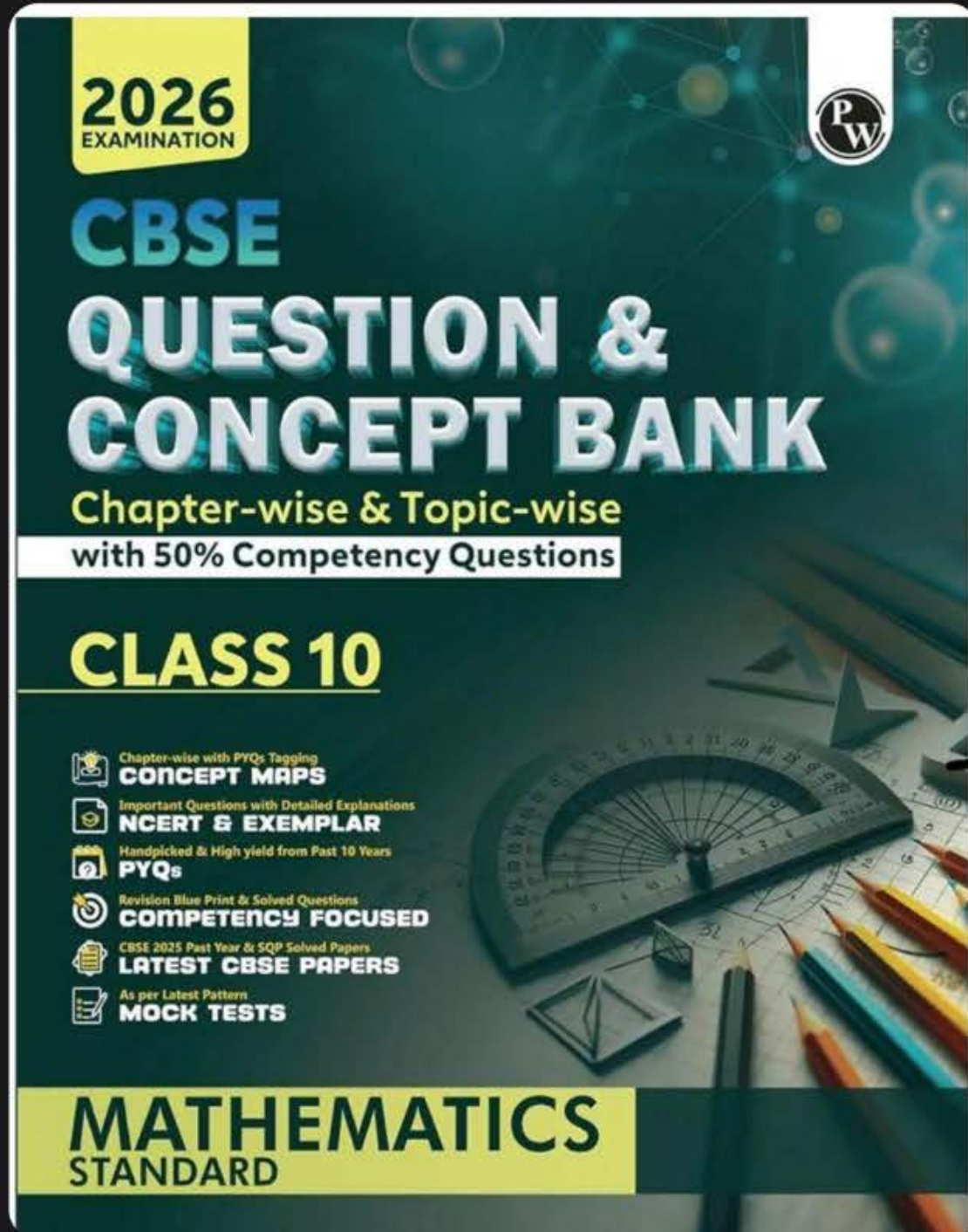


Coincident lines

#Q. Show graphically that the system of equations  $\begin{matrix} 3x - y = 2 \\ 9x - 3y = 6 \end{matrix}$  has infinitely many solutions.

Graph









**WORK HARD**

**DREAM BIG**

**NEVER GIVE UP**





**Thank**  
*You*