



UDAAN



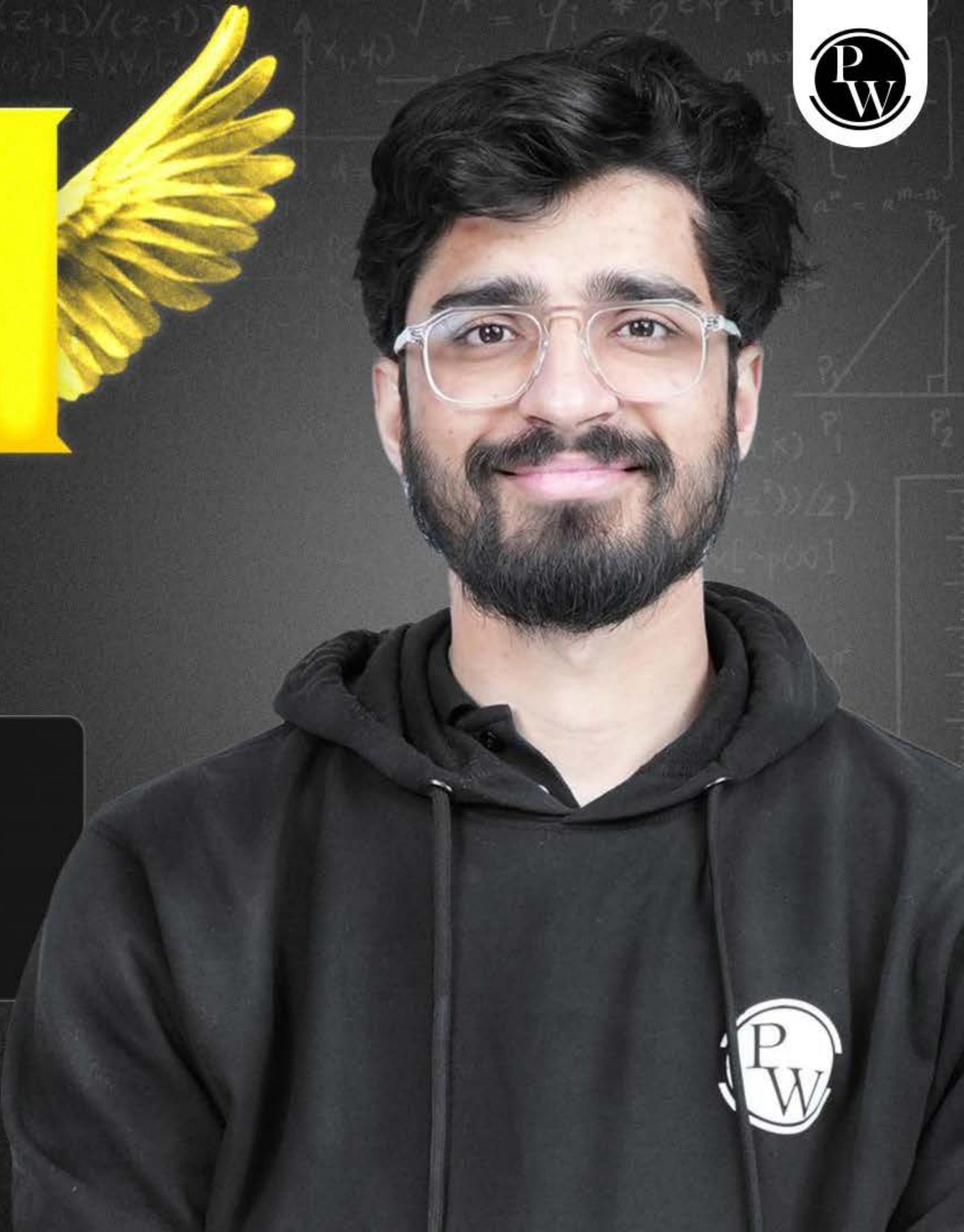
2026

POLYNOMIALS

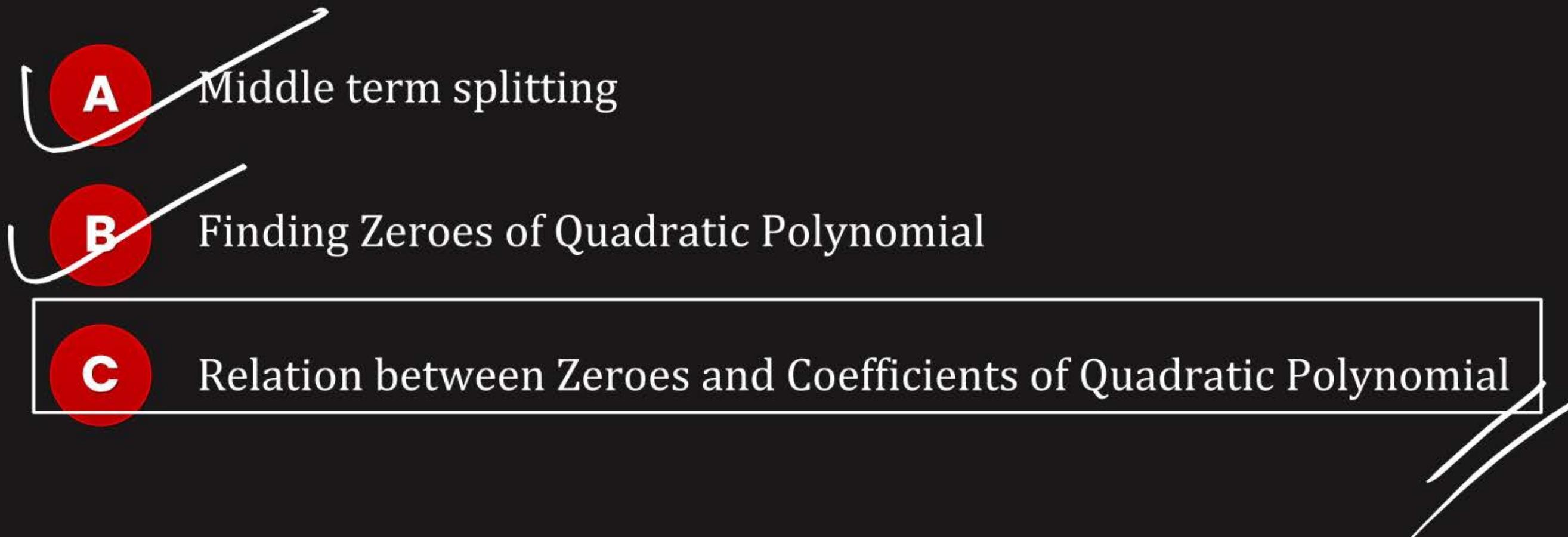
MATHS

LECTURE-3

BY-RITIK SIR



Topics *to be covered*

- A Middle term splitting
 - B Finding Zeroes of Quadratic Polynomial
 - C Relation between Zeroes and Coefficients of Quadratic Polynomial
- 
- Three red circles labeled A, B, and C are connected by white curved lines that curve upwards towards the right. A horizontal white bracket is positioned under circle C, spanning its width and extending slightly beyond it to the right. A diagonal white line starts from the bottom right corner of the bracket and extends upwards and to the left, ending near the top left corner of the slide.



RITIK SIR

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$$\textcircled{1} \quad x^2 = 9$$

$$x^2 - 9 = 0$$

$$x^2 = 9$$

$$x = \pm\sqrt{9}$$

$$x = +3, -3$$

$$\begin{array}{r|rr} 3 & 27 \\ \hline 3 & 9 \\ 3 & \} \end{array}$$

$$\textcircled{3} \quad x^2 - 4x$$

$$x^2 - 4x = 0$$

Common ...

$$(x)(x-4) = 0$$

$$x = 0$$

$$x - 4 = 0$$

$$x = 4$$

$$x^2 - 4x = 0$$

$$x^2 - 4x$$

$$x = \pm\sqrt{4x}$$

$$x = +2\sqrt{x}, -2\sqrt{x}$$

$$\textcircled{2} \quad x^2 - 27$$

$$x^2 = 27$$

$$x = \pm\sqrt{27}$$

$$x = \pm\sqrt{3 \times 3 \times 3}$$

$$x = +3\sqrt{3}, -3\sqrt{3}$$

$$\textcircled{4} \quad x^2 - 36x$$

$$x^2 - 36x = 0$$

$$(x)(x-36) = 0$$

$$x = 0$$

$$, x - 36 = 0$$

$$x = 36$$



Middle term splitting for finding zeros of quadratic polynomials

1. ~~$x^2 + 4x + 21$~~

Sum = 4, Product = -21

$$\begin{array}{r} 3 \\ \times 7 \\ \hline 21 \\ 21 \\ \hline 7 \end{array}$$

$$\underline{x^2 + 7x} - \underline{3x - 21} = 0$$

$$x(x+7) - 3(x+7) = 0$$

$$(x+7)(x-3) = 0$$

α

$$x+7=0$$

$$x=-7$$

$$x-3=0$$

$$x=3$$

2.

~~$-2x^2 + 7x - 6$~~

Sum = 7, Product = 12

$$\begin{array}{r} 2 \\ \times 6 \\ \hline 12 \\ 6 \\ \hline 2 \end{array}$$

$$\underline{-2x^2 + 4x} + \underline{3x - 6} = 0$$

$$-2x(x-2) + 3(x-2) = 0$$

$$(x-2)(-2x+3) = 0$$

α

$$x-2=0$$

$$x=2$$

$$-2x+3=0$$

$$-2x=-3$$

$$x=3/2$$

$$\begin{array}{r} 2 \\ \times 6 \\ \hline 12 \\ 6 \\ \hline 2 \end{array}$$

3. ~~$7x^2 - 19x - 6$~~

$S = -19, P = -42$

$\begin{array}{|c|c|} \hline 2 & 12 \\ \hline 3 & 21 \\ \hline 7 & 7 \\ \hline 1 & 1 \\ \hline \end{array}$

$7x^2 - 21x + 2x - 6$

$$7x(x-3) + 2(x-3) = 0$$

$$(x-3)(7x+2) = 0$$

$x-3=0$ $7x+2=0$

$x=3$ $x=-2 \frac{2}{7}$

$\cancel{x=3}$ $\cancel{x=-2 \frac{2}{7}}$

4. ~~$6x^2 + 13x + 6$~~

Sum = 13, Product = 36

$\begin{array}{|c|c|} \hline 9 & 4 \\ \hline \end{array}$

$6x^2 + 9x + 4x + 6 = 0$

$3x(2x+3) + 2(2x+3) = 0$

$$(2x+3)(3x+2) = 0$$

$2x+3=0$ $3x+2=0$

$x=-3 \frac{3}{2}$ $x=-\frac{2}{3}$

$\cancel{x=-3 \frac{3}{2}}$ $\cancel{x=-\frac{2}{3}}$

#Q. The zeroes of the polynomial $x^2 + \frac{1}{6}x - 2$ are

$$x^2 + \frac{1}{6}x - 2$$

$$\frac{x^2 + \frac{1}{6}x - 2}{1} = 0$$

$$\frac{6x^2 + x - 12}{6} = 0$$

A $-3, 4$

C $-\frac{4}{3}, \frac{3}{2}$

B $-\frac{3}{2}, \frac{4}{3}$

D $-\frac{4}{3}, -\frac{3}{2}$

$$6x^2 = 2 \times 3 \times 2 \times x \times x$$

$$9x = 3 \times 3 \times x$$

$$3x(2x+3)$$

$$-8x = -1 \times 2 \times 2 \times x$$

$$-12 = -1 \times 2 \times 2 \times 3$$

$$-4(2x+3)$$

$$6x^2 + 9x - 8x - 12 = 0$$

$$3x(2x+3) - 4(2x+3) = 0$$

$$(2x+3)(3x-4) = 0$$

$$2x+3=0 \quad 3x-4=0$$

$$x = -\frac{3}{2}, \frac{4}{3}$$

2	7	2
2	5	6
2	1	8
2	9	
3		

Find the roots

#Q. ~~Roots~~ the polynomial:

$$f(x) = x^2 - \frac{11}{6}x - \frac{5}{3}$$

$$6x^2 - 15x + 4x - 10 = 0$$

$$\begin{aligned} 6x^2 &= 2 \times 3 \times x \times x \\ -15x &= -1 \times 3 \times 5 \times x \end{aligned}$$

$$3x(2x-5) + 2(2x-5) = 0$$

$$(2x-5)(3x+2) = 0$$

$$2x = 5$$

$$x = \frac{5}{2}$$

$$3x + 2 = 0$$

$$x = -\frac{2}{3}$$

$$x^2 - \frac{11}{6}x - \frac{5}{3} = 0$$

$$\frac{6x^2 - 11x - 10}{6} = 0$$

$$6x^2 - 11x - 10 = 0$$

$$P = -60, S = -11$$

$$-15, 4$$

Verify:

$$a = 1$$

$$b = -11/6$$

$$c = -5/3$$

$$\alpha = \frac{5}{2}$$

$$\beta = -\frac{2}{3}$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\frac{5}{2} + -\frac{2}{3} = -\frac{-11/6}{1}$$

$$\frac{15-4}{6} = +\frac{11}{6}$$

$$\frac{11}{6} = \frac{11}{6}$$

$$\alpha \beta = c/a$$

$$\frac{5}{2} \times -\frac{2}{3} = -\frac{5}{3}/\frac{1}{1}$$

$$-\frac{5}{3}/\frac{1}{1} = -\frac{5}{3}$$



Relationship between the zeroes and coefficients of a Quadratic Polynomial

$$ax^2 + bx + c$$

$a \neq 0$
 $a, b, c \in \mathbb{R}$

Coefficient = a, b, c

$$\alpha = \text{alpha}$$

$$\beta = \text{beta}$$

↑
Zeroes

Q. $-5x^2 - 3x + 2$
 $a = -5, b = -3, c = 2$

Q. $5x^2 - 2x^0 + 0x$
 $a = 5, b = 0, c = -2$

$$\alpha + \beta = -\frac{b}{a}$$

(Sum of zeroes)

$$\alpha \beta = \frac{c}{a}$$

(Product of zeroes)

#Q Find the zeros of the following quadratic polynomial and verify the relationship between the zeros and their coefficients:

CBSE 2019

$$q(y) = 7y^2 - \frac{11}{3}y - \frac{2}{3}$$

$$\alpha = 2/3, \beta = -1/7, a = 7, b = -\frac{11}{3}, c = -\frac{2}{3}$$

$$7y^2 - \frac{11}{3}y - \frac{2}{3} = 0$$

$$\frac{21y^2 - 11y - 2}{3} = 0$$

$$21y^2 - 11y - 2 = 0$$

$$\rho = -42, \sigma = -11$$

$-14, 3$

~~$21y^2 - 14y + 3y - 2 = 0$~~

~~$7y(3y - 2) + 1(3y - 2) = 0$~~

$$(3y - 2)(7y + 1) = 0$$

$$3y = 2$$

$$y = 2/3$$

$$7y + 1 = 0$$

$$y = -1/7$$

~~Verify~~

$$\alpha + \beta = -b/a$$

$$\frac{2}{3} + -\frac{1}{7} = -\frac{11}{21}$$

$$\frac{14 - 3}{21} = \frac{11}{21}$$

$$\frac{11}{21} = \frac{11}{21}$$

$$\alpha\beta = c/a$$

$$\frac{2}{3} \times -\frac{1}{7} = -\frac{2}{21}$$

$$\frac{-2}{21} = -\frac{2}{21}$$

#Q. Find the zeros of the quadratic polynomial $f(x) = \underline{6x^2} - 3$, and verify the relationship between the zeros and its coefficients:

$$6x^2 - 3 = 0$$

$$6x^2 = 3$$

$$x^2 = \frac{3}{6}$$

$$x^2 = \frac{1}{2}$$

$$x = \pm \sqrt{\frac{1}{2}}$$

$$x = \frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}$$

α β

a = 6
b = 0
c = -3

$$\alpha + \beta = -b/a$$

$$\frac{1}{\sqrt{2}} + -\frac{1}{\sqrt{2}} = -\frac{0}{6}$$

$$\alpha \beta = c/a$$

$$\frac{1}{\sqrt{2}} \times \frac{-1}{\sqrt{2}} = \frac{-1}{6}$$

$$0 = 0$$

$$\frac{-1}{2} = -\frac{1}{2}$$

Hence
verified

#Q. Find the zeros of the polynomial $f(u) = 4u^2 + 8u$ and verify the relationship between the zeros and its coefficients.

$$4u^2 + 8u = 0$$
$$[4u][u+2] = 0$$

$$\alpha = 0$$
$$\beta = -2$$

$$a = 4$$
$$b = 8$$
$$c = 0$$

GPh

$$4u = 0 \quad u+2 = 0$$

$$u = 0 / u$$

$$u = 0$$

$$u = -2$$

#Q. Find the zeroes of each of the following quadratic polynomial and verify the relationship between the zeroes and their coefficients:

(i) $g(s) = 4s^2 - 4s + 1$

(ii) $g(x) = 6x^2 - 3 - 7x$



#Q. Find the zeroes of following quadratic polynomial.

$$(i) \sqrt{3}x^2 + \cancel{10}x + 7\sqrt{3}$$

$$(ii) x^2 + 2\sqrt{2}x - 6$$

Sum = $\cancel{10}$ Product = $7\sqrt{3} \times \sqrt{3}$
 $= 7x^2$
 $= -21$

$$(\sqrt{3}x+7)(x+\sqrt{3})=0$$

$$\sqrt{3}x+7=0$$

$$x+\sqrt{3}=0$$

$$x = -7/\sqrt{3}$$

$$x = -\sqrt{3}$$

$$\sqrt{3}x^2 + 7x + 3x + 7\sqrt{3} = 0$$

$$x(\sqrt{3}x+7) + 1(3x+7\sqrt{3}) = 0$$

$$x(\sqrt{3}x+7) + \sqrt{3}(\sqrt{3}x+7) = 0$$

α

β

#Q. Find the zeroes of following quadratic polynomial.

(i) $\sqrt{3}x^2 + 10x + 7\sqrt{3}$



(ii) $x^2 + 2\sqrt{2}x - 6$

$S=2\sqrt{2}, P=-6$

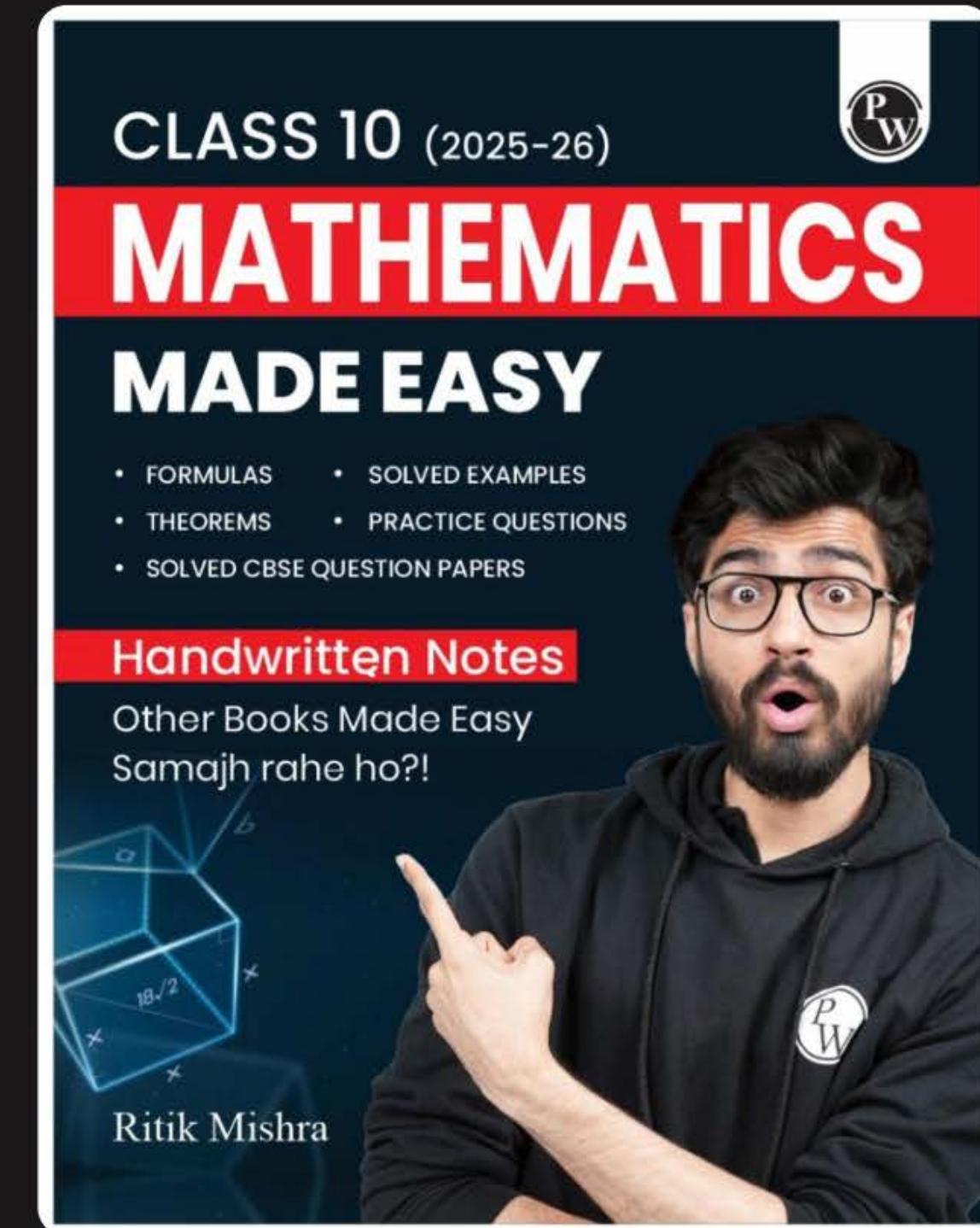
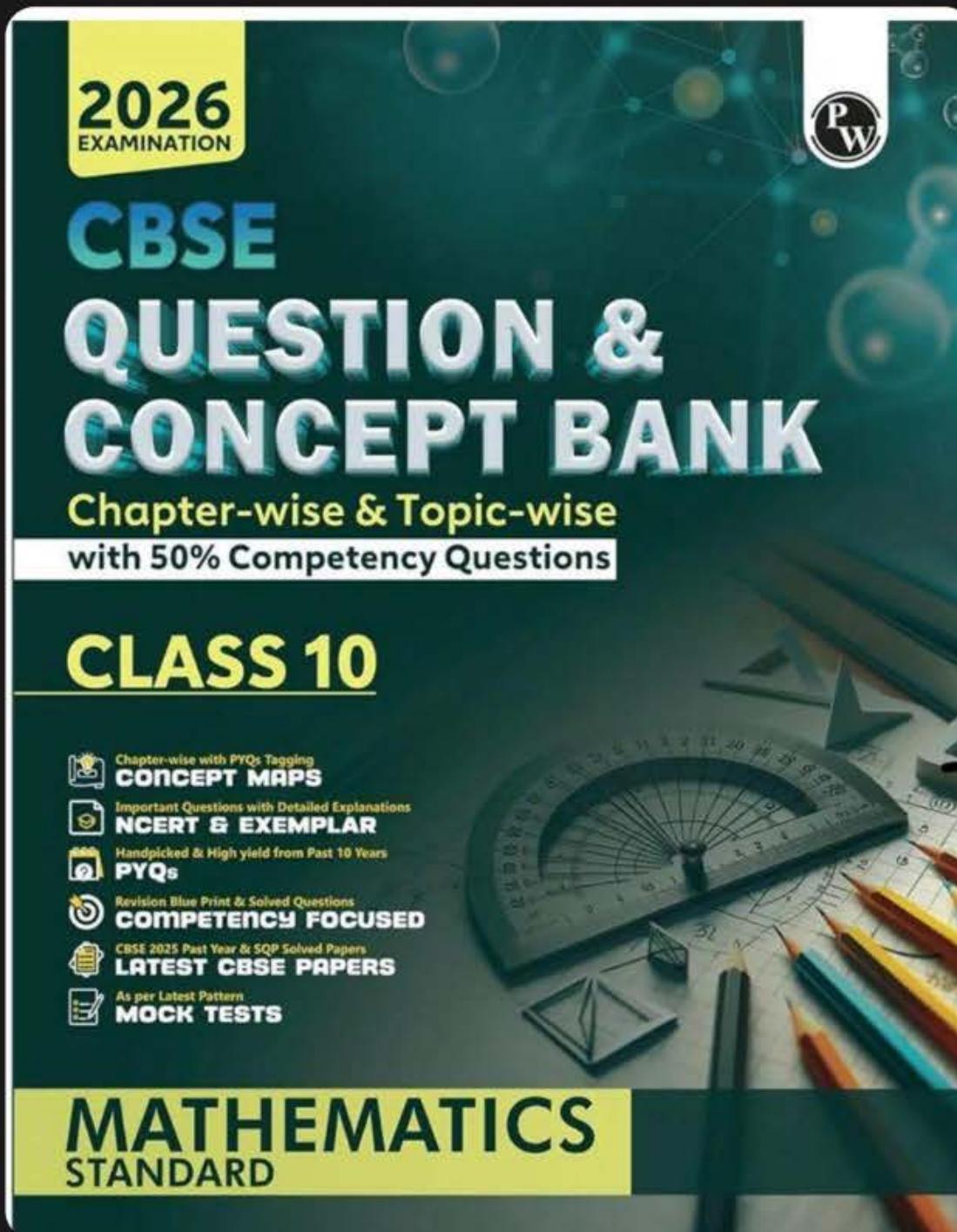
#Q. If one zero of the quadratic polynomial $kx^2 + 3x + k$ is 2, then the value of k is ~~# Graph~~

A $\frac{5}{6}$

B $-\frac{5}{6}$

C $\frac{6}{5}$

D $-\frac{6}{5}$





**WORK HARD
DREAM BIG
NEVER GIVE UP**



Thank
You