



UDAAN



2026

POLYNOMIALS

MATHS

LECTURE-4

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Topics *to be covered*



A

Questions on Relation between Zeroes and Coefficients of Quadratic Polynomial

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#Q. Find the zeroes of following quadratic polynomial.

(i) $x^2 + 2\sqrt{2}x - 6$

Sum = $2\sqrt{2}$
Product = -6

$3\sqrt{2}, -\sqrt{2}$

$$x^2 + 3\sqrt{2}x - \sqrt{2}x - 6 = 0$$

$$x(x + 3\sqrt{2}) - \sqrt{2}(x + 3\sqrt{2}) = 0$$

$$(x + 3\sqrt{2})(x - \sqrt{2}) = 0$$

$$x + 3\sqrt{2} = 0$$

$$x = -3\sqrt{2}$$

$$x - \sqrt{2} = 0$$

$$x = \sqrt{2}$$

#OT

#Q. Zeroes?

(i) $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3}$ (2014)

$S = -2\sqrt{2}$, $P = \frac{-2\sqrt{3}}{\sqrt{3}} = -2$

$-3\sqrt{2}, \sqrt{2}$

$\sqrt{3}x^2 - 3\sqrt{2}x + \sqrt{2}x - 2\sqrt{3} = 0$

$\sqrt{3}x \left[\frac{\sqrt{3}x^2}{\sqrt{3}x} - \frac{3\sqrt{2}x}{\sqrt{3}x} \right] + \sqrt{2} \left[\frac{\sqrt{2}x}{\sqrt{2}} - \frac{2\sqrt{3}}{\sqrt{2}} \right] = 0$

$\sqrt{3}x [x - \sqrt{6}] + \sqrt{2} [x - \sqrt{6}] = 0$

(ii) $3x^2 - 2\sqrt{6}x + 2$ (2012, 10)

$(x - \sqrt{6})(\sqrt{3}x + \sqrt{2}) = 0$

$x = \sqrt{6}$

$x = -\frac{\sqrt{2}}{\sqrt{3}}$

#Gap

Q $3x^2 - 256x + 2 = 0$
 Sum = -256, product = 6

$(-\sqrt{6}, -\sqrt{6})$

#GPH

$$3x^2 - 56x - 56x + 2 = 0$$

#Q. If one zero of the quadratic polynomial $kx^2 + 3x + k$ is 2, then the value of k is

A

$$\frac{5}{6}$$

B

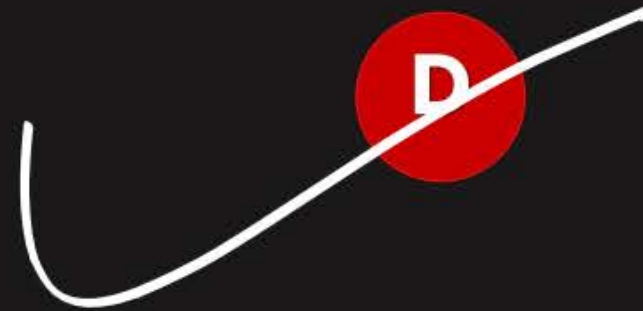
$$-\frac{5}{6}$$

C

$$\frac{6}{5}$$

D

$$-\frac{6}{5}$$



$$kx^2 + 3x + k$$

$$Zero = 2$$

$$k(2)^2 + 3(2) + k = 0$$

$$4k + 6 + k = 0$$

$$5k = -6$$

$$k = -6/5$$

#GPK



Relationship between the zeroes and coefficients of a Quadratic Polynomial

$$ax^2 + bx + c$$

$$a \neq 0$$

$$a, b, c \in \mathbb{R}$$

$$\alpha + \beta = -\frac{b}{a}$$

(sum)

$$\alpha \beta = \frac{c}{a}$$

(product)

$\textcircled{a=6} \textcircled{b=-7} \textcircled{c=2}$
 $\underline{Q} \quad 6x^2 - 7x + 2$

Sum of zeroes $= -\frac{b}{a} = -\frac{-7}{6} = \frac{7}{6}$

Product of zeroes $= \frac{c}{a} = \frac{2}{6} = \frac{1}{3}$



#Q. If the product of the zeros of the polynomial $ax^2 - 6x - 6$ is 4, find the value of a.

CBSE 2008

$$ax^2 - 6x - 6$$

$$\text{Sum} = -\frac{b}{a} = -\frac{-6}{a} = \frac{6}{a}$$

$$\text{Product} = \frac{c}{a} = \frac{-6}{a}$$

$$\text{Product} = -\frac{6}{a}$$

$$4 = -\frac{6}{a}$$

$$a = -\frac{6}{4} = -\frac{3}{2}$$

Qanda

#Q. If one zero of the polynomial $2x^2 + 3x + \lambda$ is $\frac{1}{2}$, find the value of λ and the other zero.

$$2x^2 + 3x + \lambda$$

↖ α
↗ β

$$a=2, b=3, c=\lambda$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\alpha + \beta = -\frac{3}{2}$$

$$\alpha\beta = \frac{c}{a}$$

$$\alpha\beta = \frac{\lambda}{2}$$

$$\frac{1}{2} + \beta = -\frac{3}{2}$$

$$\beta = -\frac{3}{2} - \frac{1}{2}$$

$$\beta = -\frac{4}{2}$$

$$\beta = -2$$

$$\alpha\beta = \frac{\lambda}{2}$$

$$\frac{1}{2} \times -2 = \frac{\lambda}{2}$$

$$-1 = \frac{\lambda}{2}$$

$$-2 = \lambda$$

Let $\alpha = \frac{1}{2}$

#Q. Find the value of k such that the polynomial $x^2 - (k + 6)x + 2(2k - 1)$ has sum of its zeroes equal to half of their product.

CBSE 2019

$$x^2 - (k + 6)x + 2(2k - 1)$$

$$a = 1$$

$$b = -(k + 6)$$

$$c = 2(2k - 1)$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\alpha + \beta = -\frac{-(k + 6)}{1}$$

$$\alpha + \beta = k + 6$$

$$\alpha\beta = \frac{c}{a}$$

$$\alpha\beta = \frac{2(2k - 1)}{1}$$

$$\alpha\beta = 4k - 2$$

Sum of zeroes equal to half of their product

$$\alpha + \beta = \frac{1}{2}\alpha\beta$$

$$k + 6 = \frac{4k - 2}{2}$$

$$2k + 12 = 4k - 2$$

$$12 + 2 = 4k - 2k$$

$$14 = 2k$$

$$\frac{14}{2} = k$$

$$7 = k$$

#Q. If the sum of the zeros of the quadratic polynomial $f(t) = kt^2 + 2t + 3k$ is equal to their product, find the value of k .

$$\alpha + \beta = \alpha \beta$$

$$\frac{-2}{k} = 3$$

$$\frac{-2}{3} = k$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\alpha + \beta = -\frac{2}{k}$$

$$\alpha \beta = \frac{c}{a}$$

$$\alpha \beta = \frac{3k}{k}$$

$$\alpha \beta = 3$$

A -2/3

B -3/2

C 2/3

D NOTA

$$ax^2 + bx + c$$

#Q. If one zero of the polynomial $p(x) = 6x^2 + 37x - (k - 2)$ is reciprocal of the other, then find the value of k .

CBSE 2023

Let the zeroes be α and $\frac{1}{\alpha}$

$$a=6, b=37, c=-(k-2)$$

$$\text{Sum} = -\frac{b}{a}$$

$$\text{Product} = \frac{c}{a}$$

$$\alpha + \frac{1}{\alpha} = -\frac{37}{6}$$

$$\alpha \times \frac{1}{\alpha} = \frac{-(k-2)}{6}$$

~~$$\alpha \times \frac{1}{\alpha} = \frac{-(k-2)}{6}$$~~

$$1 = \frac{-k+2}{6}$$

$$6 = -k+2$$

$$k = 2-6$$

$$k = -4$$

$$1 = \frac{-k+2}{6}$$

$$6 = -k+2$$

$$k = 2-6$$

$$k = -4$$

#Q. If one zero of the polynomial $(a^2 + 9)x^2 + 13x + 6a$ is reciprocal of the other, find the value of a .

$$a = a^2 + 9, b = 13, c = 6a$$

CBSE 2008

$$\alpha, \frac{1}{\alpha}$$

$$\text{Sum} = -\frac{b}{a}$$

$$\alpha + \frac{1}{\alpha} = -\frac{13}{a^2 + 9}$$

$$\text{Product} = \frac{c}{a}$$

$$\cancel{\alpha} \times \cancel{\frac{1}{\alpha}} = \frac{6a}{a^2 + 9}$$

$$1 = \frac{6a}{a^2 + 9}$$

$$1(a^2 + 9) = 6a$$

$$a^2 + 9 = 6a$$

$$a^2 - 6a + 9 = 0$$

$$\text{Sum} = -6, \text{product} = 9$$

$$-3, -3$$

$$a^2 - 3a - 3a + 9 = 0$$

$$a(a-3) - 3(a-3) = 0$$

$$(a-3)(a-3) = 0$$

$$a-3=0$$

$$a-3=0$$

$$a=3$$

A 3

B 4

C -3

D NOTA

#Q. If one zero of the quadratic polynomial $f(x) = 4x^2 - 8kx - 9$ is negative of the other, find the value of k .

$$ax^2 + bx + c$$

$$a=4, b=-8k, c=-9.$$

let the zeroes be

α and $-\alpha$

$$\text{Sum} = -\frac{b}{a}$$

$$\cancel{\alpha} + \cancel{-\alpha} = -\frac{-8k}{4}$$

$$0 = \frac{8k}{4}$$

$$0 = 2k$$

$$0 = k$$

$$\boxed{0 = k}$$

$$\text{Product} = \frac{c}{a}$$

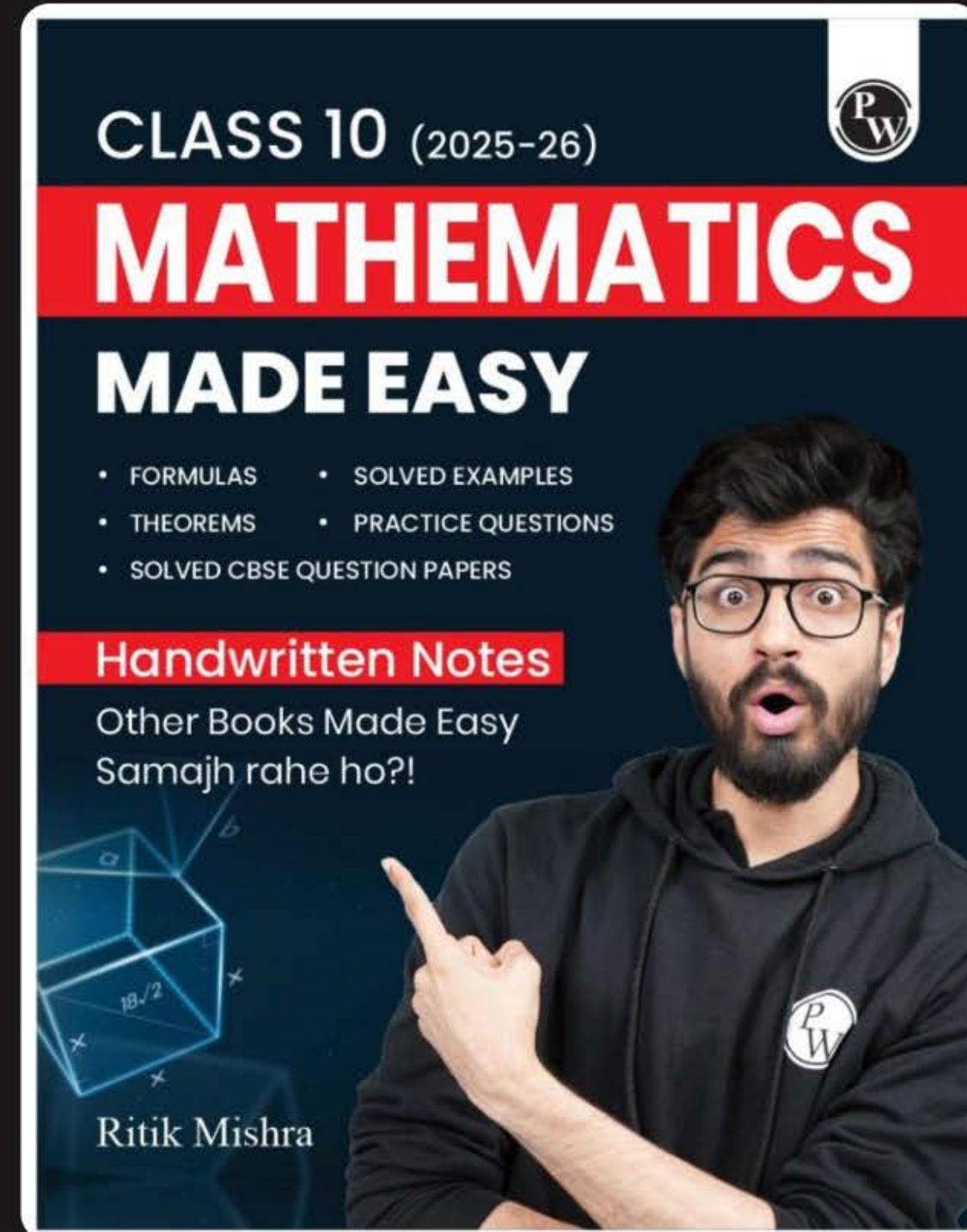
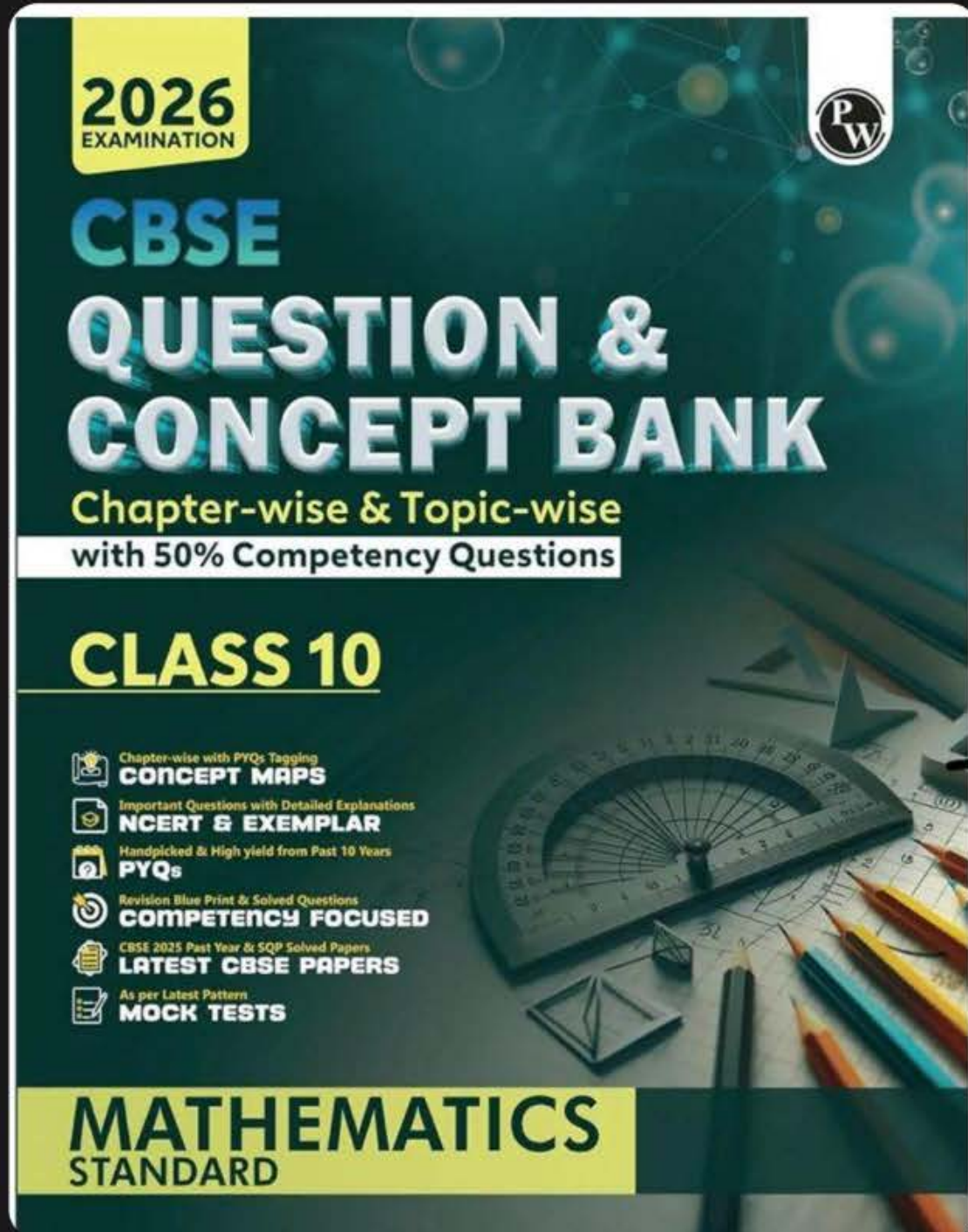
$$\alpha \times -\alpha = -\frac{9}{4}$$

A -1

B 1

☒ C 0

D NOTA





WORK HARD

DREAM BIG

NEVER GIVE UP



Thank
You