



UDAAN



2026

POLYNOMIALS

MATHS

LECTURE-1

BY-RITIK SIR



Topics

to be covered



 Meaning of Polynomials

 Types of Polynomials

 Zero of a Polynomials

 General Form of a Polynomials

 Geometrical Meaning of Zero of a Polynomials

next class,



RITIK SIR

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Constants and Variables

$2, -2, \pi,$
 $\frac{3}{2}, \frac{100}{2}, 3.14,$
 $3.1452852 \dots$

vary
 ↓
 change

$x, y, z, \pi, p \dots$

Algebraic Expression

Collection of terms.

$\rightarrow x + 2$
 $\rightarrow x^2 + y^2 - 2x + 3$

Terms

Zero is not a term.

The non-zero part of an algebraic expression separated by + or - sign are called the terms.

V
 x

$C.V$
 $2.x$
 $-3x$
 $\frac{5}{2}x$

$V.V$
 $x^2 = x \times x$
 x^2y^2
 $2x^2y^2$
 $-2xy$



Polynomials

Special A.E



Aise algebraic expressions jisme Variable ki power whole number hoti hai, unko (polynomials) kehte hain.

non-negative integer.

- $3x + 5$ ✓
- $3x^2 - 5x + 4y + 2$ ✓
- $3x^{-1} + 5x + 2$ ✗
- $x + \frac{1}{x} = x + x^{-1}$ ✗
- $\frac{x^{3/2}}{x^{1/2}} = x^{3/2 - 1/2} = x^1 = x$ ✓



#Q. Which of the following is a polynomial?

A $2x^2 + \frac{3}{x} - 5$ ~~X~~

Handwritten: x^{-1} circled, arrow pointing to denominator.

B $-3x^2 + \sqrt{2x} + 4$ ~~X~~

Handwritten: $(2x)^{1/2} = 2^{1/2} (x^{1/2})$ with arrows pointing to $\sqrt{2x}$ and $x^{1/2}$ circled.

C $\sqrt{2}x^3 + \sqrt{3}x^2 + \sqrt{5}x - 3$

Handwritten: checkmark.

D $\frac{5}{x^3} + 2x^2 - 3x + \frac{1}{7}$ ~~X~~

Handwritten: x^{-3} circled, arrow pointing to $\frac{5}{x^3}$.



Degree of a Polynomials

Highest power of variable ko degree kehte hai.

$$3x^2 - 5x + 2$$

$$d=2$$

$$-4x^4 + 5x^2 - 3x$$

$$d=4$$

$$\cancel{5x^4} - 2x + 3x - \cancel{5x^4}$$

$$d=1$$

$$1x$$



#Q. Which of the following expression are polynomials? In case of a polynomial write its degree?

- (i) $x^3 - 5x + 2$ ✓ $d=3$
- (ii) $y^2 + \sqrt{2}y - \sqrt{5}$ ✓ $d=2$
- (iii) $2\sqrt{x} + 7$ ✗
- (iv) -6 ✓ $d=0$
- (v) $4t^2 + \frac{1}{6}t + 2\sqrt{3}$ ✓ $d=2$
- (vi) $z^2 + \frac{5}{z^2} + 1$ ✗
- (vii) $1 - \sqrt{5}x$ ✓ $d=1$
- (viii) $\frac{6\sqrt{x} + x^{3/2}}{\sqrt{x}}$

$$\begin{aligned}
 \text{(viii)} \quad & \frac{6\sqrt{x} + x^{3/2}}{\sqrt{x}} \\
 &= \frac{6\cancel{\sqrt{x}}}{\cancel{\sqrt{x}}} + \frac{x^{3/2}}{\sqrt{x}} \\
 &= 6 + \frac{x^{3/2}}{x^{1/2}} \\
 &= 6 + x^{\frac{3}{2} - \frac{1}{2}} \\
 &= 6 + x^1 = 6 + x \quad \checkmark \quad d=1
 \end{aligned}$$

$$\frac{1+2}{3} = \frac{1}{3} + \frac{2}{3}$$

#Q. Write:

(i) The coefficient of x^3 in $x + 3x^2 - 5x^3 + x^4$

-5

(ii) The coefficient of x in $\sqrt{3} - 2\sqrt{2} + 6x^2 + 0x$

0

(iii) The coefficient of x^2 in $3x - 3 + x^3$

0

(iv) The constant term in $\frac{\pi}{2}x^2 + 7x - \frac{2}{5}\pi$

$-\frac{2}{5}\pi$ — constant term.

Q $-x^2 + 3x^2 + 5x^3 + 2x^2 = 5x^3 + 4x^2$

C of $x^2 = 4$

Types of polynomials

Number of terms

Monomials (1 term)

$$x, 2x^2, -3x^3, 4x^5$$

Binomials (2 terms)

$$2x + 5$$

Trinomials (3 terms)

$$-3x^2 + 5x^2 + 2x^3$$

$$2x^2 + 2x^3$$

Degree

$$d=1$$

Linear

$$d=2$$

Quadratic

$$d=3$$

Cubic

$$d=4$$

Biquadratic

$$d=0$$

Constant (non-zero)

$$d = \text{not defined}$$

Zero polynomial

$$5x^3 - 2x^2 + 3x + 5$$

$$-2x^0, 5x^0, \frac{5}{2}x^0, -100x^0$$

$$0x^0, 0x^1, 0x^2, 0x^{1000}, \dots$$



Value of a polynomial

- The value of a polynomial $p(x)$ at $x = \alpha$ is obtained by putting $x = \alpha$ in $p(x)$ and it is denoted by $p(\alpha)$.

quadratic monomial

$$g(x) = 3x^2$$

$$g(0) = \boxed{0}$$

$$g(-2) = \boxed{12}$$

$$g(3) = \boxed{27}$$

$$\text{Zero} = 0$$

$$f(x) = -5x + 2$$

$$f\left(\frac{2}{5}\right) = -\cancel{5} \cdot \frac{2}{\cancel{5}} + 2 = \boxed{0}$$

$$f(0) = -5(0) + 2 = 0 + 2 = \boxed{2}$$

$$\text{Zero} = 2/5$$

$$p(x) = x + 5$$

linear binomial

$$p(1) = 1 + 5 = \boxed{6}$$

$$p(-1) = -1 + 5 = \boxed{4}$$

$$p(0) = \boxed{5}$$

$$p(-5) = \boxed{0}$$

$$p(100) = \boxed{105}$$

$$\text{Zero} = -5$$



Zero of the Polynomial



Variable ki Value

$$\text{Poly} = 0$$

① $P(x) = -2 + x$
 $\text{Zero} = 2$

② $F(x) = 5x - 3$
 $5x - 3 = 0$
 $5x = 3$

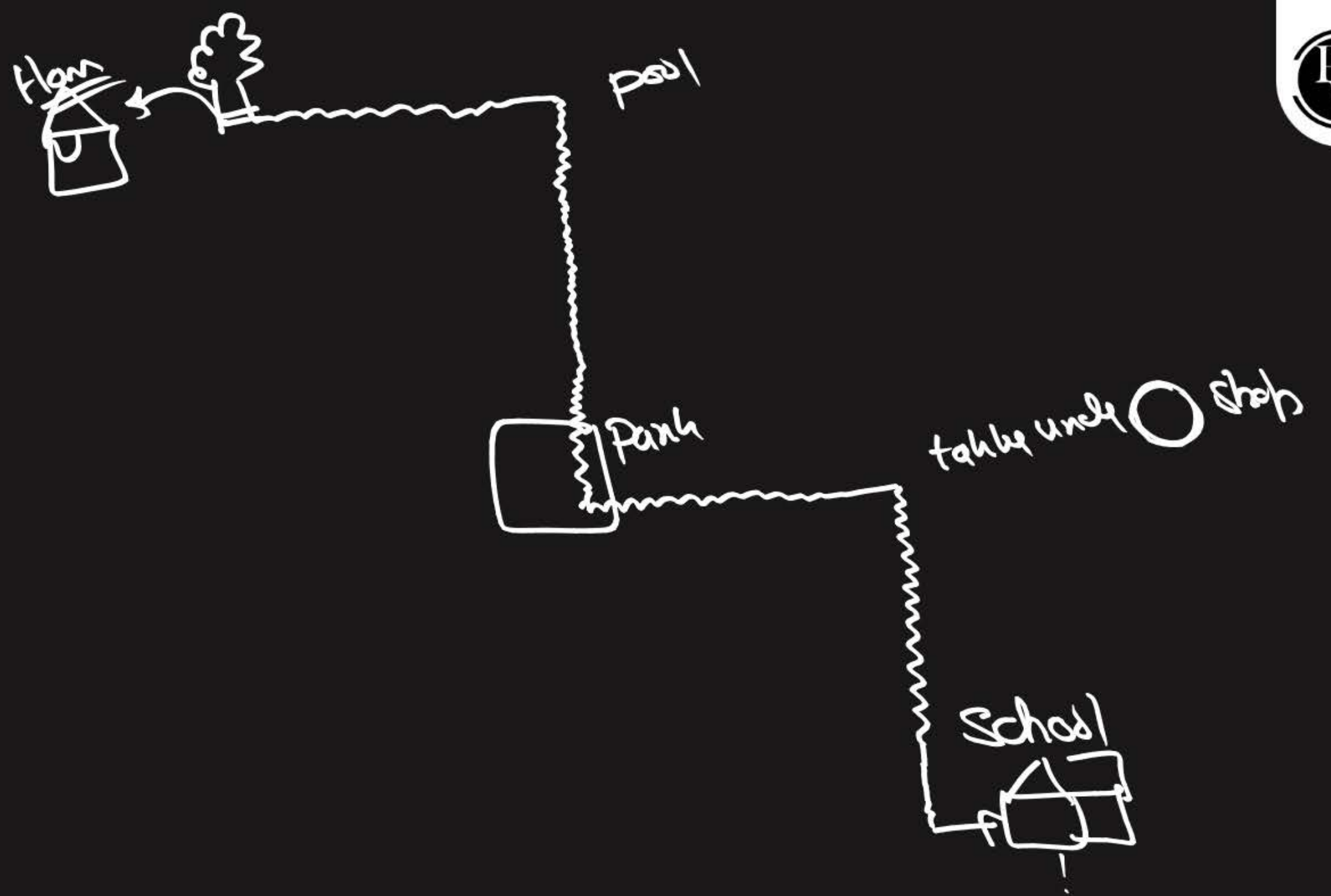
$$x = 3/5$$

$$\text{Zero} = 3/5$$

③ $g(x) = ax + b$
 $ax + b = 0$
 $ax = -b$

$$x = -\frac{b}{a}$$

$$\text{Zero} = -b/a$$



$$f(x) = x - 5$$

→ linear 'p'

zero = 5

$$f(x) = x^2 - 4$$

zero = 2, -2

$$g(x) = x^2$$

zero = 0

no. of zeroes = !!



Number of Zeroes of any Polynomial

Maximum = almost



$d=1$

Linear Polynomial

[Only 1 zero]

$d=2$

Quadratic Polynomial

[Maximum 2 zeroes]

$d=3$

Cubic Polynomial

[Maximum 3 zeroes]

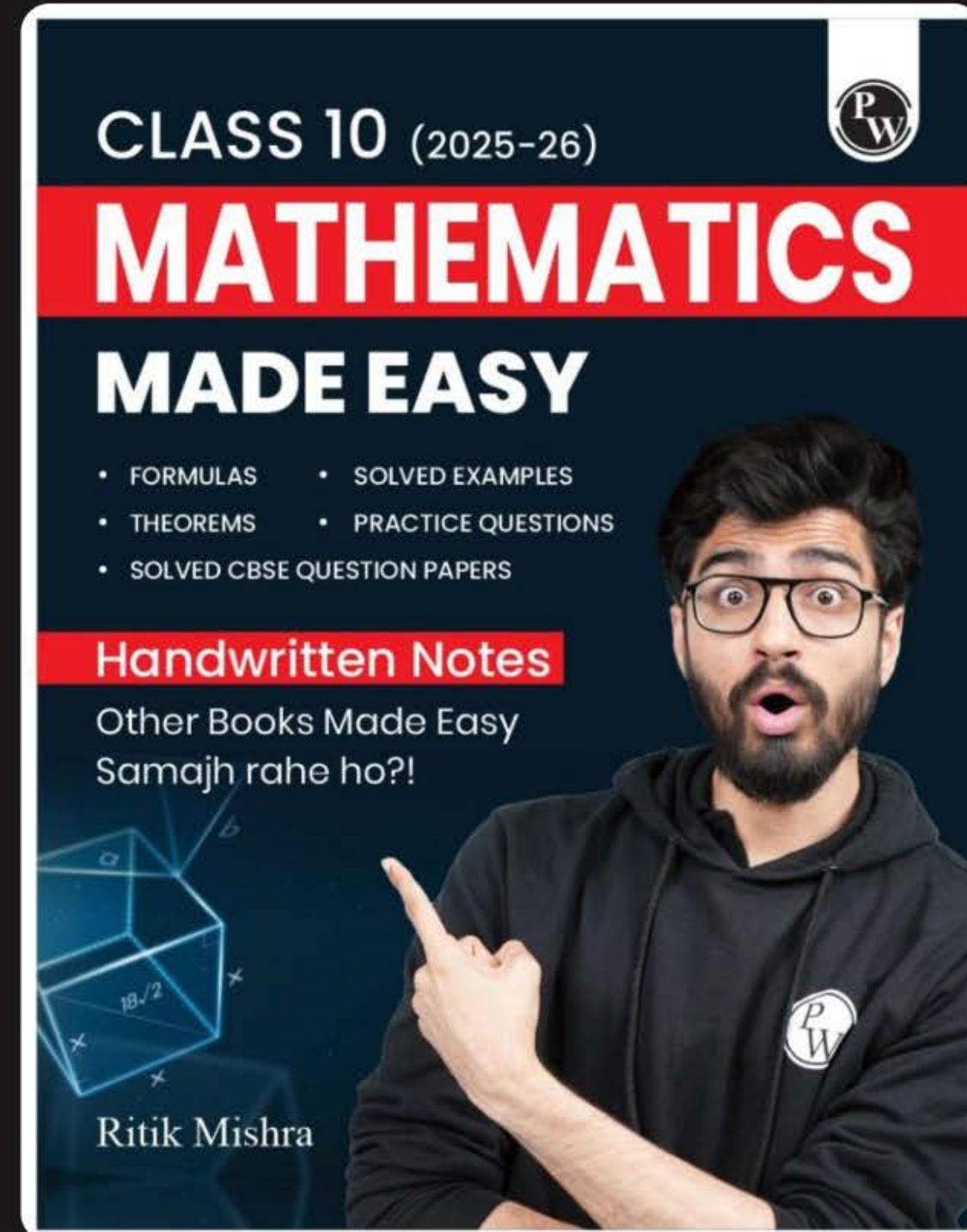
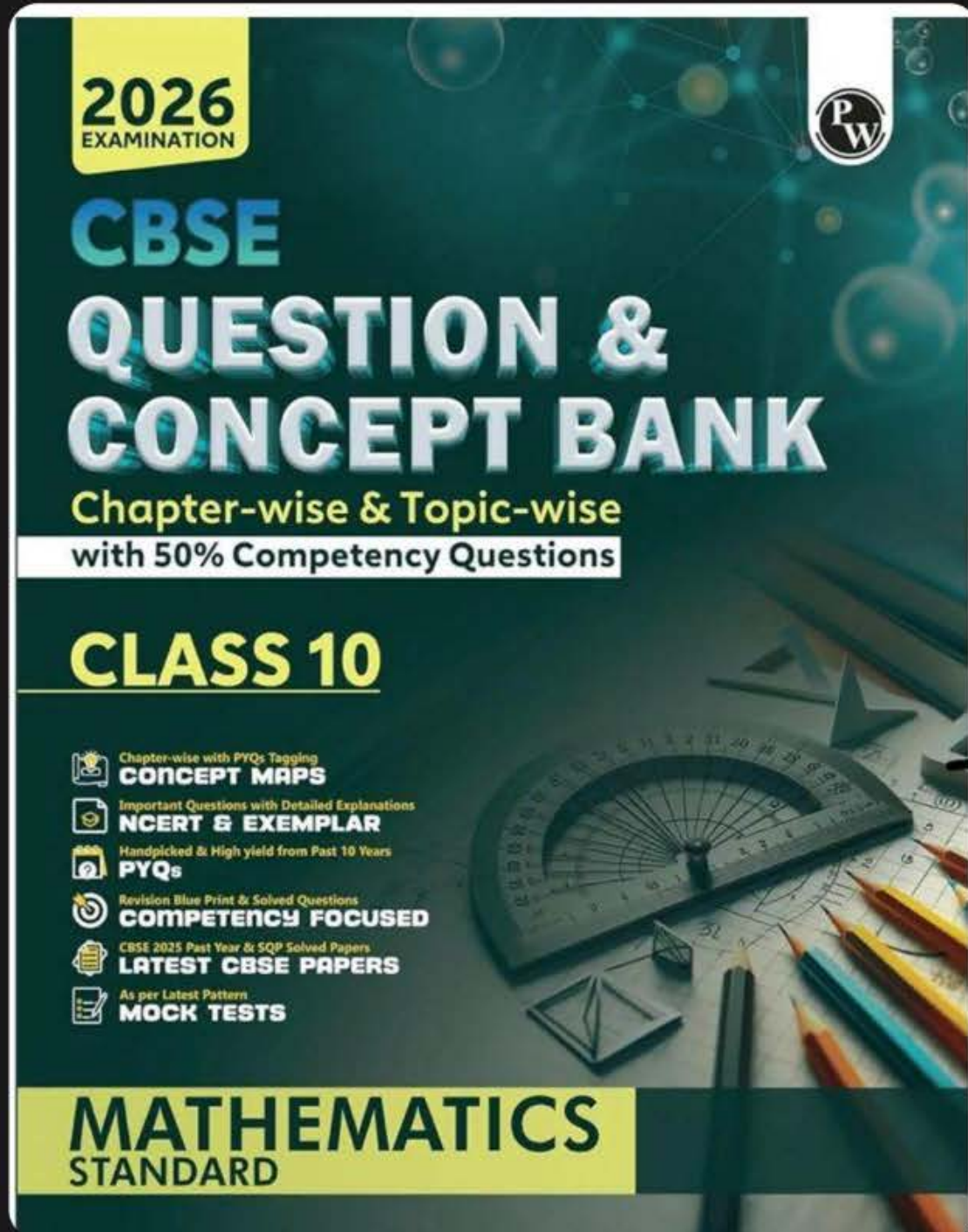
$d=7$

Maximum 7



Some Important Observations

- (i) A constant polynomial does not have any zero
- (ii) Every linear polynomial has one and only one zero.
- (iii) 0 may or may not be the zero of a given polynomial
- (iv) Number of zero of a polynomial cannot exceed its degree.





WORK HARD

DREAM BIG

NEVER GIVE UP



Thank
You