



UDAAN



2026

POLYNOMIALS

MATHS

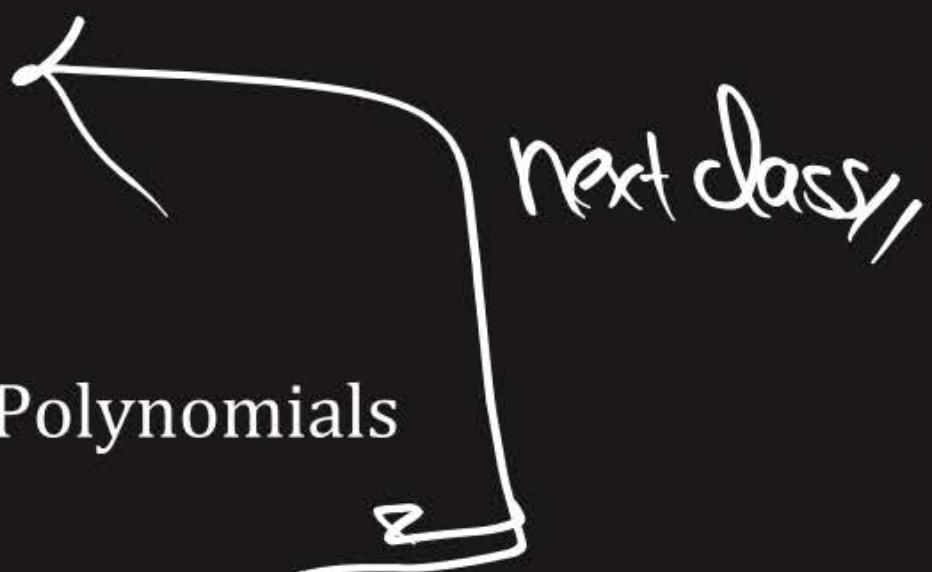
LECTURE-1

BY-RITIK SIR



Topics *to be covered*

- A Meaning of Polynomials
- B Types of Polynomials
- C Zero of a Polynomials
- D General Form of a Polynomials
- E Geometrical Meaning of Zero of a Polynomials





RITIK SIR

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Constants and Variables

2, -2, π ,
 $\frac{3}{2}$, $\frac{10}{21}$, 3.14,
3.1452852.....

$x, y, 2, \pi, \dots$

Vary
change.

Algebraic Expression

Collection of terms.

$$\rightarrow x + 2$$

$$\rightarrow x^2 + y^2 - 2x + 3$$

Terms

Zero
is not
a term.

The non-zero part of an algebraic expression separated by + or - sign are called the terms.

$$V$$

 x

$$C.V$$

 $2 \cdot x$

$$-3x$$

$$\sum x$$

$$V.V$$

 $x^2 - xy$
 x^2yz
 $2x^2yz$

$$-2xy$$



Polynomials

Special A.E



Aise algebraic expressions jisme Variable ki power whole number hoti ha, unko (polynomials) kehte hain.

- $3x + 5$ ✓
- $3x^2 - 5x + 4y + 2$ ✓
- $3x^{-1} + 5x + 2$ ✗
- $x + \frac{1}{x} = x + x^{-1}$ ✗
- $\frac{x^{3/2}}{x^{1/2}} = x^{\frac{3}{2}-\frac{1}{2}} = x^{\frac{2}{2}} = x^1$ ✓



non-negative
integer.

#Q. Which of the following is a polynomial?

A

$$2x^2 + \frac{3}{x} - 5$$

$$\cancel{x^{-1}}$$

C

$$\sqrt{2}x^3 + \sqrt{3}x^2 + \sqrt{5}x - 3$$

$$\cancel{x^{-3}}$$

B

$$-3x^2 + \sqrt{2x} + 4$$

$$\cancel{(2x)^{1/2}} = \cancel{2^{1/2}} \cancel{x^{1/2}}$$

D

$$\frac{5}{x^3} + 2x^2 - 3x + \frac{1}{7}$$

$$\cancel{x^{-3}}$$



Degree of a Polynomials

Highest power of variable ko degree kehte hai.

$$3x^2 - 5x + 2$$

$$d=2$$

$$-4x^4 + 5x^2 - 3x$$

$$d=4$$

$$\cancel{5x^4} - 2x + 3x - 5x^4$$

$$d=1$$

$$lx$$



#Q. Which of the following expression are polynomials? In case of a polynomial write its degree?

(i) $x^3 - 5x + 2$ ✓ $d=3$

(ii) $y^2 + \sqrt{2}y - \sqrt{5}$ ✓ $d=2$

(iii) $2\sqrt{x} + 7$ ✗

(iv) -6 ✓ $d=0$

(v) $4t^2 + \frac{1}{6}t + 2\sqrt{3}$ ✓ $d=2$

(vi) $z^2 + \frac{5}{z^2} + 1$ ✗

(vii) $1 - \sqrt{5}x$ ✓ $d=1$

(viii) $\frac{6\sqrt{x}+x^{3/2}}{\sqrt{x}}$

$$\begin{aligned}
 & (\text{viii}) \frac{6\sqrt{x}+x^{3/2}}{\sqrt{x}} \\
 & = \frac{6\sqrt{x}}{\sqrt{x}} + \frac{x^{3/2}}{\sqrt{x}} \\
 & = 6 + \frac{x^{3/2}}{x^{1/2}} \\
 & = 6 + x^{\frac{3}{2}-\frac{1}{2}} \\
 & = 6 + x^{\frac{2}{2}} = 6+x^1 = 6+x^1 \quad \boxed{d=1}
 \end{aligned}$$

$$\begin{aligned}
 & 1+2 = \frac{1}{3} + \frac{2}{3} \\
 & \boxed{3}
 \end{aligned}$$

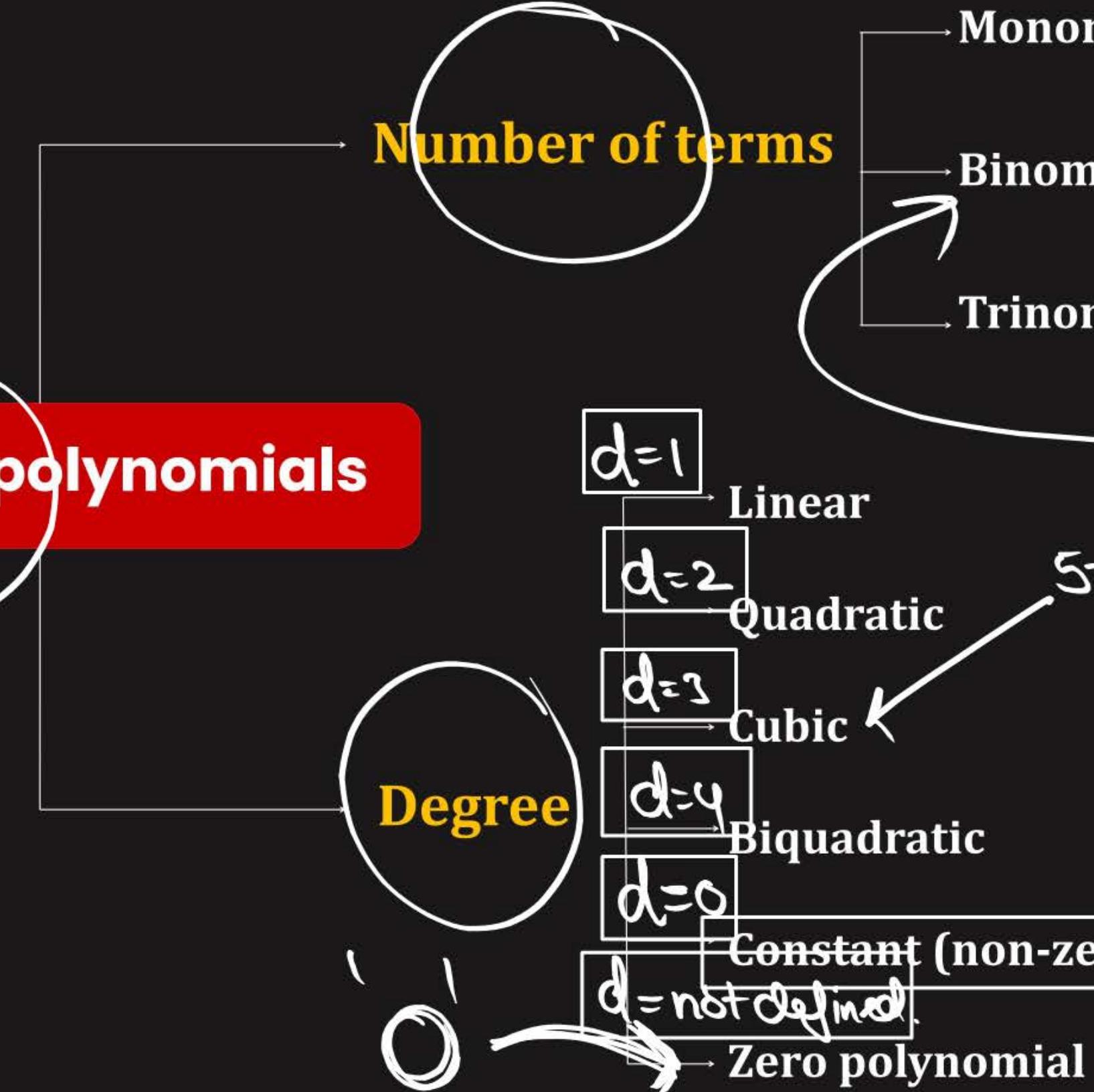
#Q. Write:

- (i) The coefficient of x^3 in $x + 3x^2 - 5x^3 + x^4$ (-5)
- (ii) The coefficient of x in $\sqrt{3} - 2\sqrt{2} + 6x^2 + ox$ (0)
- (iii) The coefficient of x^2 in $3x - 3 + x^3$ (0)
- (iv) The constant term in $\frac{\pi}{2}x^2 + 7x - \frac{2}{5}\pi$ Constant term.

0 $-x^2 + 3x^2 + 5x^3 + 2x^2 = 5x^3 + 4x^2$

'C' of $x^2 = 4$

Types of polynomials



$-2x^0, 5x^0, \frac{5x^0}{2}, -100x^0$
 $0x^0, 0x^1, 0x^2, 0x^{1000}, \dots$

$x, 2x^2, -3x^3, ux^5,$
 $2x+5$
 $-3x^2+5x^2$
 $+2x^3$
 $2x^2+2x^3$

$$5x^3 - 2x^2 + 3x + 5$$



Value of a polynomial

- The value of a polynomial $p(x)$ at $x = \alpha$ is obtained by putting $x = \alpha$ in $p(x)$ and it is denoted by $p(\alpha)$.

$$P(x) = x + 5$$

linear binomial.

$$P(1) = 1 + 5 = 6$$

$$P(-1) = -1 + 5 = 4$$

$$P(0) = 5$$

$$P(-5) = 0$$

$$P(100) = 105$$

$$g(x) = 3x^2$$

$$g(0) = 0$$

$$g(-2) = 12$$

$$g(3) = 27$$

$$\text{Zeros} = 0$$

$$f(x) = -5x + 2$$

$$f\left(\frac{2}{5}\right) = -5 \cdot \frac{2}{5} + 2 = 0$$

$$f(0) = -5(0) + 2 = 0 + 2 = 2$$

$$\text{Zeros} = 2/5$$

quadratic monomial.



Zero of the Polynomial

Variable x Value

$$\text{Poly} = 0$$

① $P(x) = -2 + x$ ③ $g(x) = ax + b$

$\text{Zero} = 2$

$$ax + b = 0$$
$$ax = -b$$

② $f(x) = 5x - 3$

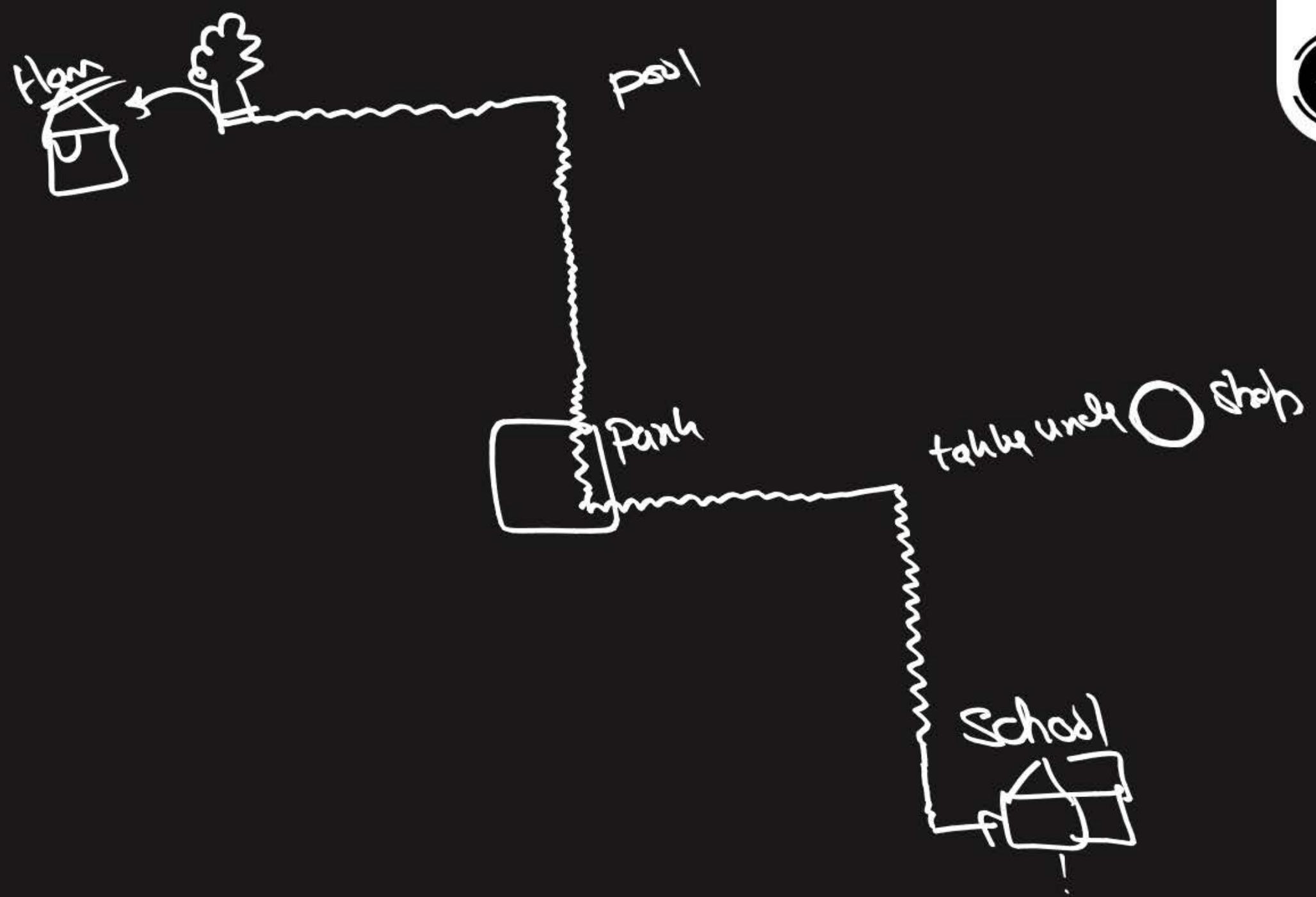
$$5x - 3 = 0$$

$$5x = 3$$

$$x = 3/5$$

$$\text{Zero} = -b/a$$

$$\text{Zero} = 3/5$$



$$f(x) = x - s$$

↑ linear 'P'

$\text{zeros} = 5$

PW

no of zeroes = 0

$$f(x) = x^2 - 4$$

$\text{zeros} = 2$

$$g(x) = x^2$$

$\text{zeros} = 0$

Number of Zeroes of any Polynomial



$d=1$

Linear Polynomial

[Only 1 zero]

$d=2$

Quadratic Polynomial

[Maximum 2 zeroes]

$d=3$

Cubic Polynomial

[Maximum 3 zeroes]

$d=7$

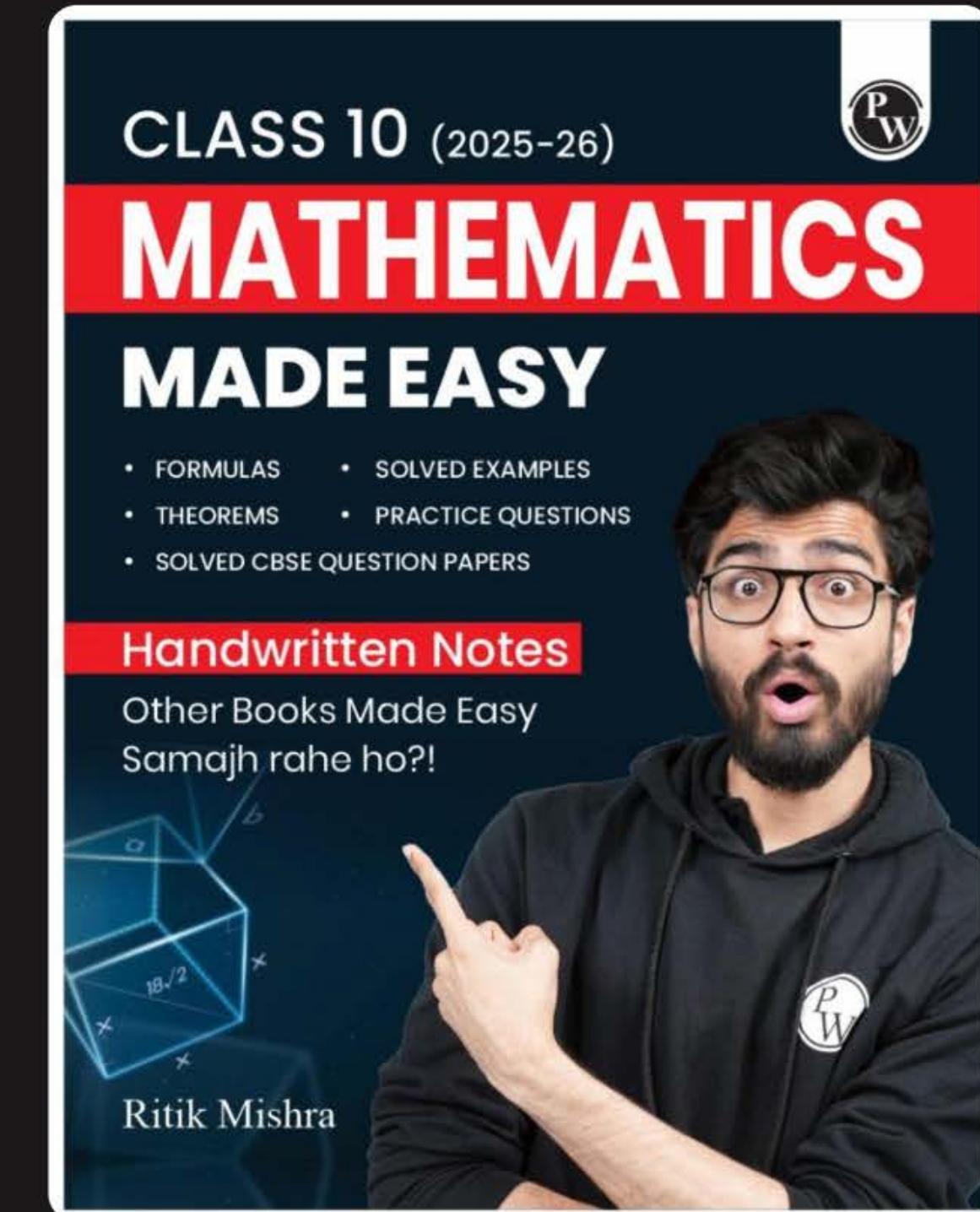
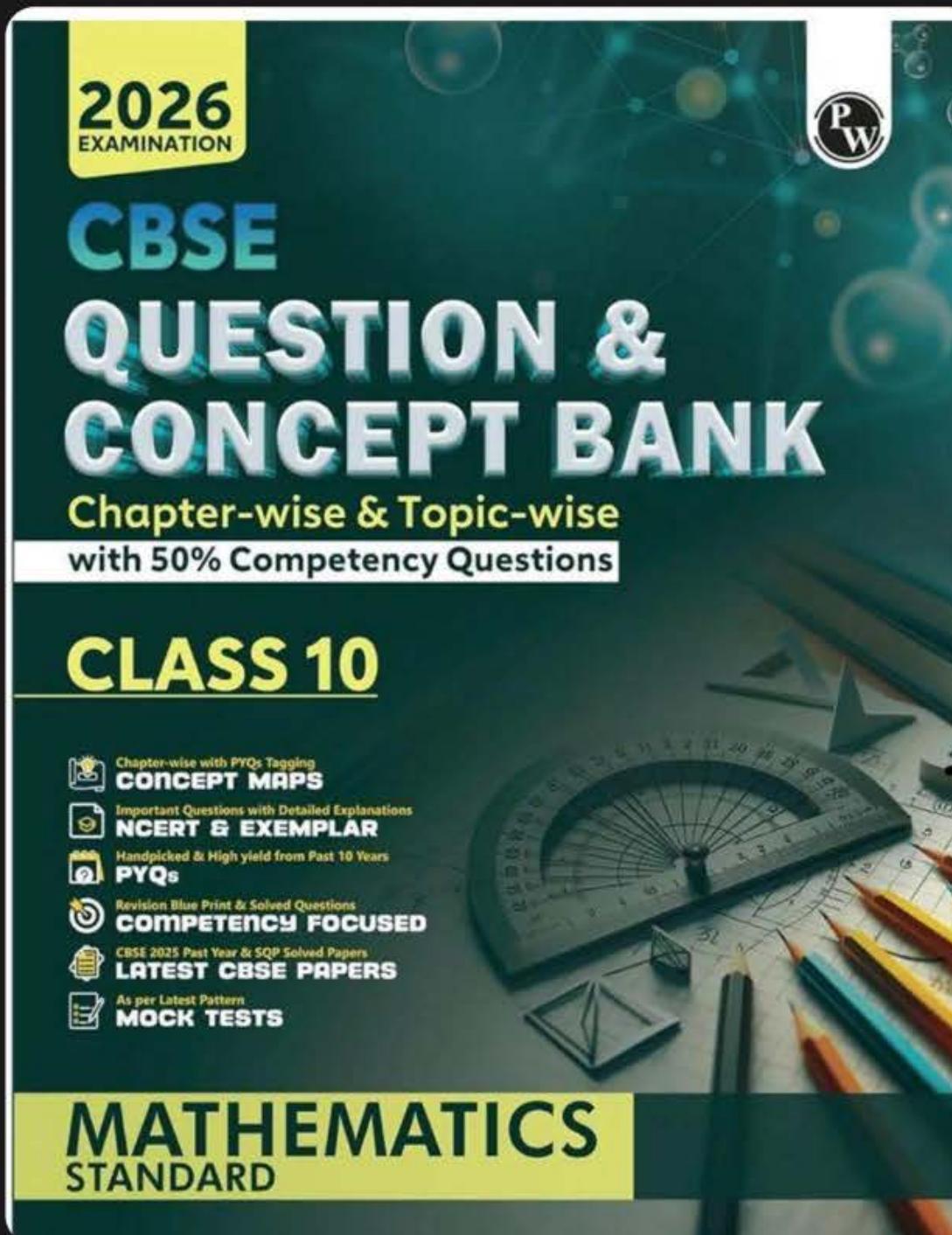
Maximum 7

Maximum = almost



Some Important Observations

- (i) A constant polynomial does not have any zero
- (ii) Every linear polynomial has one and only one zero.
- (iii) 0 may or may not be the zero of a given polynomial
- (iv) Number of zero of a polynomial cannot exceed its degree.





**WORK HARD
DREAM BIG
NEVER GIVE UP**



Thank
You