



UDAAN



2026

POLYNOMIALS

MATHS

LECTURE-3

BY-RITIK SIR



Topics *to be covered*



A Middle term splitting

B Finding Zeroes of Quadratic Polynomial

C Relation between Zeroes and Coefficients of Quadratic Polynomial

RITIK SIR

JOIN MY OFFICIAL TELEGRAM CHANNEL



①

$$x^2 = 9$$

$$x^2 - 9 = 0$$

$$x^2 = 9$$

$$x = \pm\sqrt{9}$$

$$x = +3, -3$$

$$\begin{array}{r|l} 3 & 27 \\ \hline 3 & 9 \\ 3 & 3 \\ & 1 \end{array}$$

③

$$x^2 = 4x$$

$$x^2 - 4x = 0$$

Common.....

$$(x)(x-4) = 0$$

$$x = 0$$

$$x - 4 = 0$$

$$x = 4$$

~~$$x^2 - 4x = 0$$~~

~~$$x^2 = 4x$$~~

~~$$x = \pm\sqrt{4x}$$~~

~~$$x = +25x$$~~

~~$$-25x$$~~

②

$$x^2 = 27$$

$$x^2 = 27$$

$$x = \pm\sqrt{27}$$

$$x = \pm\sqrt{9 \times 3 \times 3}$$

$$x = +3\sqrt{3}, -3\sqrt{3}$$

④

$$x^2 = 36x$$

$$x^2 - 36x = 0$$

$$(x)(x-36) = 0$$

$$x = 0$$

$$x - 36 = 0$$

$$x = 36$$



Middle term splitting for finding zeros of quadratic polynomials

1. ~~$x^2 + 4x + 21$~~

Sum = 4, product = -21

7, -3

$x^2 + 7x - 3x - 21 = 0$

$x(x+7) - 3(x+7) = 0$

$(x+7)(x-3) = 0$

$x+7=0$

$x = -7$

$x-3=0$

$x = 3$

2. ~~$-2x^2 + 7x - 6$~~

Sum = 7, product = 12

4, 3

$-2x^2 + 4x + 3x - 6 = 0$

$-2x(x-2) + 3(x-2) = 0$

$(x-2)(-2x+3) = 0$

$x-2=0$

$x = 2$

$-2x+3=0$

$-2x = -3$

$x = 3/2$

3.

$$7x^2 - 19x - 6$$

$$S = -19, P = -42$$

$$(-21, 2)$$

$$7x^2 - 21x + 2x - 6$$

$$7x(x-3) + 2(x-3) = 0$$

$$(x-3)(7x+2) = 0$$

$$x-3=0$$

$$x=3$$

$$7x+2=0$$

$$x = -2/7$$

4.

$$6x^2 + 13x + 6$$

$$\text{Sum} = 13, \text{Product} = 36$$

$$(9, 4)$$

$$6x^2 + 9x + 4x + 6 = 0$$

$$3x(2x+3) + 2(2x+3) = 0$$

$$(2x+3)(3x+2) = 0$$

$$2x+3=0$$

$$x = -3/2$$

$$3x+2=0$$

$$x = -2/3$$

$$\begin{array}{r|l} 2 & 42 \\ 3 & 21 \\ 7 & 7 \\ \hline & 1 \end{array}$$

#Q. The zeroes of the polynomial $x^2 + \frac{1}{6}x - 2$ are

$$\frac{x^2}{1} + \frac{1}{6}x - \frac{2}{1} = 0$$

$$\frac{6x^2 + x - 12}{6} = 0$$

A $-3, 4$

B $-\frac{3}{2}, \frac{4}{3}$

C $-\frac{4}{3}, \frac{3}{2}$

D $-\frac{4}{3}, -\frac{3}{2}$

$$6x^2 + x - 12 = 0$$

Sum = 1, product = -12

9, -8

$$6x^2 + 9x - 8x - 12 = 0$$

$$3x(2x+3) - 4(2x+3) = 0$$

$$(2x+3)(3x-4) = 0$$

$$x = -\frac{3}{2}, \frac{4}{3}$$

2	72
2	36
2	18
2	9
2	3
2	1

$$6x^2 = 2 \times 3 \times x \times x$$

$$9x = 3 \times 3 \times x$$

$$3x(2x+3)$$

$$-8x = -1 \times 2 \times 2 \times x$$

$$-12 = -1 \times 2 \times 2 \times 3$$

$$-4(2x+3)$$

9

13

Find the zeroes

#Q. ~~Find~~ the polynomial:

$$f(x) = x^2 - \frac{11}{6}x - \frac{5}{3}$$

$$6x^2 - 11x + 4x - 10 = 0$$

$$6x^2 = 2 \times 3 \times x \times x$$

$$-11x = -1 \times 11 \times x$$

$$3x(2x-5) + 2(2x-5) = 0$$

$$(2x-5)(3x+2) = 0$$

$$2x = 5$$

$$x = 5/2$$

$$3x+2=0$$

$$x = -2/3$$

$$x^2 - \frac{11}{6}x - \frac{5}{3} = 0$$

$$6x^2 - 11x - 10 = 0$$

$$6x^2 - 11x - 10 = 0$$

$$P = -60, S = -11$$

$$-15, 4$$

Verify:

$$a = 1$$

$$b = -11/6$$

$$c = -5/3$$

$$\alpha = 5/2$$

$$p = -2/3$$

$$\alpha + p = -b/a$$

$$\frac{5}{2} + \frac{-2}{3} = -\frac{-11/6}{1}$$

$$\frac{15-4}{6} = +11/6$$

$$11/6 = 11/6$$

$$\alpha p = c/a$$

$$\frac{5}{2} \times \frac{-2}{3} = \frac{-5/3}{1}$$

$$-5/3 = -5/3$$





Relationship between the zeroes and coefficients of a Quadratic Polynomial



$$\underline{Q} \quad -5x^2 - 3x + 2$$
$$a = -5, b = -3, c = 2$$

$$\underline{Q} \quad 5x^2 - 2x^0 + 0x$$
$$a = 5, b = 0, c = -2$$

$$ax^2 + bx + c$$

$$\begin{aligned} a &\neq 0 \\ a, b, c &\in \mathbb{R} \end{aligned}$$

Coefficient = a, b, c

$$\alpha (a) = \text{alpha}$$

$$\beta = \text{Beta}$$

↑
Zeroes

$$\alpha + \beta = -b/a$$

(Sum of zeroes)

$$\alpha \beta = c/a$$

(Product of zeroes)

#Q. Find the zeros of the following quadratic polynomial and verify the relationship between the zeros and their coefficients:

CBSE 2019

$$q(y) = 7y^2 - \frac{11}{3}y - \frac{2}{3}$$

$$\alpha = 2/3, \beta = -1/7, a = 7, b = -11/3, c = -2/3$$

$$7y^2 - \frac{11}{3}y - \frac{2}{3} = 0$$

$$21y^2 - 11y - 2 = 0$$

$$21y^2 - 11y - 2 = 0$$

$$P = -42, S = -11$$

$$-14, 3$$

$$21y^2 - 14y + 3y - 2 = 0$$

$$7y(3y-2) + 1(3y-2) = 0$$

$$(3y-2)(7y+1) = 0$$

$$3y = 2$$

$$y = 2/3$$

$$7y + 1 = 0$$

$$y = -1/7$$

Verify

$$\alpha + \beta = -\frac{b}{a}$$

$$\frac{2}{3} + -\frac{1}{7} = -\frac{-11/3}{7}$$

$$\frac{14-3}{21} = \frac{11}{21}$$

$$\frac{11}{21} = \frac{11}{21}$$

$$\alpha\beta = c/a$$

$$\frac{2}{3} \times -\frac{1}{7} = \frac{-2/3}{7}$$

$$\frac{-2}{21} = \frac{-2}{21}$$

#Q. Find the zeros of the quadratic polynomial $f(x) = 6x^2 - 3$, and verify the relationship between the zeros and its coefficients:

$$6x^2 - 3 = 0$$

$$6x^2 = 3$$

$$x^2 = \frac{3}{6}$$

$$x^2 = \frac{1}{2}$$

$$x = \pm \sqrt{\frac{1}{2}}$$

$$x = \frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}$$

α

β

$$\begin{aligned} a &= 6 \\ b &= 0 \\ c &= -3 \end{aligned}$$

$$\alpha + \beta = -b/a$$

$$\frac{1}{\sqrt{2}} + -\frac{1}{\sqrt{2}} = -\frac{0}{6}$$

$$0 = 0$$

$$\alpha \beta = c/a$$

$$\frac{1}{\sqrt{2}} \times -\frac{1}{\sqrt{2}} = \frac{-3}{6}$$

$$-\frac{1}{2} = -\frac{1}{2}$$

Hence
verified

#Q. Find the zeros of the polynomial $f(u) = 4u^2 + 8u$ and verify the relationship between the zeros and its coefficients.

#Gph

$$4u^2 + 8u = 0$$

$$[4u][u+2] = 0$$

$$4u = 0 \quad u+2 = 0$$

$$u = 0/4$$

$$u = 0$$

$$u = -2$$

$$\alpha = 0$$

$$\beta = -2$$

$$a = 4$$

$$b = 8$$

$$c = 0$$

#Q. Find the zeroes of each of the following quadratic polynomial and verify the relationship between the zeroes and their coefficients:

(i) $g(s) = 4s^2 - 4s + 1$

(ii) $g(x) = 6x^2 - 3 - 7x$

#GPR

#Q. Find the zeroes of following quadratic polynomial.

(i) $\sqrt{3}x^2 + 10x + 7\sqrt{3}$

(ii) $x^2 + 2\sqrt{2}x - 6$

Sum = 10, Product = $7\sqrt{3} \times \sqrt{3}$
 $= 7 \times 3$
 $= 21$

7, 3

$$\sqrt{3}x^2 + 7x + 3x + 7\sqrt{3} = 0$$

$$x(\sqrt{3}x + 7) + 1(3x + 7\sqrt{3}) = 0$$

$$x(\sqrt{3}x + 7) + \sqrt{3}(\sqrt{3}x + 7) = 0$$

$$(\sqrt{3}x + 7)(x + \sqrt{3}) = 0$$

$$\sqrt{3}x + 7 = 0$$

$$x = -7/\sqrt{3}$$

α

$$x + \sqrt{3} = 0$$

$$x = -\sqrt{3}$$

β

#Q. Find the zeroes of following quadratic polynomial.

(i) $\sqrt{3}x^2 + 10x + 7\sqrt{3}$

(ii) $x^2 + 2\sqrt{2}x - 6$

$S = 252, P = -6$

Gpu

#Q. If one zero of the quadratic polynomial $kx^2 + 3x + k$ is 2, then the value of k is

Graph

A

$$\frac{5}{6}$$

B

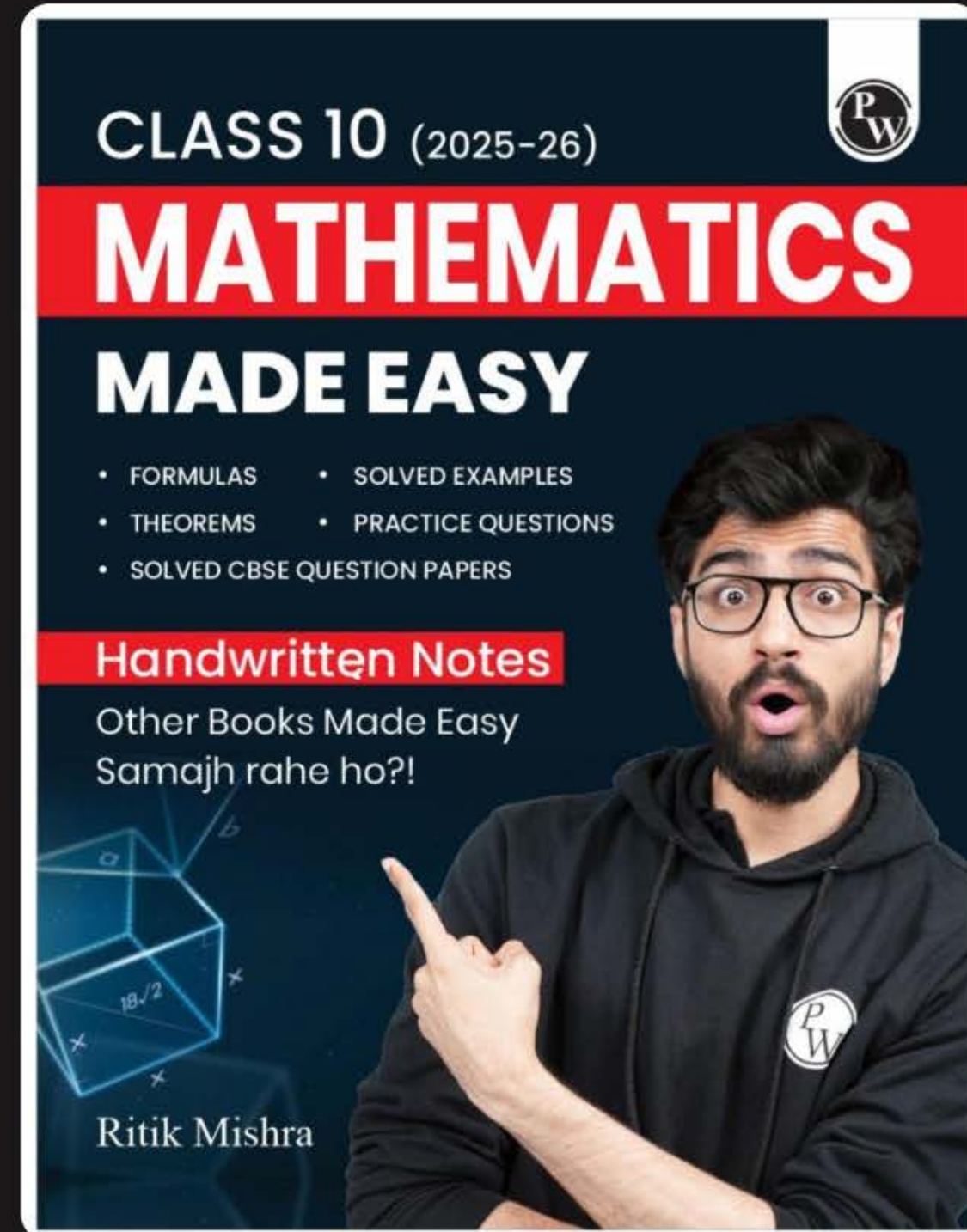
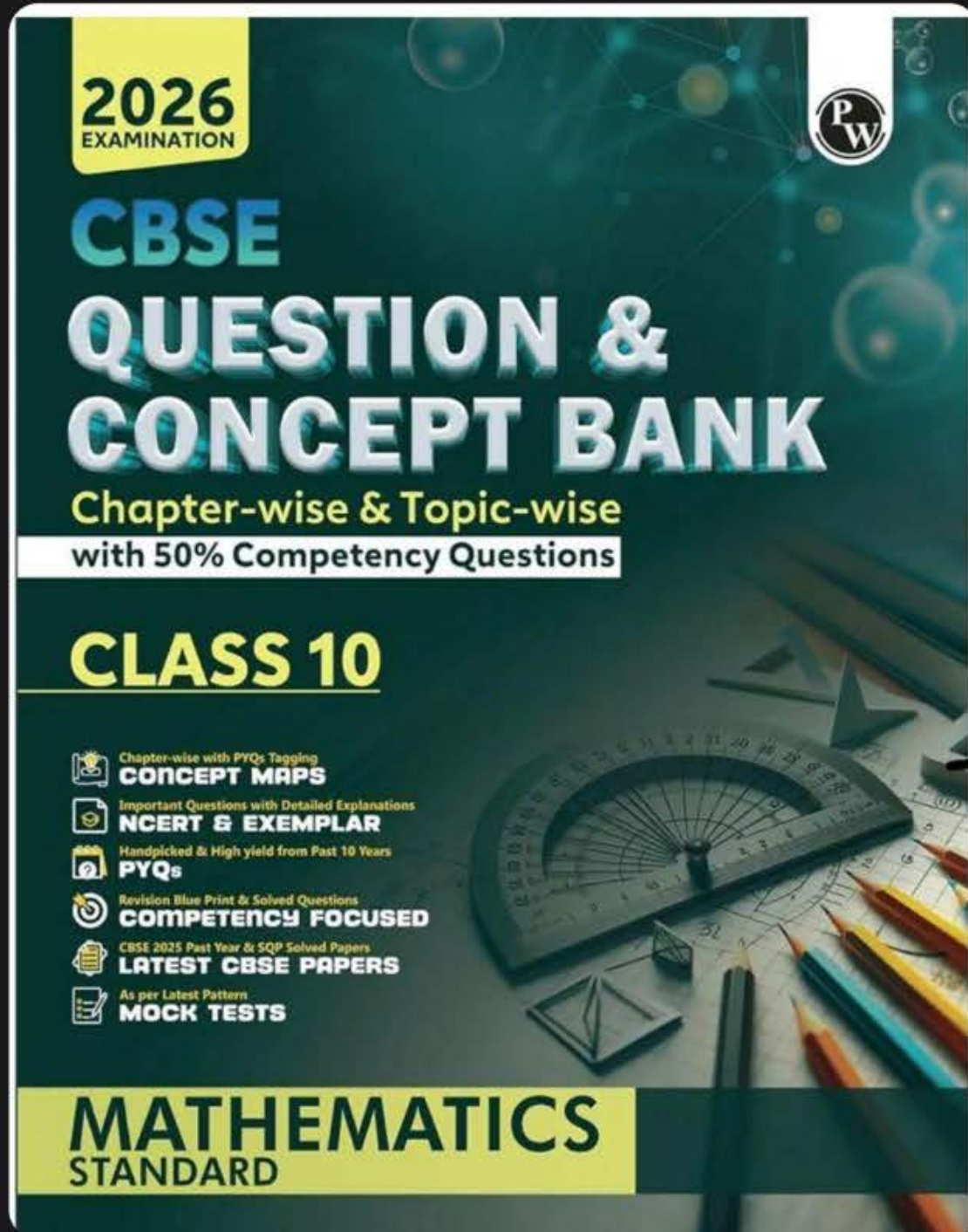
$$-\frac{5}{6}$$

C

$$\frac{6}{5}$$

D

$$-\frac{6}{5}$$





WORK HARD

DREAM BIG

NEVER GIVE UP



Thank
You