



# UDAAN



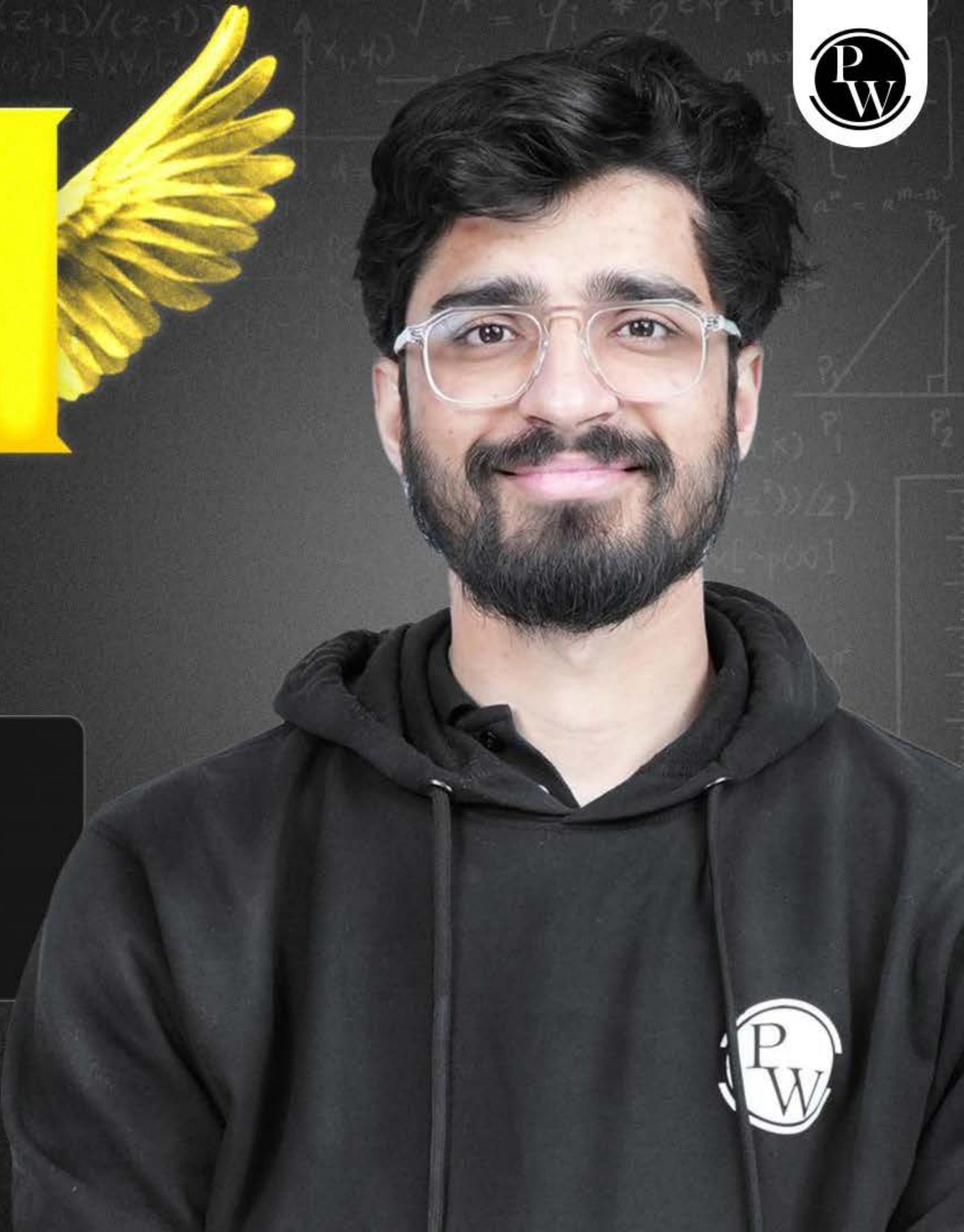
## 2026

# POLYNOMIALS

MATHS

LECTURE-4

BY-RITIK SIR



# Topics *to be covered*

**A**

Questions on Relation between Zeroses and Coefficients of Quadratic Polynomial



# RITIK SIR

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#Q. Find the zeroes of following quadratic polynomial.

(i)  $x^2 + 2\cancel{y}\cancel{x} - 6$

Sum =  $2\sqrt{2}$

Product = -6

$3\sqrt{2}, -\sqrt{2}$

$$x^2 + 3\sqrt{2}x - \sqrt{2}x - 6 = 0$$

$$\cdot x(x + 3\sqrt{2}) - \sqrt{2}(x + 3\sqrt{2}) = 0$$

$$(x + 3\sqrt{2})(x - \sqrt{2}) = 0$$

$$x + 3\sqrt{2} = 0 \quad x - \sqrt{2} = 0$$

$x = -3\sqrt{2}$

$x = \sqrt{2}$

#OT

#Q. Zeroes?

(i)  $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3}$  (2014)

$$S = -2\sqrt{2}, F = (2\sqrt{3})(\sqrt{3}) \\ = -6$$

$\therefore -3\sqrt{2}, \sqrt{2}$

$$\sqrt{3}x^2 - 2\sqrt{2}x + \sqrt{2}x - 2\sqrt{3} = 0$$

$$\sqrt{3}x \left[ \frac{\sqrt{3}x^2 - 2\sqrt{2}x}{\sqrt{3}x} \right] + \sqrt{2} \left[ \frac{\sqrt{2}x - 2\sqrt{3}}{\sqrt{2}} \right] = 0$$

$$\sqrt{3}x[x - \sqrt{6}] + \sqrt{2}[x - \sqrt{6}] = 0$$

(ii)  $3x^2 - 2\sqrt{6}x + 2$  (2012, 10)

$$(x - \sqrt{6})(\sqrt{2}x + \sqrt{2}) = 0$$

$$x = \sqrt{6}$$

$$x = -\frac{\sqrt{2}}{\sqrt{2}}$$

$$0 \quad 3x^2 - 256x + 2 = 0$$

Sum = -256, Product = 6

$$-\sqrt{6}, -\sqrt{6}$$

HGP

$$3u^2 - \sqrt{6}u - \sqrt{6}u + 2 = 0$$

~~HGPU~~

#Q. If one zero of the quadratic polynomial  $kx^2 + 3x + k$  is 2, then the value of  $k$  is

A  $\frac{5}{6}$

C  $\frac{6}{5}$

B

$-\frac{5}{6}$

D

$-\frac{6}{5}$

$$kx^2 + 3x + k$$

$$2 \cdot 2^2 + 3 \cdot 2 + k = 0$$

$$4k + 6 + k = 0$$

$$4k + 6 + k = 0$$

$$5k = -6$$

$$k = -6/5$$



## Relationship between the zeroes and coefficients of a Quadratic Polynomial

$$ax^2 + bx + c$$

$$a \neq 0$$

$$a, b, c \in \mathbb{R}$$

$$\alpha + \beta = -\frac{b}{a}$$

(sum)

$$\alpha \beta = \frac{c}{a}$$

(product)

$$Q: 6x^2 - 7x + 2$$

$a=6$     $b=-7$     $c=2$

Sum of zeroes =  $-\frac{b}{a} = -\frac{-7}{6} = \frac{7}{6}$

Product of zeroes =  $\frac{c}{a} = \frac{2}{6} = \frac{1}{3}$



#Q. If the product of the zeros of the polynomial  $ax^2 - 6x - 6$  is 4, find the value of a.

CBSE 2008

$$ax^2 - 6x - 6$$

$$\text{Sum} = -\frac{b}{a} = -\frac{-6}{a} = \frac{6}{a}$$

$$\text{Product} = \frac{c}{a} = -\frac{6}{a}$$

$$\text{Product} = -\frac{6}{a}$$

$$4 = -\frac{6}{a}$$

$$a = -6/4 = -3/2$$

#Q. If one zero of the polynomial  $2x^2 + 3x + \lambda$  is  $\frac{1}{2}$ , find the value of  $\lambda$  and the other zero.

$$2x^2 + 3x + \lambda$$

$\alpha$        $\beta$

$$a=2, b=3, c=\lambda$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\alpha + \beta = -\frac{3}{2}$$

$$\alpha \beta = \frac{c}{a}$$

$$\alpha \beta = \frac{\lambda}{2}$$

$$\frac{1}{2} + \beta = -\frac{3}{2}$$

$$\beta = -\frac{3}{2} - \frac{1}{2}$$

$$\beta = -\frac{4}{2}$$

$$\beta = -2$$

$$\alpha \beta = \frac{\lambda}{2}$$

$$-\frac{1}{2} \times -2 = \frac{\lambda}{2}$$

$$-1 = \frac{\lambda}{2}$$

$$-2 = \lambda$$

Ans:  $\alpha = \frac{1}{2}$

#Q. Find the value of  $k$  such that the polynomial  $x^2 - (k+6)x + 2(2k-1)$  has sum of its zeroes equal to half of their product.

CBSE 2019

$$\alpha + \beta = \frac{-b}{a}$$

$$\alpha \beta = \frac{c}{a}$$

$$\alpha^2 - (k+6)\alpha + 2(2k-1)$$

$$\alpha = 1$$

$$\beta = -(k+6)$$

$$c = 2(2k-1)$$

Sum of zeroes equal to half of their product

$$\alpha + \beta = \frac{1}{2} \alpha \beta$$

$$\alpha + \beta = -\frac{b}{a}$$

$$\alpha + \beta = -(k+6)$$

$$\alpha + \beta = k+6$$

$$\alpha \beta = \frac{c}{a}$$

$$\alpha \beta = 2(2k-1)$$

$$\alpha \beta = 4k-2$$

$$k+6 = \frac{4k-2}{2}$$

$$2k+12 = 4k-2$$

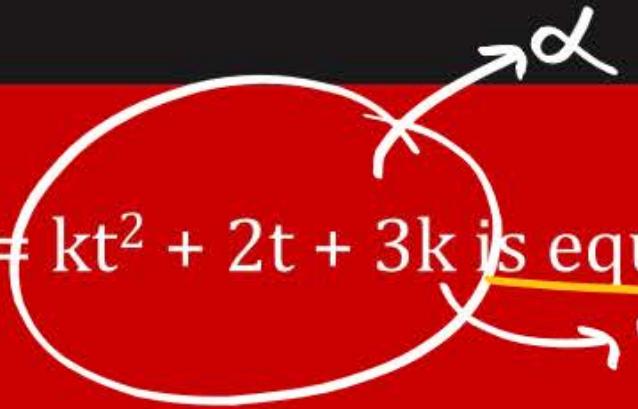
$$12+2 = 4k-2k$$

$$14 = 2k$$

$$\frac{14}{2} = 4$$

$$7 = k$$

#Q. If the sum of the zeros of the quadratic polynomial  $f(t) = kt^2 + 2t + 3k$  is equal to their product, find the value of  $k$ .



**A**  $-2/3$

$$\alpha + \beta = \alpha \beta$$

$$-\frac{2}{k} = 3$$

**B**  $-3/2$

$$-\frac{2}{k} = k$$

**C**  $2/3$

**D** NOTA

$$\alpha + \beta = -\frac{b}{a}$$

$$\alpha + \beta = -\frac{2}{k}$$

$$\alpha \beta = \frac{c}{a}$$

$$\alpha \beta = \frac{3k}{k}$$

$$\alpha \beta = 3$$

$$ax^2 + bx + c$$

#Q. If one zero of the polynomial  $p(x) = 6x^2 + 37x - (k - 2)$  is reciprocal of the other, then find the value of  $k$ .

Let the zeroes be  $\alpha$  and  $\frac{1}{\alpha}$

~~$\alpha \times \frac{1}{\alpha} = -(k-2)$~~

$$1 = -\frac{k-2}{6}$$

$$6 = -k+2$$

$$k = 2-6$$

$$k = -4$$

CBSE 2023

$$a=6, b=37, c=- (k-2)$$

$$\text{Sum} = -\frac{b}{a}$$

$$\alpha + \frac{1}{\alpha} = -\frac{37}{6}$$

$$\text{Product} = \frac{c}{a}$$

~~$\alpha \times \frac{1}{\alpha} = -\frac{(k-2)}{6}$~~

$$1 = -\frac{k-2}{6}$$

$$6 = -k+2$$

$$k = 2-6$$

$$k = -4$$

#Q. If one zero of the polynomial  $(a^2 + 9)x^2 + 13x + 6a$  is reciprocal of the other, find the value of  $a$ .

$$a = a^2 + 9, b = 13, c = 6a$$

CBSE 2008

A ✓

B

C

D NOTA

$\alpha, \frac{1}{\alpha}$

Sum =  $-\frac{b}{a}$

$$\alpha + \frac{1}{\alpha} = -\frac{13}{a^2 + 9}$$

Product =  $\frac{c}{a}$

$$\alpha \times \frac{1}{\alpha} = \frac{6a}{a^2 + 9}$$

$$1 = \frac{6a}{a^2 + 9}$$

$$1(a^2 + 9) = 6a$$

$$a^2 + 9 = 6a$$

$$a^2 - 6a + 9 = 0$$

Sum = -6, Product = 9

$-3, 3$

$$a^2 - 3a - 3a + 9 = 0$$

$$a(a-3) - 3(a-3) = 0$$

$$(a-3)(a-3) = 0$$

$$a-3=0$$

$$a-1=0$$

$a=3$

quadratic in 'a'.

#Q. If one zero of the quadratic polynomial  $f(x) = 4x^2 - 8kx - 9$  is negative of the other, find the value of  $k$ .

Let the zeroes be

$\alpha$  and  $-\alpha$

-1

B 1

C 0

D NOTA

$$ax^2 + bx + c$$

$$a=4, b=-8k, c=-9.$$

$$\text{Sum} = -\frac{b}{a}$$

$$\alpha + -\alpha = -\frac{-8k}{4}$$

$$\text{Product} = \frac{c}{a}$$

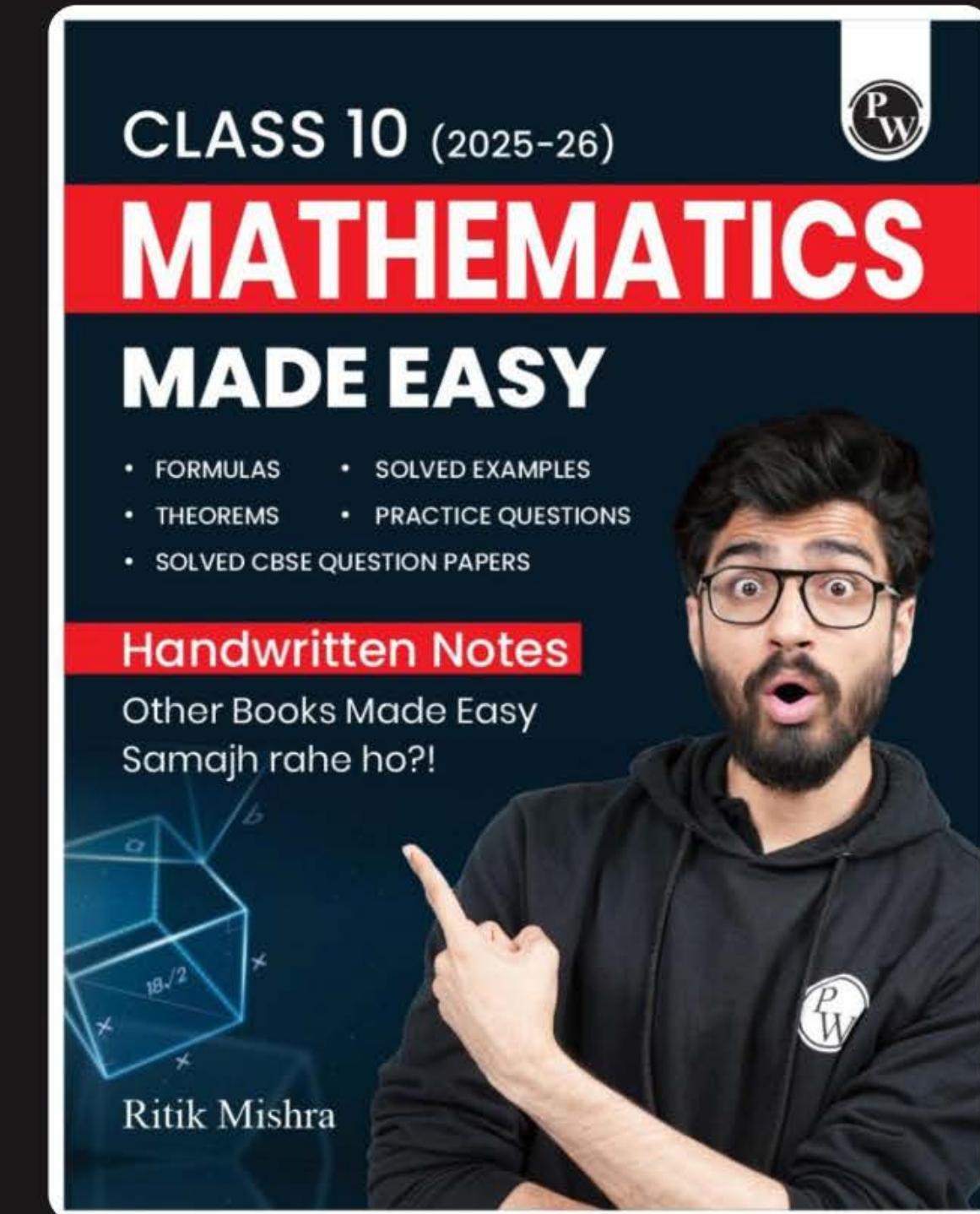
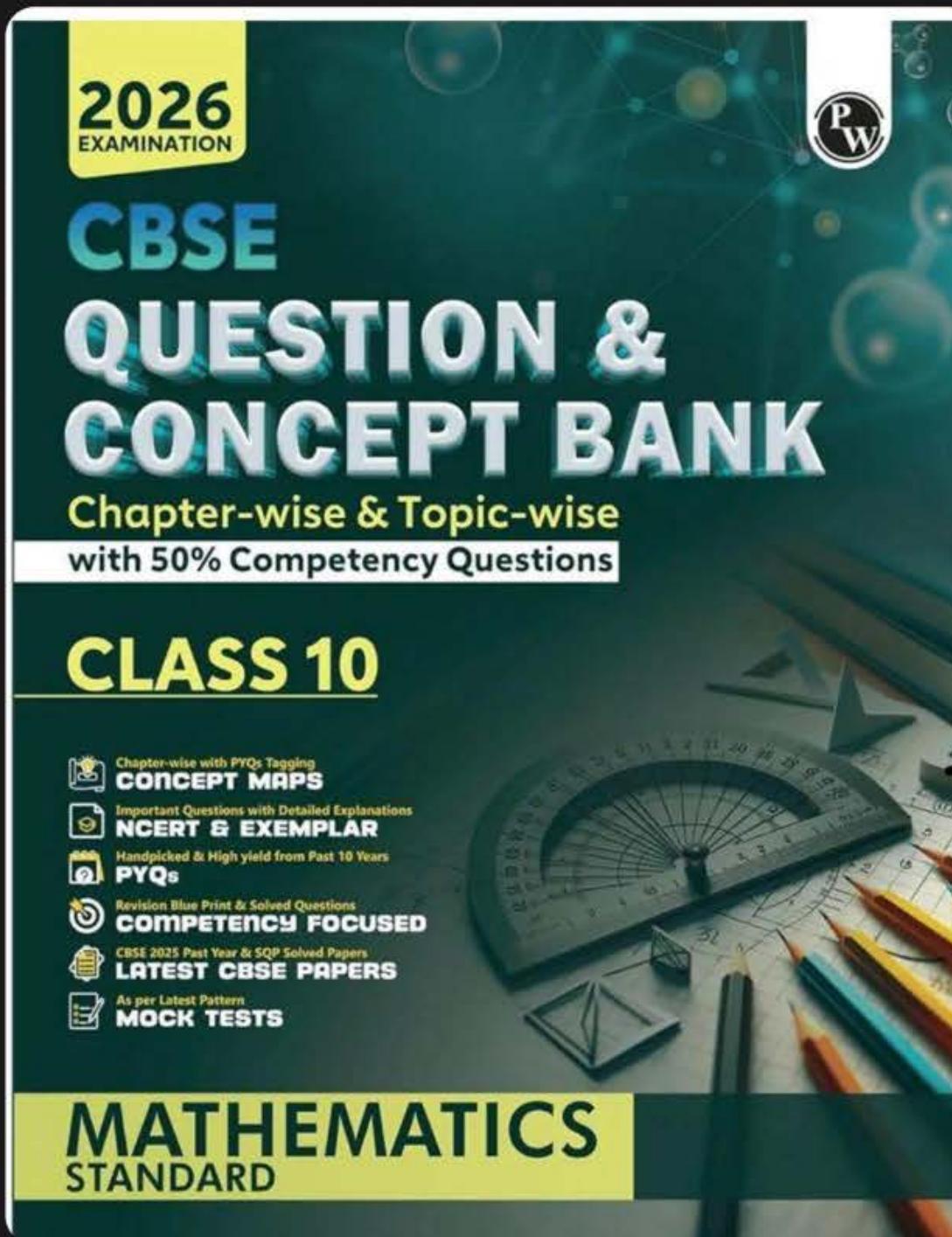
$$\alpha \times -\alpha = -\frac{9}{4}$$

$$0 = \frac{8k}{4}$$

$$0 = 2k$$

$$0 = -k$$

$$0 = k //$$





**WORK HARD  
DREAM BIG  
NEVER GIVE UP**



Thank  
*You*