

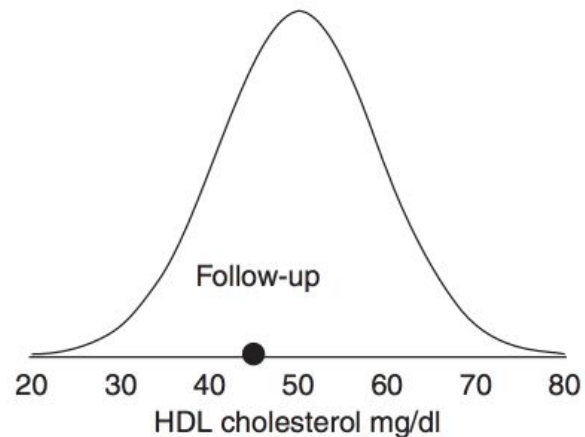
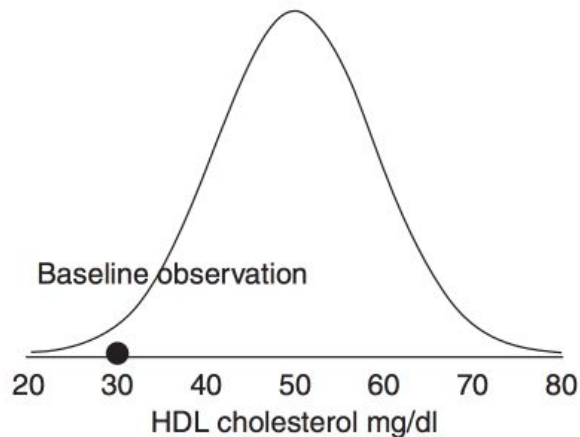
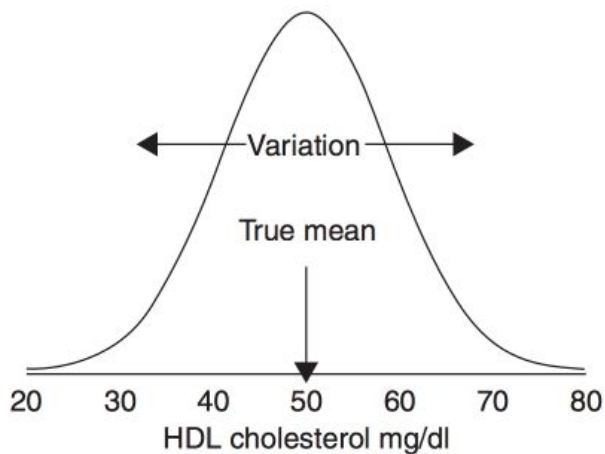
# Topic 3: Circularity & Regression

Lectures 6 & 7

- Regression to the mean
- Stopping rules
- Circular analysis

# Regression to the mean

Regression to the mean (RTM) is a statistical phenomenon that is characterized by the fact that unusually large or small measurements tend to be followed by measurements that are closer to the mean.

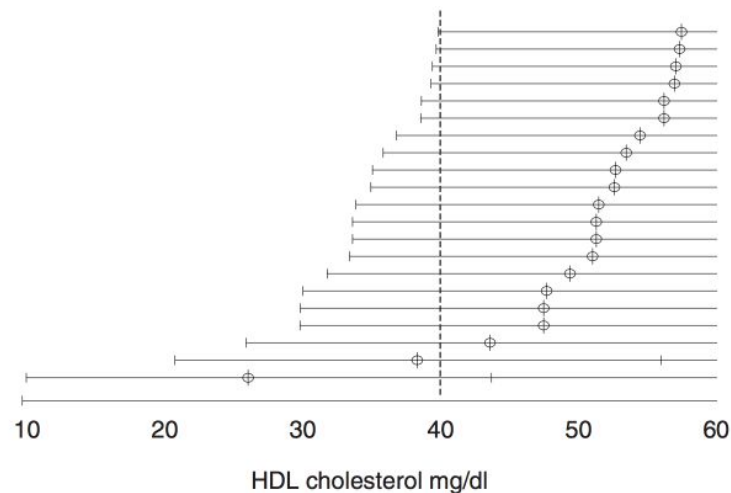
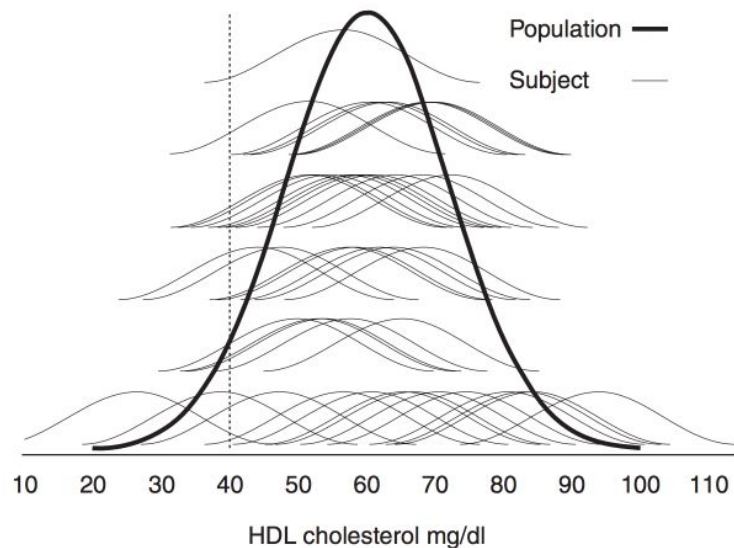


# Regression to the mean

Regression to the mean (RTM) is a statistical phenomenon that is characterized by the fact that unusually large or small measurements tend to be followed by measurements that are closer to the mean.

- Occurs when repeated measurements are made on the same subject or unit of observation.
- Can make natural variation in repeated data look like real change.
- Happens because values are observed with random error (non-systematic variation like random measurement error or random fluctuations in a subject).
- There is almost no data without random error → makes RTM a common phenomenon.

# Regression to the mean

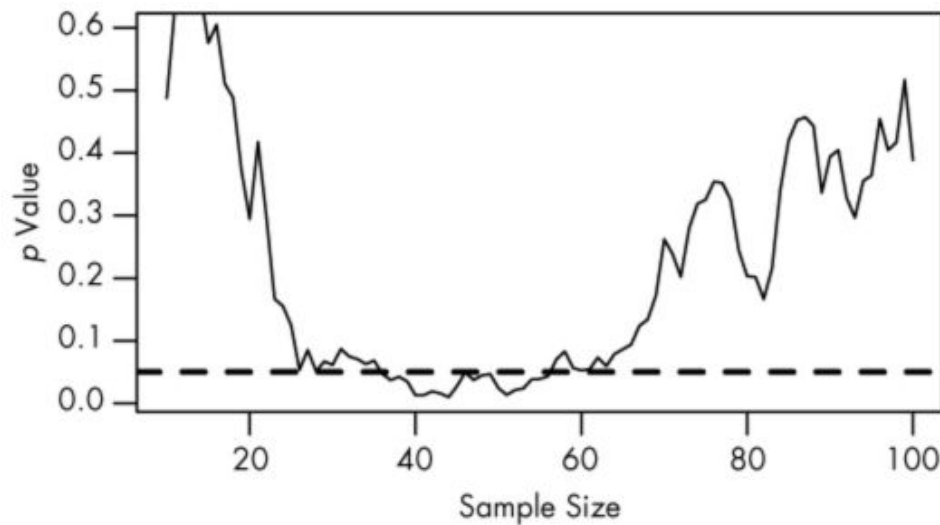


- Effect of RTM is compounded by categorizing subjects into groups based on baseline measurements.
- Variability in individual measurements  $>$  variability in the true means  $\rightarrow$  Attenuation of association (regression dilution bias).

# Regression to the mean

Longitudinally tracking the effect of drug.

- Terminate the study early if there if it is clear that the drug has an effect.
- In fact, it is *unethical* to withhold the drug from the control group.



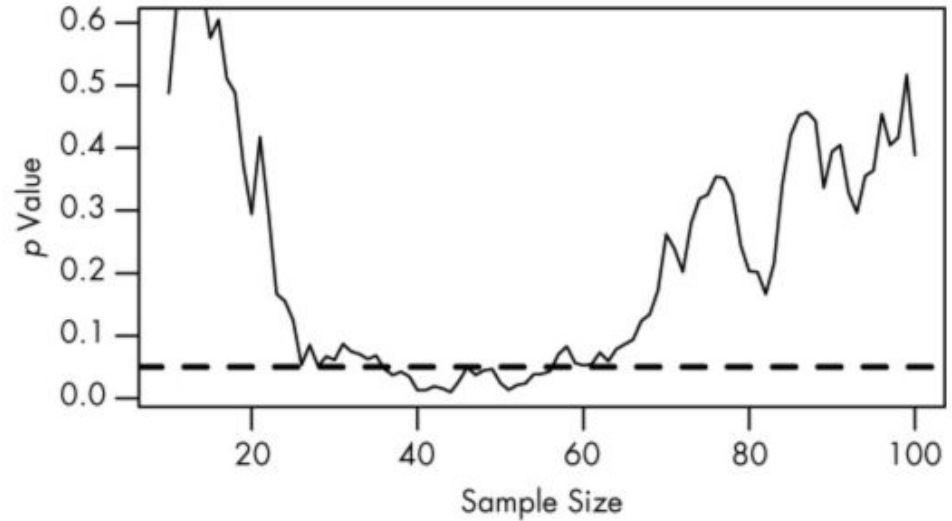
Issues:

- Null hypothesis should take varying group size into account.
- Truth inflation (lucky patients, not brilliant drugs): stopped trials exaggerate their effect by 29% more than trials that run their full course.

# Regression to the mean

Longitudinally tracking the effect of drug.

- Terminate the study early if there if it is clear that the drug has an effect.
- In fact, it is *unethical* to withhold the drug from the control group.



- Many published studies do not publish their original intended sample size or the stopping rule
- Preregistration!

# Regression to the mean

Assigning a narrative or causal reasoning from observed data is often very hard:

- Galton's observation: Tall parents had (on average) children who were shorter than them, and short parents had (on average) children who were taller than them.
- "Norway had a great first jump; he will be tense, hoping to protect his lead and will probably do worse"; "Sweden had a bad first jump and now he knows he has nothing to lose and will be relaxed, which should help him do better."
- Why it is that highly intelligent individuals tend to marry those who are less intelligent than they are?
- Depressed children treated with an energy drink improve significantly over a three-month period.

# Circular analysis & Double-dipping

Statistical analysis is often exploratory: no hypothesis in advance.

- Collect data → Poke around to see if there's something interesting → New hypotheses → Perform new experiments / Collect new data → Test the hypotheses.
- Collect data → Poke around to see if there's something interesting → New hypotheses → Take the subset of the original data that appears to show signal → Test the hypotheses.
  - Double-dipping → truth inflation.
  - Happens all the time in neuroimaging (apparently 40% of the literature), genetics, epidemiology.



# Circular analysis & Double-dipping

- Collect data → Poke around to see if there's something interesting → New hypotheses → Take the subset of the original data that appears to show signal → Test the hypotheses.
  - Null hypothesis based on random chance is wrong at the final stage.
  - Only signals with the strongest random noise make it into further analysis.
- Mitigating this problem:
  - Split data in half; Reduces power.
  - Choose hypotheses based on prior knowledge.

# Topic 4: Descriptive statistics & visualization

Lectures 8 & 9

- Descriptive statistics
- Spurious correlations
- Visualization challenges