HW1

February 5, 2022

1 1. Setup and Data Retrieval

```
[1]: import yfinance as yf
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import pandas_ta as ta
from sklearn.linear_model import LinearRegression
from sklearn.metrics import r2_score
from sklearn.metrics import mean_squared_error
```

```
[2]: msci = yf.download("XWD.TO", start="2010-01-01")
msci
```

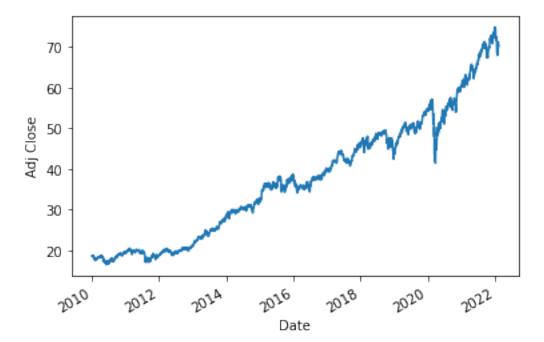
[2]:		Open	High	Low	Close	Adj Close	Volume
	Date						
	2010-01-04	22.665331	22.945892	22.665331	22.935871	18.619492	4491
	2010-01-05	22.905811	22.945892	22.865730	22.945892	18.627623	6587
	2010-01-06	22.865730	22.905811	22.775551	22.845692	18.546282	7086
	2010-01-07	22.775551	22.905811	22.755510	22.905811	18.595087	39521
	2010-01-08	22.875751	22.945892	22.835670	22.945892	18.627623	45209
		•••	•••				
	2022-01-31	69.410004	70.080002	69.349998	70.080002	70.080002	6000
	2022-02-01	70.510002	70.750000	70.160004	70.750000	70.750000	6000
	2022-02-02	71.160004	71.320000	71.010002	71.290001	71.290001	4000
	2022-02-03	70.959999	70.959999	69.879997	69.910004	69.910004	11700
	2022-02-04	70.430000	71.010002	70.139999	70.559998	70.559998	7300

[3035 rows x 6 columns]

2 2. Data Analysis and Exploration in Pandas

2.1 2.1. Plot the Adj Close column of the MSCI ETF

```
[3]: msci["Adj Close"].plot()
plt.ylabel("Adj Close")
plt.show()
```



2.2 2.2. Gather information about the data frame by looking at key statistics, i.e. the moments, data types, statistics...

The first moment (mean), the second central moment (Variance), standard deviation, median, data types are collected in the data frame shown below.

```
[4]:
                        Open
                                     High
                                                   Low
                                                             Close
                                                                     Adj Close \
                      3035.0
                                   3035.0
                                                3035.0
                                                            3035.0
                                                                        3035.0
     count
                   40.506974
                                40.630312
     mean
                                              40.3604
                                                         40.501604
                                                                     37.462726
     std
                   14.237339
                                14.289796
                                            14.175661
                                                         14.236313
                                                                     15.293977
```

min	20.440882	20.440882	19.539078	20.340681	16.512701
25%	24.974951	25.020041	24.92485	24.98497	21.478388
50%	40.480961	40.581161	40.330662	40.450901	36.3647
75%	50.901804	51.102203	50.761524	50.951904	48.560871
max	75.320641	75.430862	75.240479	75.430862	74.924858
data types	float64	float64	float64	float64	float64
variance	202.635034	204.130999	200.883146	202.605831	233.82865
median	40.480961	40.581161	40.330662	40.450901	36.3647

Volume 3035.0 count mean22681.648105 52084.230134 std 0.0 ${\tt min}$ 25% 4092.0 50% 8583.0 75% 20459.0 ${\tt max}$ 983529.0 data types int64variance 2711873200.975342 median8583.0

2.3 2.3. Get all rows where the "High" value is > 40

```
[5]: msci = msci[msci["High"] > 40]
msci
```

[5]:		Open	High	Low	Close	Adj Close	Volume
	Date						
	2015-02-13	39.939880	40.020039	39.859718	40.010021	35.659203	30539
	2015-02-18	40.060120	40.110222	39.979961	40.030060	35.677052	10479
	2015-02-19	40.340679	40.420841	40.260521	40.260521	35.882462	23253
	2015-02-20	40.270542	40.751503	40.210423	40.721443	36.293255	27545
	2015-02-23	40.731464	40.781563	40.661324	40.741482	36.311115	37325
	***	•••	•••	•••	•••	•••	
	2022-01-31	69.410004	70.080002	69.349998	70.080002	70.080002	6000
	2022-02-01	70.510002	70.750000	70.160004	70.750000	70.750000	6000
	2022-02-02	71.160004	71.320000	71.010002	71.290001	71.290001	4000
	2022-02-03	70.959999	70.959999	69.879997	69.910004	69.910004	11700
	2022-02-04	70.430000	71.010002	70.139999	70.559998	70.559998	7300

[1588 rows x 6 columns]

2.4 2.4. Drop the volume column

```
[6]: del msci["Volume"]
msci
```

```
[6]:
                       Open
                                  High
                                               Low
                                                         Close
                                                                Adj Close
     Date
     2015-02-13
                 39.939880
                             40.020039
                                                     40.010021
                                                                35.659203
                                         39.859718
                             40.110222
                                                     40.030060
     2015-02-18
                 40.060120
                                         39.979961
                                                                35.677052
                 40.340679
                             40.420841
                                         40.260521
                                                     40.260521
                                                                35.882462
     2015-02-19
                             40.751503
     2015-02-20
                 40.270542
                                         40.210423
                                                     40.721443
                                                                36.293255
     2015-02-23
                 40.731464
                             40.781563
                                         40.661324
                                                     40.741482
                                                                36.311115
                               •••
                      •••
                             70.080002
                                         69.349998
                                                     70.080002
     2022-01-31
                  69.410004
                                                                70.080002
     2022-02-01
                 70.510002
                             70.750000
                                         70.160004
                                                     70.750000
                                                                70.750000
     2022-02-02
                 71.160004
                             71.320000
                                         71.010002
                                                     71.290001
                                                                71.290001
     2022-02-03
                 70.959999
                             70.959999
                                         69.879997
                                                     69.910004
                                                                69.910004
     2022-02-04
                 70.430000
                             71.010002
                                         70.139999
                                                     70.559998
                                                                70.559998
```

2.5 2.5. Get the adjusted close price of the 01/17/2022

```
[7]: msci.loc[pd.to_datetime("2022-01-17"), "Adj Close"]
```

[7]: 72.19999694824219

[1588 rows x 5 columns]

2.6 2.6. Create a new column that stores the daily return

```
[8]: msci = msci.copy()
    msci["daily return"] = (msci["Adj Close"] - msci["Open"]) / msci["Open"]
    msci
```

```
[8]:
                                                                Adj Close
                       Open
                                  High
                                               Low
                                                        Close
    Date
     2015-02-13
                 39.939880
                             40.020039
                                        39.859718
                                                    40.010021
                                                                35.659203
                 40.060120
                             40.110222
                                        39.979961
                                                    40.030060
                                                                35.677052
     2015-02-18
     2015-02-19
                 40.340679
                             40.420841
                                        40.260521
                                                    40.260521
                                                                35.882462
                                                    40.721443
     2015-02-20
                 40.270542
                             40.751503
                                        40.210423
                                                                36.293255
     2015-02-23
                 40.731464
                             40.781563
                                        40.661324
                                                    40.741482
                                                                36.311115
     2022-01-31
                 69.410004
                             70.080002
                                        69.349998
                                                    70.080002
                                                                70.080002
     2022-02-01
                 70.510002
                             70.750000
                                        70.160004
                                                    70.750000
                                                                70.750000
     2022-02-02
                 71.160004
                             71.320000
                                        71.010002
                                                    71.290001
                                                                71.290001
     2022-02-03
                 70.959999
                             70.959999
                                        69.879997
                                                    69.910004
                                                                69.910004
     2022-02-04 70.430000
                             71.010002
                                        70.139999
                                                    70.559998
                                                                70.559998
```

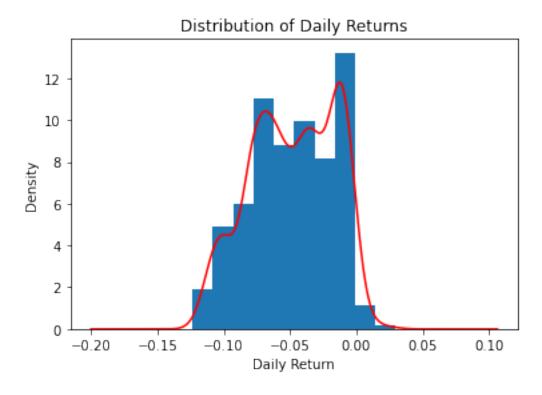
daily return Date 2015-02-13 -0.107178 2015-02-18 -0.109412 2015-02-19 -0.110514 2015-02-20 -0.098764 2015-02-23 -0.108524 2022-01-31 0.009653 2022-02-01 0.003404 2022-02-02 0.001827 2022-02-03 -0.014797 2022-02-04 0.001846

[1588 rows x 6 columns]

2.7 2.7. How are the returns distributed?

From the histogram below, we can observe an approximate bell-shaped distribution whose mean is round -0.05.

```
[9]: plt.hist(x = msci["daily return"], density = True)
    plt.xlabel("Daily Return")
    plt.title("Distribution of Daily Returns")
    msci["daily return"].plot.density(color = "red")
    plt.show()
```



```
[10]: # Check if the mean is around -0.05.

np.nanmean(msci["daily return"])
```

[10]: -0.04826754326367532

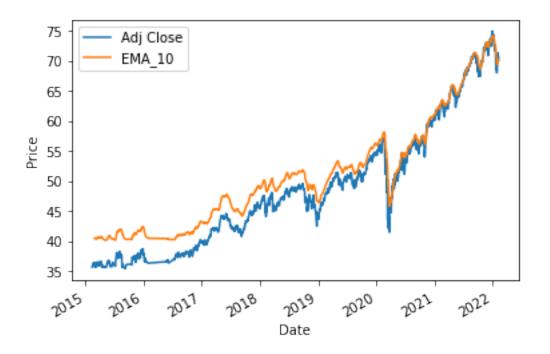
2.8 2.8. Calculate the cumulative return (Hint: cumsum())

```
[11]: msci["daily return"].cumsum()
[11]: Date
      2015-02-13
                    -0.107178
     2015-02-18
                    -0.216590
     2015-02-19
                    -0.327104
     2015-02-20
                    -0.425869
     2015-02-23
                    -0.534393
                      •••
      2022-01-31
                   -76.641138
     2022-02-01
                   -76.637734
      2022-02-02
                   -76.635907
      2022-02-03
                   -76.650704
      2022-02-04
                  -76.648859
     Name: daily return, Length: 1588, dtype: float64
```

2.9 2.9. Add a 10-day exponential moving-average "EMA 10" column to the MSCI data frame based on the "Adj Close" column (Hint: you can use pandas_ta using pip install pandas_ta)

```
[12]: msci["EMA_10"] = msci.ta.ema(signal = 10)

[13]: msci["Adj Close"].plot(), msci.ta.ema(window = 10).plot()
    plt.ylabel("Price")
    plt.legend()
    plt.show()
```

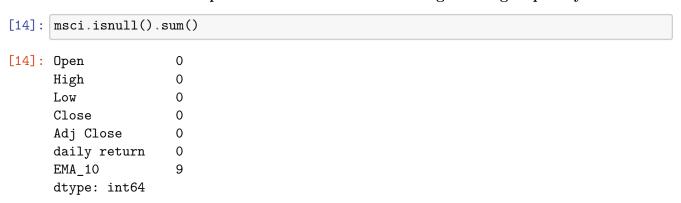


3 3. Linear Regression using Scikit-Learn

3.1 Handle Missing Values

Adding the EMA has created missing values for the first n indexes, where n is your window size (9, in our case).

3.1.1 Find and print out the number of missing values grouped by column.



There are 9 missing values in the column "EMA_10" and no missing value exists in other columns.

3.1.2 Replace missing values

Often times, if statistically reasonable (esp. in time series), we can replace missing values with their mean or mode. This can especially be done if the missing values make up only a little percentage

of the data set. Another approach would be to drop the missing entries, which will however often times decrease our performance. Try filling the missing rows of the explanatory variable with "reasonable" values (Hint: Look at the distribution of the beginning of the EMA 10 time series). Make sure there are no missing values left.

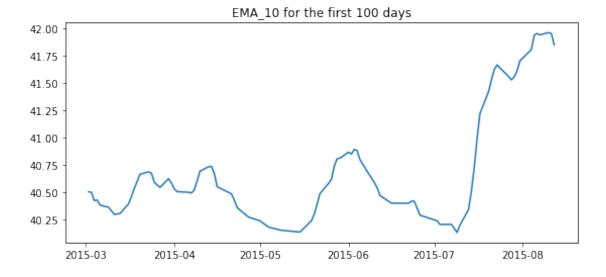
```
[15]: # Get the number of rows in our data frame.
msci.shape[0]
```

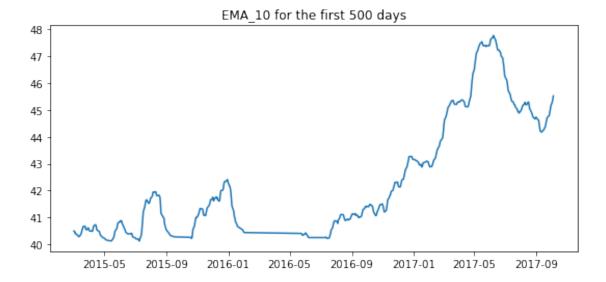
[15]: 1588

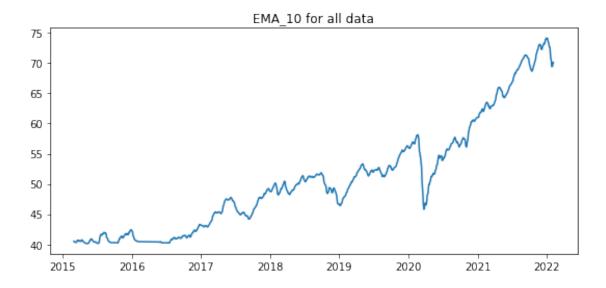
```
plt.figure()
  plt.plot(msci["EMA_10"][0:100])
  plt.subplots_adjust(right=1.3)
  plt.title("EMA_10 for the first 100 days")

plt.figure()
  plt.plot(msci["EMA_10"][0:500])
  plt.subplots_adjust(right=1.3)
  plt.title("EMA_10 for the first 500 days")

plt.figure()
  plt.plot(msci["EMA_10"])
  plt.subplots_adjust(right=1.3)
  plt.title("EMA_10"])
  plt.subplots_adjust(right=1.3)
  plt.title("EMA_10 for all data")
```







From the above we can see that, EMA_10 just slightly changed from 2015-03 to 2015-04, compared to both the first 500-days variation of EMA_10 and certainly, the total variation of EMA_10 over the time scale (from 2015 to 2022). Besides, EMA_10 is a weighted average statistic for the past 10 days, hence, the short-term data reflects more information than long-term data, so it is reasonable to replace the first 9 missing values by the average EMA_10 from 2015-03 to 2015-04.

```
[17]: msci["EMA_10"].fillna(np.nanmean(msci[msci.index < pd.

→to_datetime("2015-04-01")]["EMA_10"]), inplace = True)

msci["EMA_10"]
```

```
[17]: Date
      2015-02-13
                    40.491352
      2015-02-18
                    40.491352
      2015-02-19
                    40.491352
      2015-02-20
                    40.491352
      2015-02-23
                     40.491352
      2022-01-31
                    69.548786
      2022-02-01
                    69.767189
      2022-02-02
                    70.044064
      2022-02-03
                    70.019689
      2022-02-04
                    70.117927
      Name: EMA_10, Length: 1588, dtype: float64
[18]: # Check if there is any missign value.
      msci.isnull().sum()
[18]: Open
                       0
      High
                       0
      Low
                       0
      Close
                       0
      Adj Close
                       0
      daily return
                       0
      EMA_10
      dtype: int64
```

3.2 Write the function split_data

The function split_data takes explanatory and response time series as parameter to and splits it into X_train, X_test, y_train and y_test. In the context of linear regression, y denotes the response variable (=label) and X (=features) the explanatory variable. Other than the series, it takes the size of your train split as parameter.

Also, be sure to add docstring documentation as learnt in the Python Refresher. Furthermore, print out useful information in the function, like the shape of the initial time series as well as the subsets created.

For example: the first 80% of the time series as train, the last 20% as test.

```
[19]: def split_data(X: pd.Series, y: pd.Series, size: float) -> tuple:
    """
    Input: X: pd.Series, y: pd.Series, size: float
    X: The explanatory variable.
    y: The response variable.
    size: The proportion of training data in the time series,

Output: A tuple with length of 4.
    tuple[0]: X_train
```

```
tuple[1]: X_test
   tuple[2]: y_train
   tuple[3]: y_test
  Notice: X and y should have identical length and time scale.
  if len(X) != len(y):
      raise Exception("The inputs X and y should have identical length!")
  elif sum(~(X.index == y.index)) > 0:
      raise Exception("The inputs X and y should have identical time scale!")
  time_quantile = np.quantile(X.index, q = size)
  X_train, X_test = X[X.index < time_quantile].values, X[X.index >=_
→time_quantile].values
  y_train, y_test = y[y.index < time_quantile].values, y[y.index >=_
→time_quantile].values
  print(f"The length of the initial time series is {len(X)}.")
  print(f"The first {size*100}% of the time series as train, the last⊔
\rightarrow {round((1-size)*100)}% as test.")
  print(f"""
  X_train: {X_train}
  X test: {X test}
  y_train: {y_train}
  y_test: {y_test}
  """)
  return X_train, X_test, y_train, y_test
```

- 3.3 Run a linear regression model on the EMA and the Adj Close
- 3.3.1 3.3.1. Split the data into train and test using your custom function using 20% test size.

```
[20]: print(split_data.__doc__)
```

```
Input: X: pd.Series, y: pd.Series, size: float
X: The explanatory variable.
y: The response variable.
size: The proportion of training data in the time series,
Output: A tuple with length of 4.
tuple[0]: X_train
tuple[1]: X_test
tuple[2]: y_train
tuple[3]: y_test
```

Notice: X and y should have identical length and time scale.

```
[21]: X_train, X_test, y_train, y_test = split_data(X = msci["EMA_10"], y = msci["Adj_
      \hookrightarrowClose"], size = 0.8)
     print(split_data(X = msci["EMA_10"], y = msci["Adj Close"], size = 0.8))
     The length of the initial time series is 1588.
     The first 80.0% of the time series as train, the last 20% as test.
         X_train: [40.49135186 40.49135186 40.49135186 ... 57.1533377 56.78368343
      56.60876714]
         X_test: [56.28529285 56.12629848 56.13649247 56.32519397 56.6198664
     56.85913999
      57.22069533 57.56570283 57.95182607 58.19304984 58.55073538 58.90532954
      59.18269915 59.30943762 59.4386378 59.53706027 59.65038028 59.83783153
      59.98026989 60.10591986 60.25244776 60.23205392 60.33560801 60.42033408
      60.48054661 60.50977107 60.50817692 60.57610175 60.58795254 60.5138453
      60.45867752 60.36070738 60.36435335 60.42927877 60.53705447 60.63616544
      60.68992912 60.76488807 60.82439609 60.86397566 60.99291587 61.03282667
      61.06001553 61.03125014 61.00953616 61.07921761 61.25100493 61.48993645
      61.65081132 61.74600031 61.83481304 61.84189227 61.82582199 61.87097186
      61.94252791 62.04844122 62.13691891 62.24210297 62.35731179 62.40420611
      62.24946035 62.26130912 62.0177701 62.02437693 62.12269536 62.20860314
      62.38455774 62.5376294 62.73574305 62.8777957 62.97944637 63.09176425
      63.25653389 63.3949888 63.49916128 63.52245096 63.47774244 63.38104242
      63.30192422 63.23901319 63.04179412 62.88772053 62.9292684 62.88492349
      62.74661895 62.50775462 62.4908591 62.46610465 62.54969539 62.65270238
      62.75519912 62.80626688 62.86262451 62.91237867 62.96766155 62.97099097
      62.971893
                  63.03639473 63.03269263 62.98047416 63.02337603 63.14956838
      63.30747156 63.43302169 63.48473301 63.62359919 63.90118099 64.12282795
      64.37340458 64.59117541 64.78574779 64.96498372 65.14077975 65.249999
      65.46324353 65.67233159 65.81243245 65.88151434 65.9161742 65.89352074
      65.96972098 65.97376835 65.97343714 65.90757972 65.85369637 65.72762869
      65.67549253 65.5344581 65.45732424 65.36688761 65.39491566 65.26481453
      65.04177158 64.6734555 64.52149508 64.53562277 64.46884317 64.38141279
      64.28801716 64.28083168 64.30227975 64.38541461 64.51537502 64.58527104
      64.68253799 64.70017768 64.77655251 64.82993151 64.89364558 65.01318305
      65.12556136 65.25940927 65.33430594 65.40651587 65.54393535 65.68187523
      65.82935038 65.95001187 66.11431996 66.16677254 66.26252115 66.36636529
      66.39667448 66.44697866 66.49906747 66.57812218 66.6919921 66.77422756
      66.89616671 66.98500426 67.15242442 67.37138586 67.46491074 67.63434464
      67.82398251 67.98642891 68.15213213 68.27313258 68.30108247 68.25289871
      68.33189493 68.38377463 68.446262
                                          68.61216325 68.7460779 68.82467464
      68.8762275 68.90747626 68.88021057 69.01093544 69.1014959 69.16465997
      69.28739014 69.40966881 69.47145565 69.54751429 69.65529018 69.76533213
      69.89544714 69.97457638 70.00470461 70.15323832 70.34035234 70.44061276
```

70.49167284 70.55166687 70.61897189 70.71229758 70.79412038 70.88110665

```
71.01057552 71.06549307 71.1140697 71.24672774 71.32429497 71.34585704
 71.29244687 71.27243206 71.22872921 71.22576485 71.25248791 71.20330177
 70.98998505 70.91018807 70.85400914 70.84448115 70.81482385 70.73043776
 70.45917264 70.34107145 70.01489414 69.84639937 69.4808123 69.29647083
 69.16750767 69.14033098 69.01242978 68.7966522 68.66565162 68.66049236
 68.77651179 68.89329847 69.04897083 69.20002354 69.34911788 69.482035
 69.68187618 69.85995752 69.92367774 70.068726
                                                70.21837303 70.38635761
 70.58027509 70.78994636 71.11999418 71.39185465 71.62886085 71.780873
 71.8378388 72.00104513 72.18194503 72.31902319 72.49129769 72.64864581
 72.79378144 72.90888608 73.0067053 73.07216429 73.11296946 73.13178059
 72.96316716 72.93452052 72.74529701 72.48845473 72.4440978 72.28027696
 72.27741321 72.42446063 72.58120876 72.69852638 72.86009858 72.96861098
 73.00638234 73.21035969 73.26247502 73.26139147 73.19674123 73.33149261
 73.47089358 73.67603973 73.85857801 74.14444791 74.1563663 74.0352084
 74.09971586 73.99613093 73.84047065 73.59674872 73.39006696 73.21914514
 73.09748295 72.8415774 72.68492757 72.59675837 72.21552957 71.81088745
 71.37436312 70.86629743 70.49060754 70.03776981 69.67999342 69.41090316
 69.43073834 69.54878624 69.76718875 70.04406369 70.01968914 70.11792703]
   y_train: [35.65920258 35.67705154 35.88246155 ... 55.52363586 54.26105881
54.951530467
    y test: [53.9750061 54.54711151 55.30662918 56.28315353 57.04266739
57.03280258
 57.93041229 58.1967392 58.75897598 58.35455704 59.22257614 59.55794907
 59.48890305 58.94638824 59.0844841 59.04502869 59.22257614 59.73549652
 59.67631531 59.72563553 59.96236801 59.20285034 59.85386276 59.85386276
 59.80454254 59.69604111 59.55794907 59.93277359 59.69604111 59.24230957
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The length of the initial time series is 1588. The first 80.0% of the time series as train, the last 20% as test.

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       62.20258331, 62.19268799, 62.53902435, 62.23226929, 61.96509171,
       62.4301796 , 62.92494965 , 63.22180939 , 63.20202255 , 62.92494965 ,
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       64.8446579 , 64.95350647, 65.11183167, 64.92382812, 65.59671021,
       65.78472137, 65.61650085, 65.36911011, 65.25036621, 64.97329712,
       65.48786163, 65.17121124, 65.15142059, 64.79518127, 64.79518127,
       64.34989166, 64.62696075, 64.09261322, 64.30041504, 64.15198517,
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       63.79574203, 63.37023926, 63.19212341, 63.07338333, 63.44940567,
       63.59783554, 63.95407104, 64.29051208, 64.09261322, 64.31030273,
```

```
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68.71430206, 68.64463043, 68.58490753, 68.29627991, 69.13231659,
69.04273987, 68.9830246 , 69.37117767, 69.49062347, 69.28160858,
69.42094421, 69.66976929, 69.78919983, 70.00817108, 69.85887146,
69.66976929, 70.34655762, 70.7048645, 70.41622925, 70.24703217,
70.34655762, 70.4460907, 70.65509796, 70.68495941, 70.79444122,
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73.52999878, 73.13999939, 72.5
                                    , 72.45999908, 72.44999695,
72.55000305, 71.69000244, 71.98000336, 72.19999695, 70.5
69.98999786, 69.41000366, 68.58000183, 68.80000305, 68.
68.06999969, 68.19999695, 69.51999664, 70.08000183, 70.75
71.29000092, 69.91000366, 70.55999756]))
```

3.3.2 3.3.2. Train the model using scikit-learn

```
[22]: lr = LinearRegression(fit_intercept=True)
lr.fit(X_train.reshape(-1, 1), y_train)
```

[22]: LinearRegression()

3.3.3 Retrieve and present statistical measures and key numbers i.e. \mathbb{R}^2 , intercept and coefficient.

```
[23]: lr.coef_
```

[23]: array([1.17302995])

The coefficient(estimated slope) of our simple linear regression model is 1.17302994.

```
[24]: lr.intercept_
```

[24]: -10.923473833260871

The estimated intercept of our simple linear regression model is -10.923472656011356.

Hence, our fitted model is:

$$\hat{Y} = 1.17302994X - 10.923472656011356$$

```
[25]: r2_score(y_train, lr.predict(X_train.reshape(-1, 1)))
```

[25]: 0.984578187294296

The R^2 of our simple linear regression model is 0.9845781871086455.

```
[26]: mean_squared_error(y_train, lr.predict(X_train.reshape(-1, 1)))
```

[26]: 0.5708205565316868

The $MSE = \frac{SSE}{n-2} = \frac{\|Y - \hat{Y}\|^2}{n-2}$ (Mean Squared Error) of our simple linear regression model is 0.5708204284208702.

3.4 3.4. Visualize the results in one plot using Matplotlib.Pyplot

Create a combined plot that shows 1. the actual output 2. the predicted output 3. the training data

Make sure to add a legend and labels to each line and that every series is at the "correct" x coordinates.

```
[27]: y_predict = lr.predict(X_test.reshape(-1, 1))
```

```
plt.figure()

plt.subplots_adjust(top = 2, right = 2)

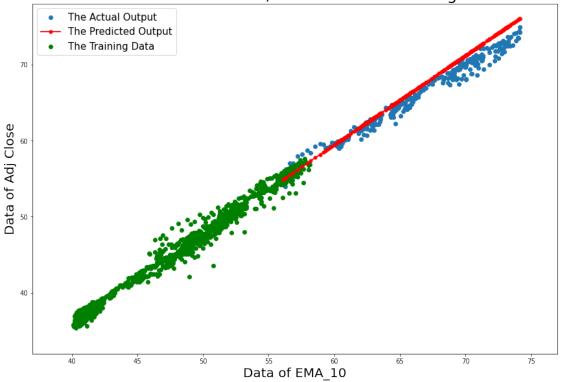
plt.xlim(round(min(msci["EMA_10"]) - 3), round(max(msci["EMA_10"]) + 3))

plt.ylim(round(min(msci["Adj Close"]) - 3), round(max(msci["Adj Close"]) + 3))

plt.scatter(X_test, y_test, label = "The Actual Output")

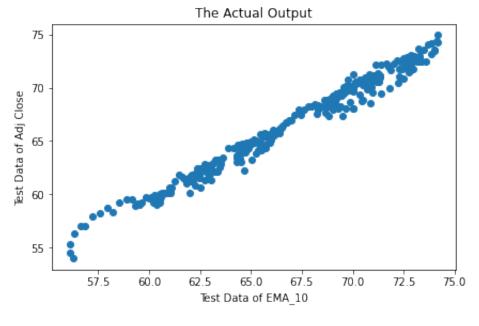
plt.plot(X_test, y_predict, label = "The Predicted Output", color = "red",
```

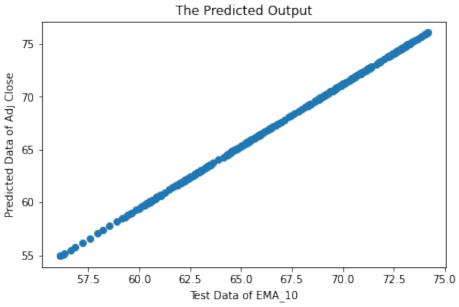




Also create subplots for each data set.

[29]: [Text(0.5, 0, 'Train Data of EMA_10'), Text(0, 0.5, 'Train Data of Adj Close')]







4 4 Optional: Basic Data Structures in Python

4.1 4.1. Create an empty dictionary

```
[30]: dic = {}
```

4.2 4.2. Update the new dictionary with any key values

```
[31]: dic["x"] = 1 dic
```

[31]: {'x': 1}

4.3 4.3. List comprehension: iterate through the following dictionaries values and return all values as string

```
new\_dict = \{0:\, 1,\, 1:\, \text{``a''},\, 2:\, 0.34,\, 3:\, True\}
```

```
1 <class 'str'>
a <class 'str'>
0.34 <class 'str'>
True <class 'str'>
```

4.4 4.4. Convert the two lists to sets and then return the union of the two

```
L1 = [\text{``A''}, \text{``B''}, \text{``C''}, \text{``D''}]

L2 = [\text{``B''}, \text{``D''}, \text{``E''}, \text{``F''}]
```

```
[33]: L1, L2 = ["A", "B", "C", "D"], ["B", "D", "E", "F"] set(L1) | set(L2)
```

[33]: {'A', 'B', 'C', 'D', 'E', 'F'}

Or alternatively:

```
[34]: set(L1 + L2)
```

[34]: {'A', 'B', 'C', 'D', 'E', 'F'}

4.5 4.5. Iterate through the first list and check if it is in the second by elementwise comparison

```
[35]: for i in L1:
    for j in L2:
        if i == j:
            print(f"Element {i} is ALSO in L2!")
            break
    else: print(f"Element {i} is NOT in L2!")

Element A is NOT in L2!
Element B is ALSO in L2!
Element C is NOT in L2!
Element D is ALSO in L2!
```