

# CM3005 Data Science

## Midterm Report

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## 1.0 Domain and Objectives

### 1.1 Domain-Specific Area

This project is situated within the domain of financial time-series analysis, specifically the analysis of long-term trends in a diversified equity portfolio. Financial markets have large volumes of time-dependant data, making them a useful area for statistical analysis and machine learning techniques.

I selected the portfolio based on a weighted combination of major US market indices and technology stocks, that has both broad market exposure and individual equity performance. These types of portfolios are commonly analysed to understand growth patterns, volatility behaviour, and the impact of market-wide events over time. This makes the domain very suited for studying regression trends.

### 1.2 Rationale for Using Linear Regression

Linear regression is used as a baseline model for financial contexts to identify long-term trends because despite short-term volatility and non-linear fluctuations, aggregated portfolio values usually have smoother behaviour over the long term. This makes linear regression an appropriate starting point for modelling portfolio growth as a function of time.

The purpose of using linear regression in this project is not to exact predictions or investment recommendations, but to evaluate whether a simple, interpretable model can capture the dominant trend in portfolio performance.

### 1.3 Project Objectives

This project evaluates the suitability of linear regression as a baseline model for analysing long-term trends in a diversified equity portfolio using historical financial data. I aim to construct a pre-process a real-world financial dataset, analyse the volatility and distribution ,then visualise the trends. I will implement and evaluate regression models and compare it with a more complex polynomial model to assess trade-offs between accuracy and interpretability.

### 1.4 Expected Contribution

This project shows how classical machine learning techniques, such as linear regression, can be applied meaningfully to financial time-series data when used for trend analysis rather than short-term prediction. The findings reveal the pros and cons, as well as

limitations of linear regression in capturing portfolio-level behaviour and show how diversification improves model stability. The methodology can be transferred to other domains that also use time-series data over a long time.

## 2.0 Dataset Description

### 2.1 Data Source

The dataset was obtained from Yahoo Finance, a widely used financial data platform that gives historical market data (Yahoo Finance, 2025). Yahoo Finance is used in academic and industry context for analysis and it is a reliable site for studying trends.

### 2.2 Dataset Composition

The dataset consists of four financial instruments

- S&P 500 Index
- NASDAQ-100 Index
- Apple Inc. (AAPL) stock
- Microsoft Corporation (MSFT) stock

### 2.3 Dataset Structure and Size

Each CSV file has around 2,700 daily observations between January 2015 to December 2025. The use of multiple CSV files means the dataset was not initially in First Normal Form (1NF), requiring transformation during the data preparation stage. After pre-processing and merging, the final dataset consists of a single time-series table where each row represents one trading day and each column represents an individual asset or the constructed portfolio.

### 2.4 Data Types

The raw data includes date fields and numerical variables such as opening price, closing price, adjusted closing price, and trading volume. I retained only the date and adjusted closing price. Adjusted closing price refers to actions like stock splits and dividends.

### 2.5 Suitability for Linear Regression

The dataset has a clear long-term trend that is suitable for regression. The dataset also contains real-world imperfections, such as missing values and differing trading calendars, which requires pre-processing.

## 3.0 Data Preparation

### 3.1 Data Acquisition and Initial Inspection

I retrieved the data from Yahoo Finance using the Python `yfinance` library.

The data was downloaded as separate CSV files to reflect real-world financial data acquisition practices, where data is often gathered from different places. Each CSV

contains daily observations including open, high, low, close, adjusted close prices and trading volume.

```
In [1]: # Install dependency required for Yahoo Finance data acquisition (run once)
%pip install -q yfinance

import os
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import yfinance as yf
from scipy.stats import skew, kurtosis

from sklearn.linear_model import LinearRegression
from sklearn.model_selection import train_test_split, KFold, cross_val_score
from sklearn.metrics import mean_squared_error, mean_absolute_error, r2_score
from sklearn.preprocessing import PolynomialFeatures
```

Note: you may need to restart the kernel to use updated packages.

```
In [2]: # -----
# 3.1 Data acquisition (Yahoo Finance)
# -----

# Directory for raw CSV downloads
RAW_DIR = "data_raw"
os.makedirs(RAW_DIR, exist_ok=True)

# Study period (end date is exclusive in yfinance, but works as intended for dai
START_DATE = "2015-01-01"
END_DATE = "2025-12-22"

# Symbols used to download the portfolio components
tickers = {
    "SP500": "^GSPC",
    "NASDAQ": "^NDX",
    "AAPL": "AAPL",
    "MSFT": "MSFT"
}

def download_and_save(symbol: str, out_name: str) -> None:
    """Download daily price data for a symbol and save it as a CSV in RAW_DIR."""
    df = yf.download(
        symbol,
        start=START_DATE,
        end=END_DATE,
        interval="1d",
        auto_adjust=False,
        progress=False,
        group_by="column"
    )

    # Move index (date) into a normal column for CSV storage
    df = df.reset_index()

    # Flatten MultiIndex columns (sometimes returned by yfinance)
    if isinstance(df.columns, pd.MultiIndex):
        df.columns = [col[0] if col[0] != "" else col[1] for col in df.columns]
```

```

# Standardise column names for consistent downstream processing
df.columns = [str(c).strip().replace(" ", "_") for c in df.columns]

out_path = os.path.join(RAW_DIR, f"{out_name}.csv")
df.to_csv(out_path, index=False)
print(f"Saved {out_name}: {df.shape}")

# Download and store each asset as a separate CSV (multi-file dataset)
for name, sym in tickers.items():
    download_and_save(sym, name)

```

Saved SP500: (2759, 7)  
 Saved NASDAQ: (2759, 7)  
 Saved AAPL: (2759, 7)  
 Saved MSFT: (2759, 7)

```

In [3]: # Quick inspection of downloaded files
for f in os.listdir(RAW_DIR):
    df_tmp = pd.read_csv(os.path.join(RAW_DIR, f))
    print(f, df_tmp.shape)
    display(df_tmp.head())

```

AAPL.csv (2759, 7)

	Date	Adj_Close	Close	High	Low	Open	Volume
0	2015-01-02	24.237553	27.332500	27.860001	26.837500	27.847500	212818400
1	2015-01-05	23.554743	26.562500	27.162500	26.352501	27.072500	257142000
2	2015-01-06	23.556961	26.565001	26.857500	26.157499	26.635000	263188400
3	2015-01-07	23.887276	26.937500	27.049999	26.674999	26.799999	160423600
4	2015-01-08	24.805079	27.972500	28.037500	27.174999	27.307501	237458000

MSFT.csv (2759, 7)

	Date	Adj_Close	Close	High	Low	Open	Volume
0	2015-01-02	39.858456	46.759998	47.419998	46.540001	46.660000	27913900
1	2015-01-05	39.491928	46.330002	46.730000	46.250000	46.369999	39673900
2	2015-01-06	38.912270	45.650002	46.750000	45.540001	46.380001	36447900
3	2015-01-07	39.406685	46.230000	46.459999	45.490002	45.980000	29114100
4	2015-01-08	40.565956	47.590000	47.750000	46.720001	46.750000	29645200

NASDAQ.csv (2759, 7)

	Date	Adj_Close	Close	High	Low	Open	Volume
0	2015-01-02	4230.240234	4230.240234	4276.709961	4206.459961	4258.600098	1435150000
1	2015-01-05	4160.959961	4160.959961	4210.959961	4151.850098	4206.549805	1794470000
2	2015-01-06	4110.830078	4110.830078	4176.259766	4090.330078	4174.779785	2167320000
3	2015-01-07	4160.000000	4160.000000	4169.970215	4126.390137	4139.850098	1957950000
4	2015-01-08	4240.549805	4240.549805	4247.930176	4192.629883	4195.490234	2105450000

SP500.csv (2759, 7)

	Date	Adj_Close	Close	High	Low	Open	Volume
0	2015-01-02	2058.199951	2058.199951	2072.360107	2046.040039	2058.899902	2708700000
1	2015-01-05	2020.579956	2020.579956	2054.439941	2017.339966	2054.439941	3799120000
2	2015-01-06	2002.609985	2002.609985	2030.250000	1992.439941	2022.150024	4460110000
3	2015-01-07	2025.900024	2025.900024	2029.609985	2005.550049	2005.550049	3805480000
4	2015-01-08	2062.139893	2062.139893	2064.080078	2030.609985	2030.609985	3934010000

## 3.2 Data Cleaning

```
In [4]: # -----
# 3.2 Cleaning
# -----

FILES = {
    "SP500": os.path.join(RAW_DIR, "SP500.csv"),
    "NASDAQ": os.path.join(RAW_DIR, "NASDAQ.csv"),
    "AAPL": os.path.join(RAW_DIR, "AAPL.csv"),
    "MSFT": os.path.join(RAW_DIR, "MSFT.csv"),
}

def load_clean_price_series(path: str, series_name: str) -> pd.DataFrame:
    """Load one CSV, clean it, and return a tidy Date + Adjusted Close series."""
    df = pd.read_csv(path)

    # Standardise column names
    df.columns = [c.strip().lower().replace(" ", "_") for c in df.columns]

    # Convert date column to datetime and sort chronologically
    df["date"] = pd.to_datetime(df["date"], errors="coerce")
    df = df.dropna(subset=["date"]).sort_values("date")

    # Ensure adjusted close exists (best practice for historical price analysis)
```

```

if "adj_close" not in df.columns:
    raise ValueError(f"{series_name}: 'Adj Close' column not found. Columns

# Keep only atomic columns needed for analysis and rename to series_name
out = df[["date", "adj_close"]].rename(columns={"adj_close": series_name})

# Ensure numeric values and remove invalid rows
out[series_name] = pd.to_numeric(out[series_name], errors="coerce")
out = out.dropna(subset=[series_name])

return out.reset_index(drop=True)

# Load and clean each time series independently (one DataFrame per asset)
series_list = []
for name, path in FILES.items():
    s = load_clean_price_series(path, name)
    print(name, s.shape, "from", os.path.basename(path))
    display(s.head())
    series_list.append(s)

```

SP500 (2759, 2) from SP500.csv

	date	SP500
0	2015-01-02	2058.199951
1	2015-01-05	2020.579956
2	2015-01-06	2002.609985
3	2015-01-07	2025.900024
4	2015-01-08	2062.139893

NASDAQ (2759, 2) from NASDAQ.csv

	date	NASDAQ
0	2015-01-02	4230.240234
1	2015-01-05	4160.959961
2	2015-01-06	4110.830078
3	2015-01-07	4160.000000
4	2015-01-08	4240.549805

AAPL (2759, 2) from AAPL.csv

	date	AAPL
0	2015-01-02	24.237553
1	2015-01-05	23.554743
2	2015-01-06	23.556961
3	2015-01-07	23.887276
4	2015-01-08	24.805079

MSFT (2759, 2) from MSFT.csv

	date	MSFT
0	2015-01-02	39.858456
1	2015-01-05	39.491928
2	2015-01-06	38.912270
3	2015-01-07	39.406685
4	2015-01-08	40.565956

### 3.3 Transformation to First Normal Form (1NF)

```
In [5]: # -----
# 3.3 1NF transformation
# -----

# Merge into a single 1NF table: one row per date, one column per asset
df_1nf = series_list[0]
for nxt in series_list[1:]:
    df_1nf = df_1nf.merge(nxt, on="date", how="outer")

df_1nf = df_1nf.sort_values("date").reset_index(drop=True)

# Handle missing values due to different trading calendars by forward-filling
price_cols = ["SP500", "NASDAQ", "AAPL", "MSFT"]
df_1nf[price_cols] = df_1nf[price_cols].ffill()

# Drop any remaining missing rows (typically at the start before any prices exist)
df_1nf = df_1nf.dropna(subset=price_cols).reset_index(drop=True)

df_1nf.head(), df_1nf.shape
```

```
Out[5]: (   date      SP500      NASDAQ      AAPL      MSFT
0 2015-01-02  2058.199951  4230.240234  24.237553  39.858456
1 2015-01-05  2020.579956  4160.959961  23.554743  39.491928
2 2015-01-06  2002.609985  4110.830078  23.556961  38.912270
3 2015-01-07  2025.900024  4160.000000  23.887276  39.406685
4 2015-01-08  2062.139893  4240.549805  24.805079  40.565956,
(2759, 5))
```

### 3.4 Data Normalisation

The raw dataset was initially stored across multiple CSV files, one for each financial instrument. This structure is not in the First Normal Form (1NF), as the data is distributed across separate tables representing the same entity (time-series price data).

To transform the dataset into 1NF, all cleaned price series were merged into a single table using the date attribute as the primary key. Each row represents one trading day, and each column represents a single attribute (SP500, NASDAQ, AAPL, MSFT prices). Missing values caused by different trading calendars were handled using forward-filling.

```
In [6]: # -----
# 3.4 Normalisation + portfolio construction
# -----
```

```
# Portfolio weights (must sum to 1.0)
WEIGHTS = {"SP500": 0.45, "NASDAQ": 0.25, "AAPL": 0.15, "MSFT": 0.15}

# Normalise each series to a common baseline (start value = 100) for comparabili
indexed = df_1nf[price_cols].div(df_1nf[price_cols].iloc[0]).mul(100)

# Weighted portfolio value (indexed)
df_1nf["portfolio"] = sum(indexed[c] * WEIGHTS[c] for c in price_cols)

df_1nf[["date"] + price_cols + ["portfolio"]].head()
```

```
Out[6]:
```

	date	SP500	NASDAQ	AAPL	MSFT	portfolio
0	2015-01-02	2058.199951	4230.240234	24.237553	39.858456	100.000000
1	2015-01-05	2020.579956	4160.959961	23.554743	39.491928	98.207541
2	2015-01-06	2002.609985	4110.830078	23.556961	38.912270	97.301620
3	2015-01-07	2025.900024	4160.000000	23.887276	39.406685	98.491901
4	2015-01-08	2062.139893	4240.549805	24.805079	40.565956	100.764552

## 4.0 Statistical Analysis

### 4.1 Measures of Central Tendency

This section examines the central tendency of each financial time series using the mean and median. These measures provide insight into the typical value of each asset and the constructed portfolio over the study period.

### 4.2 Measures of Spread

Measures of spread describe the variability of each series. Standard deviation is used to quantify volatility, while minimum and maximum values indicate the range of observed prices during the study period.

### 4.3 Distribution Characteristics

Distribution characteristics were analysed using skewness and kurtosis. Skewness indicates the asymmetry of price movements, while kurtosis measures the presence of extreme values. These metrics are particularly relevant in financial time series, which often deviate from normal distributions.

```
In [7]: # -----
# 4.0 Statistical analysis (summary measures)
# -----

# Series included in statistical summary
analysis_cols = ["SP500", "NASDAQ", "AAPL", "MSFT", "portfolio"]

stats_summary = []
for col in analysis_cols:
    series = df_1nf[col]
    stats_summary.append({
```



```

    "Series": col,
    "Mean": series.mean(),
    "Median": series.median(),
    "Standard Deviation": series.std(),          # volatility proxy
    "Minimum": series.min(),
    "Maximum": series.max(),
    "Skewness": skew(series),
    "Kurtosis": kurtosis(series, fisher=True)     # excess kurtosis
})

stats_df = pd.DataFrame(stats_summary)
stats_df

```

Out[7]:

	Series	Mean	Median	Standard Deviation	Minimum	Maximum	Skewness
0	SP500	3606.353424	3269.959961	1318.312181	1829.079956	6901.000000	0.644
1	NASDAQ	11115.317771	10101.830078	5829.363604	3947.800049	26119.849609	0.631
2	AAPL	105.902417	87.734055	73.940394	20.604082	286.190002	0.443
3	MSFT	205.465399	191.269852	142.779045	34.437153	541.057373	0.529
4	portfolio	287.401532	253.859229	161.773834	92.229008	675.188581	0.528

## 4.4 Interpretation of Statistical Findings

The results show that individual assets such as AAPL and the NASDAQ index exhibit higher standard deviation compared to the portfolio, indicating greater price volatility. In contrast, the portfolio demonstrates reduced variability, highlighting the stabilising effect of diversification.

Positive skewness across most series suggests the presence of large upward price movements over time, while kurtosis values indicate heavy-tailed distributions, reflecting the occurrence of extreme market events such as the COVID-19 crash.

Among the analysed measures, standard deviation is the most informative, as it directly reflects investment risk and volatility, making it particularly relevant for financial decision-making.

## 5.0 Data Visualisation

### 5.1 Portfolio Allocation Visualisation

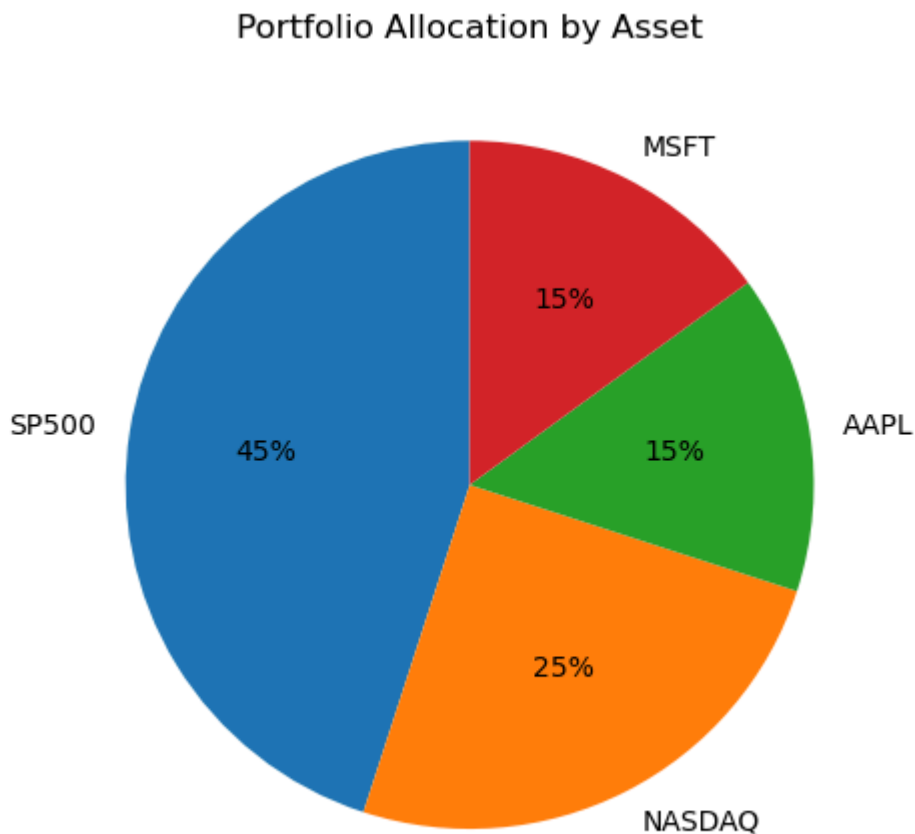
```

In [8]: # -----
# 5.0 Visualisation (key plots)
# -----

# Portfolio weight allocation (communication of portfolio construction)
plt.figure()
plt.pie(WEIGHTS.values(), labels=WEIGHTS.keys(), autopct="%1.0f%%", startangle=90)
plt.title("Portfolio Allocation by Asset")

```

```
plt.tight_layout()
plt.show()
```

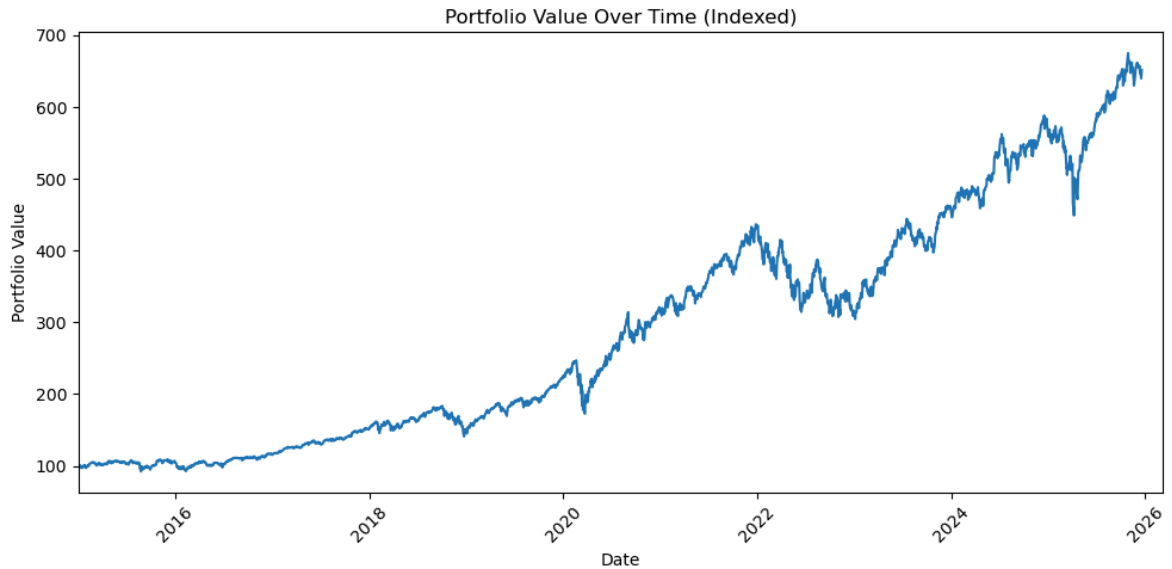


This visualisation shows the portfolio composition based on predefined weights. The allocation emphasises broad market exposure through the S&P 500 and NASDAQ indices, complemented by individual technology stocks. This diversified structure reduces reliance on a single asset and helps stabilise portfolio performance over time.

## 5.2 Time-Series Visualisation

```
In [9]: # Portfolio value over time (trend + volatility over the study period)
min_date = df_1nf["date"].min()
max_date = df_1nf["date"].max()
padding_days = int((max_date - min_date).days * 0.02)

plt.figure(figsize=(10, 5))
plt.plot(df_1nf["date"], df_1nf["portfolio"])
plt.title("Portfolio Value Over Time (Indexed)")
plt.xlabel("Date")
plt.ylabel("Portfolio Value")
plt.xlim(min_date, max_date + pd.Timedelta(days=padding_days))
plt.xticks(rotation=45)
plt.tight_layout()
plt.show()
```



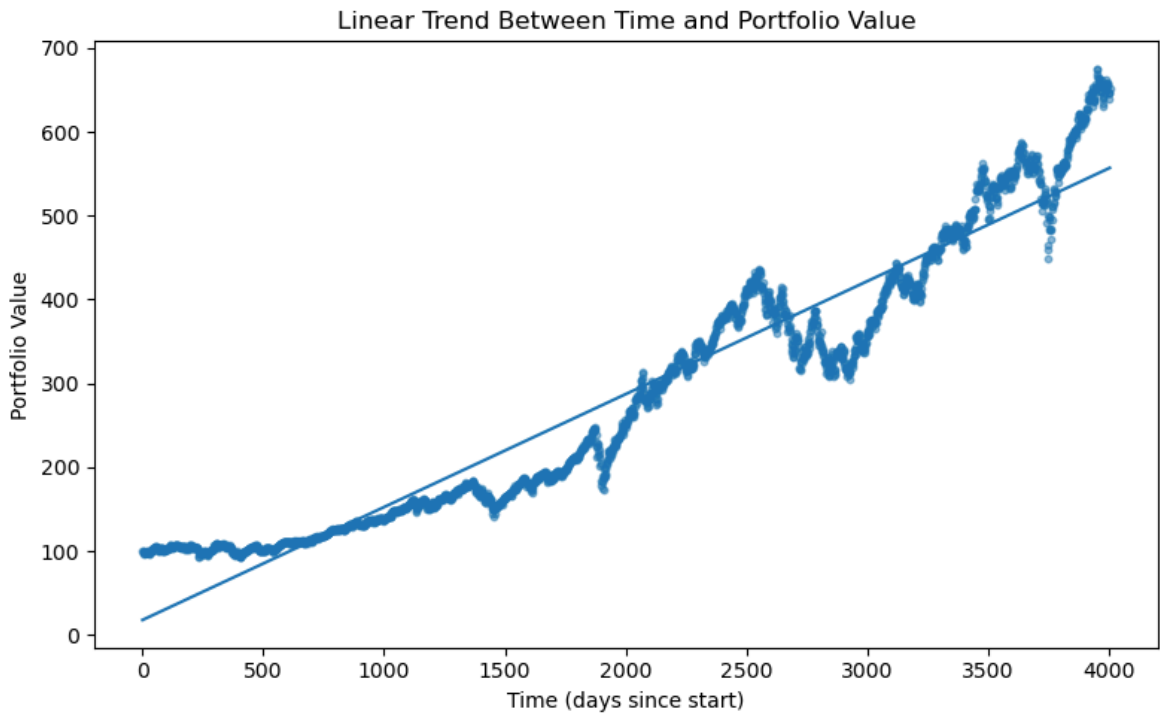
The time-series plot reveals a clear long-term upward trend in portfolio value, with periods of increased volatility. Significant market events, like the COVID-19 market shock, are visible as sharp declines followed by recoveries. A pronounced decline is observed around early 2020, corresponding to the COVID-19 market shock, followed by a gradual recovery. Despite short-term fluctuations, the overall linear trend supports the suitability of regression-based modelling.

### 5.3 Feature–Target Relationship

```
In [10]: # Convert date to a numeric time index for regression modelling
df_1nf["t"] = (df_1nf["date"] - df_1nf["date"].min()).dt.days

# Scatter + fitted line to visualise linear relationship between time and portfo
coef = np.polyfit(df_1nf["t"], df_1nf["portfolio"], 1)
trend = np.poly1d(coef)

plt.figure(figsize=(8, 5))
plt.scatter(df_1nf["t"], df_1nf["portfolio"], s=10, alpha=0.5)
plt.plot(df_1nf["t"], trend(df_1nf["t"]))
plt.title("Linear Trend Between Time and Portfolio Value")
plt.xlabel("Time (days since start)")
plt.ylabel("Portfolio Value")
plt.tight_layout()
plt.show()
```



This visualisation highlights the relationship between time and portfolio value. While short-term volatility is present, the data points cluster around an increasing linear trend. This supports the use of linear regression as a baseline model for capturing long-term portfolio growth (Scikit-learn, 2024).

## 5.4 Most Informative Visualisation

Among the visualisations presented, the time-series plot of portfolio value is the most informative. It simultaneously conveys long-term growth, short-term volatility, and the impact of major market events. Without this visual representation, identifying trends and structural changes in the data would be significantly more difficult. The plot provides strong visual justification for the application of regression techniques in subsequent modelling.

## 6.0 Linear Regression Model

### 6.1 Feature and Target Selection

```
In [11]: # -----  
# 6.0 Linear regression model (baseline)  
# -----  
  
# Feature (time index) and target (portfolio value)  
X = df_1nf[["t"]]  
y = df_1nf["portfolio"]
```

### 6.2 Model Construction

```
In [12]: # Time-series split: train first, test later (prevents data leakage)  
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, shuffle
```

```
# Fit baseline linear regression model
model = LinearRegression()
model.fit(X_train, y_train); # semicolon suppresses notebook object display
```

### 6.3 Model Results

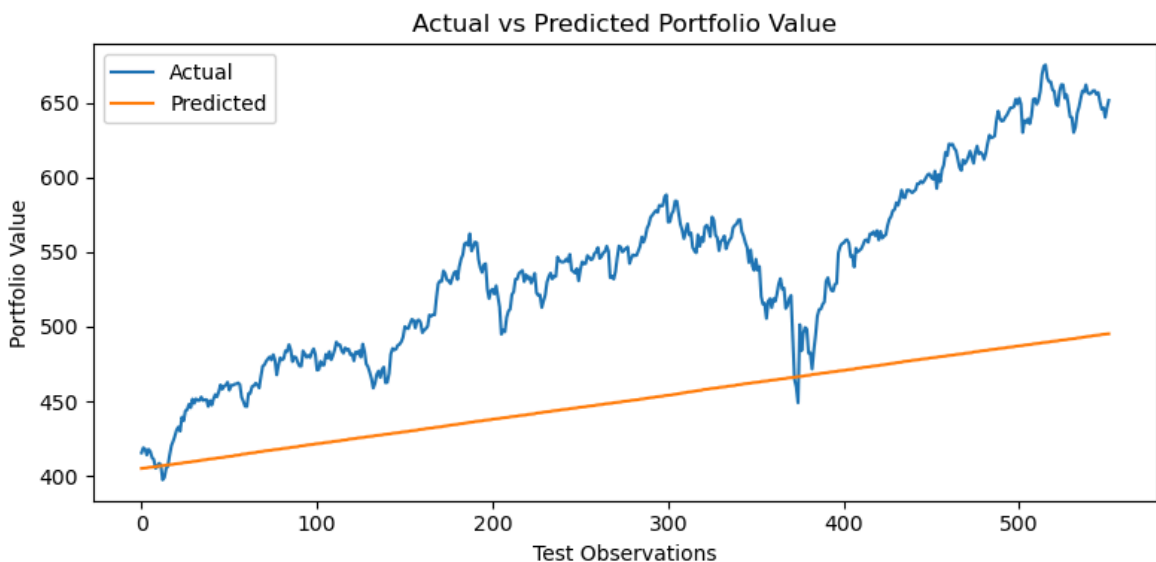
```
In [13]: # Predict on the test split
y_pred = model.predict(X_test)

# Evaluate model performance
rmse = np.sqrt(mean_squared_error(y_test, y_pred))
mae = mean_absolute_error(y_test, y_pred)
r2 = r2_score(y_test, y_pred)

print(f"RMSE: {rmse:.2f}")
print(f"MAE: {mae:.2f}")
print(f"R²: {r2:.4f}")
```

RMSE: 97.04  
MAE: 87.90  
R²: -1.3239

```
In [14]: # Visual comparison of actual vs predicted values on the test split
plt.figure(figsize=(8, 4))
plt.plot(y_test.values, label="Actual")
plt.plot(y_pred, label="Predicted")
plt.title("Actual vs Predicted Portfolio Value")
plt.xlabel("Test Observations")
plt.ylabel("Portfolio Value")
plt.legend()
plt.tight_layout()
plt.show()
```



This is a plot for actual versus predicted portfolio values over the test period. The x-axis represents the test observations (trading days), while the y-axis shows the indexed portfolio value. The predicted line illustrates the linear regression model's ability to capture the long-term trend but not short-term market fluctuations.

## 7.0 Model Validation

## 7.1 Validation Strategy

```
In [15]: # -----  
# 7.0 Validation (cross-validation)  
# -----  
  
# Cross-validation to assess model robustness across different splits  
kf = KFold(n_splits=5, shuffle=True, random_state=42)  
cv_rmse = np.sqrt(-cross_val_score(model, X, y, scoring="neg_mean_squared_error")  
print("Cross-validation RMSE per fold:", cv_rmse)  
print("Mean CV RMSE:", cv_rmse.mean())
```

Cross-validation RMSE per fold: [43.00371249 42.88827282 44.54239962 45.06811906 43.68615029]

Mean CV RMSE: 43.83773085649226

## 7.2 Validation Results

The model was validated using 5-fold cross-validation. RMSE values across folds were consistent, ranging from approximately 42.9 to 45.1, with a mean RMSE of 43.84. The limited variation between folds suggest the model is stable and is good at generalising unseen data. The model is able to capture an underlying trend in the portfolio data rather than overfitting.

## 8.0 Feature Engineering

### 8.1 Engineered Features

```
In [16]: # -----  
# 8.0 Feature engineering (polynomial features)  
# -----  
  
# Engineer polynomial features from time to capture non-linear trend behaviour  
poly = PolynomialFeatures(degree=2, include_bias=False)  
X_poly = poly.fit_transform(X)
```

### 8.2 Model Re-evaluation

```
In [17]: # Fit and evaluate a polynomial regression model using the same time-series split  
X_train_p, X_test_p, y_train_p, y_test_p = train_test_split(X_poly, y, test_size=0.2)  
  
poly_model = LinearRegression()  
poly_model.fit(X_train_p, y_train_p)  
  
y_pred_p = poly_model.predict(X_test_p)  
  
rmse_p = np.sqrt(mean_squared_error(y_test_p, y_pred_p))  
r2_p = r2_score(y_test_p, y_pred_p)  
  
print(f"Polynomial RMSE: {rmse_p:.2f}")  
print(f"Polynomial R²: {r2_p:.4f}")
```

Polynomial RMSE: 36.31

Polynomial R²: 0.6747

Polynomial features were generated from the time variable to enable the model to capture non-linear trend behaviours.

## **9.0 Evaluation and Discussion**

### **9.1 Model Performance Evaluation**

The performance of the linear regression model was evaluated using RMSE (Root Mean Squared Error), MAE (Mean Absolute Error), and  $R^2$ . I selected RMSE to be the main evaluation metric because it penalises larger prediction errors which is useful for financial analysis where large deviations can have big impacts to the results. The linear model returned stable RMSE values across cross-validation folds (mean RMSE  $\approx 43.8$ ), meaning there is a consistent performance and robustness.

### **9.2 Strengths and Limitations**

The main strength of linear regression model is that its easy to interpret. The relationship between time and portfolio value is very clear, so we understand long-term growth trends easily. Cross-validation results further indicate that the model generalises well and is not too sensitive to the chosen train-test split.

However, the model has limitations. Financial time-series data can show volatility and sudden changes during market stress caused by certain events. These effects are not fully captured by a simple linear model as shown by increased residuals during volatile periods. This is where additional considerations is required (Brownlee, 2020). Polynomial regression somewhat solves this problem, but it brings a risk of overfitting and reduced transparency.

### **9.3 Contribution to the Domain**

This project shows that linear regression is useful for a effective baseline model for analysing long-term trends in diversified equity portfolios. By aggregating multiple assets into a single portfolio, volatility is reduced and trend behaviour becomes more stable, improving model suitability.

### **9.4 Transferability**

The methodology I used in this project can be transferred to other domain-specific areas that also has time-dependant data with some trends. The same method can be used to other financial portfolios, market indices, or other economic studies. Beyond the field of finance, this way of data pre-processing, statistical analysis, visualisation, regression modelling, and validation can be used in fields such as sustainability analysis, demand forecasting, and population growth modelling. However, for research that needs short-term prediction or capturing abrupt structural changes, more complex models may be required.

## **10.0 Originality and Extension**

This project goes beyond basic linear regression because I applied it to a real-world situation where I combined different financial datasets and evaluated model performance at the portfolio level rather than on individual assets alone. The inclusion of cross-validation and polynomial feature engineering further demonstrates a critical assessment of model robustness and accuracy, going beyond a minimal implementation.

## 11.0 Conclusion

This project studied the use of linear regression on long-term trends in a diversified portfolio. Through data pre-processing and analysis, we learn that linear regression is an effective and interpretable baseline model to capture long-term portfolio growth trends. While more complex models can improve accuracy, linear regression is still valuable for its simplicity, robustness and transferability to other time-series data.

## 12.0 References

Scikit-learn (2024) Linear Regression. Available at: [https://scikit-learn.org/stable/modules/generated/sklearn.linear\\_model.LinearRegression.html#](https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LinearRegression.html#) (Accessed: December 2025).

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