

Assignment No 3

1) Find the sequence that minimize Elapsed time required to complete the following tasks on two machine?

Task I II III IV V VI VII VIII IX

Machine A

4 10 8 18 12 16 14 10 8

Machine B 12 16 14 8 6 18 6 16 22

→ Step ①

Tasks	Machine A	Machine B
I	4	12
II	10	16
III	8	14
IV	18	8
V	12	6
VI	16	18
VII	14	6
VIII	10	16
IX	8	12

- Select the least processing time occur in machine A & machine column
- If the least processing time is A₂ then select 2th job first
- If B₅ then select 5th job first
- Here, least processing time is 4 which is a machine A

∴ Keep Job I to LHS and T₁ least processing time or machine 3 then keep that job on RHS

A I III ~~IX~~ II VIII VII IV VII V B

Job	machine A		machine B	
	intime	outtime	Intime	outtime.
I	0	4	4	16
II	4	12	16	30
IX	12	20	30	52
II	20	30	52	68
VIII	30	40	68	84
VII	40	56	84	102
IV	56	74	102	110
VII	74	88	110	116
V	88	100	116	122.

Total elapsed time = 122 hr

Total idle time = 4 hr

Idle time for A = 22 hr

Q2 A book binder has one printing press, one binding machine & manuscripts of seven different books. The time required for performing printing and binding operation for different books are given below:

Books	1	2	3	4	5	6	7
Printing time (hr)	20	90	80	20	120	15	65
Binding time (hr)	25	60	75	30	90	35	50

→ Step ①

Books	printing time (hr)	Binding time (hr)
1	20	25
2	90	60
3	80	75
4	20	30
5	120	90
6	15	35
7	65	50

- Select the least processing time occur in printing time & Binding time column
- In the least processing time for then select rth job first
- If the B then select sth job first.
- Here least processing time is 15 which printing time
- ∴ Keep job 6 to left side and its least processing time is binding time then keep that job at Rth.

A ~~6~~ 1 4 5 3 2 7 B

Books	Printing time (hr)		Binding time (hr)	
	In time	out time	In time	out time
6	0	15	15	50
1	15	35	50	75
4	35	55	75	105
5	55	175	175	265
3	175	255	265	340
2	255	345	345	405
7	345	410	410	460

Total elapsed time = 460 hr

Idle time 95 hr

Idle time for A = 50 hr.

Q3 Find the sequence that minimizes the total elapsed time required to complete the following work.

Task	1	2	3	4	5
Machine A	5	7	6	9	5
Machine B	2	1	4	5	3
Machine C	3	7	5	6	7

→ Step ①

Tasks	Machine		
	A	B	C
1	5	2	3
2	7	1	7
3	6	1	7
4	9	5	6
5	5	3	7

minimum time for A = 3

maximum time for B = 5

minimum time for C = 3

① minimum time \geq maximum time
for A for B.

Condition ① is not satisfy then convert the given problem into two m/c problem

1. $G = A + B$

2. $H = B + C$

Task machine

	G	H
1	7	5
2	8	8
3	10	9
4	14	11
5	8	10

G 2 5 4 3 1 H

Task	A		B		C	
	Intime	outime	intime	outime	Intime	outime.
2	0	7	7 8	8	8	15
5	7	12	12	15	15	22
4	12	21	21	26	26	32
3	21	27	27	31	32	37
1	27	32	32	34	37	40.

Total elapsed time = 40 hr

Total Idle time = 12 hr.

Q 4) Determine the optimal ~~opt~~ sequence of performing 5 jobs y machine that minimizes total elapsed time. The machine or each job is required in the order ABCD and processing timing in hrs are show follows.

Job	m_1	m_2	m_3	m_4
J_1	24	9	12	21
J_2	27	6	15	15
J_3	18	12	15	24
J_4	36	15	3	27
J_5	21	3	6	9

Find ① Total elapsed time ② idle time

→ Steps ①

$$\min(m_1) = 18$$

$$\max(m_2, m_3) = (15, 15) = 15$$

$$\min(m_4) = 9$$

here

$$\textcircled{a} \min(m_1) \geq \max(m_2, m_3)$$

The Condition (a) is satisfy now & check the Constant for each job

$$\text{for } J_1 \quad m_2, m_3 = a + 12 = 21$$

$$\text{for } J_2 \quad m_2 + m_3 = 6 + 15 = 21$$

$$\text{for } J_3 \quad m_2 + m_3 = 12 + 15 = 27$$

$$\text{for } J_4 \quad m_2 + m_3 = 15 + 3 = 18.$$

here: $m_2 + m_3 \neq C$

Step ② :- we define two machine G & H such that

$$G = m_1 + m_2 + m_3$$

$$H = m_2 + m_3 + m_4$$

Job	G	H
J1	45	42
J2	48	36
J3	45	51
J4	54	45
J5	30	18

Optimal Sequence is

G · J1 J2 J3 J4 J5 H

Job	M1		M2		M3		M4	
	in	out	in	out	in	out	in	out
J1	0	24	24	33	33	45	45	66
J2	24	42	42	54	54	69	69	93
J3	42	78	78	93	93	96	96	123
J4	78	105	105	111	111	126	126	141
J5	105	126	126	129	129	135	141	150

Total elapsed time = 150 hr

Idle time for $m_1 = 24$ hr

Idle time for $m_2 = 24 + 9 + 24 + 12 + 15 + 21 = 105$ hr.

Idle time for $m_3 = 33 + 9 + 24 + 15 + 3 + 15 = 99$ hr.

Idle time for $m_4 = 45 + 3 + 3 + 3 + 0 = 54$ hr.

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