

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT BGE	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics (SH551)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) If $u = (x-1)^3 - 3xy^2 + 3y^2$, determine V so that $u + iv$ is an analytic function of $x+iy$. [5]
 b) Define an analytic function. Express Cauchy Riemann equations $u_x = v_y$ and $u_y = -v_x$ in polar form. [5]
2. a) Find the bilinear transformation which maps points $z_1 = 1, z_2 = i, z_3 = -1$ into the points $w_1 = i, w_2 = -1, w_3 = -i$ respectively. [5]
 b) Evaluate $\int_0^{1+i} (x^2 + iy) dz$ along the path $y = x^2$ [5]
3. a) Express $f(z) = \frac{1}{(z^2 - 3z + 2)}$ as Laurent's series in the region $1 < |z| < 2$. [5]
 b) Evaluate $\int_0^{2\pi} \frac{1}{5 - 4 \sin \theta} d\theta$ by contour integration method in complex plane. [5]
4. a) Find z-transform of: [5]
 i) te^{-at}
 ii) $\sin at$
 b) State and prove final value theorem for z- transform. [5]
5. a) Find the inverse z-transform of $\frac{2z^2 - 5z}{(z-2)(z-3)}$ by using partial fraction method. [5]
 b) Solve difference equation $x(k+2) - 3x(k+1) + 2x(k) = 4^k$ for $x(0) = 0$ and $x(1) = 1$. [5]
6. Derive one dimensional wave equation and obtain its solution. [10]
7. Solve one dimensional heat equation: [10]

$$\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2} \text{ under the conditions:}$$

- i) u is not infinite as $t \rightarrow \infty$
 - ii) $\frac{\partial u}{\partial x} = 0$ for $x = 0$ and $x = l$
 - iii) $u(x, 0) = l - x^2$ for $t = 0$; between $x = 0$ and $x = l$
8. a) Find Fourier integral representation of $f(x) = e^{-x}, x > 0$ and hence evaluate

$$\int_0^\infty \frac{\cos(sx)}{s^2 + 1} ds \quad [5]$$

- b) Find the Fourier cosine transform of $f(x) = e^{-|x|}$ and hence, by Parseval's identity,

$$\text{shown that } \int_0^\infty \frac{1}{(1+x^2)^2} dx = \frac{\pi}{4} \quad [5]$$

Exam.	Regular / Back		
Level	BE	Full Marks	80
Programme	BEL, BEX, RCT, BGE	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics (SH551)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ All questions carry equal marks.
- ✓ Assume suitable data if necessary.

1. Determine the analytic function $f(z) = u + iv$ if $u = \log \sqrt{x^2 + y^2}$.
2. State and prove Cauchy's integral formula.
3. Find the Taylor's series of $f(z) = \frac{1}{1-z}$ about $z = 3i$.
4. Evaluate the integral: $\oint_C \frac{z^2 dz}{(z+1)(z+3)}$ where $C: |z| = 4$, using residue theorem.
5. Define conformal mapping, show that $w = \frac{az+b}{cz+d}$ is invariant to

$$\left(\frac{w-w_1}{w-w_3} \right) \times \left(\frac{w_2-w_3}{w_2-w_1} \right) = \left(\frac{z-z_1}{z-z_3} \right) \times \left(\frac{z_2-z_3}{z_2-z_1} \right)$$
6. Using contour integration, evaluate real integral: $\int_{-\infty}^{+\infty} \frac{x^2 dx}{(x^2+a^2)(x^2+b^2)}$
7. Find the z-transform of $x(z) = \cosh t \sinh t$.
8. State and prove "final value theorem" for the z-transform.
9. Find the inverse z-transform of $x(z) = \frac{z}{z^2 + 7z + 10}$.
10. Using z-transform solve the difference equation:
 $x(K+2) + 6x(K+1) + 9x(K) = 2^K$; $x_0 = x_1 = 0$.
11. Derive one-dimensional heat equation.
12. Solve the wave equation for a tightly stretched string of length 'l' fixed at both ends if the initial deflection in $y(x, 0) = lx - x^2$ and the initial velocity is zero.
13. Solve $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ under the conditions $u(0, y) = u(l, y) = u(x, 0) = 0$, $u(x, a) = \sin\left(\frac{\pi x}{l}\right)$
14. Derive the wave equation (vibrating of a string).
15. Find the Fourier cosine transform of $f(x) = e^{-\alpha x}$ and hence show that $\int_0^{\infty} \frac{\cos py}{\gamma^2 + \beta^2} d\gamma = \frac{\pi}{2\beta} e^{-p\beta}$.
16. Find the Fourier integral representation of the function $f(x) = e^{-x}$, $x \geq 0$ with $f(-x) = f(x)$.
Hence evaluate $\int_0^{\infty} \frac{\cos(sx)}{s^2 + 1} ds$.

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT, BGE	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics (SI551)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) Determine the analytic function $f(z) = u + iv$ if $u = 3x^2y - y^3$. [5]
 b) Find the linear transformation which maps the points $z = 0, 1, \infty$ into the points $w = -3, -1, 1$ respectively. Find also fixed points of the transformation. [5]
2. a) State and prove Cauchy's integral formula. [5]
 b) Evaluate $\int_C \frac{e^{2z}}{(z-1)(z-2)} dz$ where C is the circle $|z| = 3$. [5]
3. a) Find the first four terms of the Taylor's series expansion of the complex function $f(z) = \frac{z+1}{(z-3)(z-4)}$ about the centre $z = 2$. [5]
 b) Evaluate $\int_C \frac{4-3z}{z(z-1)(z-2)} dz$ where C is the circle $|z| = \frac{3}{2}$. [5]

OR

Evaluate $\int_0^{2\pi} \frac{1}{\cos\theta + 2} d\theta$ by contour integration in the complex plane.

4. Derive one dimensional heat equation $u_t = c^2 u_{xx}$ and solve it completely. [10]
5. Find all possible solution of Laplace equation $u_{xx} + u_{yy} = 0$. Using this, hence solve $u_{xx} + u_{yy} = 0$, under the conditions $u(0, y) = 0$, $u(x, y) = 0$ when $y \rightarrow \infty$ and $u(x, 0) = \sin x$. [10]
6. a) Find the z-transform of $\sin K\theta$. Use it to find the $z[a^K \sin K\theta]$. [5]
 b) If $z[x(K)] = \frac{2z^2 + 3z + 12}{(z-1)^4}$, find the value of $x(2)$ and $x(3)$. [5]
7. a) Find the inverse z-transform of $x(z) = \frac{3z^3 + 2z}{(z-3)^2(z-2)}$ by using inversion integral method. [5]
 b) Using z-transform solve the difference equation $x(K+2) - 4x(K+1) + 4x(K) = 2^K$ given that $x(0) = 0$, $x(1) = 1$. [5]
8. a) Find the Fourier sine integral of the function $f(x) = e^{-Kx}$ and hence show that $\int_0^\infty \frac{\lambda \sin \lambda x}{\lambda^2 + \beta^2} d\lambda = \frac{\pi}{2} e^{-Kx}$, $x > 0$, $K > 0$ [5]
 b) Find the Fourier sine transform of e^{-x} , $x \geq 0$ and hence show that $\int_0^\infty \frac{x \sin mx}{x^2 + 1} dx = \frac{\pi}{2} e^{-m}$, $m > 0$. [5]

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BFI, BEX, BCT	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

Subject: - Instrumentation I (EE552)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) Discuss the analog and digital measurement system with the help of their respective block diagrams. [6]
- b) An ac bridge circuit is working at 1000 Hz. Arm AB has $0.2 \mu\text{F}$ pure capacitance, arm BC has 500Ω pure resistance, arm CD contains an unknown impedance and arm DA has 300Ω resistance in parallel with $0.1 \mu\text{F}$ capacitor. Find the constant of arm CD considering it as a series circuit. [10]
2. a) What is loading effect of a potentiometer? Show that the error will be maximum when the slider of the potentiometer is at midpoint of the potentiometer. [8]
- b) Determine the thermoelectric sensitivity and emf developed in a thermocouple made of copper and constantan for a temperature of 50°C between its junction. Given that thermo electric emf of copper and constantan against platinum are $7.4 \mu\text{V}/^\circ\text{C}$ and $-34.4 \mu\text{V}/^\circ\text{C}$ respectively. [4]
- c) Explain how the flow of fluid can be measured by using Hot Wire Anemometers. [4]
3. a) Prove that "Linear relationship between capacitance and separation distance between two plates can be achieved by using differential arrangement". [8]
- b) Describe the construction and working of linear variable differential transformer for the measurement of displacement. [8]
4. a) Show how can an R-2R ladder network be used to generate a binary weighted sequence of current. [6]
- b) Highlight the advantages of optical fiber transmission over conventional data transmission system. [4]
- c) What is an instrumentation amplifier? Derive the expression for its gain. [6]
5. a) Explain the constructional detail and operating principle of a single phase induction type energy meter. [8]
- b) A 3-bit DAC has a voltage range of (0 - 12) V. Calculate the
 - i) weight of LSB
 - ii) weight of MSB
 - iii) exact range of the converter
 - iv) percentage error

If now, the bit of the converter is increased to 6, show by how much amount the error is increased or decreased? Justify your answer.

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics (SH551)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Show that $u(x, y) = x^2 + 2xy - y^2$ is a harmonic function and determine $v(x, y)$ in such a way that $f(z) = u(x, y) + iv(x, y)$ is analytic. [5]
2. Define complex integral. State and prove Cauchy integral formula. [5]

OR

- Obtain bilinear transformation which maps $-i, 0, i$ to $-1, i, 1$. [5]
3. Evaluate $\int_C \frac{e^{2z}}{(z-1)(z-2)} dz$ where C is $|z| = 3$ using Cauchy's integral formula. [5]
4. Obtain the Laurent series which represents the function $f(z) = \frac{z^2 - 1}{(z+2)(z+3)}$ $2 < |z| < 3$. [5]
5. Find the Laurent series of $f(z) = \frac{1}{4+z^2}$ about the point $z = i$. [5]
6. State and prove Taylor series of a function $f(z)$. [5]
7. Derive one dimensional wave equation $u_{tt} = c^2 u_{xx}$ and solve it completely. [10]
8. Solve one dimensional heat equation $\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}$ under the boundary condition $\frac{\partial u}{\partial x} = 0$ when $x = 0$ and $x = L$ and initial condition $u(x, 0) = x$ for $0 < x < L$. [10]
9. Find Z transform of (a) te^{-at} and (b) $\sin at$. [5]
10. Find the inverse z-transform (a) $\frac{z-4}{(z-1)(z-2)^2}$ (b) $\frac{z}{z^2 - 3z + 2}$. [5]
11. Obtain the Z transform of $x(t) = (1 - e^{-at})$, $a > 0$ and hence evaluate $x(\infty)$ by using final value theorem. [5]
12. Solve using z-transform the difference equation $x(K+2) + 2x(K+1) + 3x(K) = 0$. [5]
13. Find the Fourier sine transform of $f(x) = e^{-x}$, $x \geq 0$ and hence evaluate $\int_0^\infty \frac{x \sin x}{(1+x^2)} dx$. [5]
14. State and prove convolution theorem of Fourier transform. [5]

Exam.	New Batch (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics (SH551)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define analytic function. Show that the function $f(z) = \frac{1}{z^4}$ is analytic except $z = 0$ [5]
2. Define complex integral. Evaluate $\int_C \log z \, dz; C: |z| = 1$ [5]

ORObtain a bilinear transformation which maps $-i, 0, i$ to $-1, i, 1$.

3. Evaluate $\int_0^{1+i} (x^2 + iy) \, dz$ along the path $y = x$. [5]
4. Find the Taylor series of $f(z) = \frac{1}{4+z^2}$ about the point $z = i$. [5]
5. Evaluate the integrals by residue theorem $\int_C \frac{1 - \cos z}{z^3} \, dz$ [5]
6. State Cauchy's Residue theorem and use it to evaluate $\int_C \frac{z^2}{3+4z+z^2} \, dz$ where C is $|z| = 2$ [5]

OREvaluate $\int_0^{2\pi} \frac{d\theta}{\cos \theta + 2}$ by contour integration in complex plane.

7. Derive the one dimensional wave equation. [10]
8. A rod of length L has its ends A and B maintained at 0° and 100° respectively until steady state prevails. If the changes are made by reducing the temperature of end B to 85° and increasing that of end A to 15° , then find the temperature distribution in the rod at a time t . [10]
9. Find the z -transform of (i) $e^{-at} \sin \omega t$ (ii) $\cos at$ [5]
10. Obtain inverse Z -transform of (i) $\frac{z+2}{(z-2)(z-3)}$, (ii) $\frac{z}{(z-2)(z-1)}$ [5]
11. If $x(k) = 0$ for $k < 0$ and $Z\{x(k)\} = X(z)$ for $k > 0$ then prove that $Z\{x(k-n)\} = z^{-n} X(z) - z^{-n} \sum_{k=0}^{n-1} x(k)z^{-k}$ where $n = 0, 1, 2, \dots$ [5]
12. Solve the difference equation $x(k+2) - 4x(k+1) + 4x(k) = 0$ with conditions, $x(0) = 0, x(1) = 1$ [5]
13. Find the cosine transform of $f(x) = e^{-mx}$ $m > 0$ show that $\int_0^\infty \frac{\cos px}{x^2 + B^2} = \frac{\pi}{2B} e^{-mB}$ [5]
14. Find the Fourier transform of $g(x) = \begin{cases} 1-x^2 & \text{if } -1 < x < 1; \\ 0, & \text{if otherwise.} \end{cases}$ [5]

and hence use it to evaluate $\int_0^\infty \left(\frac{x \cos x - \sin x}{x^3} \right) \cos(x/2) \, dx$

25 TRIBHUVAN UNIVERSITY
INSTITUTE OF ENGINEERING
Examination Control Division
2069 Bhadra

Exam.	Regular (2066 & Later Batch)		
Level	BE	Full Marks	30
Programme	BEL, BEX, BCT	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics (SH551)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ All questions carry equal marks.
- ✓ Assume suitable data if necessary.

1. Determine the analytic function $f(z) = u(x, y) + iv(x, y)$ if $u(x, y) = x^2 - y^2$.
2. Define complex integral. Evaluate: $\oint_C (z+1)dz$ where C is the square with vertices at $z = 0, z = 1, z = 1+i$ and $z = i$.

OR

Find linear fractional transformation mapping of: $-2 \mapsto \infty, 0 \mapsto \frac{1}{2}, 2 \mapsto \frac{3}{4}$.

3. a) State Cauchy's integral formula and evaluate the integral $\oint_C \frac{4-3z}{z(z-1)(z-2)} dz$, where C is circle $|z| = \frac{3}{2}$.

- b) Obtain the Laurent series which represents the function $f(z) = \frac{1}{(1+z^2)(z+2)}$ when $|z| < 2$.

4. a) Find the Taylor's series expansion of $f(z) = \frac{1}{z^2+4}$ about the point $z = i$.
- b) Evaluate $\oint_C \tan z \, dz$ where C is a circle $|z| = 2$ by Cauchy's residue theorem.

OR

Evaluate $\int_0^{2\pi} \frac{\cos 3\theta}{5-4\cos\theta} d\theta$ by contour integration in the complex plane.

5. Find the z-transforms of: (i) $\cos h(at) \sin(bt)$ (ii) $n.(n-1); n = k$
6. Find the inverse z-transforms of: (i) $\frac{Z}{Z^2-3Z+2}$ (ii) $\frac{Z}{(Z+1)^2(Z-1)}$
7. a) State and prove convolution theorem for z-transform.
- b) Solve by using z-transform the difference equation $x(k+2) + 2x(k+1) + 3x(k) = 0$ given that $x(0) = 0$ and $x(1) = 2$

8. Solve $\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial t}$ given that $u = 0$ as $t \rightarrow \infty$ as well as $u = 0$ at $x = 0$ and $x = l$.
9. Solve $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$, which satisfies the condition $u(0, y) = u(L, y) = u(x, 0) = 0$ and $u(x, a) = \sin\left(\frac{n\pi x}{L}\right)$.

OR

The diameter of a semi-circular plate of radius a is kept at 0°C and the temperature at the semi-circular boundary is u_0 . Find the steady state temperature in the plate.

10. Find the Fourier integral representation of the function $f(x) = e^{-x}$, $x \geq 0$ with $f(-x) = f(x)$.

Hence evaluate $\int_0^\infty \frac{\cos(sx)}{s^2 + 1} ds$.

11. Find the Fourier transform of:

$$f(x) = 1 - x^2, |x| < 1$$

$$= 0, |x| > 1 \text{ and hence evaluate}$$

$$\int_0^\infty \left(\frac{x \cos x - \sin x}{x^3} \right) \cos \frac{x}{2} dx.$$

Exam.	Regular		
Level	BE	Full Marks	80
Programme	DEL, DEX, BCT	Pass Marks	32
Year / Part	II / II	Time	3 hrs.

Subject: - Applied Mathematics

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ All questions carry equal marks.
- ✓ Assume suitable data if necessary.

1. a) State necessary conditions for a function $f(z)$ to be analytic. Show that the function $f(z) = \log z$ is analytic everywhere except at the origin.

b) Find the linear fractional transformation that maps the points $z_1 = -i$, $z_2 = 0$ and $z_3 = i$ into points $w_1 = -1$, $w_2 = i$, $w_3 = 1$ respectively.

2. a) State and prove Cauchy's integral formula.

b) Write the statement of Cauchy's integral formula. Use it to evaluate the integral

$$\oint_C \frac{e^z}{(z-1)(z-3)} dz \text{ where } C \text{ is the circle } |z| = 2.$$

3. a) Write the statement of Taylor's theorem. Find the Laurent series for the function

$$f(z) = \frac{1}{z^2 - 3z + 2} \text{ in the region } 1 < |z| < 2.$$

b) State Cauchy-residue theorem. Using it evaluate $\oint_C \frac{\sin z}{z^6} dz$ where $C: |z| = 1$.

OR

Evaluate $\int_0^{2\pi} \frac{d\theta}{2 + \cos \theta}$ by contour integration in the complex plane.

4. a) Show that the Z-transform of $\cos k\theta$ is $\frac{z(z - \cos \theta)}{z^2 - 2z \cos \theta + 1}$. Use this result to find Z-transform of $a^k \cos k\theta$.

b) Obtain the inverse Z-transform of $\frac{2z^3 + z}{(z-2)^2(z-1)}$, using partial fraction method.

5. a) Solve the difference equation $x(k+2) - x(k+1) + 0.25x(k) = u(k)$ where $x(0) = 1$ and $x(1) = 2$ and $u(k)$ is unit step function.

b) State and prove shifting theorem of z-transform.

6. Derive one-dimensional wave equation governing transverse vibration of string and solve it completely.

7. Solve the one dimensional heat equation $\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}$ under the conditions:

- a) u is not infinite as $t \rightarrow \infty$
- b) $\frac{\partial u}{\partial x} = 0$ for $x = 0$ and $x = l$ and
- c) $u(x, 0) = lx - x^2$ for $t = 0$ between $x = 0$ and $x = l$

OR

The diameter of a semi circular plate of radius a is kept at 0°C and temperature at the semi circular boundary is $T^\circ\text{C}$. Show that the steady temperature in the plate is given

$$\text{by } u(r, \theta) = \frac{4T}{\pi} \sum_{n=1}^{\infty} \frac{1}{2n-1} \left(\frac{r}{a}\right)^{2n-1} \sin(2n-1)\theta$$

8. a) Find the Fourier cosine integral representation of the function $f(x) = e^{-kx}$ ($x > 0, k > 0$) and hence show that

$$\int_0^{\infty} \frac{\cos \omega x}{k^2 + \omega^2} d\omega = \frac{\pi}{2k} e^{-kx} \quad (x > 0, k > 0)$$

- b) Obtain Fourier sine transform of e^{-x} , ($x > 0$) and hence evaluate $\int_0^{\infty} \frac{x^2}{(1+x^2)^2} dx$.

22. TRIBHUVAN UNIVERSITY
INSTITUTE OF ENGINEERING
Examination Control Division
2067 Mangsir

Exam. Level	Regular / Back	
	BE	Full Marks : 80
Programme	BEL, BEX, BCT	Pass Marks : 32
Year / Part	II / II	Time : 3 hrs.

Subject: - Applied Mathematics

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt any Six questions.
- ✓ All questions carry equal marks.
- ✓ Assume suitable data if necessary.

1. a) State Cauchy - Riemann equations in polar form. Show that $f(z) = \sin z$ is analytic in the entire z -plane.
b) State and prove Cauchy's integral formula.
2. a) State Laurent series. Find Taylor series of $f(z) = \cos z$ about $z = \frac{\pi}{4}$.
b) Define pole of order m . Find the residue of $f(z) = \frac{z^2 e^z}{(z-2)^3}$ at its pole.
3. a) Determine the Z-transform of
i) $t^2 e^{-at}$
ii) $e^{-at} \cos \omega t$
b) State initial value theorem for Z-transform. If Z-transform of a function is given by
$$X(z) = \frac{(1 - e^{-1})z^{-1}}{(1 - z^{-1})(1 - e^{-1}z^{-1})}$$
, determine $x(0)$, $x(1)$ and $x(2)$.
4. a) Find inverse Z- transform of
i) $x(z) = \frac{z+2}{z^2 - 5z + 6}$ (by partial fraction method)
ii) $x(z) = \frac{z+2}{z^2 + 7z + 10}$ (by inversion integral method)
b) Solve the difference equation: $x(k+2) - 4x(k+1) + 4x(k) = 0$ Where $x(0) = 1$ and $x(1) = 0$.
5. Derive one dimensional wave equation and obtain its solution.
6. Solve: $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ subject to the conditions, $u(0, y) = u(\ell, y) = u(x, 0) = 0$, and
$$u(x, a) = \sin\left(\frac{n\pi x}{\ell}\right)$$
7. Define convolution for Fourier transform. Verify convolution theorem for
 $f(x) = g(x) = e^{-x^2}$.
8. Maximize: $z = x_1 + 3x_2$ subject to
 $x_1 + 2x_2 \leq 10$, $x_1 \leq 5$, and $x_2 \leq 4$; $x_1, x_2 \geq 0$
by using simplex method.
