

For the general divide-and-conquer recurrence relation $T(n)$, the *Master Theorem* makes it straightforward to determine divide-and-conquer (and even some decrease-and-conquer) algorithms' efficiency classes. Bear in mind what it does **not** do. It does **NOT** give you an *explicit solution* (a function in terms of n only) to the $T(n)$ recurrence relation.

The theorem states that for $T(n) = aT(n/b) + f(n)$, where $f(n)$ computes the cost of dividing the problem into smaller ones and of combining their solutions:

If

$T(1)$	=	c ,
a	>	0 ,
b	>	1 ,
c	>	0 ,
n	=	$b^k, k = 0, 1, 2, \dots$ (n is a power of b),
d	\geq	0 , and
$f(n)$	\in	$\Theta(n^d)$,

then

$$a < b^d \rightarrow T(n) \in \Theta(n^d);$$

$$a = b^d \rightarrow T(n) \in \Theta(n^d \log n);$$

$$a > b^d \rightarrow T(n) \in \Theta(n^{\log_b a});$$

where the logs are \log_b , log to the base b .