CE 311K: Control flow - Branching and Iterations

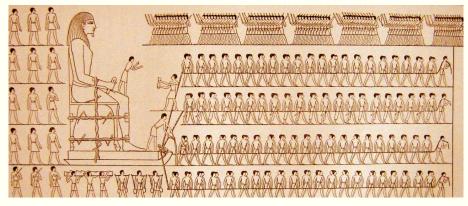
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Fall 2020

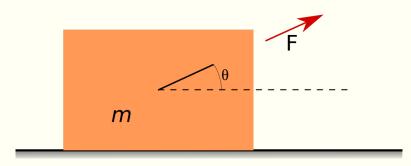
- Numerical solution of a sliding block
- 2 Bisection method

What is the optimal angle to pull the statue?



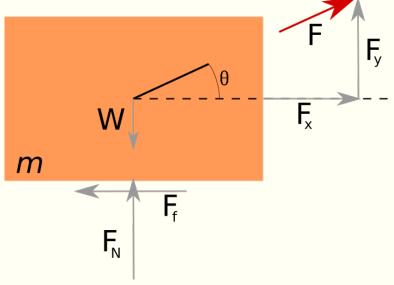
A wall painting from the tomb of Djehutihotep (credit: martinhumanities.com)

Numerical solution of a sliding block: Approximation



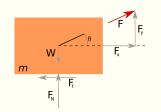
What is the optimal angle to pull the block applying the least amount of force?

Numerical solution of a sliding block: Forces



Numerical solution of a sliding block: Forces

$$F_x = F \cos \theta$$
 & $F_y = F \sin \theta$
 $F_f = \mu \cdot F_N = \mu \cdot W - \mu F_y = \mu mg - \mu F \sin \theta$
Vertical forces $\sum F_{vert} \uparrow : F_y + F_N - W = 0$
 $F_N = mg - F \sin \theta$
Horizontal forces $\sum F_{hor} \rightarrow : F_x - F_f = 0$
 $F \cos \theta - \mu mg + \mu F \sin \theta = 0$



$$F = \frac{\mu \cdot mg}{(\cos \theta + \mu \sin \theta)}$$

Numerical solution of a sliding block: Compute force

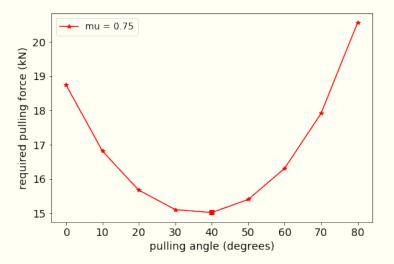
• Given W = 25kN(2500 kg), $\theta = 45^{\circ}$ and $\mu = 0.75 (35^{\circ})$:

$$F = \frac{0.75 \times 25}{\cos(45) + 0.75\sin(45)} = 15.15 \,\text{kN}.$$

• Given $W=25kN(2500\,\mathrm{kg})$ and $\mu=0.75$, what's the optimum θ ?

QNumerical solution of a sliding block: Optimal theta?

Given $W = 25 \, \text{kN}(2500 \, \text{kg})$ and $\mu = 0.75$, what's the optimum θ ?



Lists

- A list is a sequence of data. (mutable)
- An 'array' in most other languages is a similar concept, but Python lists are more general than most arrays as they can hold a mixture of types.
- A list is constructed using square brackets:

```
>>> a = [0, 10, 20, 30, 40, 50, 60, 70, 80]
>>> print(a)
[0, 10, 20, 30, 40, 50, 60, 70, 80]
>>> type(a)
<class 'list'>
>>> len(a)
10
>>> a.append(90)
>>> print(a)
[0, 10, 20, 30, 40, 50, 60, 70, 80, 90]
```

Iterating through a list: for loops

Looping over each item in a list (or more generally a sequence) is called 'iterating'. We iterate over the members of the lab group using the syntax:

```
for each item in list do
    print(item)
```

```
for item in list:
    print(item)
```

▲ Indentation matters in python!

Looping over each item in a list (or more generally a sequence) is called iterating. We iterate over the members of the lab group using the syntax: for each item in list do print(item)

for item in list: print(item)

• Indentation matters in python!

Variables defined inside a for loop is not accessible outside.

np.arange()

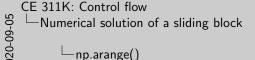
The np.arange() returns a sequence of numbers:

```
range(stop)
```

stop: Number of integers (whole numbers) to generate, starting from zero. eg. np.arange(3) yields a sequence of [0, 1, 2].

```
np.arange([start], stop[, step])
```

- start: Starting number of the sequence.
- stop: Generate numbers up to, but not including this number.
- *step*: Difference between each number in the sequence.



np.arange()

The np.arange() returns a sequence of numbers

range (atop)

stop: Number of integers (whole numbers) to generate, starting from zero
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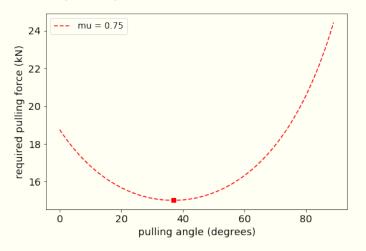
 start: Starting number of the sequence.
- stop: Generate numbers up to, but not including this number.
- step: Difference between each number in the sequence.

Note that:

- All parameters can be positive or negative.
- range() (and Python in general) is 0-index based, meaning list indexes start at 0, not 1

Numerical solution of a sliding block: Optimal theta?

Given $W = 25 \, \text{kN}(2500 \, \text{kg})$ and $\mu = 0.75$, what's the optimum θ ?



Identifying optimum requires conditional statements

Comparison on int, float and strings

i and j are variable names and comparisons below evaluate to a Boolean

- i > j
- i >= j
- i < j</pre>
- i <=j
- i == j: equality test, True if i is the same as j
- i != j: in equality test, True if i is not the same as j

Logic operators on bools

a and b are variable names with Boolean values

- not a: True if a is False
 False if a is True
- a and b: True if both are True.
- a or b: True if either or both are True.

В	${\tt A}$ and ${\tt B}$	A or B
True	True	True
False	False	True
True	False	True
False	False	False
	True False True	True True False False True False

Designing a smart window: if condition



- An electric window opener, attached to a rain sensor and a temperature gauge, might be controlled by the following program:
- If raining: close window
- If too hot (80F): open window
- If too cold (66F): close window
- Otherwise: do nothing and leave window as it is

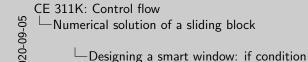
Designing a smart window: if condition

```
# If raining, close the window
if raining:
        close_window()
# If the temperature is over 80 F, open window
elif temperature > 80: # else if
        open_window()
# If the temperature is below 66 F, close window
elif temperature < 66:
        close_window()
```

continue

else:

Otherwise, do nothing and leave window as it is



If the temperature is over 80 F. open window open window() # If the temperature is below 66 F, close window elif temperature < 66: close window()

If raining, close the window if raining:

close window()

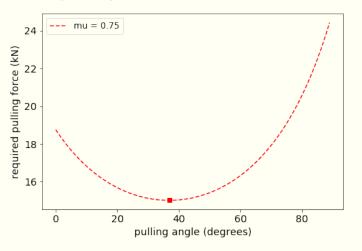
elif temperature > 80: # else if

Otherwise, do nothing and leave window as it is continue

<condition> has a value True or False evaluate expressions in that block if <condition> is True

Numerical solution of a sliding block: Optimal theta?

Given $W = 25 \, \text{kN}(2500 \, \text{kg})$ and $\mu = 0.75$, what's the optimum θ ?



Identify optimum with an if conditional statement

- Numerical solution of a sliding block
- 2 Bisection method

Calculate the optimum angle to pull for a given force

• Given $F=17.5\,\mathrm{kN}(1750\,\mathrm{kg}),~W=25\,\mathrm{kN}$ and $\mu=0.75,$ what's θ ?

$$Try \ \theta = 60^{\circ}: \ F = \frac{0.75 \times 25}{\cos(60) + 0.75\sin(60)} = 16.31 \text{ kN}.$$

$$Try \ \theta = 70^{\circ}: \ F = \frac{0.75 \times 25}{\cos(70) + 0.75\sin(70)} = 17.91 \text{ kN}.$$

$$Try \ \theta = 65^{\circ}: \ F = \frac{0.75 \times 25}{\cos(65) + 0.75\sin(65)} = 17.00 \text{ kN}.$$

$$Try \ \theta = 67.5^{\circ}: \ F = \frac{0.75 \times 25}{\cos(67.5) + 0.75\sin(67.5)} = 17.43 \text{ kN}.$$

This is bisection method!

What are the characteristics of a numerical solution?

- A numerical recipe is a sequence of simple steps
- Flow of control as each step is executed.
- Yields an approximate numerical answer (a finite number) for the problem
- These solutions can be very accurate
- Most answers are determined in an iterative approach (numerical method: mathematical / computer-aided technique) until a desired minimum/acceptable accuracy is obtained
- Typically, a finite set of iterations (steps) are used in the numerical method to obtain a solution. A means of determining when to stop.

Numerical solution of a sliding block: Friction angles

