## CE 311K: Control flow - Branching and Iterations

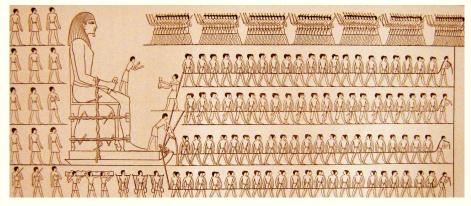
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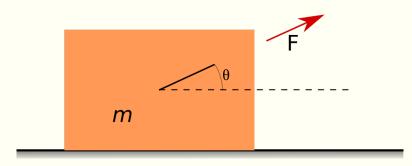
- Numerical solution of a sliding block
- 2 Bisection method

## What is the optimal angle to pull the statue?



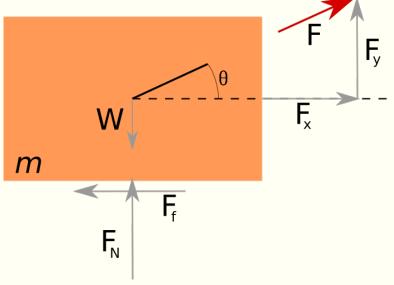
A wall painting from the tomb of Djehutihotep (credit: martinhumanities.com)

#### Numerical solution of a sliding block: Approximation



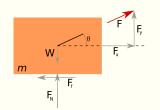
What is the optimal angle to pull the block applying the least amount of force?

### Numerical solution of a sliding block: Forces



#### Numerical solution of a sliding block: Forces

$$F_x = F \cos \theta$$
 &  $F_y = F \sin \theta$   
 $F_f = \mu \cdot F_N = \mu \cdot W - \mu F_y = \mu mg - \mu F \sin \theta$   
Vertical forces  $\sum F_{vert} \uparrow : F_y + F_N - W = 0$   
 $F_N = mg - F \sin \theta$   
Horizontal forces  $\sum F_{hor} \rightarrow : F_x - F_f = 0$   
 $F \cos \theta - \mu mg + \mu F \sin \theta = 0$ 



$$F = \frac{\mu \cdot mg}{(\cos \theta + \mu \sin \theta)}$$

## Numerical solution of a sliding block: Compute force

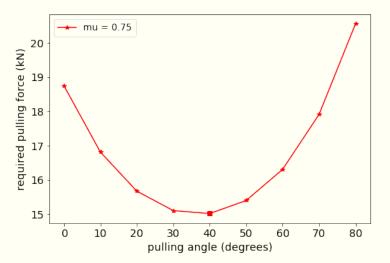
• Given W = 25kN(2500 kg),  $\theta = 45^{\circ}$  and  $\mu = 0.75 (35^{\circ})$ :

$$F = \frac{0.75 \times 25}{\cos(45) + 0.75\sin(45)} = 15.15 \,\text{kN}.$$

• Given  $W=25kN(2500\,\mathrm{kg})$  and  $\mu=0.75$ , what's the optimum  $\theta$ ?

### QNumerical solution of a sliding block: Optimal theta?

Given  $W = 25 \, \text{kN}(2500 \, \text{kg})$  and  $\mu = 0.75$ , what's the optimum  $\theta$ ?



#### Lists

- A list is a sequence of data. (mutable)
- An 'array' in most other languages is a similar concept, but Python lists are more general than most arrays as they can hold a mixture of types.
- A list is constructed using square brackets:

```
>>> a = [0, 10, 20, 30, 40, 50, 60, 70, 80]
>>> print(a)
[0, 10, 20, 30, 40, 50, 60, 70, 80]
>>> type(a)
<class 'list'>
>>> len(a)
10
>>> a.append(90)
>>> print(a)
[0, 10, 20, 30, 40, 50, 60, 70, 80, 90]
```

#### Iterating through a list: for loops

Looping over each item in a list (or more generally a sequence) is called 'iterating'. We iterate over the members of the lab group using the syntax:

```
for each item in list do
    print(item)
```

```
for item in list:
    print(item)
```

▲ Indentation matters in python!

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for item in list: print(item) • Indentation matters in python!

Variables defined inside a for loop is not accessible outside.

### np.arange()

We need a new library called 'numpy', we are going to import the new library. import numpy as np The np.arange() returns a sequence of numbers:

```
range(stop)
```

stop: Number of integers (whole numbers) to generate, starting from zero. eg. np.arange(3) yields a sequence of [0, 1, 2].

```
np.arange([start], stop[, step])
```

- *start*: Starting number of the sequence.
- stop: Generate numbers up to, but not including this number.
- *step*: Difference between each number in the sequence.

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Numerical solution of a sliding block

-np.arange()

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range(stop)

stop: Number of integers (whole numbers) to generate, starting from zero. eg. np.arange(3) yields a sequence of [0, 1, 2].

np.arange([start], stop[, step])
 start: Starting number of the sequence.

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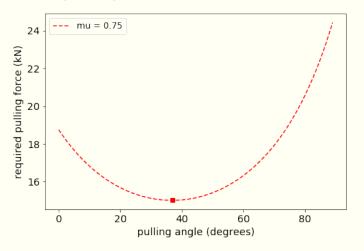
step: Difference between each number in the sequence.

#### Note that:

- All parameters can be positive or negative.
- range() (and Python in general) is 0-index based, meaning list indexes start at 0, not 1

## Numerical solution of a sliding block: Optimal theta?

Given  $W = 25 \, \text{kN}(2500 \, \text{kg})$  and  $\mu = 0.75$ , what's the optimum  $\theta$ ?



Identifying optimum requires conditional statements

### Comparison on int, float and strings

i and j are variable names and comparisons below evaluate to a Boolean

- i > j
- i >= j
- i < j
- i <=j
- i == j: equality test, True if i is the same as j
- i != j: in equality test, True if i is not the same as j

#### Logic operators on bools

a and b are variable names with Boolean values

- not a: True if a is False
   False if a is True
- a and b: True if both are True.
- a or b: True if either or both are True.

В	${\tt A}$ and ${\tt B}$	A or B
True	True	True
False	False	True
True	False	True
False	False	False
	True False True	True True False False True False

#### Designing a smart window: if condition



- An electric window opener, attached to a rain sensor and a temperature gauge, might be controlled by the following program:
- If raining: close window
- If too hot (80F): open window
- If too cold (66F): close window
- Otherwise: do nothing and leave window as it is

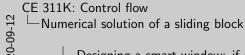
# Designing a smart window: if condition

```
# If raining, close the window
if raining:
        close_window()
# If the temperature is over 80 F, open window
elif temperature > 80: # else if
        open_window()
# If the temperature is below 66 F, close window
elif temperature < 66:
        close_window()
```

continue

else:

# Otherwise, do nothing and leave window as it is



 $-\mathsf{Designing}$  a smart window: if condition

# If the temperature in over 80 F, open window elif temperature > 80: # slee if open\_window() # If the temperature is below 66 F, close window elif temperature < 66: Close window()

# If raining, close the window if raining:

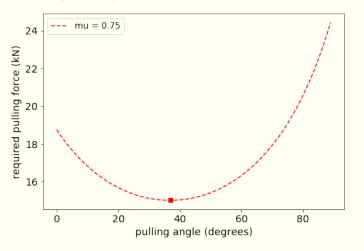
close window()

# Otherwise, do nothing and leave window as it is else:
continue

<condition> has a value True or False
evaluate expressions in that block if <condition> is True

## Numerical solution of a sliding block: Optimal theta?

Given  $W = 25 \, \text{kN}(2500 \, \text{kg})$  and  $\mu = 0.75$ , what's the optimum  $\theta$ ?



Identify optimum with an if conditional statement

- Numerical solution of a sliding block
- 2 Bisection method

### Calculate the optimum angle to pull for a given force

• Given  $F=17.5\,\mathrm{kN}(1750\,\mathrm{kg}),~W=25\,\mathrm{kN}$  and  $\mu=0.75,$  what's  $\theta$ ?

$$Try \ \theta = 60^{\circ}: \ F = \frac{0.75 \times 25}{\cos(60) + 0.75\sin(60)} = 16.31 \text{ kN}.$$

$$Try \ \theta = 70^{\circ}: \ F = \frac{0.75 \times 25}{\cos(70) + 0.75\sin(70)} = 17.91 \text{ kN}.$$

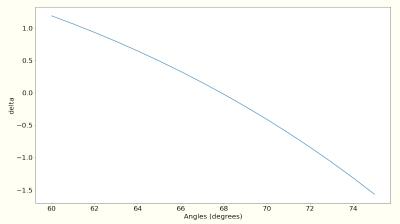
$$Try \ \theta = 65^{\circ}: \ F = \frac{0.75 \times 25}{\cos(65) + 0.75\sin(65)} = 17.00 \text{ kN}.$$

$$Try \ \theta = 67.5^{\circ}: \ F = \frac{0.75 \times 25}{\cos(67.5) + 0.75\sin(67.5)} = 17.43 \text{ kN}.$$

This is bisection method!

### Calculate the optimum angle to pull for a given force

• Given  $F=17.5\,\mathrm{kN}(1750\,\mathrm{kg}),~W=25\,\mathrm{kN}$  and  $\mu=0.75,$  what's  $\theta$ ?



#### What are the characteristics of a numerical solution?

- A numerical recipe is a sequence of simple steps
- Flow of control as each step is executed.
- Yields an approximate numerical answer (a finite number) for the problem
- These solutions can be very accurate
- Most answers are determined in an iterative approach (numerical method: mathematical / computer-aided technique) until a desired minimum/acceptable accuracy is obtained
- Typically, a finite set of iterations (steps) are used in the numerical method to obtain a solution. A means of determining when to stop.

#### Numerical solution of a sliding block: Friction angles

