


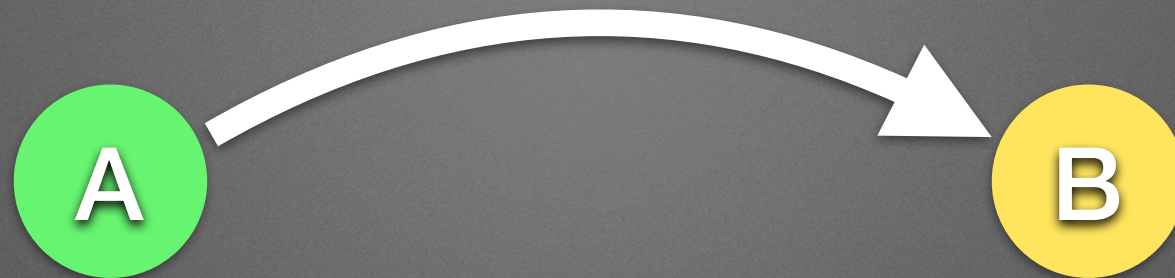


Tennis Players Network

Chia-Hung Yang

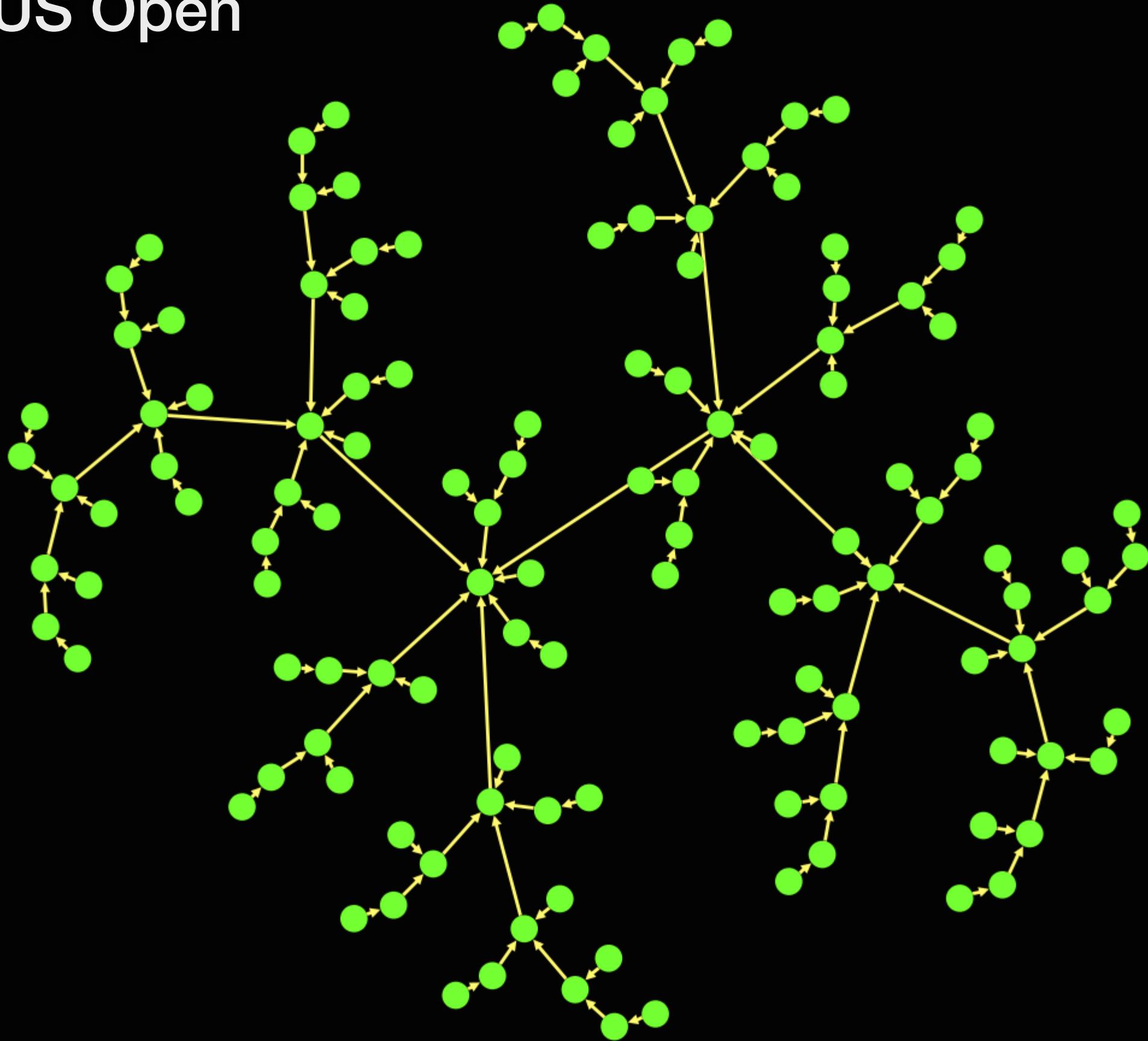
 Ivo Karlovic	H 2 H	Ivo Karlovic	H 2 H	Ivo Karlovic	H 2 H	
 Federico Delbonis		76 ⁶ 67 ⁶ 76 ⁵		76 ⁹ 76 ⁵		
 Janko Tipsarevic	H 2 H	Janko Tipsarevic	H 2 H		H 2 H	Gael Monfils
 Taro Daniel		62 64				76 ⁶ 76 ⁶
 Gilles Simon	H 2 H	Gilles Simon	H 2 H	Gael Monfils		
 Philipp Kohlschreiber		75 46 60		61 64		
 Yuichi Sugita	H 2 H	Gael Monfils	H 2 H			
 Gael Monfils		63 61				

of sets B won over A

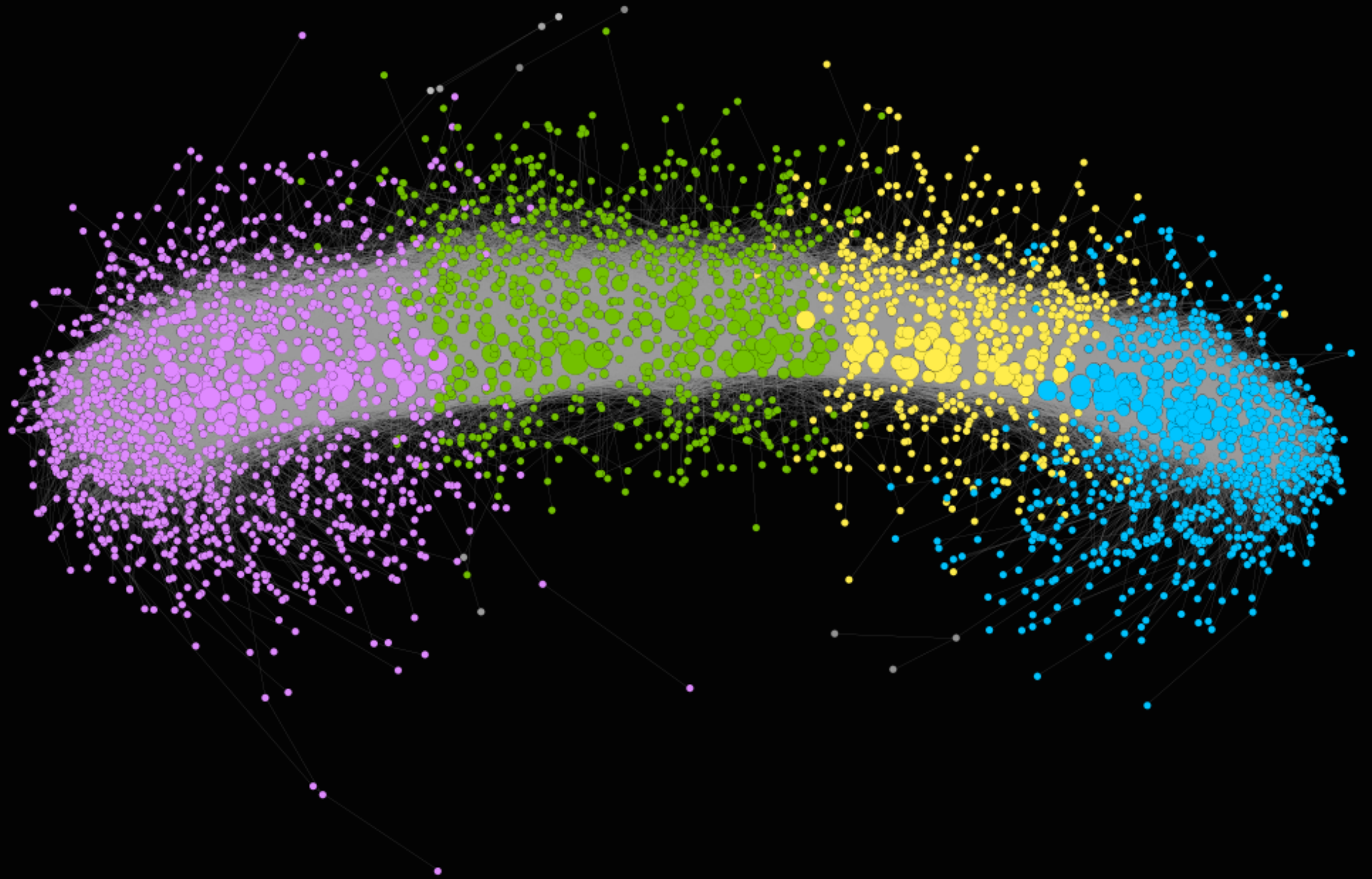


- Directly related to players' performance
- Weighted and directed
- Collect data from 1976 to 2015
- $N = 3230$; $L = 106774$

2015 US Open



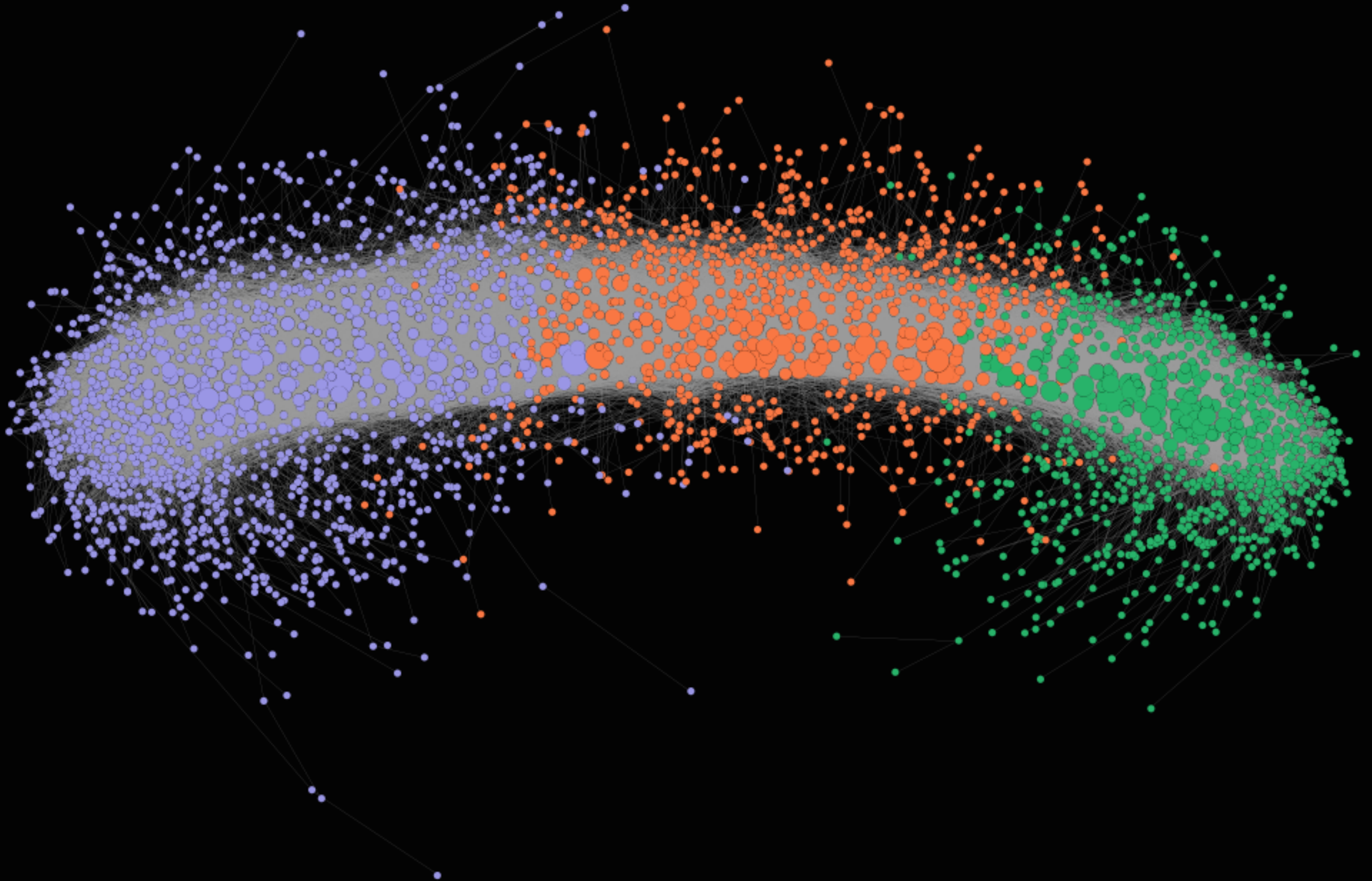
1976 ~ 2015



1976~1989

1990~2002

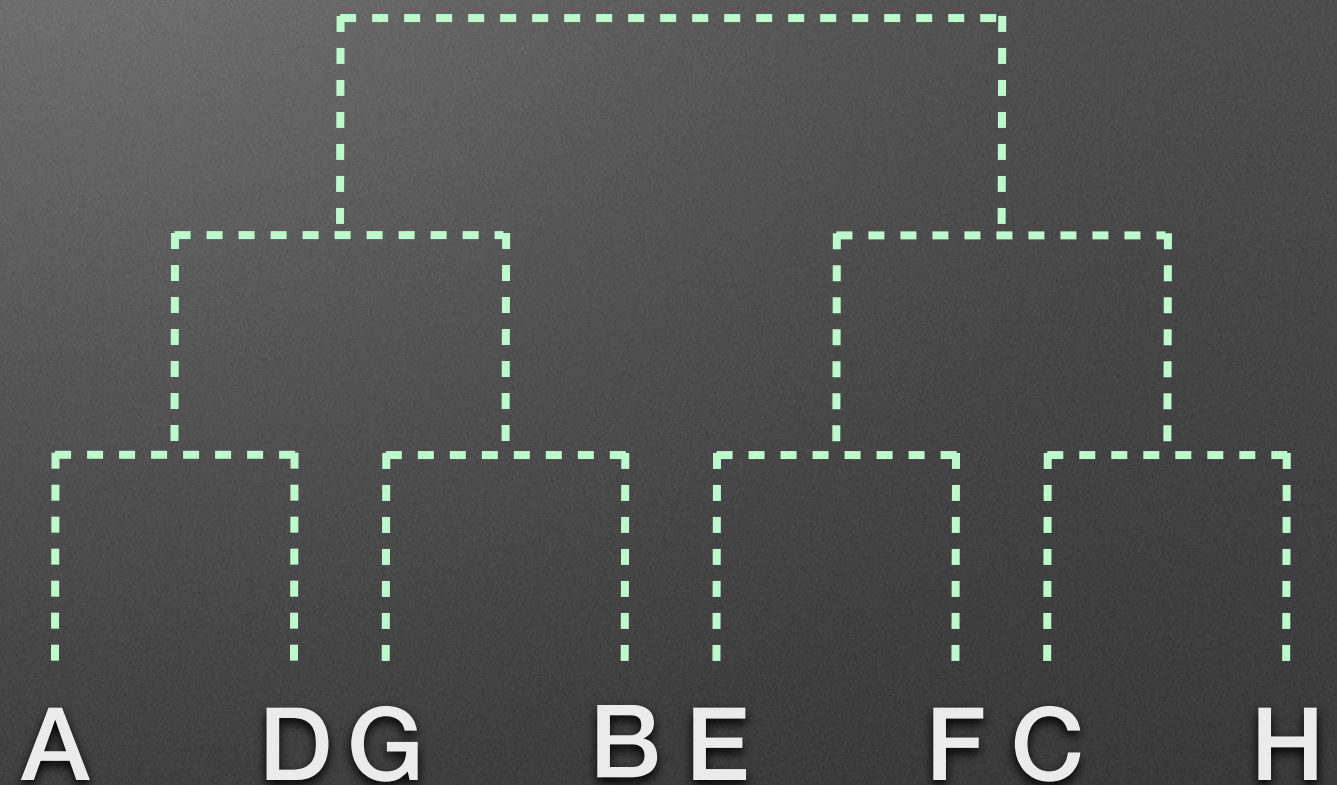
2003~2015



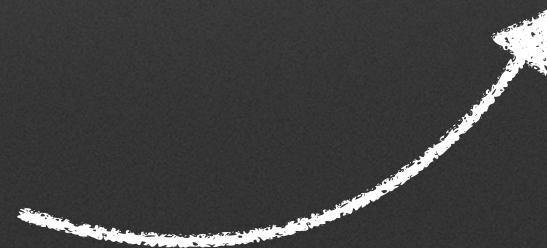
Null Model

(players are indistinguishable)

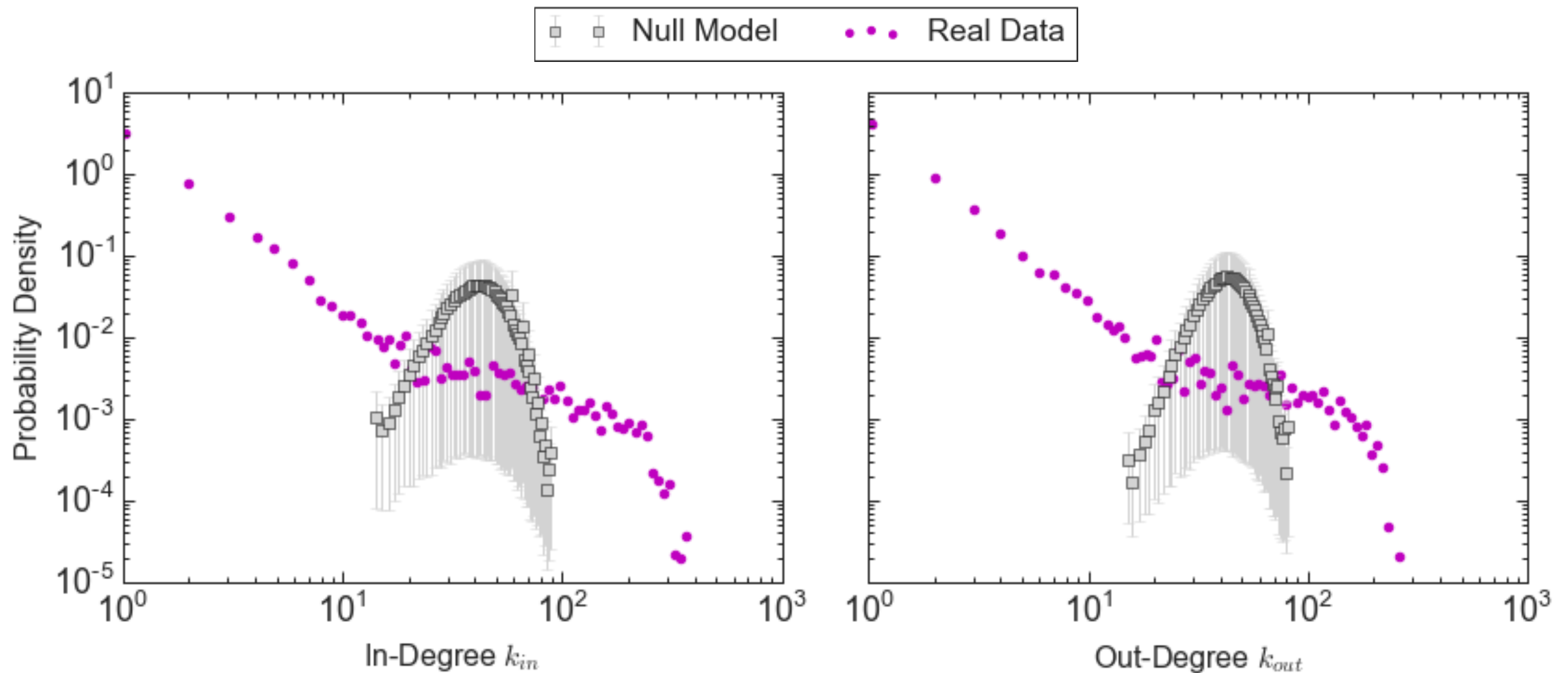
- Randomly choose players from the pool
- Each player wins a set with probability $1/2$



Tennis
Professionals
Pool



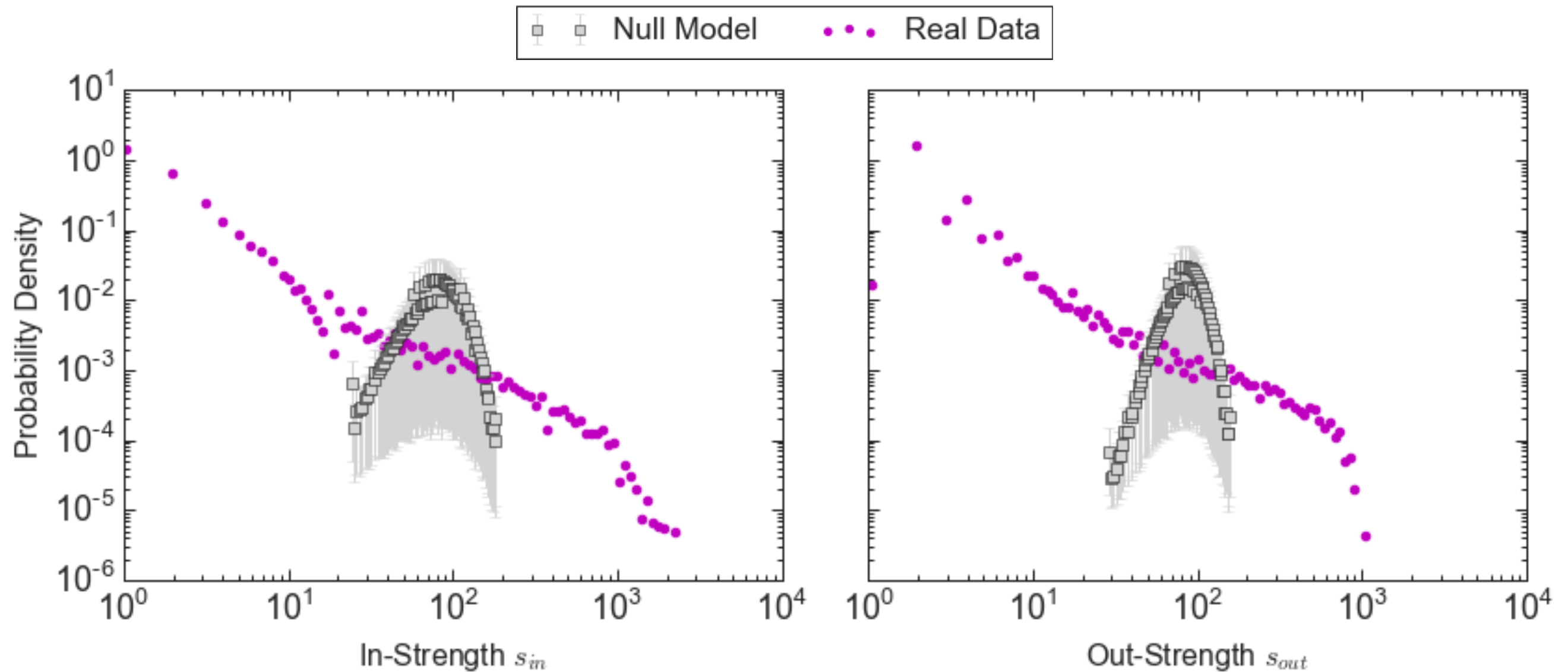
Degree Distribution



Real Data $\langle k_{in} \rangle = 33.040$

Null Model $\langle k_{in} \rangle = 46.493 \pm 0.045$

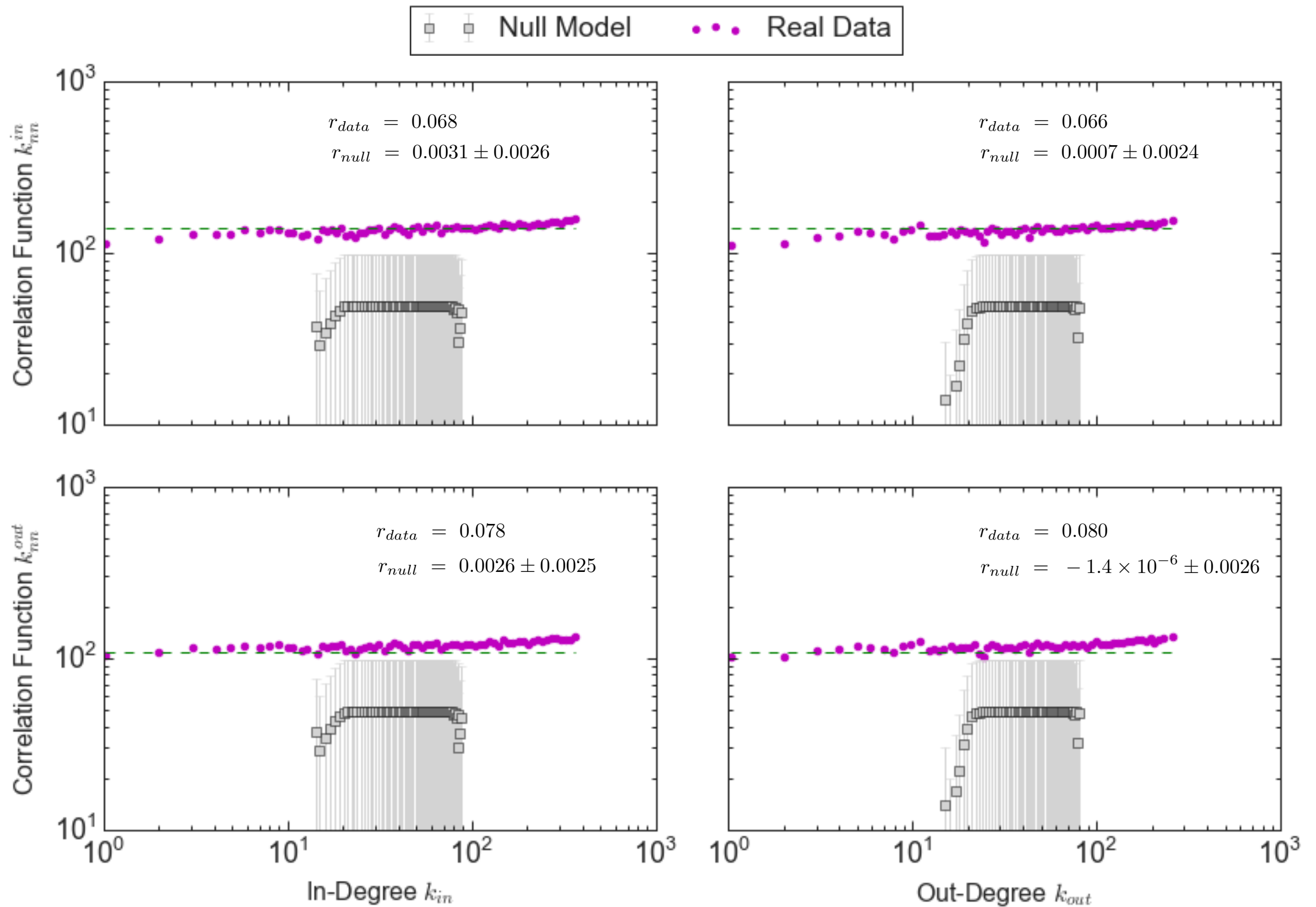
Strength Distribution



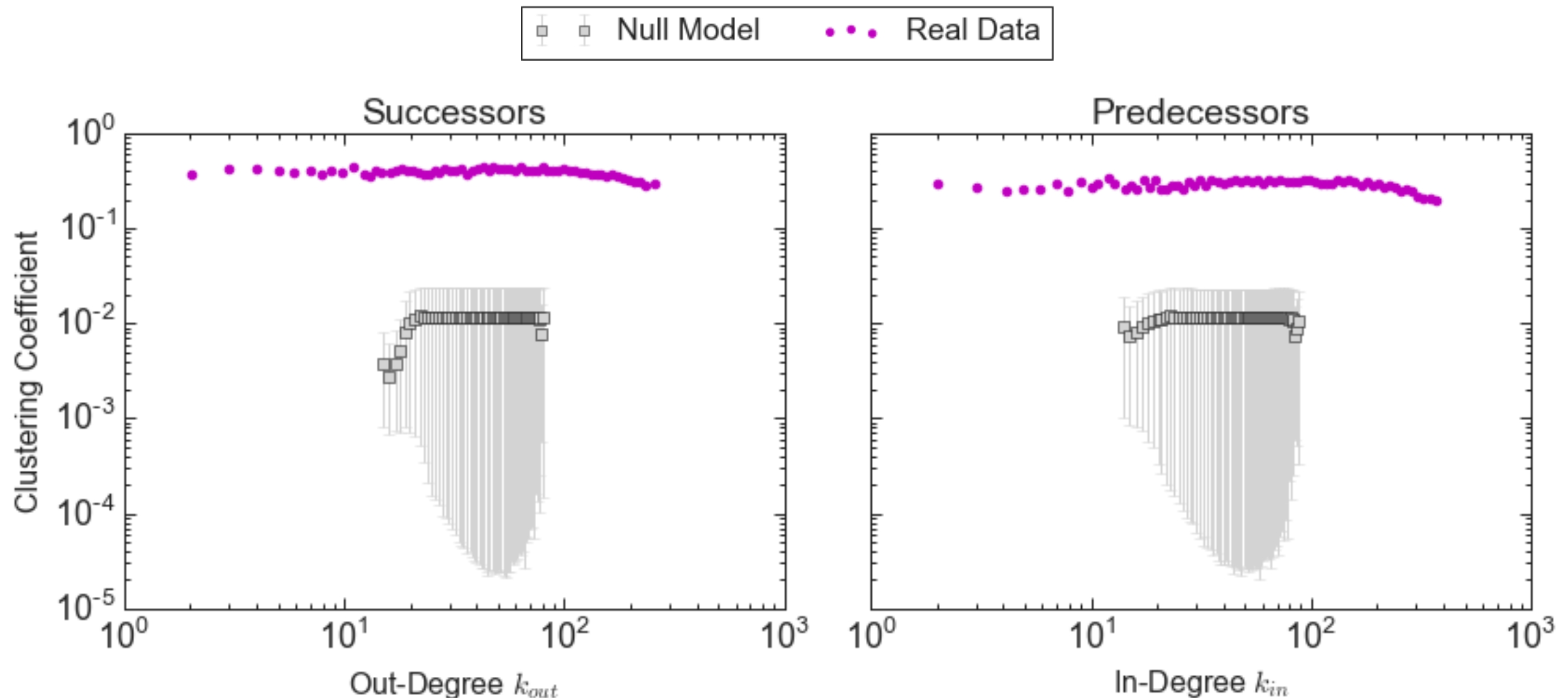
Real Data $\langle s_{in} \rangle = 95.369$

Null Model $\langle s_{in} \rangle = 90.244 \pm 0.053$

Degree Correlation



Clustering Coefficient



Real Data $\langle C_{out} \rangle = 0.297$

$\langle C_{in} \rangle = 0.173$

Null Model $\langle C_{out} \rangle = 0.012 \pm 8.0 \times 10^{-5}$

$\langle C_{in} \rangle = 0.012 \pm 7.7 \times 10^{-5}$

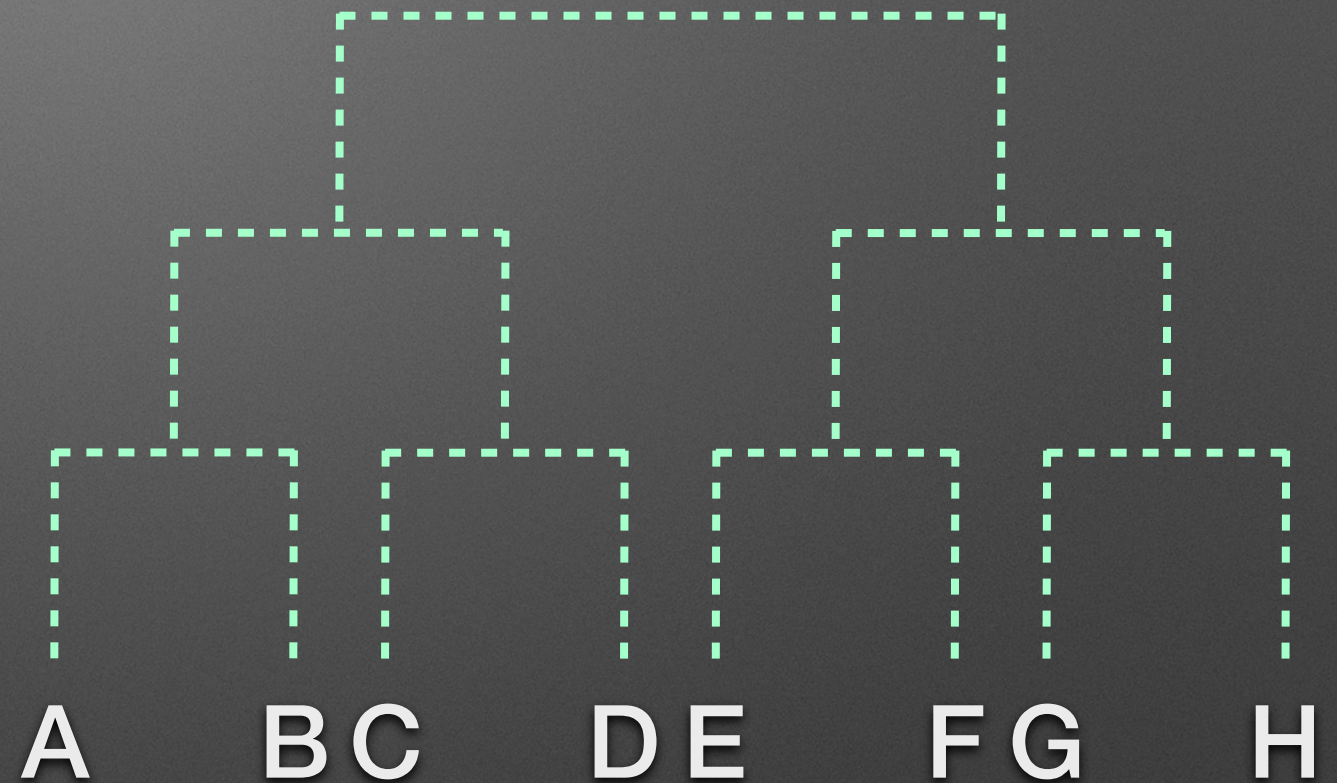
Components

	Number of strongly connected components
Real Data	841
Null Model	1

	Component size	Frquency	Average distance
Real Data	1	830	0.00
	2	10	1.00
	2368	1	3.15 (2.58 for null model)

Intrinsic Skill Modelling

- Assign each player a intrinsic skill parameter ψ following some distribution $\rho(\psi)$.
- Simulate tournaments given their initial draw from the data.
- The probability that a player wins a set is proportional to his intrinsic skill.



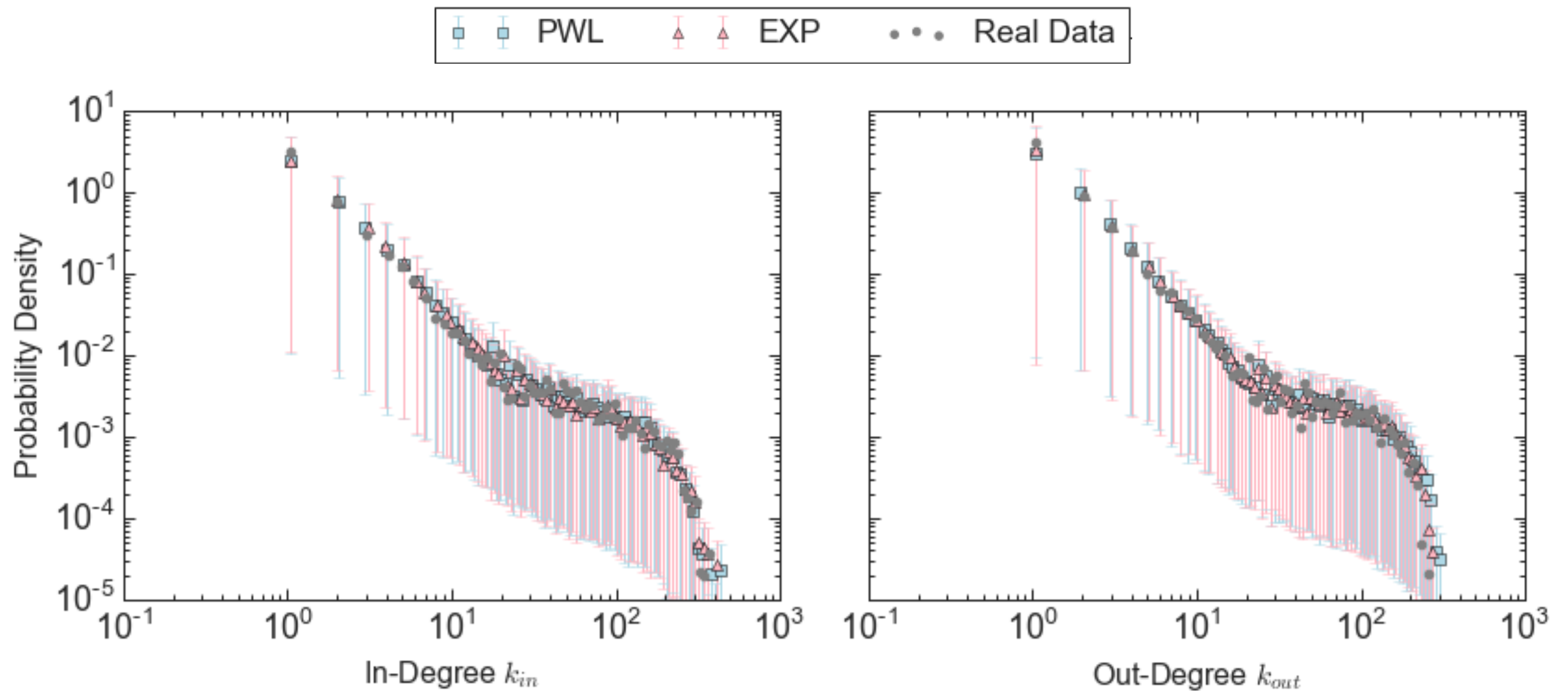
$$P\{A \text{ wins}\} = \frac{\psi(A)}{\psi(A) + \psi(B)}$$

$$P\{B \text{ wins}\} = \frac{\psi(B)}{\psi(A) + \psi(B)}$$

**Does the intrinsic skill distribution
have heavy-tail?**

Power-law vs Exponential

Degree Distribution



Real Data

$$\langle k_{in} \rangle = 33.040$$

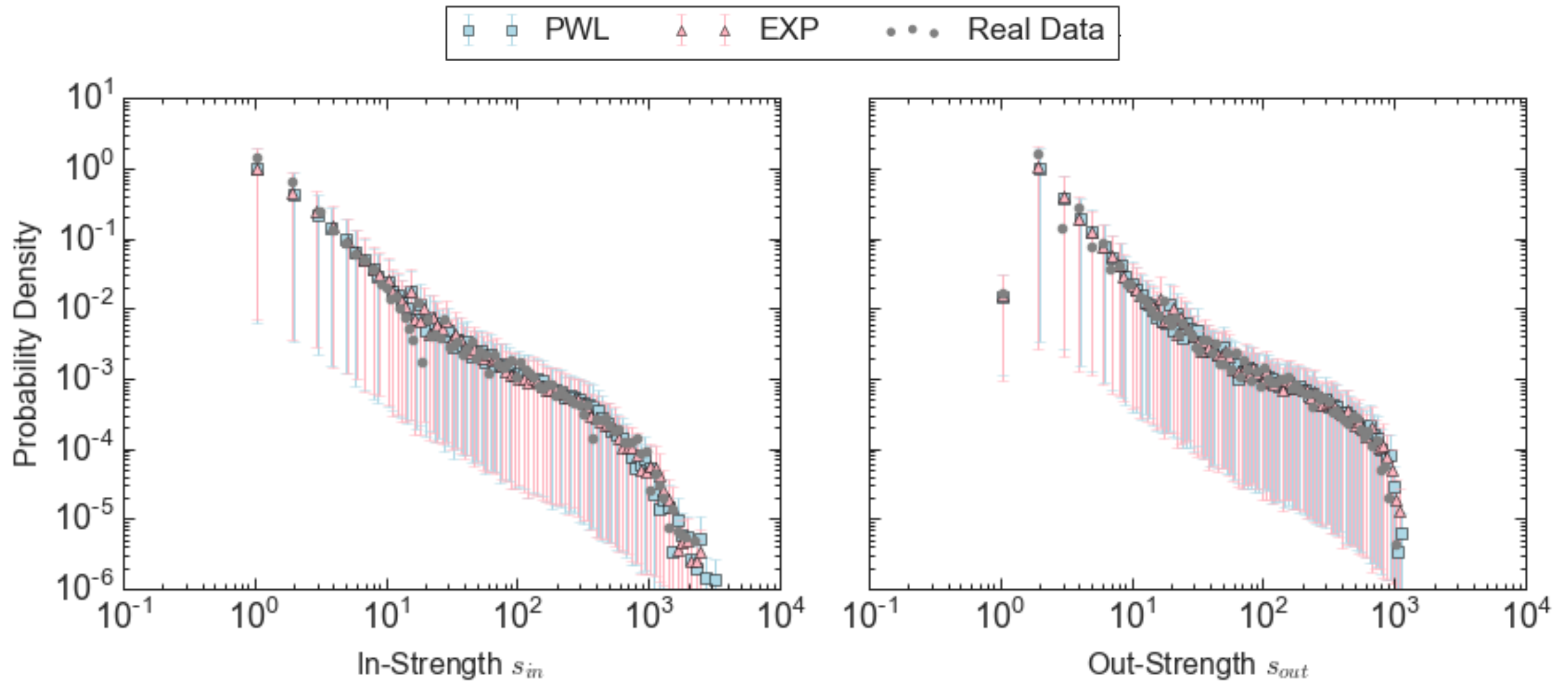
PWL

$$\langle k_{in} \rangle = 37.845 \pm 0.058$$

EXP

$$\langle k_{in} \rangle = 36.452 \pm 0.044$$

Strength Distribution



Real Data

$$\langle s_{in} \rangle = 95.369$$

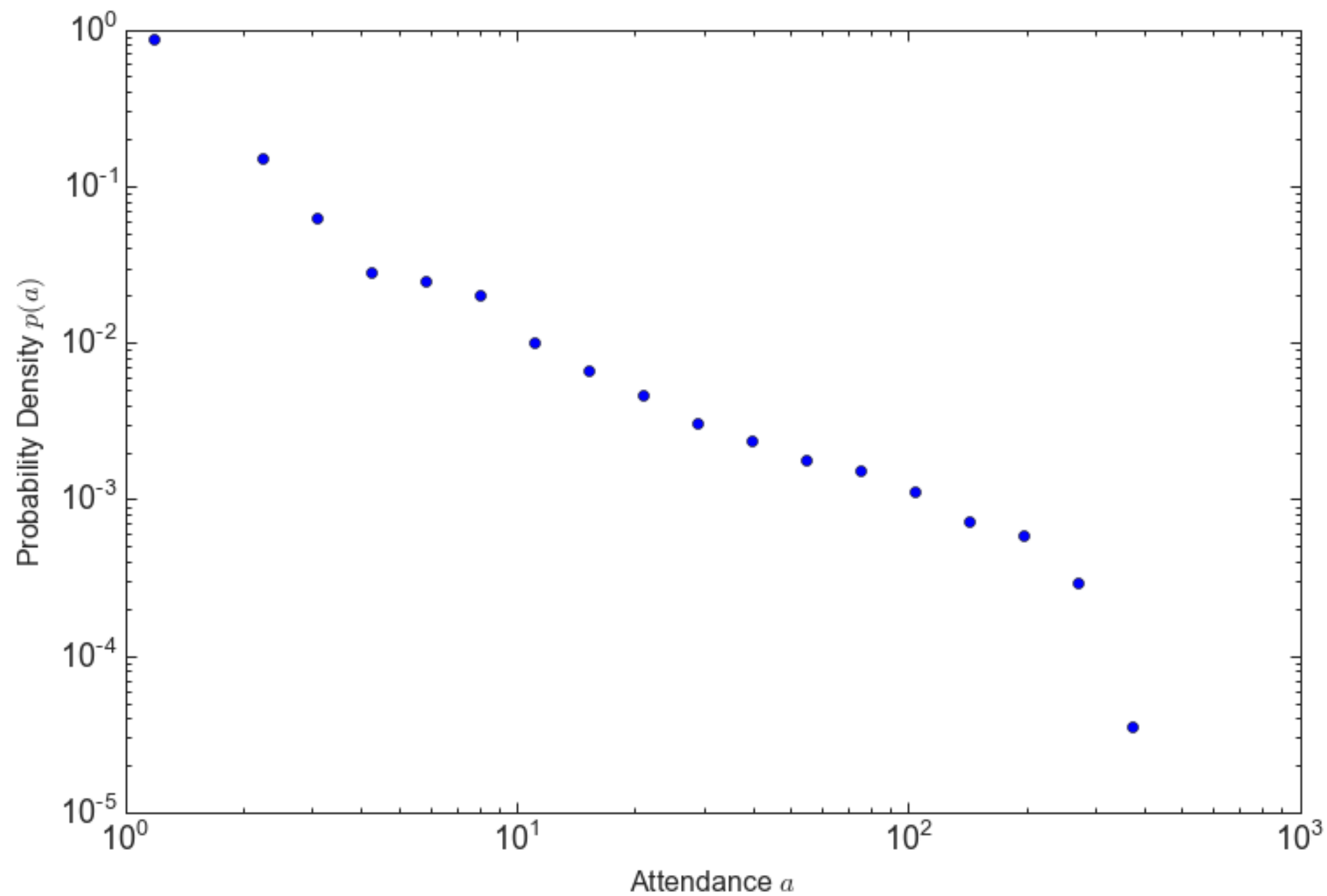
PWL

$$\langle s_{in} \rangle = 111.811 \pm 0.067$$

EXP

$$\langle s_{in} \rangle = 110.295 \pm 0.061$$

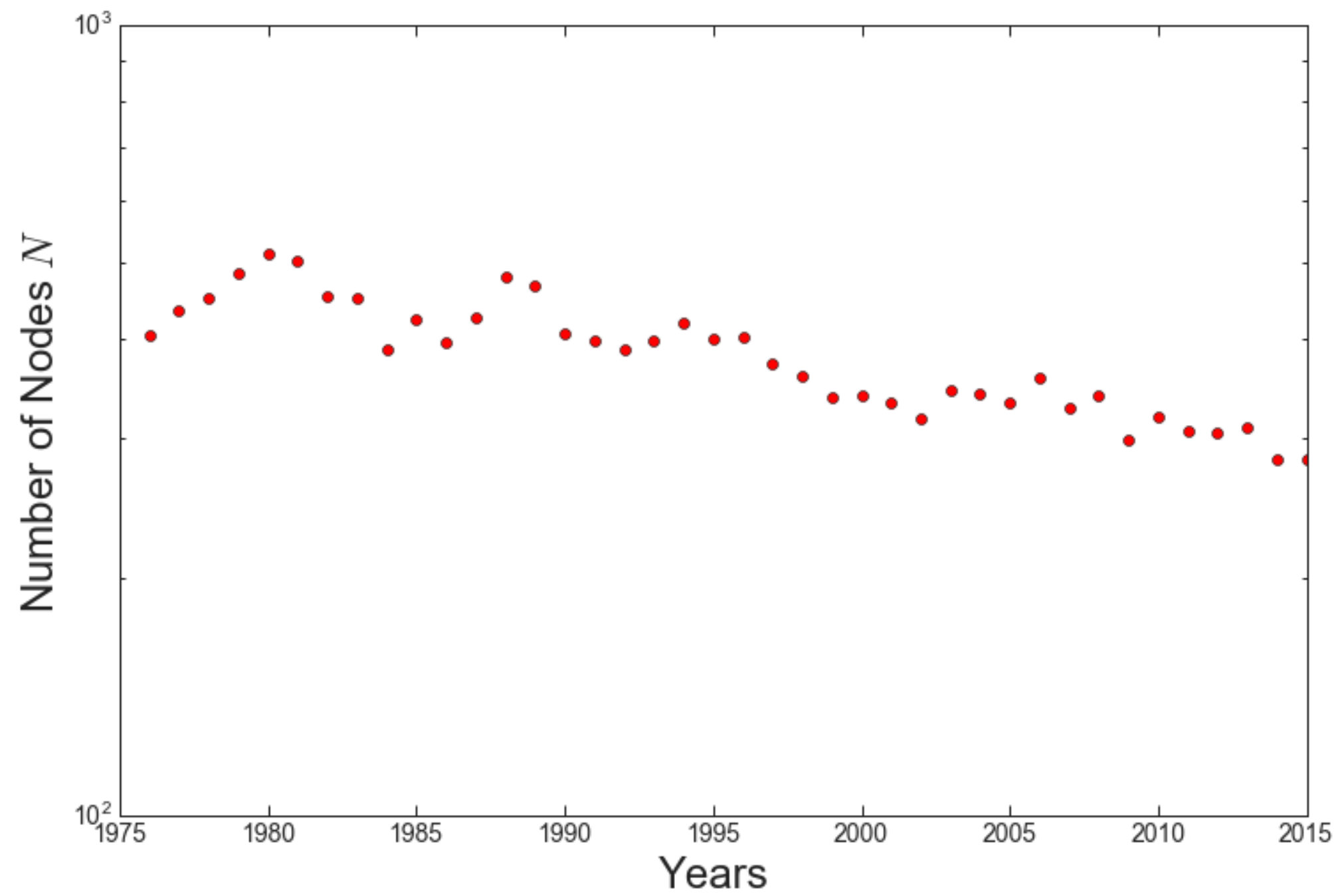
Tournament Attendance

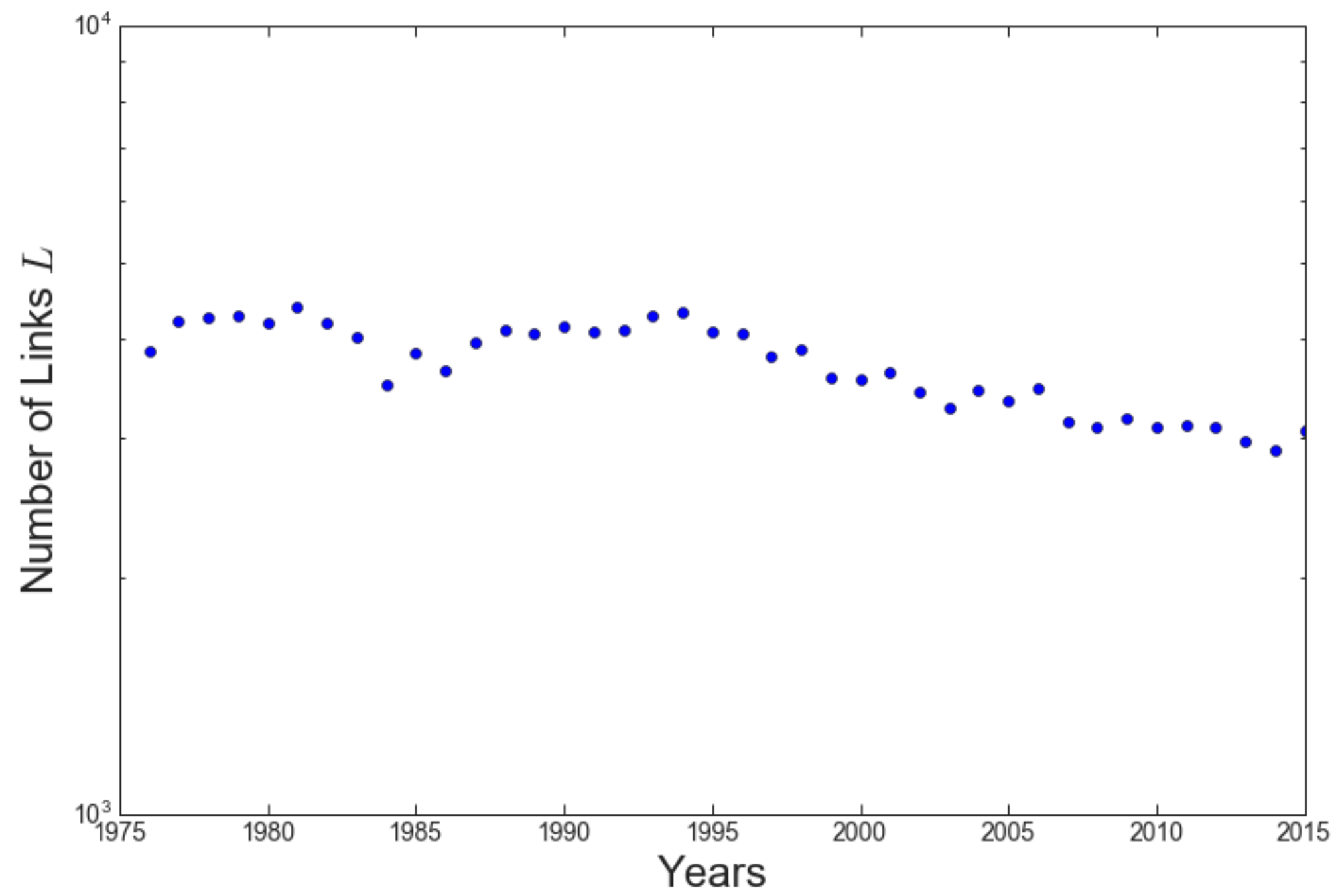


Conclusion

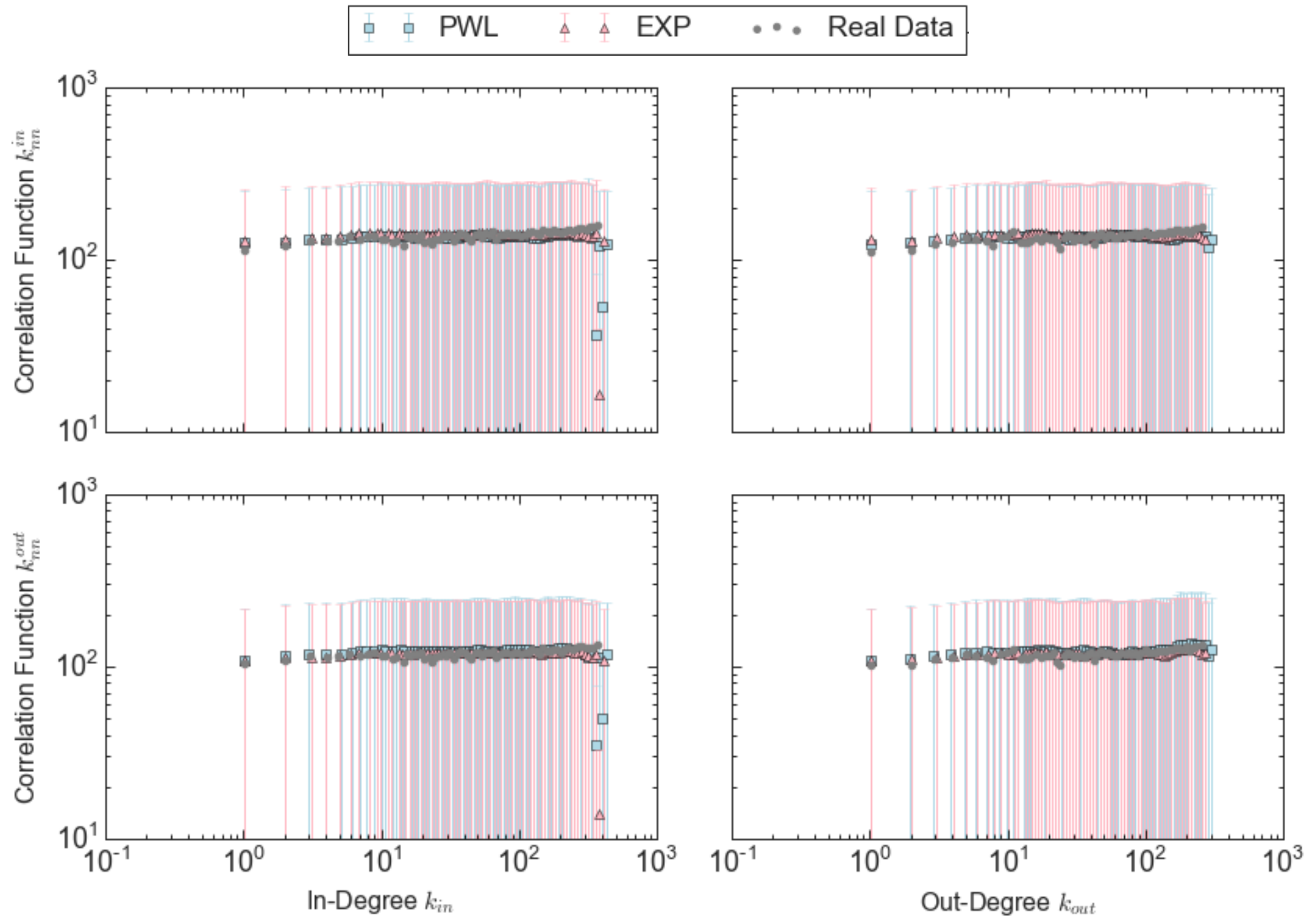
- The community structure reflects players of different generation.
- The tennis player network is neutral but highly clustered.
- The numbers of sets that players won own heterogeneity.

Appendix





Degree Correlation



Clustering Coefficient

