



# **Path Planning via Reinforcement Learning for Robotic Catheters Performing Percutaneous Coronary Interventions in a Deformable Environment**

Advisor: Prof. Elena De Momi

Co-advisor: Zhen Li, Ph.D. candidate

Author: Chiara Lambranzi 944336

Academic Year 2021/22

Department of Electronics, Information and Bioengineering  
Master of Science – Biomedical Engineering



## Clinical scenario

- Cardiovascular diseases main cause of death in developed countries<sup>[1]</sup>
- 147.438 PCIs in Italy in 2021<sup>[2]</sup>

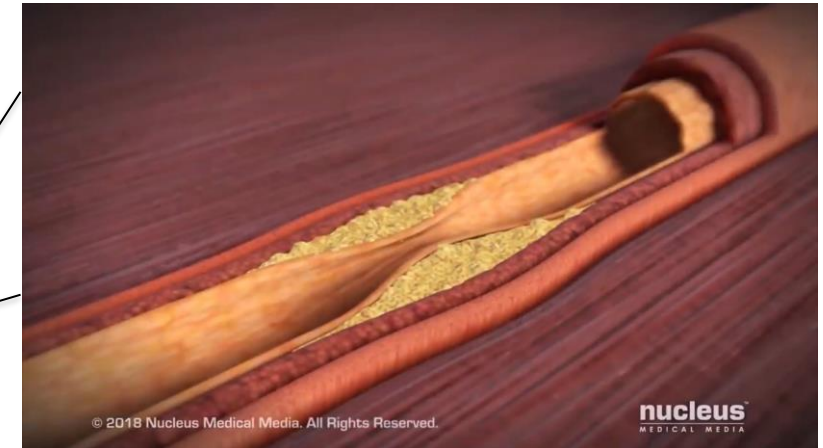
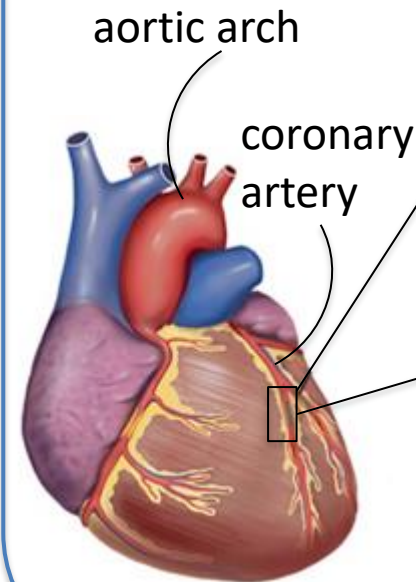
## Risks

- X-ray and contrast dye exposure
- Collision with delicate anatomy

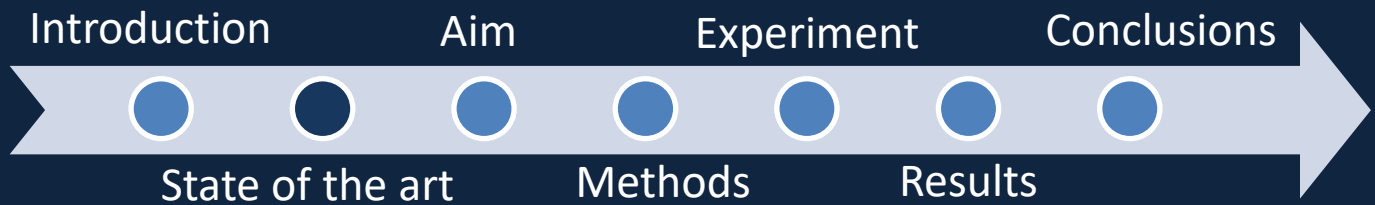
## Solution

- Aortic model from MRI
- Guidance with path planning in PCI procedure to reduce collision

## PERCUTANEOUS CORONARY INTERVENTION (PCI)

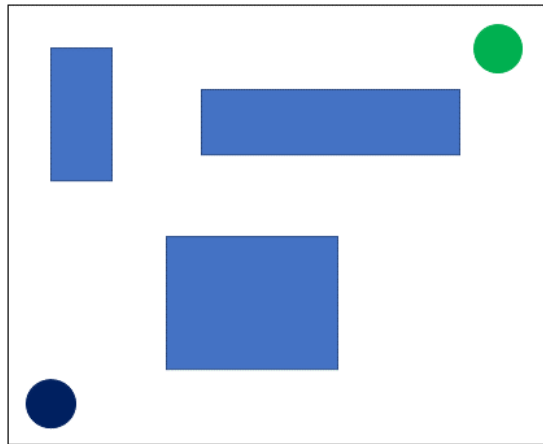


# State of the art



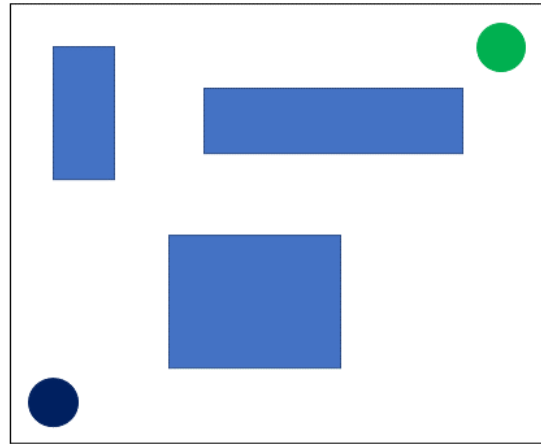
Path planning: find a collision-free motion between an initial and a final configuration within a specified environment

Node based



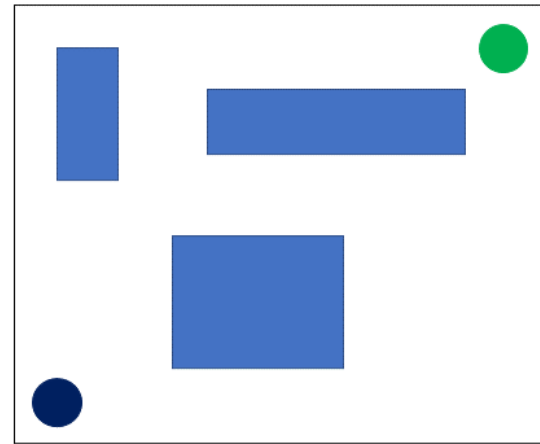
Dijkstra's Algorithm

Sampling based



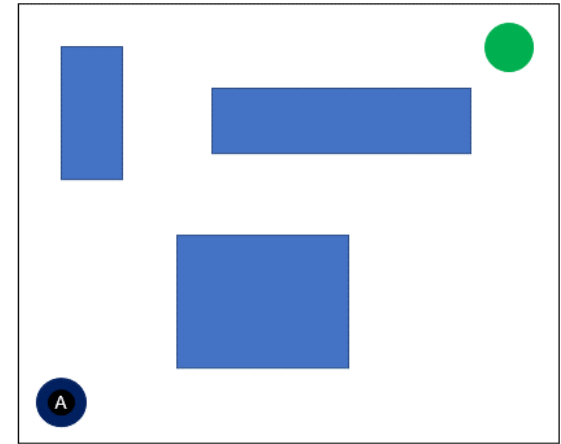
Rapidly-exploring Random  
Tree

Optimization based



Bézier interpolation

Learning based



Reinforcement Learning

# Aim of the work

Introduction

Aim

Experiment

Conclusions

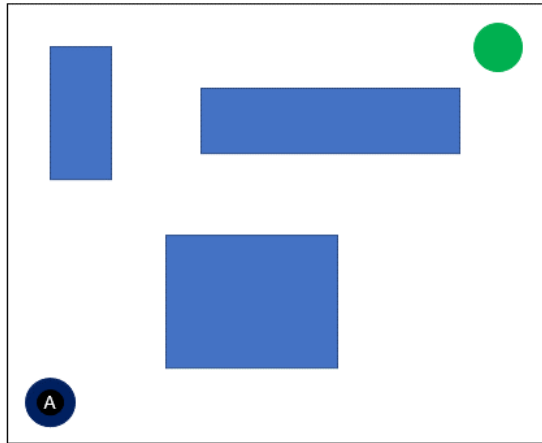


State of the art

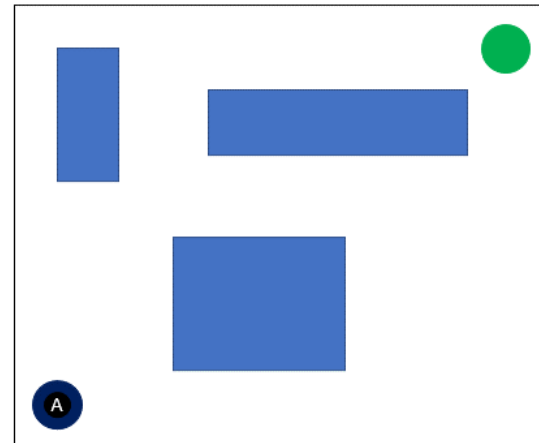
Methods

Results

Learning based path planning algorithm



Direct RL

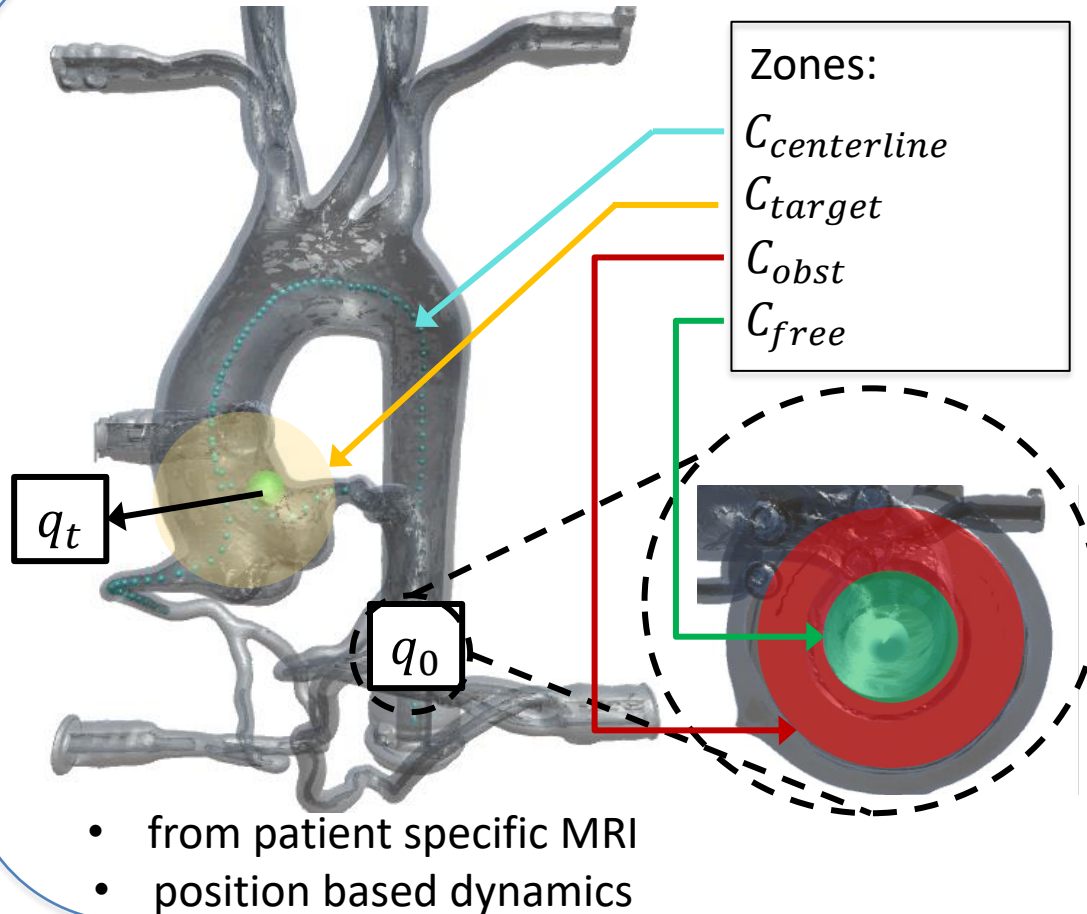


Inverse RL  
Learning From Demonstrations

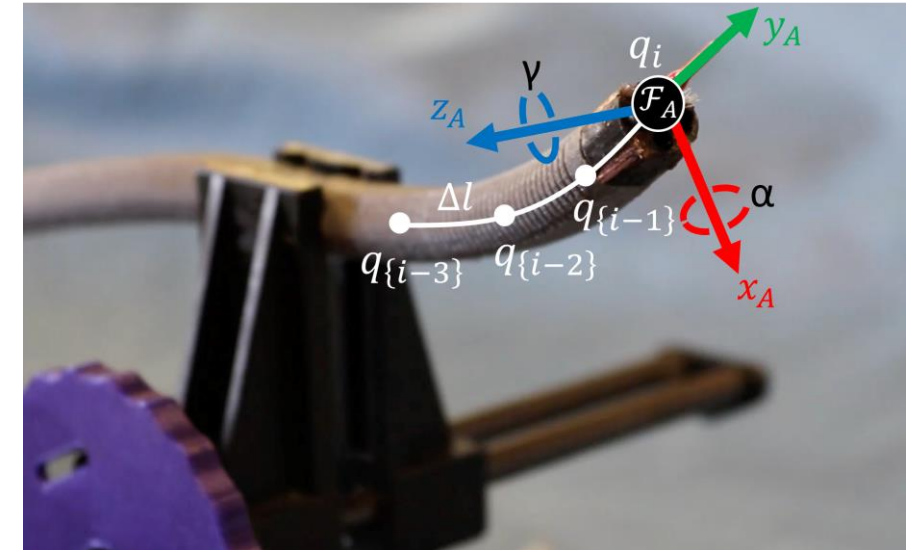
PCI navigation on 3D deformable  
environment  
Replanning



## DYNAMIC ENVIRONMENT

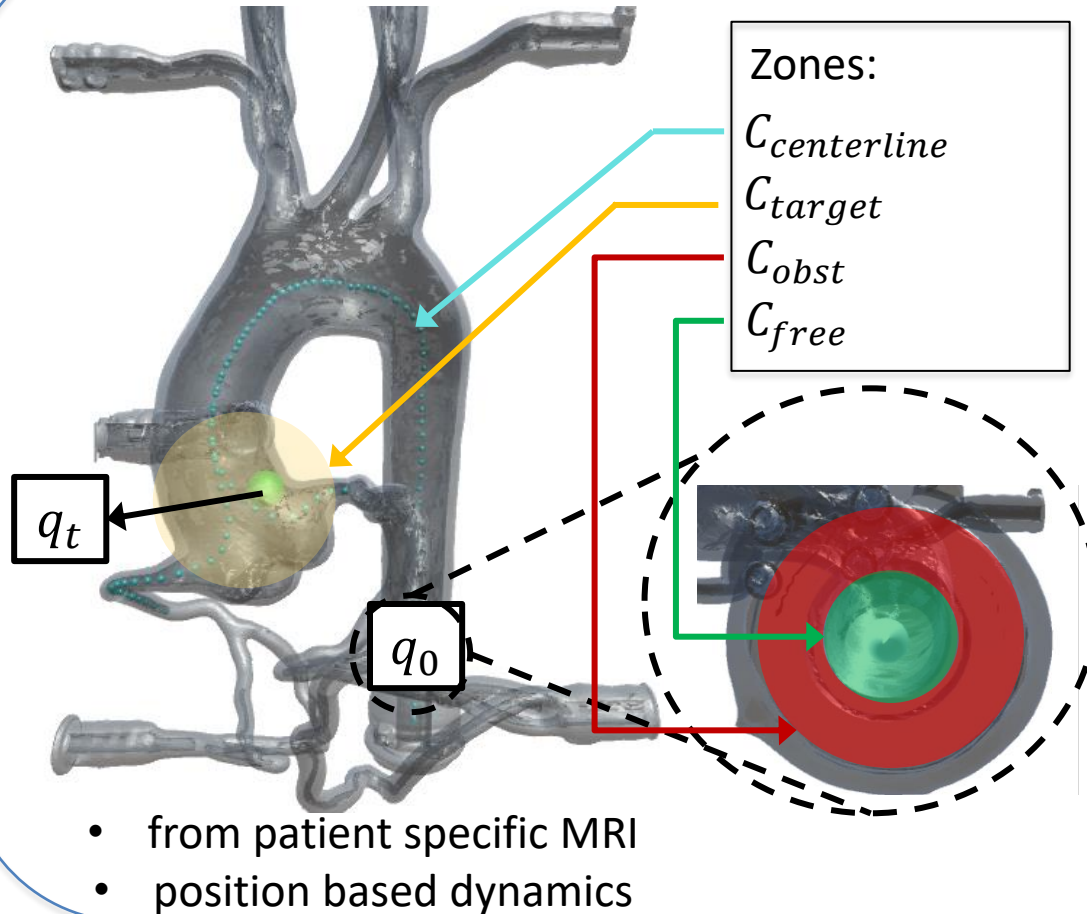


## CATHETER



- Follow the leader model
- DOF: insertion, x-z rotation

## DYNAMIC ENVIRONMENT



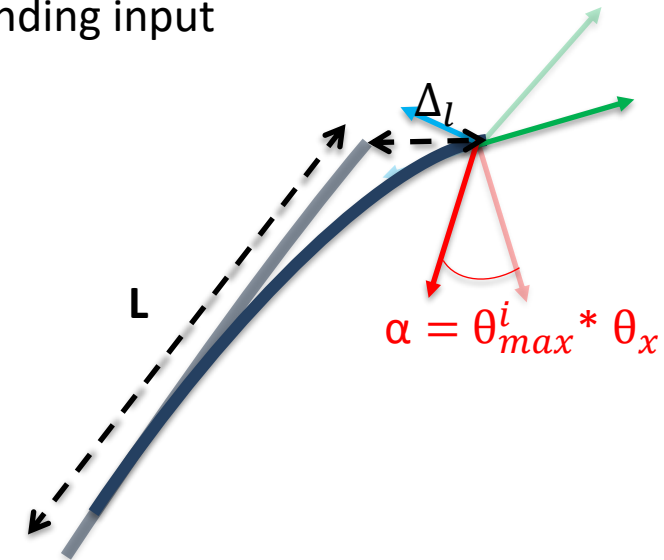
## CATHETER

### BENDING CONSTRAINT

$$\theta_{max}^i = \frac{\theta_{max} * \Delta l}{L}$$

$\theta_{max}$ : maximum bending angle

$\theta_x$ : x-bending input





# Reinforcement Learning

Introduction

Aim

Experiment

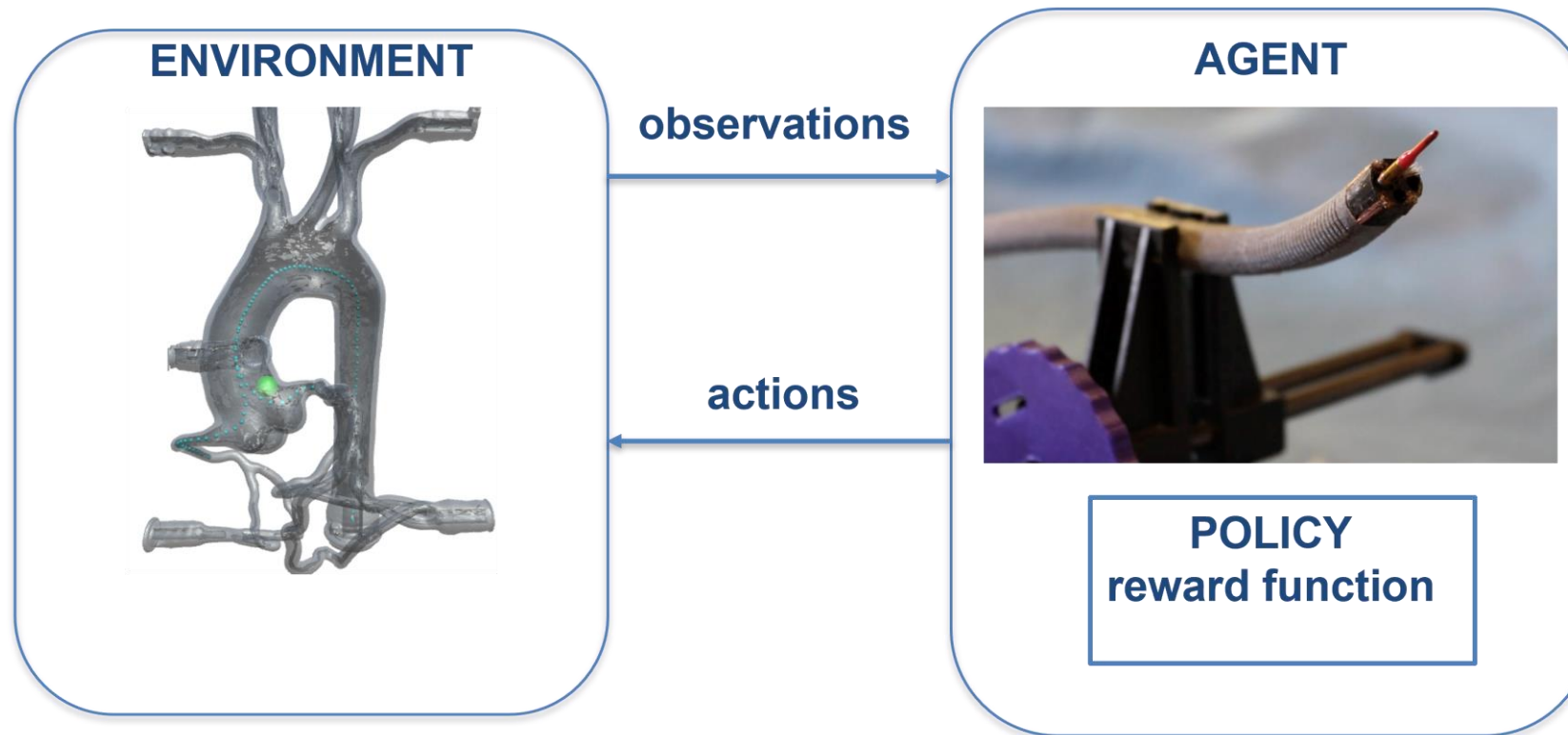
Conclusions



State of the art

Methods

Results





## REWARD FUNCTION

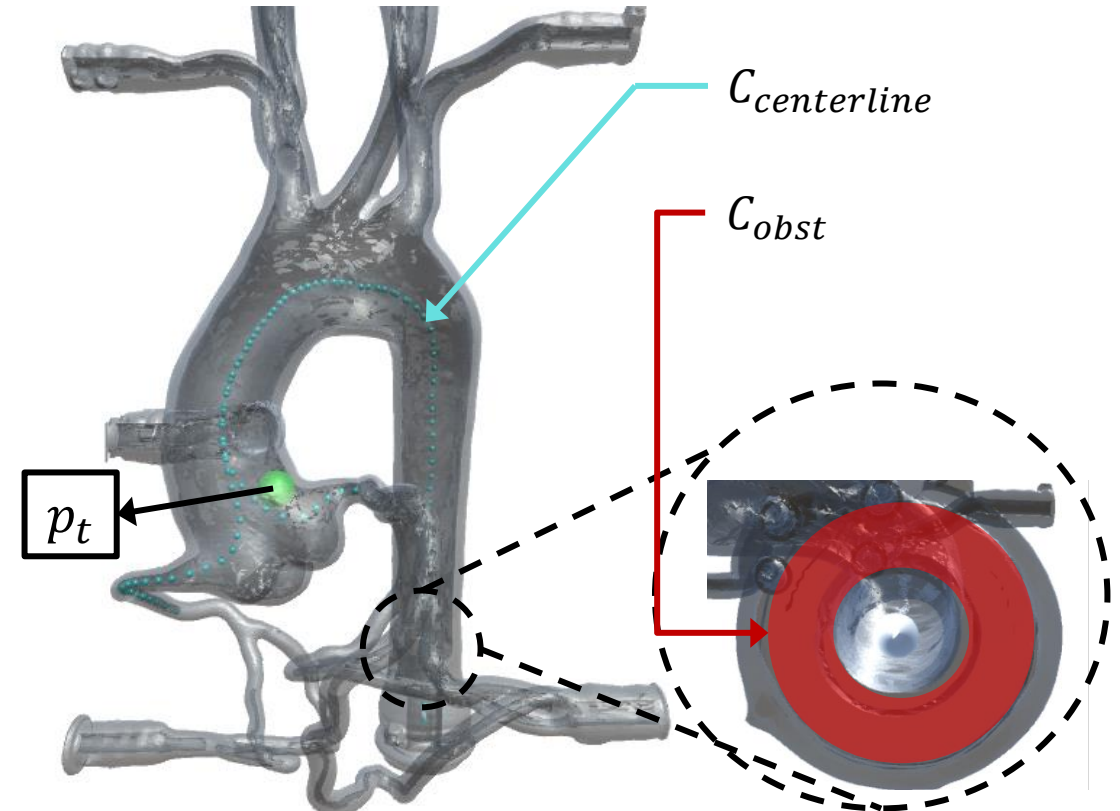
$$r_t = r_{end} + r_{in}$$

$$r_{end} = \begin{cases} r_{obst} & \text{if } q_i \in C_{obst} \\ r_{target} & \text{if } ||p_i - p_t|| < \varepsilon \end{cases}$$

$$r_{in} = r_{step} + r_{centerline} + r_{bending}$$

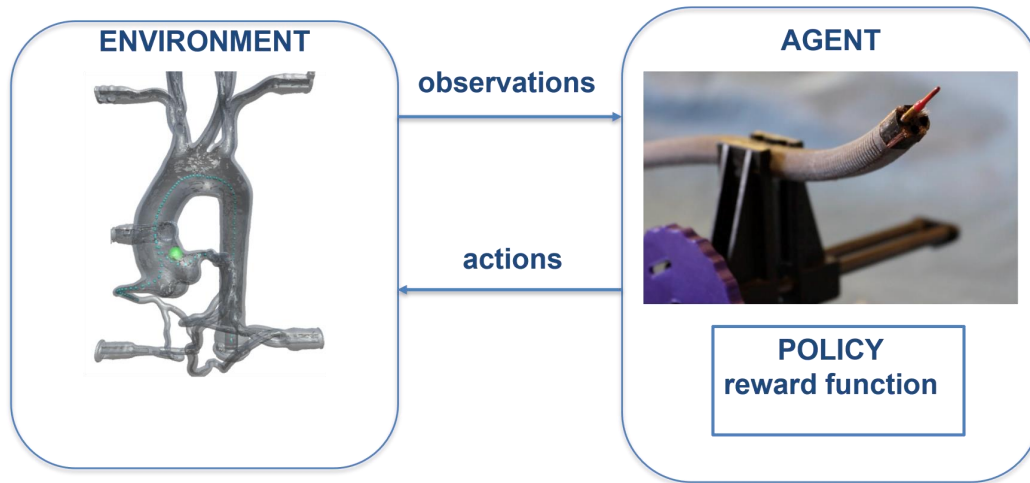
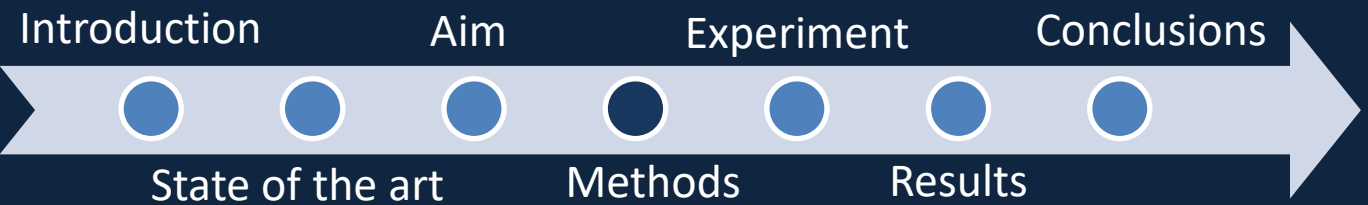
$r_{step}$ : time-step reward

$r_{bending}$ : high angle reward





# Reinforcement Learning



## REWARD FUNCTION

$$r_t = r_{end} + r_{in}$$

$$r_{end} = \begin{cases} r_{obst} & \text{if } q_i \in C_{obst} \\ r_{target} & \text{if } ||p_i - p_t|| < \varepsilon \end{cases}$$

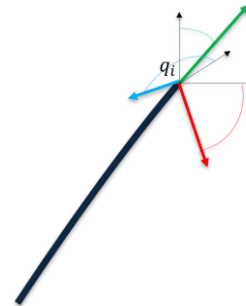
$$r_{in} = r_{step} + r_{centerline} + r_{bending}$$

## ACTIONS

$$A = [\alpha, \gamma, \Delta_l]$$

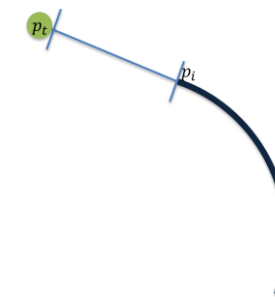
## OBSERVATIONS

pose  $q_i$



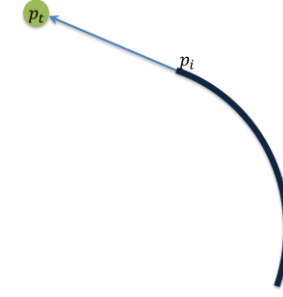
target distance

$$o_{dis} = \frac{||p_t - p_i||}{d_{max}}$$



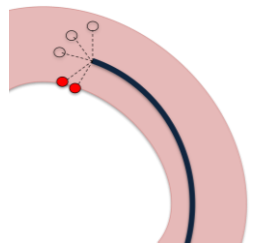
target direction

$$o_{dir} = p_t - p_i$$

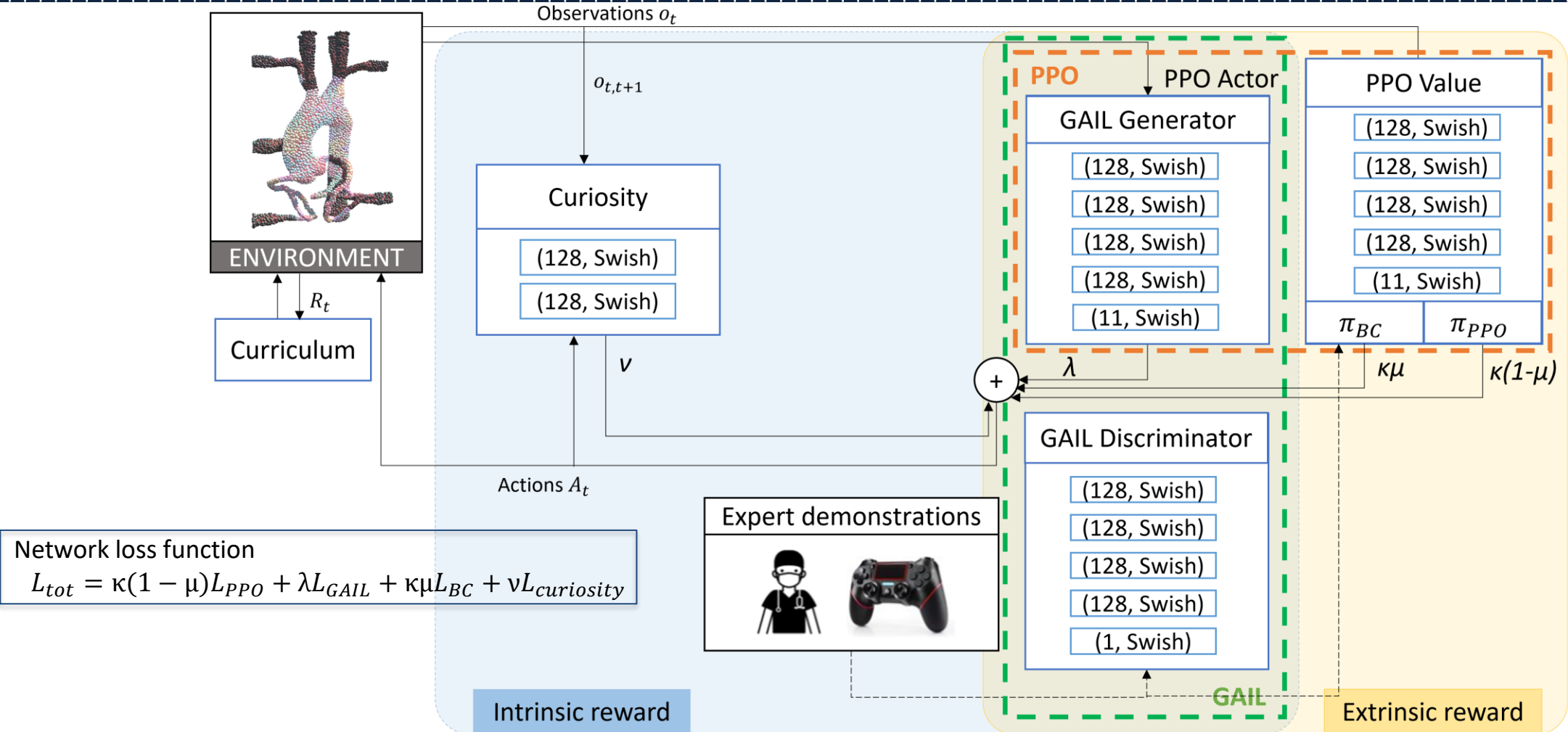
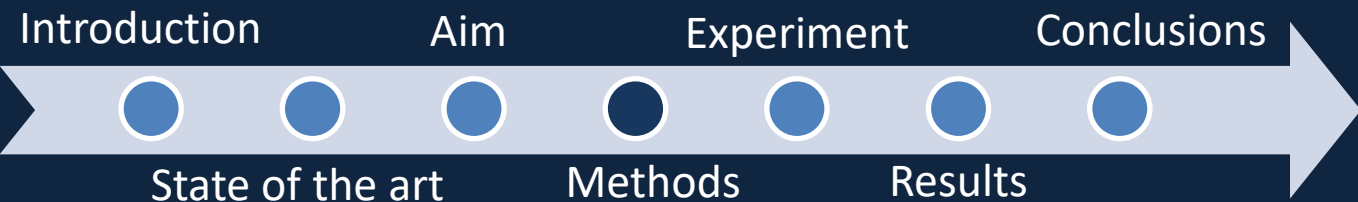


raycast

$$o_{ray}$$



# Network Architecture



# Performance metrics



## Success rate

$$\delta = n_s/n$$

$n_s$ : successful tests

$n$ : total tests

## Collision number

$$\varepsilon = \sum_{i=t_0}^{i=t_f} c(i), c(i) = \begin{cases} 0, & \text{if } q_i \in C_{free} \\ 1, & \text{otherwise} \end{cases}$$

$t_0, t_f$ : start time, stop time

$c(i)$ : permitted collisions

$q_i$ : agent pose at time  $i$

## Targeting error

$$T_a = \min ||q_t - q_i||$$

$q_t$ : target pose

## Duration

$$T = t_f - t_0$$

# Experimental protocol

Introduction

Aim

Experiment

Conclusions



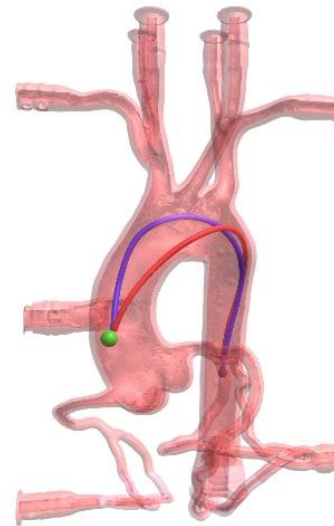
State of the art

Methods

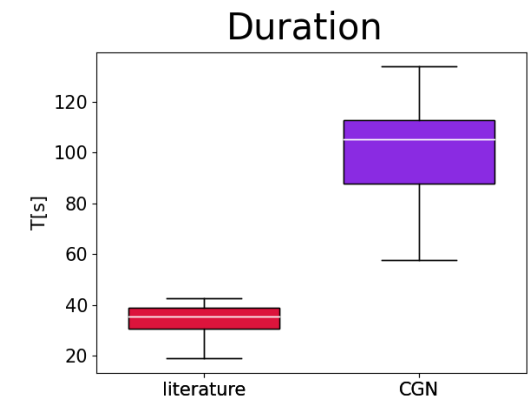
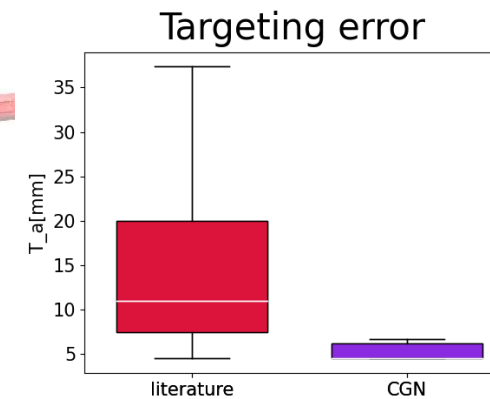
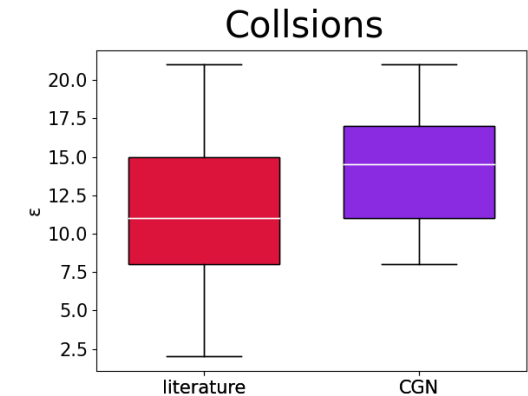
Results

- 60 demonstrations from 1 expert (student)
- 5 million steps training
- 100 tests with the trained network
- 3 possible starting poses
- 5 possible target positions

## Comparison with literature

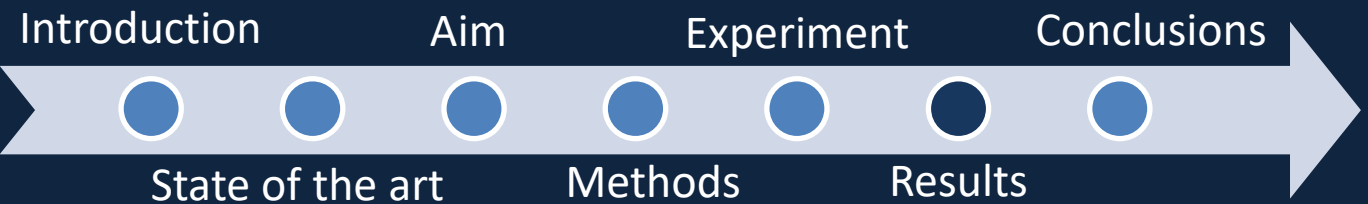


	$\delta$
literature	14%
CGN	68%



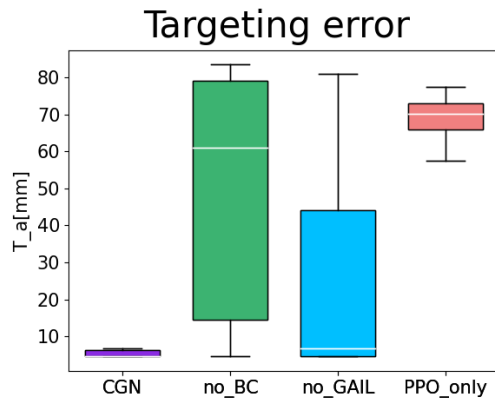
$p < 0.05$  using Kruskal-Wallis test

# Ablation study

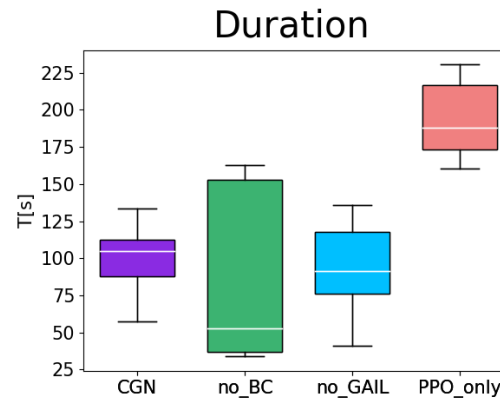
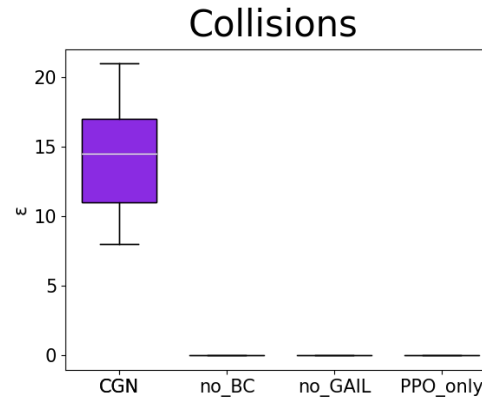


## Ablation study

	$\delta$
CGN	68%
no_BC	8%
no_GAIL	41%
PPO_only	0%



$p < 0.05$  using Kruskal-Wallis test



module	symbol	value
PPO	$\kappa$	0.2
BC	$\mu$	0.7
GAIL	$\lambda$	0.8
curiosity	$v$	0.02

Network loss function

$$L_{tot} = \kappa(1 - \mu)L_{PPO} + \lambda L_{GAIL} + \kappa\mu L_{BC} + vL_{curiosity}$$

# Replanning

Introduction

Aim

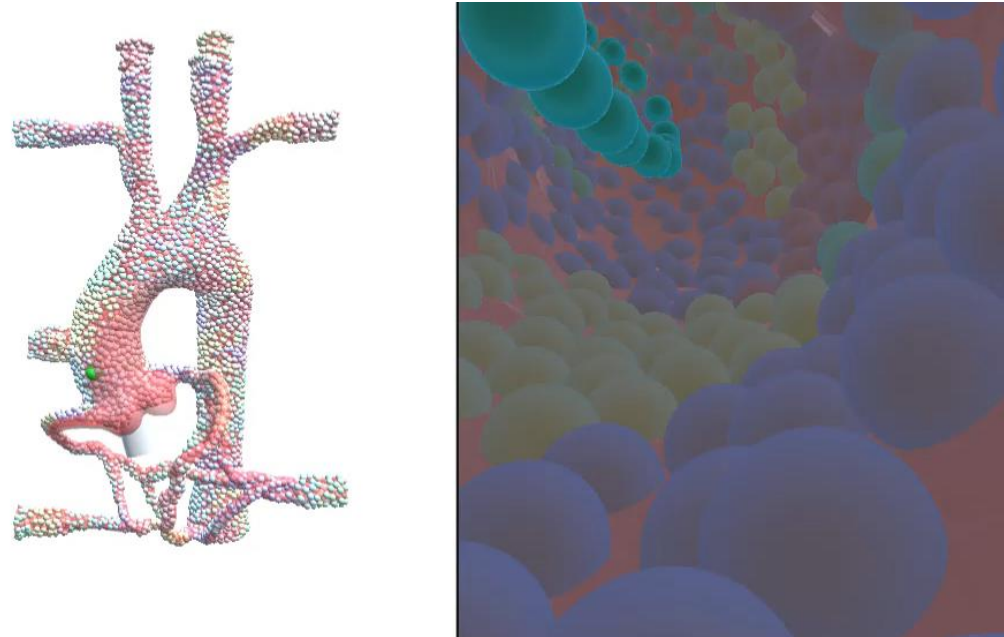
Experiment

Conclusions

State of the art

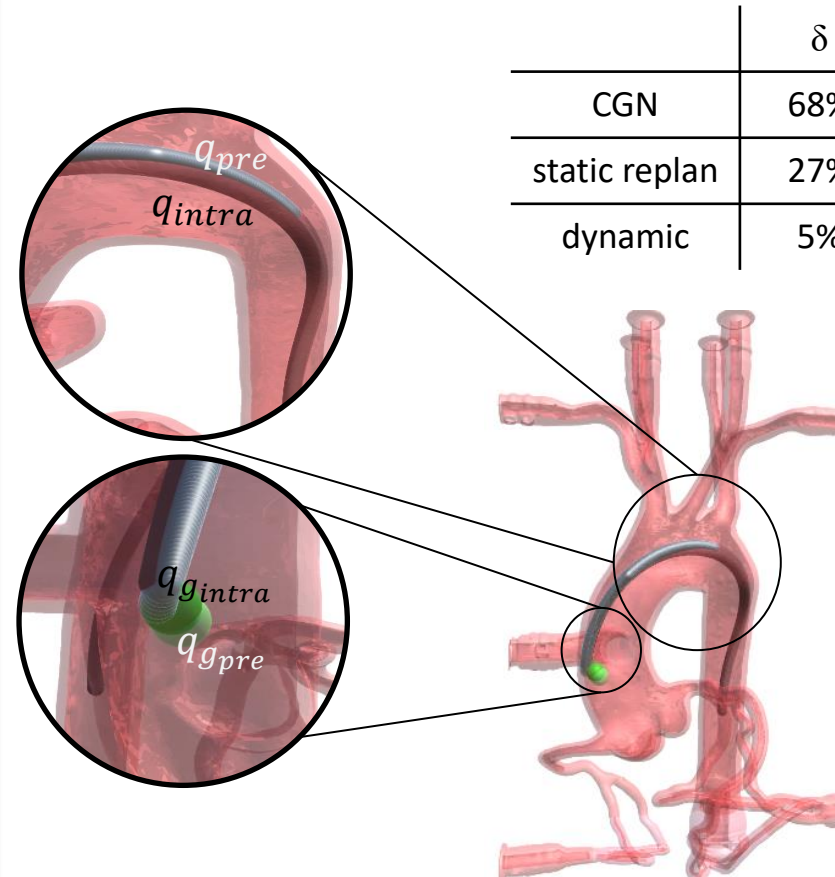
Methods

Results

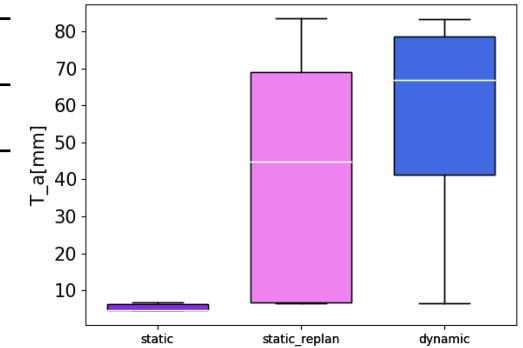


Graphical user interface:  
external view and catheter view

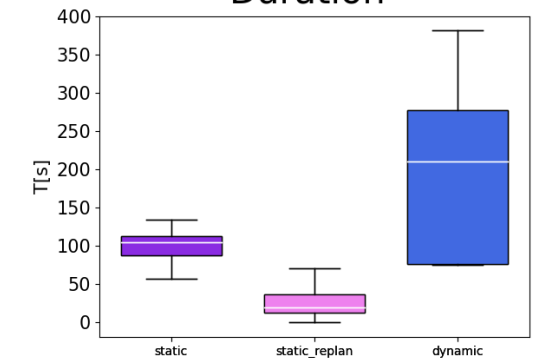
## Static and dynamic replanning



### Targeting error



### Duration



$p < 0.05$  using Kruskal-Wallis test



# Conclusions and future work



## Results

- Viable path and replanning
- Validation in a deformable environment
- Respect of physical constraints

## Limitations

- Cumbersome model
- Limited precision for replanning



## Future work

- Test on different aortic models
- Improve duration and precision of replanning



**Thank you for your attention!**  
**Questions?**

Department of Electronics, Information and Bioengineering  
Master of Science – Biomedical Engineering

# In vitro validation

Introduction

Aim

Experiment

Conclusions



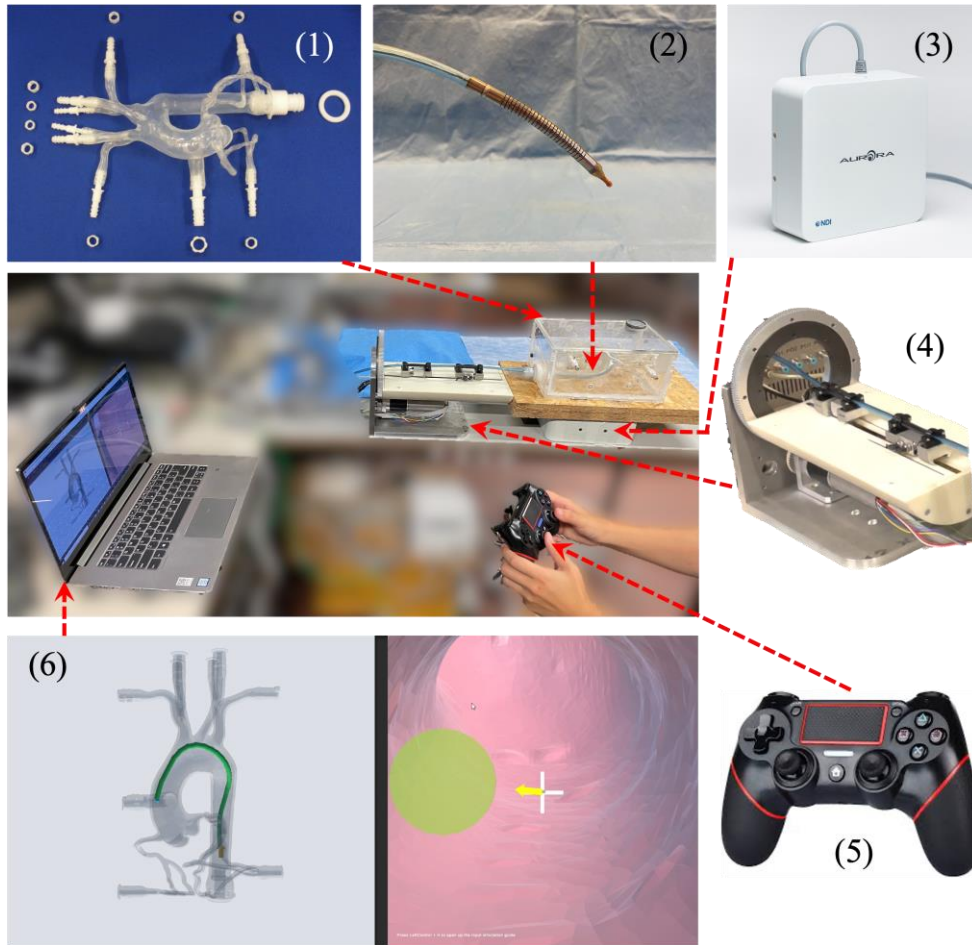
State of the art

Methods

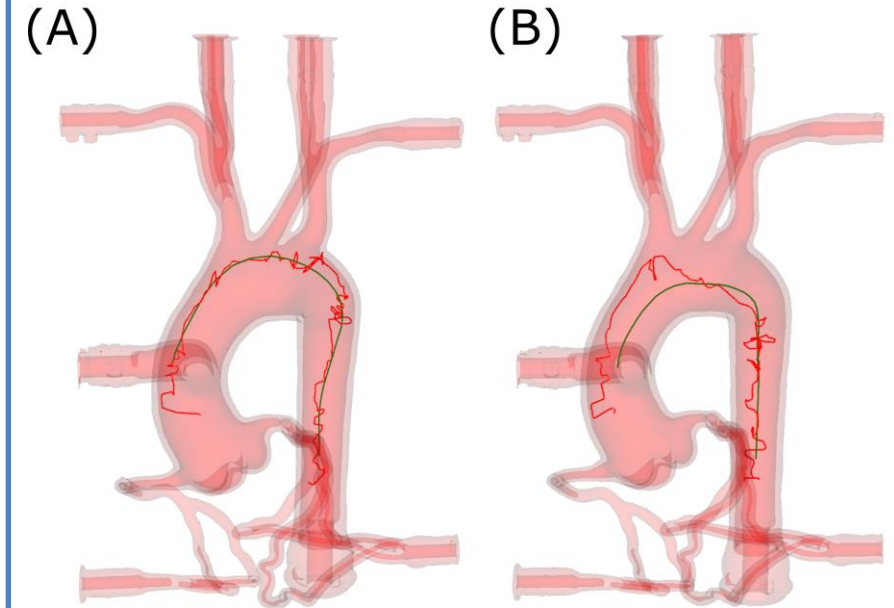
Results

## SETUP

- 1) Silicone phantom
- 2) Catheter
- 3) EM sensor
- 4) Actuator
- 5) Controller
- 6) GUI
- 7) Provided path



## RESULTS



- (A) Tip position following the Curriculum GAIL path
- (B) Tip position following the centerline