

# Singular Spectrum Analysis

make test data

```
In[1]:= len = 200
```

```
Out[1]= 200
```

line

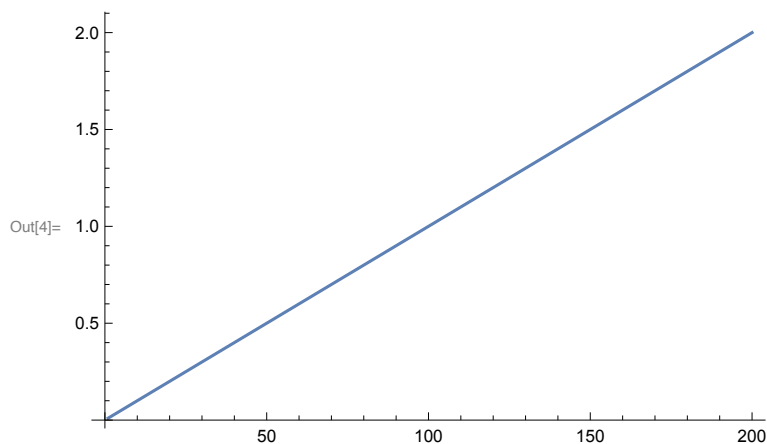
```
In[2]:= a1 = Table[N[2 * i / len], {i, len}];
```

```
In[3]:= Export["~/ssa_20211008/graph1.csv", a1, "CSV"]
```

```
Out[3]= ~/ssa_20211008/graph1.csv
```

line

```
In[4]:= ListPlot[a1, Joined → True]
```



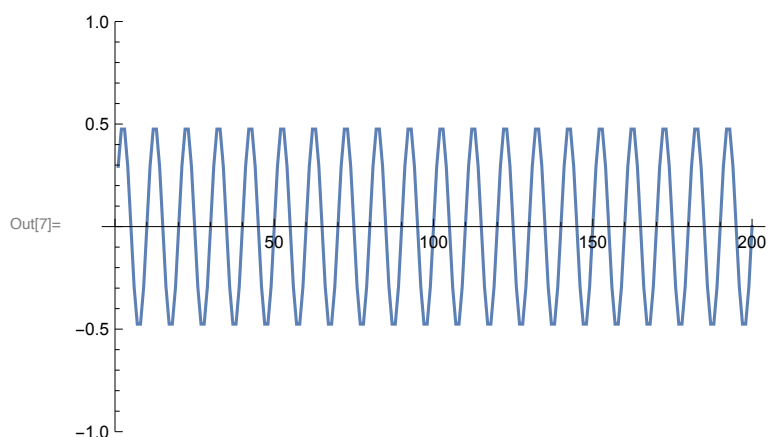
sine wave

```
In[5]:= a2 = Table[0.5 * Sin[2 Pi (20 * i / len)], {i, len}];
```

```
In[6]:= Export["~/ssa_20211008/graph2.csv", a2, "CSV"]
```

```
Out[6]= ~/ssa_20211008/graph2.csv
```

```
In[7]:= ListPlot[a2, Joined → True, PlotRange → {-1, 1}]
```



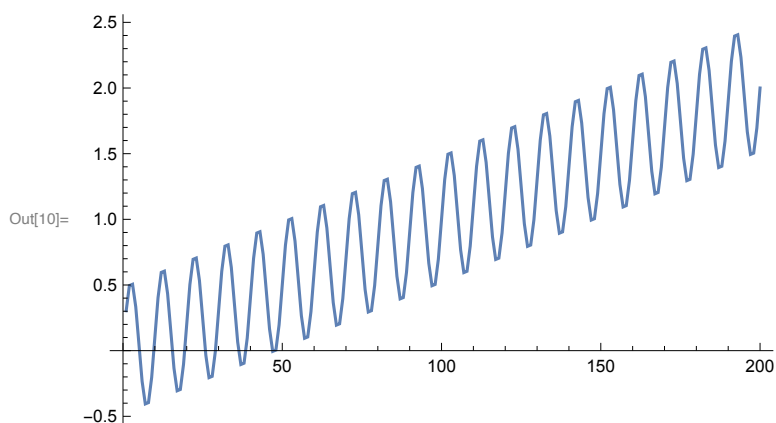
## superposition of curves

```
In[8]:= c = a1 + a2;
```

```
In[9]:= Export["~/ssa_20211008/graph3.csv", c, "CSV"]
```

```
Out[9]= ~/ssa_20211008/graph3.csv
```

```
In[10]:= ListPlot[c, Joined → True]
```



## decomposition of curve by singular spectral analysis

```
In[11]:= c[[1]]
```

```
Out[11]= 0.303893
```

```
In[12]:= Length[c]
```

```
Out[12]= 200
```

```
Out[[#]] = 200
```

```
Out[[#]] = 200
```

```
Out[[#]] = 0
```

```
In[13]:= Dimensions[c]
```

```
Out[13]= {200}
```

```
Out[13]= {200}
```

```
Out[13]= {200}
```

```
In[14]:= m = Length[c]
```

```
Out[14]= 200
```

```
In[15]:= n = Floor[m/2]
```

```
Out[15]= 100
```

```
In[16]:= m - n + 1
```

```
Out[16]= 101
```

```
In[17]:= % + n
```

```
Out[17]= 201
```

```
In[18]:= x = N[Table[c[[i + j - 1]], {i, m - n + 1}, {j, n}]];
```

```
In[19]:= Dimensions[x]
```

```
Out[19]= {101, 100}
```

```
In[20]:= ? SingularValueDecomposition
```

Symbol

SingularValueDecomposition[ $m$ ] gives the singular value decomposition for a numerical matrix  $m$  as a list of matrices  $\{u, w, v\}$ , where  $w$  is a diagonal matrix and  $m$  can be written as  $u.w.Conjugate[Transpose[v]]$ .

SingularValueDecomposition[ $\{m, a\}$ ] gives the generalized singular value decomposition of  $m$  with respect to  $a$ .

SingularValueDecomposition[ $m, k$ ] gives the singular value decomposition associated with the  $k$  largest singular values of  $m$ .

SingularValueDecomposition[ $m, UpTo[k]$ ] gives the decomposition for the  $k$  largest singular values, or as many as are available.

SingularValueDecomposition[ $\{m, a\}, k$ ] gives the generalized singular value decomposition associated with the  $k$  largest singular values.

```
In[21]:= uu = SingularValueDecomposition[x];
```

```
In[22]:= Dimensions[uu]
```

```
Out[22]= {3}
```

```
In[23]:= u = uu[[1]];
```

```
In[24]:= w = uu[[2]];
```

```
In[25]:= v = uu[[3]];
```

```
In[26]:= Dimensions[u]
```

```
Out[26]= {101, 101}
```

```
In[27]:= Dimensions[w]
```

```
Out[27]= {101, 100}
```

```
In[28]:= Dimensions[v]
```

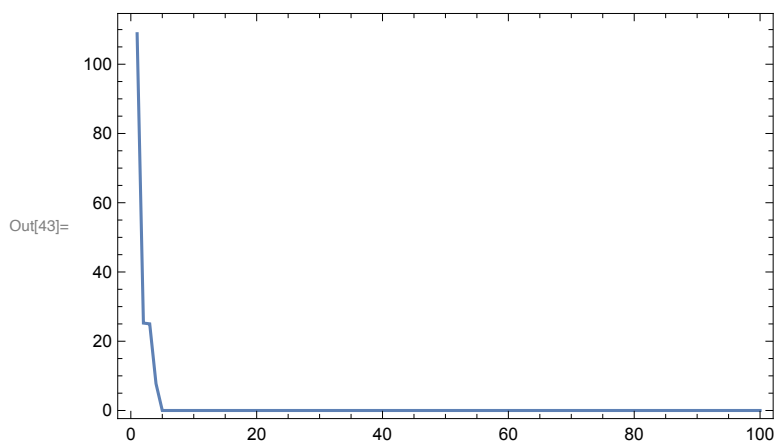
```
Out[28]= {100, 100}
```

```
In[42]:= Print[n]
```

```
100
```

## distribution of singular values

```
In[43]:= ListPlot[Table[{i, w[[i, i]]}, {i, n}],  
Joined -> True, PlotRange -> All, Axes -> False, Frame -> True]
```



```
In[30]:= sn[xx_] := Module[{i, j, k, n, n1, x, sum}, x = {};  
  {n1, n} = Dimensions[xx];  
  j = 0; sum = 0;  
  Do[Do[If[k ≤ n, sum = sum + xx[[i - k + 1, k]]; j = j + 1], {k, i}];  
  x = Append[x, sum/j]; sum = 0; j = 0, {i, n1}];  
  j = 0; sum = 0;  
  Do[Do[If[k ≤ n1, sum = sum + xx[[n1 - k + 1, k + i - 1]];  
    j = j + 1], {k, n - i + 1}];  
  x = Append[x, sum/j]; sum = 0; j = 0, {i, 2, n}];  
  Return[x]]
```

---

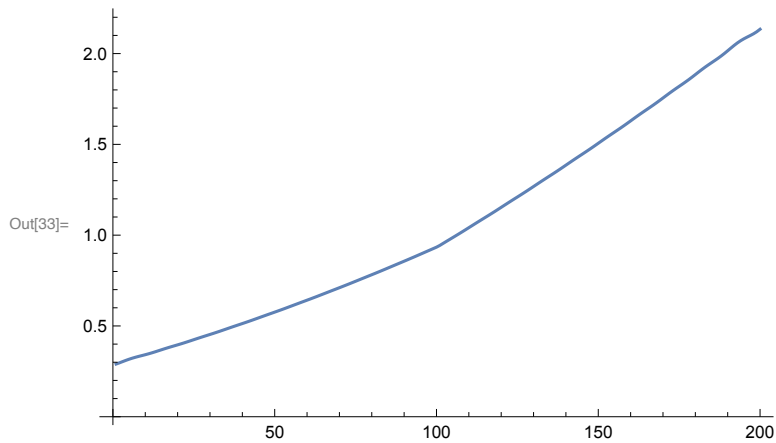
## 0

## trend

```
In[31]:= xx = Sum[w[[i, i]] × Outer[Times, Transpose[u][[i]], Transpose[v][[i]]], {i, 1}];
```

```
In[32]:= y1 = sn[xx];
```

```
In[33]:= ListPlot[y1, Joined → True, PlotRange → All]
```



## elements except trend

```
In[34]:= xx = Sum[w[[i, i]] × Outer[Times, Transpose[u][[i]], Transpose[v][[i]]], {i, 2, 3}];
```

```
In[35]:= y1 = sn[xx];
```

```
In[36]:= ListPlot[y1, Joined → True]
```

