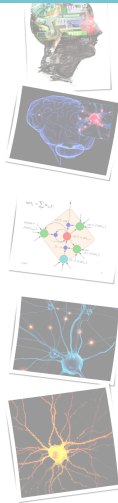


A (gentle) introduction to Reinforcement Learning (with some links to causal reasoning)

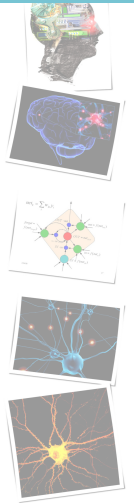
Spyros Samothrakis
Research Fellow, IADS
University of Essex

September 15, 2016



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Introduction & Motivation
Markov Decision Process (MDPs)
Planning
Model Free Reinforcement Learning
Causality



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WHAT IS REINFORCEMENT LEARNING?

- *Reinforcement learning is the study of how animals and artificial systems can learn to optimize their behavior in the face of rewards and punishments* – Peter Dyan, Encyclopedia of Cognitive Science
- **Not** supervised learning - the animal/agent is not provided with examples of optimal behaviour, it has to be discovered!
- **Not** unsupervised learning either - we have more guidance than just observations

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LINKS TO OTHER FIELDS

- It subsumes most artificial intelligence problems
- Forms the basis of most modern intelligent agent frameworks
- Ideas drawn from a wide range of contexts, including psychology (e.g., Skinner's "Operant Conditioning"), philosophy, neuroscience, operations research, **Cybernetics**

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EXAMPLES OF REINFORCEMENT LEARNING CLOSER TO CS

- Play backgammon/chess/go/poker/any game (at human or superhuman level)
- Helicopter control
- Learn how to walk/crawl/swim/cycle
- Elevator scheduling
- Optimising a petroleum refinery
- Optimal drug dosage

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THE MARKOV DECISION PROCESS

- The primary abstraction we are going to work with is the Markov Decision Process (MDP).
- MDPs capture the dynamics of a mini-world/universe/environment
- An MDP is defined as a tuple $\langle S, A, T, R, \gamma \rangle$ where:
 - S , $s \in S$ is a set of states
 - A , $a \in A$ is a set of actions
 - $R : S \times A$, $R(s, a)$ is a function that maps state-actions to rewards
 - $T : S \times S \times A$, with $T(s'|s, a)$ being the probability of an agent landing from state s to state s' after taking a
 - γ is a discount factor - the impact of time on rewards

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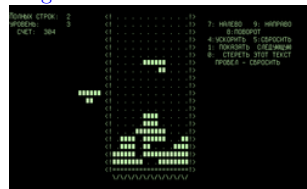
THE MARKOV PROPERTY AND STATES

- ▶ States represent sufficient statistics.
- ▶ Markov Property ensures that we only care about the present in order to act - we can safely ignore past states
- ▶ Think Tetris - all information can be captured by a single screen-shot

First DOS Version



Original Tetris



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AGENTS, ACTIONS AND TRANSITIONS

- ▶ An agent is an entity capable of actions
- ▶ An MDP can capture any environment that is inhabited either by
 - ▶ Exactly one agent
 - ▶ Multiple agents, but only one is adaptive
- ▶ Notice how actions are part of the MDP - notice also how the MDP is a “world model”
- ▶ The agent is just a “brain in a vat”
- ▶ The agent perceives states/rewards and outputs actions
- ▶ Transitions specify the effects of actions in the world (e.g., in Tetris, you push a button, the block spins)

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REWARDS AND THE DISCOUNT FACTOR

- ▶ Rewards describe state preferences
- ▶ Agent is happier in some states of the MDP (e.g., in Tetris when the block level is low, a fish in water, pacman with a high score)
- ▶ Punishment is just low/negative reward (e.g., being eaten in pacman)
- ▶ γ , the discount factor,
 - ▶ Describes the impact of time on rewards
 - ▶ “I want it now”, the lower γ is the less important future rewards are
- ▶ There are no “springs/wells of rewards” in the real world
 - ▶ What is “human nature”?

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EXAMPLES OF REWARD SCHEMES

- ▶ Scoring in most video games
- ▶ The distance a robot walked for a bipedal robot
- ▶ The amount of food an animal eats
- ▶ Money in modern societies
- ▶ Army Medals (“Gamification”)
- ▶ Vehicle routing
 - ▶ (-Fuel spent on a flight)
 - ▶ (+ Distance Covered)
- ▶ Cold/Hot
- ▶ Do you think there is an almost universal reward in modern societies?

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LONG TERM THINKING

- ▶ It might be better to delay satisfaction
- ▶ Immediate reward is not always the maximum reward
- ▶ In some settings there are no immediate rewards at all (e.g., most solitaire games)
- ▶ MDPs and RL capture this
- ▶ “Not going out tonight, study”
- ▶ Long term investment

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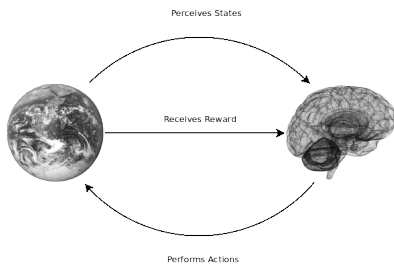
POLICY

- ▶ The MDP (the world) is populated by an agent (an actor)
- ▶ You can take actions (e.g., move around, move blocks)
- ▶ The type of actions you take under a state is called the *policy*
- ▶ $\pi : S \times A$, $\pi(s, a) = P(a|s)$, a probabilistic mapping between states and actions
- ▶ Finding an optimal policy is *mostly* what the RL problem is all about

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THE FULL LOOP

- ▶ See how the universe described by the MDP defines actions, not just states and transitions
- ▶ An agent needs to act upon what it perceives
- ▶ Notice the lack of body - “brain in a vat”. Body is assumed to be part of the world.



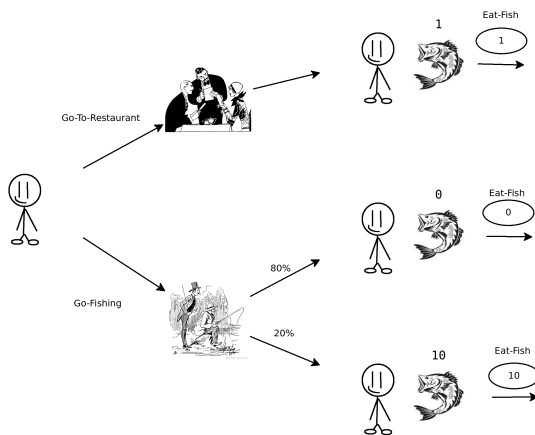
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FISHING TOON

- ▶ Assume a non-player character (let's call her *toon*)
- ▶ Toon is Hungry!
- ▶ Eating food is rewarding
- ▶ Has to choose between going fishing or going to the restaurant (to eat fish)
 - ▶ Fishing can get you better quality of fish (more reward), but you might also get no fish at all (no reward)!
 - ▶ Going to the restaurant is a low-risk, low-reward alternative

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FISHING TOON: PICTORIAL DEPICTION



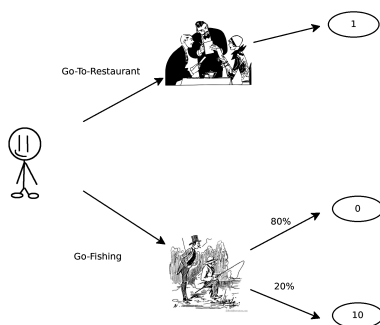
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EXPECTED REWARD

- ▶ Our toon has to choose between two different actions
- ▶ **Go-To-Restaurant** or **Go-Fishing**
- ▶ We assume that toon is interested in maximising *the expected sum of happiness/reward*
- ▶ We can help the toon reason using the tree backwards

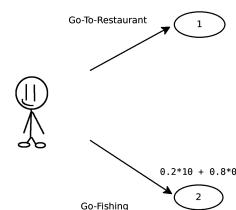
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REASONING BACKWARDS (1)



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REASONING BACKWARDS (2)



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CORRECT ACTION

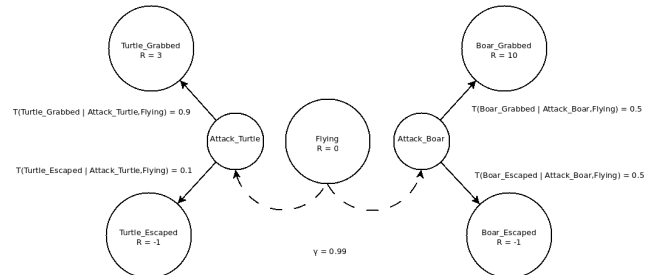
- ▶ Toon should go Go-Fishing
- ▶ **Would you do the same?**
- ▶ **Would a pessimist toon do the same?**
- ▶ We just went through the following equation:

$$Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \max_{a' \in A} Q^*(s', a')$$

- ▶ Looks intimidating - but it's really simple
- ▶ Let's have a look at another example
 - ▶ How about toon goes to the restaurant after failing to fish?
 - ▶ How would that change the reward structure?

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EXAMPLE MDP - EAGLEWORLD



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AGENT GOALS

- ▶ The agent's goal is to maximise its long term reward

$$\mathbb{E}_{\pi} \left[\sum_{t=0}^{\infty} \gamma^t R(s^t, a^t) \right]$$
- ▶ Risk Neutral Agent - think of the EagleWorld example
- ▶ Rewards can be anything, but most organisms receive rewards only in a very limited amount of states (e.g., fish in water)
- ▶ What if your reward signal is only money?
 - ▶ Sociopathic, egotistic, greed-is-good Gordon Gekko (*Wall Street*, 1987)
 - ▶ No concept of "externalities" - agents might wreak havoc for marginal reward gains
 - ▶ Same applies to all "compulsive agents" - think Chess

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SEARCHING FOR A GOOD POLICY

- ▶ One can possibly search through all combinations of policies until she finds the best
- ▶ Slow, does not work in larger MDPs
- ▶ Exploration/Exploitation dilemma
 - ▶ How much time/effort should be spend exploring for solutions?
 - ▶ How much time should be spend exploiting good solutions?

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PLANNING

- ▶ Who was doing the thinking in the previous example (You? The eagle?)
- ▶ An agent has access to model, i.e., has a copy of the MDP (the outside world) in its mind
- ▶ Using that copy, it tries to "think" what is the best route of action
- ▶ It then executes this policy on the real world MDP
- ▶ You can't really copy the world inside your head, but you can copy the dynamics
- ▶ "This and that will happen if I push the chair"
- ▶ Thinking, introspection. . .
- ▶ If the model is learned, sometimes it's called "Model Based RL"

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BELLMAN EXPECTATION EQUATIONS / BELLMAN BACKUPS

- ▶ The two most important equations related to MDP
- ▶ Recursive definitions
 - ▶ $V^{\pi}(s) = \sum_{a \in A} \pi(s, a) \left(R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^{\pi}(s') \right)$
 - ▶ $Q^{\pi}(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \sum_{a' \in A} \pi(s', a') Q^{\pi}(s', a')$
- ▶ **Called V-Value(s) (state-value function) and Q-Value(s) (state-action value function) respectively**
- ▶ Both calculate the expected rewards under a certain policy

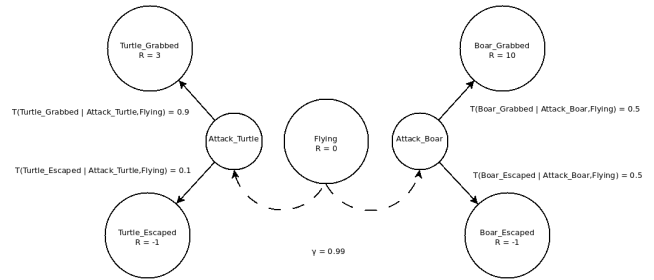
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LINK BETWEEN V^π AND Q^π

- V and Q are interrelated
- $V^\pi(s) = \sum_{a \in A} \pi(s, a) Q^\pi(s, a)$
- $Q^\pi(s, a) = R(s, a) + \sum_{s' \in S} T(s'|s, a) V^\pi(s')$

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EXAMPLE MDP - EAGLEWORLD - RANDOM POLICY



$$\begin{aligned} \pi(\text{Flying}, \text{Attack_Boar}) &= 0.5, \pi(\text{Flying}, \text{Attack_Turtle}) = 0.5 \\ Q(\text{Flying}, \text{Attack_Boar}) &= 0.99 * (10 * 0.5 + 0.5 * -1) = 4.455 \\ Q(\text{Flying}, \text{Attack_Turtle}) &= 0.99 * (0.9 * 3 + 0.1 * -1) = 2.574 \\ V^\pi(\text{Flying}) &= \\ 0.5, Q^\pi(\text{Flying}, \text{Attack_Turtle}) + 0.5, Q(\text{Flying}, \text{Attack_Boar}) &= 3.5145 \end{aligned}$$

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OPTIMAL POLICY AND THE BELLMAN OPTIMALITY EQUATION

- An optimal policy can be defined in terms of Q -values
- It is the policy that maximises Q values
- $V^*(s) = \max_{a \in A} R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^*(s')$
- $Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \max_{a' \in A} Q^*(s', a')$
- $\pi^*(s, a) = \begin{cases} 1 & \text{if } a = \arg \max_{a' \in A} Q^*(s, a') \\ 0 & \text{otherwise} \end{cases}$

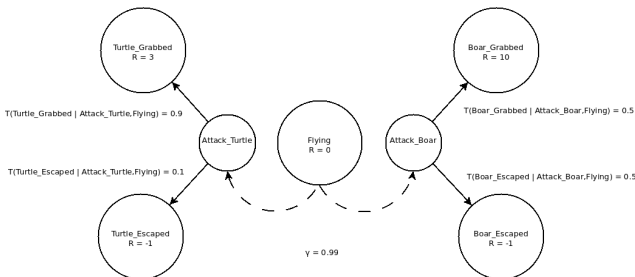
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LINK BETWEEN V^* AND Q^*

- Again, they are interrelated
- $V(s)^* = \max_{a \in A} Q^*(s, a)$
- $Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^*(s')$

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EXAMPLE MDP - EAGLEWORLD - OPTIMAL POLICY



$$\begin{aligned} Q(\text{Flying}, \text{Attack_Boar}) &= 0.99 * (10 * 0.5 + 0.5 * -1) = 4.455 \\ Q(\text{Flying}, \text{Attack_Turtle}) &= 0.99 * (0.9 * 3 + 0.1 * -1) = 2.574 \\ \pi^*(\text{Flying}, \text{Attack_Boar}) &= 1, \pi^*(\text{Flying}, \text{Attack_Turtle}) = 0 \\ V^*(\text{Flying}) &= Q(\text{Flying}, \text{Attack_Boar}) = 4.455 \end{aligned}$$

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AGENTS REVISITED

- An Agent can be composed of a number of things
- A policy
- A Q-Value/and or V-Value Function
- A Model of the environment (the MDP)
- Inference/Learning Mechanisms
- ...
- An agent has to be able to *create a policy* either on the fly or using Q-Values
- The Model/Q/V-Values serve as intermediate points towards constructing a policy

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SIMPLIFYING ASSUMPTIONS

- Assume deterministic transitions
- Thus, taking an action on a state will lead only to ONE other possible state for some action a_c
 - $T(s'|s, a_i) = \begin{cases} 1 & \text{if } a_i = a_c \\ 0 & \text{otherwise} \end{cases}$
 - $V^*(s) = \max_{a \in A} [R(s, a) + \gamma V^*(s')]$
 - $Q(s, a) = R(s, a) + \gamma \max_{a' \in A} Q(s', a')$
- It is easier now to solve for problems that have loops in them
- We can also attempt to learn Q-Values without a model!
- All we need in order to find the optimal policy is $Q(s, a)$

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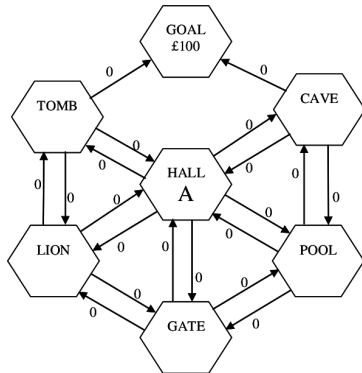
DETERMINISTIC Q-LEARNING (1)

- The policy is deterministic from start to finish
- We will use $\pi(s) = \arg \max_{a \in A} Q(s, a)$ to denote the optimal policy
- The algorithm now is:
 - Initialise all $Q(s, a)$ to low values
 - Repeat:
 - Select an action a using an exploration policy
 - $Q(s, a) \leftarrow R(s, a) + \gamma \max_{a' \in A} Q(s', a')$
 - $s \leftarrow s'$
- Also known as “Dynamic Programming”, “Value Iteration”

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AN EXAMPLE (1)

(From Paul Scott's ML lecture notes)



$$R(\text{HALL}, \text{To} - \text{CAVE}) = 0$$

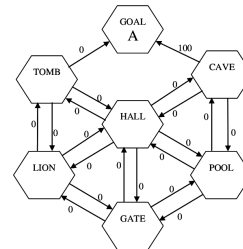
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AN EXAMPLE (2)

Next suppose the agent, now in state CAVE, selects action To - GOAL

$R(\text{CAVE}, \text{To} - \text{GOAL}) = 100$, $Q(\text{GOAL}, a) = 0$ for all actions (there are no actions)

Hence $Q(\text{CAVE}, \text{To} - \text{GOAL}) = 100 + \gamma * 0 = 100$



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AN EXAMPLE (3)

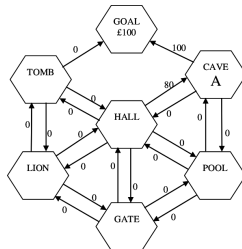
Let's start at hall again and select the same action To-CAVE

$R(\text{HALL}, \text{To} - \text{CAVE}) = 0$, $Q(\text{CAVE}, \text{GOAL}) = 100$

$Q(\text{CAVE}, a) = 0$ for all other actions a

Hence $\max_{a \in A} Q(\text{CAVE}, a) = 100$, if $\gamma = 0.8$,

$Q(\text{HALL}, \text{To} - \text{CAVE}) = 0 + \gamma * 100 = 80$



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EXPLORATION / EXPLOITATION

- How do we best explore?
- Choose actions at random - but this can be very slow
- ϵ - greedy is the most common method
- Act ϵ -greedily
 - $\pi^\epsilon(s, a) = \begin{cases} a = \arg \max_{a \in A} Q(s, a) & \text{if } 1 - \epsilon + \epsilon/|A| \\ U_a & \text{otherwise} \end{cases}$
 - ϵ -greedy means acting greedily with probability $1 - \epsilon$, random otherwise
- When you are done, act greedily $\pi(s) = \arg \max_{a \in A} Q(s, a)$

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ALGORITHMS FOR NON-DETERMINISTIC SETTINGS

- ▶ What can we do if the MDP is not deterministic?
- ▶ Q-learning
 - ▶ $Q(s, a) \leftarrow Q(s, a) + \eta \left[R(s, a) + \gamma \max_{a' \in A} Q(s', a') - Q(s, a) \right]$
- ▶ SARSA(0)
 - ▶ $Q(s, a) \leftarrow Q(s, a) + \eta [R(s, a) + \gamma Q(s', a') - Q(s, a)]$
- ▶ SARSA(1)/MC,
 - ▶ $Q(s, a) \leftarrow Q(s, a) + \eta [v_\tau - Q(s, a)]$
 - ▶ $v_\tau \leftarrow R(s, a) + \gamma R(s', a') + \dots \gamma^2 R(s'', a'') + \gamma^{\tau-1} R(s^\tau, a^\tau)$
- ▶ η is a small learning rate, e.g., $\eta = 0.001$

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SARSA VS Q-LEARNING VS MC

- ▶ MC: updated using the whole chain
 - ▶ Possibly works better when the markov property is violated
- ▶ SARSA: update based on the next action you actually took
 - ▶ On Policy learning
- ▶ Q-Learning: update based on the best possible next action
 - ▶ Will learn optimal policy even if acting off-policy

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MONTE CARLO CONTROL (1)

- ▶ Remember Q is just a mean/average
- ▶ MC (Naive Version)
 - ▶ Start at any state, initialise $Q_0(s, a)$ as you visit states/actions
 - ▶ Act ϵ -greedily
- ▶ Add all reward you have seen so far to

$$v_\tau^\tau = R(s', a') + \gamma R(s'', a'') + \gamma^2 R(s''', a''') + \gamma^{\tau-1} R(s^\tau, a^\tau)$$
 for episode i
- ▶ $Q_n(s, a) = E_{\pi^\epsilon}[v_\tau^i] = \frac{1}{n} \sum_{i=1}^n v_\tau^i$, where n is the times a state is visited

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MONTE CARLO CONTROL (2)

- ▶ ϵ -greedy means acting greedily $1 - \epsilon$, random otherwise
- ▶ Better to calculate mean incrementally

$$Q_n(s, a) = E_{\pi_n}[v_\tau^i]$$

$$Q_n(s, a) = \frac{1}{n} \sum_{i=1}^n v_\tau^i$$

$$Q_n(s, a) = \frac{1}{n} (v_\tau^1 + v_\tau^2 \dots v_\tau^{n-1} + v_\tau^n)$$

$$Q_n(s, a) = \frac{1}{n} \left(\sum_{i=1}^{n-1} v_\tau^i + v_\tau^n \right)$$

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MONTE CARLO CONTROL (3)

by definition

$$Q_{n-1}(s, a) = \frac{1}{n-1} \sum_{i=1}^{n-1} v_\tau^i \implies (n-1)Q_{n-1}(s, a) = \sum_{i=1}^{n-1} v_\tau^i$$

$$Q_n(s, a) = \frac{1}{n} ((n-1)Q_{n-1}(s, a) + v_\tau^n)$$

$$Q_n(s, a) = \frac{1}{n} (Q_{n-1}(s, a)n - Q_{n-1}(s, a) + v_\tau^n)$$

$$Q_n(s, a) = \frac{Q_{n-1}(s, a)n}{n} + \frac{-Q_{n-1}(s, a) + v_\tau^n}{n}$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \frac{\overbrace{v_\tau^n - Q_{n-1}(s, a)}^{\text{MC-Error}}}{n}$$

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MONTE CARLO CONTROL (4)

- ▶ But π^n changes continuously, so the distribution of rewards is non-stationary

$$Q_n(s, a) = Q_{n-1}(s, a) + \frac{1}{n} [v_\tau^n - Q_{n-1}(s, a)] \rightarrow \text{Bandit case}$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [v_\tau^n - Q_{n-1}(s, a)] \rightarrow \text{Full MDP case}$$

- ▶ A Bandit can be seen as MDP with a chain of length one (i.e. s) - like the initial EagleWorld, η is a learning rate (e.g., 0.001)

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MONTE CARLO CONTROL (5)

- ▶ Start at any state, initialise $Q_0(s, a)$ as you visit states/actions
- ▶ Act ϵ -greedily
- ▶ Wait until episode ends, i.e. a terminal state is hit - ϵ set to some low value, e.g., 0.1
- ▶ Add all reward you have seen so far to $v_\tau^i = R(s, a) + \gamma R(s', a') + \dots \gamma^2 R(s'', a'') + \gamma^{\tau-1} R(s^\tau, a^\tau)$ for episode i
- ▶ $Q_n(s, a) = Q_{n-1}(s, a) + \eta [v_\tau^n - Q_{n-1}(s, a)]$

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FROM MONTE CARLO CONTROL TO SARDA AND Q-LEARNING

- ▶ With MC we update using the rewards from the whole chain
- ▶ Can we update incrementally?

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [v_\tau^n - Q_{n-1}(s, a)]$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma R(s', a') + \dots \gamma^2 R(s'', a'') + \gamma^{\tau-1} R(s^\tau, a^\tau) - Q_{n-1}(s, a)]$$

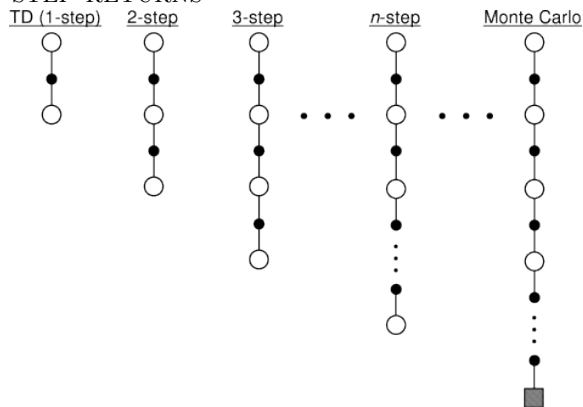
$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma (R(s', a') + \dots \gamma R(s'', a'') + \gamma^{\tau-2} R(s^\tau, a^\tau)) - Q_{n-1}(s, a)]$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma (v_\tau^n(s', a') - Q_{n-1}(s, a))]$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma Q_{n-1}(s', a') - Q_{n-1}(s, a)]$$

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N-STEP RETURNS



From Temporal Different to Monte Carlo (From Sutton & Burto)

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LET'S GO OVER THE TOON EXAMPLE, WITHOUT A MODEL

- ▶ ϵ - greedy, with $\epsilon = 0.1$

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FUNCTION APPROXIMATION

- ▶ There is usually some link between states
- ▶ We can train function approximators incrementally to model $Q(s, a)$
- ▶ We now have $Q(s, a; \theta)$, where θ are the parameters
- ▶ Examples include Linear function approximators, Neural Networks, n-tuple networks
- ▶ Not easy to do, few convergence guarantees
 - ▶ But with some effort, this works pretty well

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FAMOUS FUNCTION APPROXIMATION EXAMPLES

- ▶ Computer GO
- ▶ Car Driving
- ▶ Can you name another problem?

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<h2 data-bbox="99 275 250 302">PLATFORMS</h2> <ul data-bbox="144 459 724 537" style="list-style-type: none"> ▶ Let's look at open AI gym ▶ A lot of modern work is a combination of RL with Neural Networks <p data-bbox="753 756 797 772">49 / 56</p>	<h2 data-bbox="829 275 1520 302">RELATIONSHIP TO THE REST OF MACHINE LEARNING</h2> <ul data-bbox="875 369 1495 674" style="list-style-type: none"> ▶ How can one learn a model of the world? <ul data-bbox="920 405 1495 527" style="list-style-type: none"> ▶ Possibly by breaking it down into smaller, abstract chunks <ul data-bbox="966 436 1170 459" style="list-style-type: none"> ▶ Unsupervised Learning ▶ ... and learning what effects ones actions have the environment <ul data-bbox="966 501 1149 527" style="list-style-type: none"> ▶ Supervised Learning ▶ RL weaves all fields of Machine Learning (and possibly Artificial Intelligence) into one coherent whole ▶ The purpose of all learning is action! <ul data-bbox="920 627 1484 674" style="list-style-type: none"> ▶ You need to be able to recognise faces so you can create state ▶ ... and act on it <p data-bbox="1484 756 1528 772">50 / 56</p>
INTRODUCTION & MOTIVATION · MARKOV DECISION PROCESS (MDPs) · PLANNING · MODEL FREE REINFORCEMENT LEARNING · C	INTRODUCTION & MOTIVATION · MARKOV DECISION PROCESS (MDPs) · PLANNING · MODEL FREE REINFORCEMENT LEARNING · C
<h2 data-bbox="99 825 358 852">CAUSALITY (BONUS)</h2> <ul data-bbox="144 1016 586 1068" style="list-style-type: none"> ▶ We often colloquially say “A is caused by B” ▶ Can you discuss the meaning of this? <p data-bbox="753 1306 797 1323">51 / 56</p>	<h2 data-bbox="829 825 1081 852">COUNTERFACTUALS</h2> <ul data-bbox="875 974 1373 1134" style="list-style-type: none"> ▶ If I take action a I land on state s ▶ What if I don't take action a? ▶ “Experimenter forced you to pick up smoking” vs ▶ “Experimenter observed that you smoked” ▶ Will you get lung disease? ▶ The experimenter takes the actions vs observes <p data-bbox="1484 1306 1528 1323">52 / 56</p>
INTRODUCTION & MOTIVATION · MARKOV DECISION PROCESS (MDPs) · PLANNING · MODEL FREE REINFORCEMENT LEARNING · C	INTRODUCTION & MOTIVATION · MARKOV DECISION PROCESS (MDPs) · PLANNING · MODEL FREE REINFORCEMENT LEARNING · C
<h2 data-bbox="99 1375 355 1402">WHAT IS THE LINK?</h2> <ul data-bbox="144 1493 716 1724" style="list-style-type: none"> ▶ Off-policy evaluation learning ▶ Let's see an example <ul data-bbox="190 1556 586 1608" style="list-style-type: none"> ▶ Features are color of hair, height, smoking ▶ Reward is -1000 (lung disease), 1 (healthy) ▶ This would have been supervised learning if we knew the policy! ▶ Let's see a possible example of data ▶ Can you write down an example policy? <p data-bbox="753 1852 797 1869">53 / 56</p>	<h2 data-bbox="829 1375 992 1402">CONCLUSION</h2> <ul data-bbox="875 1543 1484 1650" style="list-style-type: none"> ▶ RL is a massive topic ▶ We have shown the tip of iceberg ▶ Rabbit hole goes <i>deep</i> - both on the application level and the theory level <p data-bbox="1484 1852 1528 1869">54 / 56</p>

FURTHER STUDY (1)

- ▶ **Tom Mitchell, Chapter 13**
- ▶ David Silver's UCL Course:
<http://www0.cs.ucl.ac.uk/staff/D.Silver/web/Teaching.html>
 - ▶ Some ideas in these lecture notes taken from there
 - ▶ Probably the best set of notes there is on the subject
 - ▶ Online at <http://www.machinelearningtalks.com/tag/rl-course/>
- ▶ Reinforcement Learning, by Richard S. Sutton and Andrew G. Barto
 - ▶ Classic book
 - ▶ Excellent treatment of most subjects

FURTHER STUDY (2)

- ▶ Artificial Intelligence: A Modern Approach by Stuart J. Russell and Peter Norvig
 - ▶ The Introductory A.I. Textbook
 - ▶ Chapters 16 and 21
- ▶ Algorithms for Reinforcement Learning by Csaba Szepesvari
 - ▶ Very "Mathematical", but a good resource that provides a very unified view of the field
- ▶ Reinforcement Learning: State-Of-The-Art by Marco Wiering (Editor), Martijn Van Otterlo (Editor)
 - ▶ Edited Volume