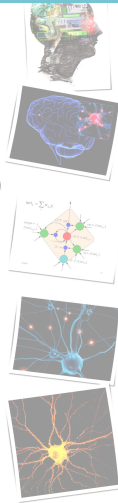


# A (gentle) introduction to Reinforcement Learning ( with some links to causal reasoning)

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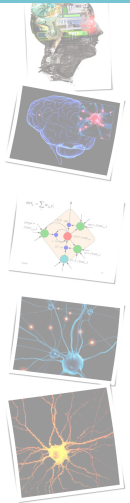
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Introduction & Motivation

Markov Decision Process (MDPs)

Planning

Model Free Reinforcement Learning



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## WHAT IS REINFORCEMENT LEARNING?

- *Reinforcement learning is the study of how animals and artificial systems can learn to optimize their behavior in the face of rewards and punishments* – Peter Dyan, Encyclopedia of Cognitive Science
- **Not** supervised learning - the animal/agent is not provided with examples of optimal behaviour, it has to be discovered!
- **Not** unsupervised learning either - we have more guidance than just observations

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## LINKS TO OTHER FIELDS

- It subsumes most artificial intelligence problems
- Forms the basis of most modern intelligent agent frameworks
- Ideas drawn from a wide range of contexts, including psychology (e.g., Skinner's "Operant Conditioning"), philosophy, neuroscience, operations research, **Cybernetics**

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## EXAMPLES OF REINFORCEMENT LEARNING CLOSER TO CS

- Play backgammon/chess/go/poker/any game (at human or superhuman level)
- Helicopter control
- Learn how to walk/crawl/swim/cycle
- Elevator scheduling
- Optimising a petroleum refinery
- Optimal drug dosage

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## THE MARKOV DECISION PROCESS

- The primary abstraction we are going to work with is the Markov Decision Process (MDP).
- MDPs capture the dynamics of a mini-world/universe/environment
- An MDP is defined as a tuple  $\langle S, A, T, R, \gamma \rangle$  where:
  - $S$ ,  $s \in S$  is a set of states
  - $A$ ,  $a \in A$  is a set of actions
  - $R : S \times A$ ,  $R(s, a)$  is a function that maps state-actions to rewards
  - $T : S \times S \times A$ , with  $T(s'|s, a)$  being the probability of an agent landing from state  $s$  to state  $s'$  after taking  $a$
  - $\gamma$  is a discount factor - the impact of time on rewards

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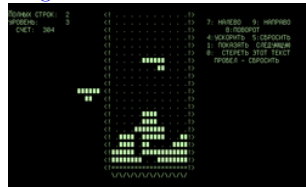
## THE MARKOV PROPERTY AND STATES

- ▶ States represent sufficient statistics.
- ▶ Markov Property ensures that we only care about the present in order to act - we can safely ignore past states
- ▶ Think Tetris - all information can be captured by a single screen-shot

First DOS Version



Original Tetris



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## AGENTS, ACTIONS AND TRANSITIONS

- ▶ An agent is an entity capable of actions
- ▶ An MDP can capture any environment that is inhabited either by
  - ▶ Exactly one agent
  - ▶ Multiple agents, but only one is adaptive
- ▶ Notice how actions are part of the MDP - notice also how the MDP is a “world model”
- ▶ The agent is just a “brain in a vat”
- ▶ The agent perceives states/rewards and outputs actions
- ▶ Transitions specify the effects of actions in the world (e.g., in Tetris, you push a button, the block spins)

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## REWARDS AND THE DISCOUNT FACTOR

- ▶ Rewards describe state preferences
- ▶ Agent is happier in some states of the MDP (e.g., in Tetris when the block level is low, a fish in water, pacman with a high score)
- ▶ Punishment is just low/negative reward (e.g., being eaten in pacman)
- ▶  $\gamma$ , the discount factor,
  - ▶ Describes the impact of time on rewards
  - ▶ “I want it now”, the lower  $\gamma$  is the less important future rewards are
- ▶ There are no “springs/wells of rewards” in the real world
  - ▶ What is “human nature”?

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## EXAMPLES OF REWARD SCHEMES

- ▶ Scoring in most video games
- ▶ The distance a robot walked for a bipedal robot
- ▶ The amount of food an animal eats
- ▶ Money in modern societies
- ▶ Army Medals (“Gamification”)
- ▶ Vehicle routing
  - ▶ (-Fuel spent on a flight)
  - ▶ (+ Distance Covered)
- ▶ Cold/Hot
- ▶ Do you think there is an almost universal reward in modern societies?

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## LONG TERM THINKING

- ▶ It might be better to delay satisfaction
- ▶ Immediate reward is not always the maximum reward
- ▶ In some settings there are no immediate rewards at all (e.g., most solitaire games)
- ▶ MDPs and RL capture this
- ▶ “Not going out tonight, study”
- ▶ Long term investment

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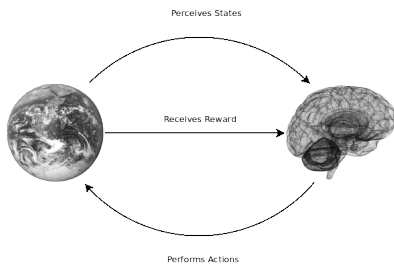
## POLICY

- ▶ The MDP (the world) is populated by an agent (an actor)
- ▶ You can take actions (e.g., move around, move blocks)
- ▶ The type of actions you take under a state is called the *policy*
- ▶  $\pi : S \times A$ ,  $\pi(s, a) = P(a|s)$ , a probabilistic mapping between states and actions
- ▶ Finding an optimal policy is *mostly* what the RL problem is all about

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## THE FULL LOOP

- ▶ See how the universe described by the MDP defines actions, not just states and transitions
- ▶ An agent needs to act upon what it perceives
- ▶ Notice the lack of body - “brain in a vat”. Body is assumed to be part of the world.



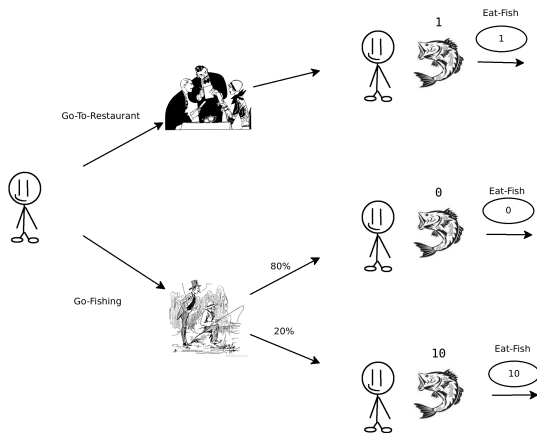
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## FISHING TOON

- ▶ Assume a non-player character (let's call her *toon*)
- ▶ Toon is Hungry!
- ▶ Eating food is rewarding
- ▶ Has to choose between going fishing or going to the restaurant (to eat fish)
  - ▶ Fishing can get you better quality of fish (more reward), but you might also get no fish at all (no reward)!
  - ▶ Going to the restaurant is a low-risk, low-reward alternative

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## FISHING TOON: PICTORIAL DEPICTION



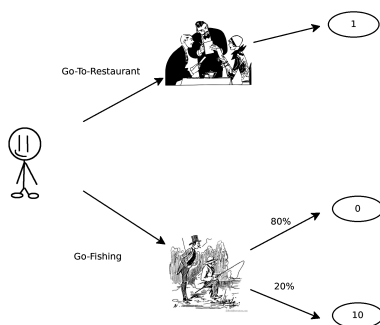
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## EXPECTED REWARD

- ▶ Our toon has to choose between two different actions
- ▶ **Go-To-Restaurant** or **Go-Fishing**
- ▶ We assume that toon is interested in maximising *the expected sum* of happiness/reward
- ▶ We can help the toon reason using the tree backwards

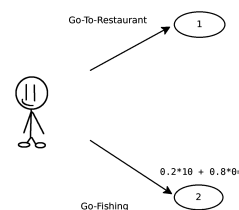
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## REASONING BACKWARDS (1)



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## REASONING BACKWARDS (2)



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## CORRECT ACTION

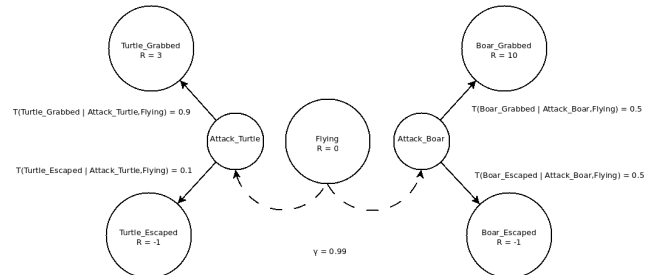
- ▶ Toon should go Go-Fishing
- ▶ **Would you do the same?**
- ▶ **Would a pessimist toon do the same?**
- ▶ We just went through the following equation:

$$Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \max_{a' \in A} Q^*(s', a')$$

- ▶ Looks intimidating - but it's really simple
- ▶ Let's have a look at another example
  - ▶ How about toon goes to the restaurant after failing to fish?
  - ▶ How would that change the reward structure?

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## EXAMPLE MDP - EAGLEWORLD



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## AGENT GOALS

- ▶ The agent's goal is to maximise its long term reward
 
$$\mathbb{E}_{\pi} \left[ \sum_{t=0}^{\infty} \gamma^t R(s^t, a^t) \right]$$
- ▶ Risk Neutral Agent - think of the EagleWorld example
- ▶ Rewards can be anything, but most organisms receive rewards only in a very limited amount of states (e.g., fish in water)
- ▶ What if your reward signal is only money?
  - ▶ Sociopathic, egotistic, greed-is-good Gordon Gekko (*Wall Street*, 1987)
  - ▶ No concept of "externalities" - agents might wreak havoc for marginal reward gains
  - ▶ Same applies to all "compulsive agents" - think Chess

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## SEARCHING FOR A GOOD POLICY

- ▶ One can possibly search through all combinations of policies until she finds the best
- ▶ Slow, does not work in larger MDPs
- ▶ Exploration/Exploitation dilemma
  - ▶ How much time/effort should be spend exploring for solutions?
  - ▶ How much time should be spend exploiting good solutions?

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## PLANNING

- ▶ Who was doing the thinking in the previous example (You? The eagle?)
- ▶ An agent has access to model, i.e., has a copy of the MDP (the outside world) in its mind
- ▶ Using that copy, it tries to "think" what is the best route of action
- ▶ It then executes this policy on the real world MDP
- ▶ You can't really copy the world inside your head, but you can copy the dynamics
- ▶ "This and that will happen if I push the chair"
- ▶ Thinking, introspection. . .
- ▶ If the model is learned, sometimes it's called "Model Based RL"

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## BELLMAN EXPECTATION EQUATIONS / BELLMAN BACKUPS

- ▶ The two most important equations related to MDP
- ▶ Recursive definitions
  - ▶  $V^{\pi}(s) = \sum_{a \in A} \pi(s, a) \left( R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^{\pi}(s') \right)$
  - ▶  $Q^{\pi}(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \sum_{a' \in A} \pi(s', a') Q^{\pi}(s', a')$
- ▶ **Called V-Value(s) (state-value function) and Q-Value(s) (state-action value function) respectively**
- ▶ Both calculate the expected rewards under a certain policy

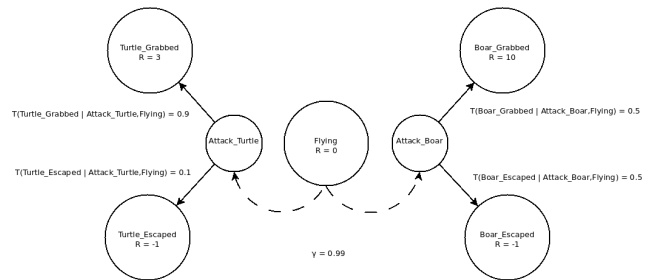
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LINK BETWEEN  $V^\pi$  AND  $Q^\pi$ 

- $V$  and  $Q$  are interrelated
- $V^\pi(s) = \sum_{a \in A} \pi(s, a) Q^\pi(s, a)$
- $Q^\pi(s, a) = R(s, a) + \sum_{s' \in S} T(s'|s, a) V^\pi(s')$

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## EXAMPLE MDP - EAGLEWORLD - RANDOM POLICY



$$\begin{aligned} \pi(\text{Flying}, \text{Attack\_Boar}) &= 0.5, \pi(\text{Flying}, \text{Attack\_Turtle}) = 0.5 \\ Q(\text{Flying}, \text{Attack\_Boar}) &= 0.99 * (10 * 0.5 + 0.5 * -1) = 4.455 \\ Q(\text{Flying}, \text{Attack\_Turtle}) &= 0.99 * (0.9 * 3 + 0.1 * -1) = 2.574 \\ V^\pi(\text{Flying}) &= \\ 0.5, Q^\pi(\text{Flying}, \text{Attack\_Turtle}) + 0.5, Q(\text{Flying}, \text{Attack\_Boar}) &= 3.5145 \end{aligned}$$

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## OPTIMAL POLICY AND THE BELLMAN OPTIMALITY EQUATION

- An optimal policy can be defined in terms of Q-values
- It is the policy that maximises  $Q$  values
- $V^*(s) = \max_{a \in A} R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^*(s')$
- $Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \max_{a' \in A} Q^*(s', a')$
- $\pi^*(s, a) = \begin{cases} 1 & \text{if } a = \arg \max_{a \in A} Q^*(s, a) \\ 0 & \text{otherwise} \end{cases}$

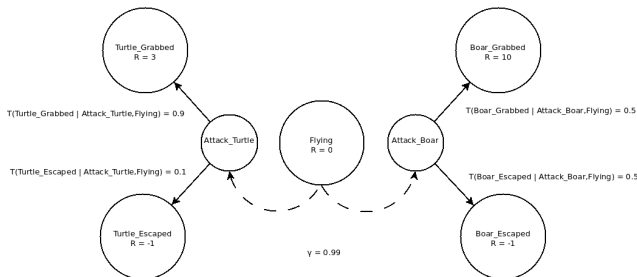
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LINK BETWEEN  $V^*$  AND  $Q^*$ 

- Again, they are interrelated
- $V(s)^* = \max_{a \in A} Q^*(s, a)$
- $Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^*(s')$

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## EXAMPLE MDP - EAGLEWORLD - OPTIMAL POLICY



$$\begin{aligned} Q(\text{Flying}, \text{Attack\_Boar}) &= 0.99 * (10 * 0.5 + 0.5 * -1) = 4.455 \\ Q(\text{Flying}, \text{Attack\_Turtle}) &= 0.99 * (0.9 * 3 + 0.1 * -1) = 2.574 \\ \pi^*(\text{Flying}, \text{Attack\_Boar}) &= 1, \pi^*(\text{Flying}, \text{Attack\_Turtle}) = 0 \\ V^*(\text{Flying}) &= Q(\text{Flying}, \text{Attack\_Boar}) = 4.455 \end{aligned}$$

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## AGENTS REVISITED

- An Agent can be composed of a number of things
- A policy
- A Q-Value/and or V-Value Function
- A Model of the environment (the MDP)
- Inference/Learning Mechanisms
- ...
- An agent has to be able to *create a policy* either on the fly or using Q-Values
- The Model/Q/V-Values serve as intermediate points towards constructing a policy

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## SIMPLIFYING ASSUMPTIONS

- Assume deterministic transitions
- Thus, taking an action on a state will lead only to ONE other possible state for some action  $a_c$ 
  - $T(s'|s, a_i) = \begin{cases} 1 & \text{if } a_i = a_c \\ 0 & \text{otherwise} \end{cases}$
  - $V^*(s) = \max_{a \in A} [R(s, a) + \gamma V^*(s')]$
  - $Q(s, a) = R(s, a) + \gamma \max_{a' \in A} Q(s', a')$
- It is easier now to solve for problems that have loops in them
- We can also attempt to learn Q-Values without a model!
- All we need in order to find the optimal policy is  $Q(s, a)$

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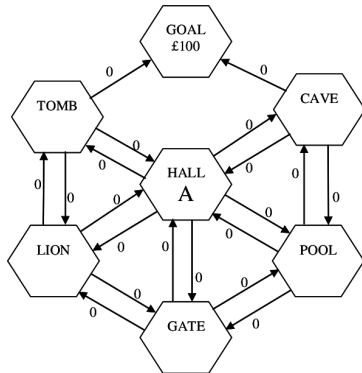
## DETERMINISTIC Q-LEARNING (1)

- The policy is deterministic from start to finish
- We will use  $\pi(s) = \arg \max_{a \in A} Q(s, a)$  to denote the optimal policy
- The algorithm now is:
  - Initialise all  $Q(s, a)$  to low values
  - Repeat:
    - Select an action  $a$  using an exploration policy
    - $Q(s, a) \leftarrow R(s, a) + \gamma \max_{a' \in A} Q(s', a')$
    - $s \leftarrow s'$
- Also known as “Dynamic Programming”, “Value Iteration”

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## AN EXAMPLE (1)

(From Paul Scott's ML lecture notes)



$$R(\text{HALL}, \text{To} - \text{CAVE}) = 0$$

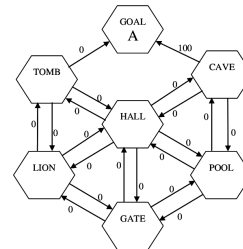
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## AN EXAMPLE (2)

Next suppose the agent, now in state CAVE, selects action To - GOAL

$R(\text{CAVE}, \text{To} - \text{GOAL}) = 100$ ,  $Q(\text{GOAL}, a) = 0$  for all actions (there are no actions)

Hence  $Q(\text{CAVE}, \text{To} - \text{GOAL}) = 100 + \gamma * 0 = 100$



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## AN EXAMPLE (3)

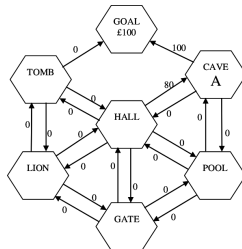
Let's start at hall again and select the same action To-CAVE

$R(\text{HALL}, \text{To} - \text{CAVE}) = 0$ ,  $Q(\text{CAVE}, \text{GOAL}) = 100$

$Q(\text{CAVE}, a) = 0$  for all other actions  $a$

Hence  $\max_{a \in A} Q(\text{CAVE}, a) = 100$ , if  $\gamma = 0.8$ ,

$Q(\text{HALL}, \text{To} - \text{CAVE}) = 0 + \gamma * 100 = 80$



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## EXPLORATION / EXPLOITATION

- How do we best explore?
- Choose actions at random - but this can be very slow
- $\epsilon$  - greedy is the most common method
- Act  $\epsilon$ -greedily
  - $\pi^\epsilon(s, a) = \begin{cases} a = \arg \max_{a \in A} Q(s, a) & \text{if } 1 - \epsilon + \epsilon/|A| \\ U_a & \text{otherwise} \end{cases}$
  - $\epsilon$ -greedy means acting greedily with probability  $1 - \epsilon$ , random otherwise
- When you are done, act greedily  $\pi(s) = \arg \max_{a \in A} Q(s, a)$

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## ALGORITHMS FOR NON-DETERMINISTIC SETTINGS

- ▶ What can we do if the MDP is not deterministic?
- ▶ Q-learning
  - ▶  $Q(s, a) \leftarrow Q(s, a) + \eta \left[ R(s, a) + \gamma \max_{a' \in A} Q(s', a') - Q(s, a) \right]$
- ▶ SARSA(0)
  - ▶  $Q(s, a) \leftarrow Q(s, a) + \eta [R(s, a) + \gamma Q(s', a') - Q(s, a)]$
- ▶ SARSA(1)/MC,
  - ▶  $Q(s, a) \leftarrow Q(s, a) + \eta [v_\tau - Q(s, a)]$
  - ▶  $v_\tau \leftarrow R(s, a) + \gamma R(s', a') + \dots \gamma^2 R(s'', a'') + \gamma^{\tau-1} R(s^\tau, a^\tau)$
- ▶  $\eta$  is a small learning rate, e.g.,  $\eta = 0.001$

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## SARSA VS Q-LEARNING VS MC

- ▶ MC: updated using the whole chain
  - ▶ Possibly works better when the markov property is violated
- ▶ SARSA: update based on the next action you actually took
  - ▶ On Policy learning
- ▶ Q-Learning: update based on the best possible next action
  - ▶ Will learn optimal policy even if acting off-policy

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## MONTE CARLO CONTROL (1)

- ▶ Remember Q is just a mean/average
- ▶ MC (Naive Version)
  - ▶ Start at any state, initialise  $Q_0(s, a)$  as you visit states/actions
  - ▶ Act  $\epsilon$ -greedily
- ▶ Add all reward you have seen so far to
 
$$v_\tau = R(s', a') + \gamma R(s'', a'') + \gamma^2 R(s''', a''') + \gamma^{\tau-1} R(s^\tau, a^\tau)$$
 for episode  $i$
- ▶  $Q_n(s, a) = E_{\pi^\epsilon}[v_\tau^i] = \frac{1}{n} \sum_{i=1}^n v_\tau^i$ , where  $n$  is the times a state is visited

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## MONTE CARLO CONTROL (2)

- ▶  $\epsilon$ -greedy means acting greedily  $1 - \epsilon$ , random otherwise
- ▶ Better to calculate mean incrementally

$$Q_n(s, a) = E_{\pi_n}[v_\tau^i]$$

$$Q_n(s, a) = \frac{1}{n} \sum_{i=1}^n v_\tau^i$$

$$Q_n(s, a) = \frac{1}{n} (v_\tau^1 + v_\tau^2 \dots v_\tau^{n-1} + v_\tau^n)$$

$$Q_n(s, a) = \frac{1}{n} \left( \sum_{i=1}^{n-1} v_\tau^i + v_\tau^n \right)$$

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## MONTE CARLO CONTROL (3)

by definition

$$Q_{n-1}(s, a) = \frac{1}{n-1} \sum_{i=1}^{n-1} v_\tau^i \implies (n-1)Q_{n-1}(s, a) = \sum_{i=1}^{n-1} v_\tau^i$$

$$Q_n(s, a) = \frac{1}{n} ((n-1)Q_{n-1}(s, a) + v_\tau^n)$$

$$Q_n(s, a) = \frac{1}{n} (Q_{n-1}(s, a)n - Q_{n-1}(s, a) + v_\tau^n)$$

$$Q_n(s, a) = \frac{Q_{n-1}(s, a)n}{n} + \frac{-Q_{n-1}(s, a) + v_\tau^n}{n}$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \frac{\overbrace{v_\tau^n - Q_{n-1}(s, a)}^{\text{MC-Error}}}{n}$$

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## MONTE CARLO CONTROL (4)

- ▶ But  $\pi^n$  changes continuously, so the distribution of rewards is non-stationary

$$Q_n(s, a) = Q_{n-1}(s, a) + \frac{1}{n} [v_\tau^n - Q_{n-1}(s, a)] \rightarrow \text{Bandit case}$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [v_\tau^n - Q_{n-1}(s, a)] \rightarrow \text{Full MDP case}$$

- ▶ A Bandit can be seen as MDP with a chain of length one (i.e.  $s$ ) - like the initial EagleWorld,  $\eta$  is a learning rate (e.g., 0.001)

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## MONTE CARLO CONTROL (5)

- ▶ Start at any state, initialise  $Q_0(s, a)$  as you visit states/actions
- ▶ Act  $\epsilon$ -greedily
- ▶ Wait until episode ends, i.e. a terminal state is hit -  $\epsilon$  set to some low value, e.g., 0.1
- ▶ Add all reward you have seen so far to  

$$v_\tau^i = R(s, a) + \gamma R(s', a') + \dots \gamma^2 R(s'', a'') + \gamma^{\tau-1} R(s^\tau, a^\tau)$$
for episode  $i$
- ▶  $Q_n(s, a) = Q_{n-1}(s, a) + \eta [v_\tau^n - Q_{n-1}(s, a)]$

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## FROM MONTE CARLO CONTROL TO SARDA AND Q-LEARNING

- ▶ With MC we update using the rewards from the whole chain
- ▶ Can we update incrementally?

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [v_\tau^n - Q_{n-1}(s, a)]$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma R(s', a') + \dots \gamma^2 R(s'', a'') + \gamma^{\tau-1} R(s^\tau, a^\tau) - Q_{n-1}(s, a)]$$

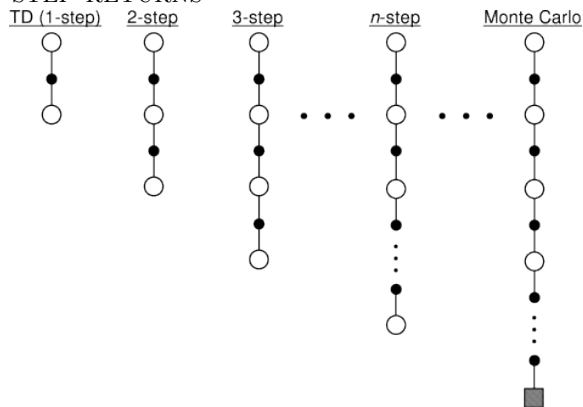
$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma (R(s', a') + \dots \gamma R(s'', a'') + \gamma^{\tau-2} R(s^\tau, a^\tau)) - Q_{n-1}(s, a)]$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma (v_\tau^{n, (s', a')}) - Q_{n-1}(s, a)]$$

$$Q_n(s, a) = Q_{n-1}(s, a) + \eta [R(s, a) + \gamma Q_{n-1}(s', a') - Q_{n-1}(s, a)]$$

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## N-STEP RETURNS



From Temporal Different to Monte Carlo (From Sutton &amp; Burto)

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## LET'S GO OVER THE TOON EXAMPLE, WITHOUT A MODEL

- ▶  $\epsilon$  - greedy, with  $\epsilon = 0.1$

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## FUNCTION APPROXIMATION

- ▶ There is usually some link between states
- ▶ We can train function approximators incrementally to model  $Q(s, a)$
- ▶ We now have  $Q(s, a; \theta)$ , where  $\theta$  are the parameters
- ▶ Examples include Linear function approximators, Neural Networks, n-tuple networks
- ▶ Not easy to do, few convergence guarantees
  - ▶ But with some effort, this works pretty well

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## FAMOUS FUNCTION APPROXIMATION EXAMPLES

- ▶ Computer GO
- ▶ Car Driving
- ▶ Can you name another problem?

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<h2 data-bbox="99 275 250 302">PLATFORMS</h2> <ul data-bbox="142 459 724 537" style="list-style-type: none"> <li>▶ Let's look at open AI gym</li> <li>▶ A lot of modern work is a combination of RL with Neural Networks</li> </ul> <p data-bbox="753 758 797 772">49 / 56</p>	<h2 data-bbox="831 275 1523 302">RELATIONSHIP TO THE REST OF MACHINE LEARNING</h2> <ul data-bbox="875 369 1498 674" style="list-style-type: none"> <li>▶ How can one learn a model of the world? <ul data-bbox="919 405 1498 527" style="list-style-type: none"> <li>▶ Possibly by breaking it down into smaller, abstract chunks <ul data-bbox="963 436 1174 457" style="list-style-type: none"> <li>▶ Unsupervised Learning</li> </ul> </li> <li>▶ ... and learning what effects ones actions have the environment <ul data-bbox="963 499 1149 520" style="list-style-type: none"> <li>▶ Supervised Learning</li> </ul> </li> </ul> </li> <li>▶ RL weaves all fields of Machine Learning (and possibly Artificial Intelligence) into one coherent whole</li> <li>▶ The purpose of all learning is action! <ul data-bbox="919 625 1484 674" style="list-style-type: none"> <li>▶ You need to be able to recognise faces so you can create state</li> <li>▶ ... and act on it</li> </ul> </li> </ul> <p data-bbox="1484 758 1528 772">50 / 56</p>
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<h2 data-bbox="99 827 358 854">CAUSALITY (BONUS)</h2> <ul data-bbox="142 1016 586 1066" style="list-style-type: none"> <li>▶ We often colloquially say “A is caused by B”</li> <li>▶ Can you discuss the meaning of this?</li> </ul> <p data-bbox="753 1310 797 1325">51 / 56</p>	<h2 data-bbox="831 827 1081 854">COUNTERFACTUALS</h2> <ul data-bbox="875 974 1373 1131" style="list-style-type: none"> <li>▶ If I take action <math>a</math> I land on state <math>s</math></li> <li>▶ What if I don't take action <math>a</math>?</li> <li>▶ “Experimenter forced you to pick up smoking” vs</li> <li>▶ “Experimenter observed that you smoked”</li> <li>▶ Will you get lung disease?</li> <li>▶ The experimenter takes the actions vs observes</li> </ul> <p data-bbox="1484 1310 1528 1325">52 / 56</p>
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<h2 data-bbox="99 1379 355 1407">WHAT IS THE LINK?</h2> <ul data-bbox="142 1495 716 1724" style="list-style-type: none"> <li>▶ Off-policy evaluation learning</li> <li>▶ Let's see an example <ul data-bbox="186 1558 586 1606" style="list-style-type: none"> <li>▶ Features are color of hair, height, smoking</li> <li>▶ Reward is -1000 (lung disease), 1 (healthy)</li> </ul> </li> <li>▶ This would have been supervised learning if we knew the policy!</li> <li>▶ Let's see a possible example of data</li> <li>▶ Can you write down an example policy?</li> </ul> <p data-bbox="753 1854 797 1869">53 / 56</p>	<h2 data-bbox="831 1379 992 1407">CONCLUSION</h2> <ul data-bbox="875 1543 1487 1648" style="list-style-type: none"> <li>▶ RL is a massive topic</li> <li>▶ We have shown the tip of iceberg</li> <li>▶ Rabbit hole goes <i>deep</i> - both on the application level and the theory level</li> </ul> <p data-bbox="1484 1854 1528 1869">54 / 56</p>

## FURTHER STUDY (1)

- ▶ **Tom Mitchell, Chapter 13**
- ▶ David Silver's UCL Course:  
<http://www0.cs.ucl.ac.uk/staff/D.Silver/web/Teaching.html>
  - ▶ Some ideas in these lecture notes taken from there
  - ▶ Probably the best set of notes there is on the subject
  - ▶ Online at <http://www.machinelearningtalks.com/tag/rl-course/>
- ▶ Reinforcement Learning, by Richard S. Sutton and Andrew G. Barto
  - ▶ Classic book
  - ▶ Excellent treatment of most subjects

## FURTHER STUDY (2)

- ▶ Artificial Intelligence: A Modern Approach by Stuart J. Russell and Peter Norvig
  - ▶ The Introductory A.I. Textbook
  - ▶ Chapters 16 and 21
- ▶ Algorithms for Reinforcement Learning by Csaba Szepesvari
  - ▶ Very "Mathematical", but a good resource that provides a very unified view of the field
- ▶ Reinforcement Learning: State-Of-The-Art by Marco Wiering (Editor), Martijn Van Otterlo (Editor)
  - ▶ Edited Volume