An introduction

to

Reinforcement Learning (with an intro to neural networks and causal reasoning)

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November 14, 2016



Markov Decision Process (MDPs)

Planning

Model Free Reinforcement Learning

Causality







#### What is Reinforcement Learning?

- ► Reinforcement learning is the study of how animals and artificial systems can learn to optimize their behavior in the face of rewards and punishments - Peter Dyan, Encyclopedia of Cognitive Science
- ▶ Not supervised learning the animal/agent is not provided with examples of optimal behaviour, it has to be discovered!
- ▶ Not unsupervised learning either we have more guidance than just observations

#### Links to other fields

- ▶ It subsumes most artificial intelligence problems
- ► Forms the basis of most modern intelligent agent frameworks
- ► Ideas drawn from a wide range of contexts, including psychology (e.g., Skinner's "Operant Conditioning"), philosophy, neuroscience, operations research, Cybernetics
- ▶ Modern Reinforcement Learning research has fused with Neural Networks Research

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## Examples of Reinforcement Learning Closer TO CS

- ▶ Play backgammon/chess/go/poker/any game (at human or superhuman level)
- ► Helicopter control
- ► Learn how to walk/crawl/swim/cycle
- ► Elevator scheduling
- ▶ Optimising a petroleum refinery
- ► Optimal drug dosage
- ► Create NPCs

## THE MARKOV DECISION PROCESS

- ightharpoonup The primary abstraction we are going to work with is the Markov Decision Process (MDP).
- ► MDPs capture the dynamics of a mini-world/universe/environment
- ▶ An MDP is defined as a tuple  $\langle S, A, T, R, \gamma \rangle$  where:
  - $S, s \in S$  is a set of states
  - ▶ A,  $a \in A$  is a set of actions
  - ▶  $R: S \times A$ , R(s, a) is a function that maps state-actions to rewards
  - ▶  $T: S \times S \times A$ , with T(s'|s,a) being the probability of an agent landing from state s to state s' after taking a
  - ightharpoonup is a discount factor the impact of time on rewards

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# INTRODUCTION & MOTIVATION MARKOV DECISION PROCESS (MDPS) PLANNING MODEL FREE REINFORCEMENT LEARNING

#### THE MARKOV PROPERTY AND STATES

#### ► States represent sufficient statistics.

- ► Markov Property ensures that we only care about the present in order to act we can safely ignore past states
- ► Think Tetris all information can be captured by a single screen-shot



► Pick a game



## AGENTS, ACTIONS AND TRANSITIONS

- ► An agent is an entity capable of actions
- ► An MDP can capture any environment that is inhabited either by
  - ► Exactly one agent
  - ▶ Multiple agents, but only one is adaptive
- ► Notice how actions are part of the MDP notice also how the MDP is a "world model"
- ► The agent is just a "brain in a vat"
- ▶ The agent perceives states/rewards and outputs actions
- ► Transitions specify the effects of actions in the world (e.g., in Tetris, you push a button, the block spins)

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More on States, agents and actions

▶ What would be state in the game?

▶ Do agents/NPCs have access to it?

▶ Do agents/NPCs have access to actions

► Do agents/NPCs have access to transitions?

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# LEARNING C INTRODUCTION & MOTIVATION MARKOV DECISION PROCESS (MDPS) PLANNING MODEL FREE REINFORCEMEN REWARDS AND THE DISCOUNT FACTOR

- ► Rewards describe state preferences
- ► Agent is happier in some states of the MDP (e.g., in Tetris when the block level is low, a fish in water, pacman with a high score)
- ► Punishment is just low/negative reward (e.g., being eaten in pacman)
- $\triangleright \gamma$ , the discount factor,
  - $\blacktriangleright$  Describes the impact of time on rewards
  - $\blacktriangleright$  "I want it now", the lower  $\gamma$  is the less important future rewards are
- ▶ There are no "springs/wells of rewards" in the real world
  - ► What is "human nature"?

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#### Examples of Reward Schemes

- ► Scoring in most video games
- $\blacktriangleright$  The distance a robot walked for a bipedal robot
- $\blacktriangleright$  The amount of food an animal eats
- ► Money in modern societies
- ► Army medals ("Gamification")
- ► Vehicle routing
  - ► (-Fuel spent on a flight)
  - ► (+ Distance Covered)
- ► Cold/Hot
- Do you think there is an almost universal reward in modern societies?

## Long Term Thinking

- ightharpoonup It might be better to delay satisfaction
- ▶ Immediate reward is not always the maximum reward
- ► In some settings there are no immediate rewards at all (e.g., most solitaire games)
- $\blacktriangleright$  MDPs and RL capture this
- ► "Not going out tonight, study"
- $\blacktriangleright$  Long term investment

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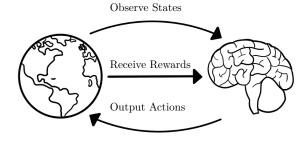
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#### Policy

- ► The MDP (the world) is populated by an agent (an actor)
- ► You can take actions (e.g., move around, move blocks)
- ► The type of actions you take under a state is called the *policy*
- $ightharpoonup \pi: S \times A, \, \pi(s,a) = P(a|s), \, a \text{ probabilistic mapping between}$ states and actions
- $\blacktriangleright$  Finding an optimal policy is mostly what the RL problem is all about

#### THE FULL LOOP

- ▶ See how the universe described by the MDP defines actions, not just states and transitions
- ► An agent needs to act upon what it perceives
- ▶ Notice the lack of body "brain in a vat". Body is assumed to be part of the world.

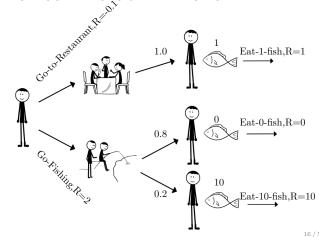


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#### FISHING TOON

- ► Assume a non-player character (let's call her toon)
- ► Toon is Hungry!
- $\blacktriangleright$  Eating food is rewarding
- ▶ Has to choose between going fishing or going to the restaurant (to eat fish)
  - ► Fishing can get you better quality of fish (more reward), but you might also get no fish at all (no reward)!
  - ▶ Going to the restaurant is a low-risk, low-reward alternative

## FISHING TOON: PICTORIAL DEPICTION



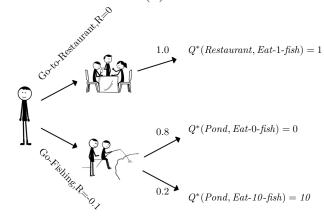
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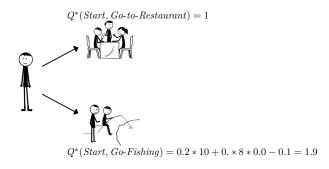
#### SUM OF EXPECTED REWARDS

- $\blacktriangleright$  Our toon has to choose between two different actions
- ► Go-To-Restaurant or Go-Fishing
- ▶ We assume that toon is interested in maximising the expected sum of happiness/reward
- ▶ We can help the toon reason using the tree backwards

## Reasoning Backwards (1)



## Reasoning Backwards (2)



## Correct Action

- ► Toon should go Go-Fishing
- Would you do the same?
- Would a pessimist toon do the same?
- ▶ We just went through the following equation:

$$Q^*(s,a) = R(s,a) + \gamma \sum_{s' \in S} T(s'|s,a) \max_{a' \in A} Q^*(s',a')$$

- ▶ Looks intimidating but it's really simple
- ▶ Let's have a look at another example
  - ► How about toon goes to the restaurant after failing to fish?
  - ▶ How would that change the reward structure?

## Agent Goals

- ▶ The agent's goal is to maximise its long term reward  $\mathbb{E}_{\pi} \left[ \sum_{t=0}^{\infty} \gamma^{t} R\left(s^{t}, a^{t}\right) \right]$
- ► Risk Neutral Agent think of the example above
- ▶ Rewards can be anything, but most agents receive rewards only in a very limited amount of states (e.g., fish in water)
- ▶ What if your reward signal is only money?
  - ► Sociopathic, egotistic, greed-is-good Gordon Gekko (Wall Street, 1987)
  - ▶ No concept of "externalities" agents might wreak havoc for marginal reward gains
  - ▶ Same applies to all "compulsive agents" think Chess

## Searching for a good Policy

- ▶ One can possibly search through all combinations of policies until she finds the best
- ► Slow, does not work in larger MDPs
- ► Exploration/Exploitation dilemma
  - ► How much time/effort should be spend exploring for solutions?
  - ▶ How much time should be spend exploiting good solutions?

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## PLANNING

- ► An agent has access to model, i.e. has a copy of the MDP (the outside world) in its mind
- ▶ Using that copy, it tries to "think" what is the best route of action
- ▶ It then executes this policy on the real world MDP
- You can't really copy the world inside your head, but you can copy the dynamics
- ▶ "This and that will happen if I push the chair"
- ► Thinking, introspection...
- ▶ If the model is learned, sometimes it's called "Model Based RL"

## Bellman Expectation Equations / Bellman BACKUPS

- ▶ The two most important equations related to MDP
- ► Recursive definitions
- $\begin{array}{l} \blacktriangleright \ V^\pi(s) = \sum\limits_{a \in A} \pi(s,a) \left( R(s,a) + \gamma \sum\limits_{s' \in S} T(s'|s,a) \, V^\pi(s') \right) \\ \blacktriangleright \ Q^\pi(s,a) = R(s,a) + \gamma \sum\limits_{s' \in S} T(s'|s,a) \sum\limits_{a' \in A} \pi(s',a') \, Q^\pi(s',a') \end{array}$
- ► Called V-Value(s) (state-value function) and Q-Value(s) (state-action value function) respectively
- ▶ Both calculate the expected rewards under a certain policy

## Link between $V^{\pi}$ and $Q^{\pi}$

## lacktriangledown V and Q are interrelated

$$V^{\pi}(s) = \sum_{a \in A} \pi(s, a) Q^{\pi}(s, a)$$

• 
$$Q^{\pi}(s, a) = R(s, a) + \sum_{s' \in S} T(s'|s, a) V^{\pi}(s')$$

► V-values are defined on states, Q-values on policies!

## OPTIMAL POLICY AND THE BELLMAN OPTIMALITY EQUATION

► An optimal policy can be defined in terms of Q-values

$$\blacktriangleright$$
 It is the policy that maximises  $Q$  values

• 
$$V^*(s) = \max_{a \in A} R(s, a) + \gamma \sum_{s \in C} T(s'|s, a) V^*(s')$$

• 
$$Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \max_{a' \in A} Q^*(s', a')$$

$$V^*(s) = \max_{a \in A} R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^*(s')$$

$$V^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) \max_{a' \in A} Q^*(s', a')$$

$$\pi^*(s, a) = \begin{cases} 1 & \text{if } a = \arg\max_{a \in A} Q^*(s, a) \\ 0 & \text{otherwise} \end{cases}$$

# Link between $V^*$ and $Q^*$

#### ► Again, they are interrelated

$$V(s)^* = \max_{a \in A} Q^*(s, a)$$

• 
$$Q^*(s, a) = R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^*(s')$$

- ▶ Let's assume that toon has another option
- ► She can go and buy and eat some meat with a reward of 1.5
- ▶ Or go down the fish route
- ► Write down the MDP
  - $\blacktriangleright$  Find out the new Q and V values with:
  - ▶ Toon acting randomly on choosing a decision point

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- ► Toon choosing action Go-Fishing
- ▶ Toon choosing action Go-to-Restaurant

#### Agents Revisited

- ▶ An Agent can be composed of a number of things
- ► A policy
- ► A Q-Value/and or V-Value Function
- ► A Model of the environment (the MDP)
- ► Inference/Learning Mechanisms
- ► An agent has to be able to discover a policy either on the fly or using Q-Values
- The Model/Q/V-Values serve as intermediate points towards constructing a policy
- Not all RL algorithms used that (but most do)...

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#### SIMPLIFYING ASSUMPTIONS

- ► Assume deterministic transitions
- ► Thus, taking an action on a state will lead only to ONE other possible state for some action  $a_c$

$$\begin{array}{l} \bullet \quad T(s'|s,a_i) = \left\{ \begin{array}{ll} 1 & \text{if } a_i = a_c \\ 0 & \text{otherwise} \end{array} \right. \\ \bullet \quad V^*(s) = \max_{a \in A} \left[ R(s,a) + \gamma \, V^*(s') \right] \\ \bullet \quad Q^*(s,a) = R(s,a) + \gamma \max_{a' \in A} Q(s',a') \end{array}$$

$$V^*(s) = \max [R(s, a) + \gamma V^*(s')]$$

$$P^*(s,a) = R(s,a) + \gamma \max_{a} Q(s',a')$$

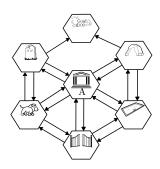
- ▶ It is easier now to solve for problems that have loops in them
- ▶ We can also attempt to learn Q-Values without a model!
- ▶ All we need in order to find the optimal policy is Q(s, a)

## DETERMINISTIC Q-LEARNING (1)

- ▶ The policy is deterministic from start to finish
- ▶ We will use  $\pi(s) = \arg \max Q(s, a)$  to denote the optimal policy
- ▶ The algorithm now is:
  - ▶ Initialise all Q(s, a) to low values
  - - ightharpoonup Select an action a using an exploration policy
    - $PQ(s, a) \leftarrow R(s, a) + \gamma \max_{a' \in A} Q(s', a')$
  - ► Also known as "Dynamic Programming", "Value Iteration"

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## AN EXAMPLE (1)



R(HALL, To-CAVE) = 0Q(CAVE, a) = 0 for all actions a

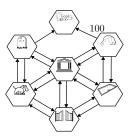
## An Example (2)

Next suppose the agent, now in state CAVE, selects action To - GOAL

 $R(CAVE, To\text{-}GOAL) = 100, \ Q(GOAL, a) = 0 \text{ for all actions (there})$ are no actions)

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Hence  $Q(CAVE, To\text{-}GOAL) = 100 + \gamma * 0 = 100$ 



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## An Example (3)

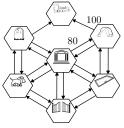
Let's start at hall again and select the same action To-CAVE

$$R(HALL, To - CAVE) = 0, \ Q(CAVE, GOAL) = 100$$

Q(CAVE, a) = 0 for all other actions a

Hence  $\max_{a} Q(CAVE, a) = 100$ , if  $\gamma = 0.8$ ,

 $Q(HALL, To - CAVE) = 0 + \gamma * 100 = 80$ 



## EXPLORATION / EXPLOITATION

- ▶ How do we best explore?
- Choose actions at random but this can be very slow
- $\epsilon greedy$  is the most common method
- ▶ Act ε-greedily

  - $\epsilon$ -greedy means acting greedily with probability  $1 \epsilon$ , random otherwise
- ▶ When you are done, act greedily  $\pi(s) = \arg \max Q(s, a)$

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# ALGORITHMS FOR NON-DETERMINISTIC SETTINGS

- ▶ What can we do if the MDP is not deterministic?

$$P Qs, a) \leftarrow Q(s, a) + \eta \left[ R(s, a) + \gamma \max_{a' \in A} Q(s', a') - Q(s, a) \right]$$

► SARSA(0)

- $\qquad \qquad \bullet \quad Q(s,a) \leftarrow \, Q(s,a) + \eta \left[ R(s,a) + \gamma \, Q(s',a') \, Q(s,a) \right]$
- ► SARSA(1)/MC,
  - $Q(s,a) \leftarrow Q(s,a) + \eta \left[ v_{\tau} Q(s,a) \right]$  $\qquad \qquad \mathbf{v}_{\tau} \leftarrow R(s,a) + \gamma R(s',a') + \ldots \gamma^2 R(s'',a'') + \gamma^{\tau-1} R(s^{\tau},a^{\tau})$
- ▶  $\eta$  is a small learning rate, e.g.,  $\eta = 0.001$

#### SARSA VS Q-LEARNING VS MC

- ▶ MC: updated using the whole chain
  - ▶ Possibly works better when the markov property is violated
- ► SARSA: update based on the next action you actually took
  - ▶ On Policy learning
- ▶ Q-Learning: update based on the best possible next action
  - ► Will learn optimal policy even if acting off-policy

## Monte Carlo Control (1)

- ► Remember Q is just a mean/average
- ► MC (Naive Version)
  - ▶ Start at any state, initialise  $Q_0(s, a)$  as you visit states/actions
  - ▶ Act ε-greedily
- ▶ Add all reward you have seen so far to  $\mathbf{v}_{\tau}^{i} = R(s', a') + \gamma R(s'', a'') + \gamma^{2} R(s''', a''') + \gamma^{\tau-1} R(s^{\tau}, a^{\tau})$  for
- ▶  $Q_n(s,a) = E_{\pi^{\epsilon}}[\mathbf{v}_{\tau}^i] = \frac{1}{n} \sum_{i=1}^n \mathbf{v}_{\tau}^i$ , where n is the times a state is

## Monte Carlo Control (2)

- $\triangleright$   $\epsilon$ -greedy means acting greedily  $1 \epsilon$ , random otherwise
- ▶ Better to calculate mean incrementaly

$$\begin{split} Q_n(s,a) &= E_{\pi_n}[\mathbf{v}_{\tau}^{\mathbf{i}}] \\ Q_n(s,a) &= \frac{1}{n} \sum_{i=1}^n \mathbf{v}_{\tau}^{\mathbf{i}} \\ Q_n(s,a) &= \frac{1}{n} \left( \mathbf{v}_{\mathbf{t}}^{\mathbf{t}} + \mathbf{v}_{\tau}^2 .... \mathbf{v}_{\tau}^{\mathbf{n}-1} + \mathbf{v}_{\tau}^{\mathbf{n}} \right) \\ Q_n(s,a) &= \frac{1}{n} \left( \sum_{i=1}^{n-1} \mathbf{v}_{\tau}^{\mathbf{i}} + \mathbf{v}_{\tau}^{\mathbf{n}} \right) \end{split}$$

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## Monte Carlo Control (3)

by definition

$$Q_{n-1}(s,a) = \frac{1}{n-1} \sum_{i=1}^{n-1} \mathbf{v}_{\tau}^{i} \implies (n-1)Q_{n-1}(s,a) = \sum_{i=1}^{n-1} \mathbf{v}_{\tau}^{i}$$

$$Q_{n}(s, a) = \frac{1}{n} ((n-1)Q_{n-1}(s, a) + \mathbf{v}_{\tau}^{\mathbf{n}})$$

$$Q_{n}(s, a) = \frac{1}{n} (Q_{n-1}(s, a)n - Q_{n-1}(s, a) + \mathbf{v}_{\tau}^{\mathbf{n}})$$

$$Q_{n}(s, a) = \frac{Q_{n-1}(s, a)n}{n} + \frac{-Q_{n-1}(s, a) + \mathbf{v}_{\tau}^{\mathbf{n}}}{n}$$

$$\mathbf{MC-Error}$$

$$Q_{n}(s, a) = Q_{n-1}(s, a) + \underbrace{\mathbf{v}_{\tau}^{\mathbf{n}} - Q_{n-1}(s, a)}_{n}$$

## Monte Carlo Control (4)

▶ But  $\pi^n$  changes continuously, so the distribution of rewards is non-stationary

$$\begin{split} Q_n(s,a) &= Q_{n-1}(s,a) + \frac{1}{n} \left[ \mathbf{v}_{\tau}^{\mathbf{n}} - Q_{n-1}(s,a) \right] \to \textbf{Bandit case} \\ Q_n(s,a) &= Q_{n-1}(s,a) + \eta \left[ \mathbf{v}_{\tau}^{\mathbf{n}} - Q_{n-1}(s,a) \right] \to \textbf{Full MDP case} \end{split}$$

► A Bandit can be seen as MDP with a chain of length one (i.e. s) - like the initial EagleWorld,  $\eta$  is a learning rate (e.g., 0.001)

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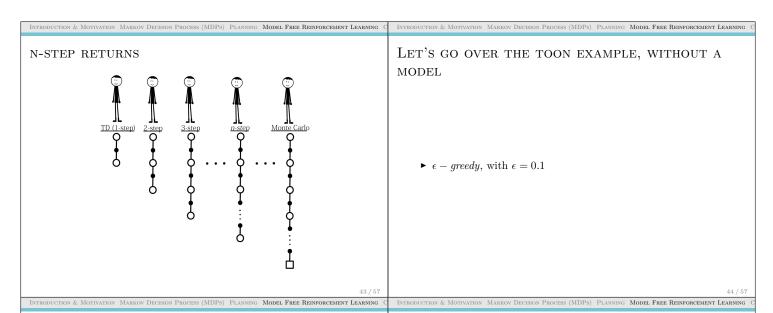
## Monte Carlo Control (5)

- ▶ Start at any state, initialise  $Q_0(s, a)$  as you visit states/actions
- Act  $\epsilon$ -greedily
- ▶ Wait until episode ends, i.e. a terminal state is hit  $\epsilon$  set to some low value, e.g., 0.1
- ▶ Add all reward you have seen so far to  $\mathbf{v}_{\tau}^{\rm i}=R(s,a)+\gamma R(s',a')+...\gamma^2 R(s'',a'')+\gamma^{\tau-1}R(s^\tau,a^\tau)$  for episode i
- $Q_n(s, a) = Q_{n-1}(s, a) + \eta \left[ v_{\tau}^n Q_{n-1}(s, a) \right]$

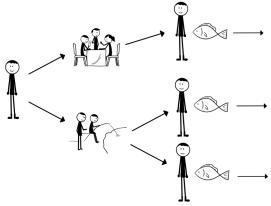
## FROM MONTE CARLO CONTROL TO SARSA AND Q-Learning

- ▶ With MC we update using the rewards from the whole chain
- ► Can we update incrementally?

$$\begin{split} Q_n(s,a) &= Q_{n-1}(s,a) + \eta \left[ \mathbf{v}_{\tau}^{\mathbf{n}} - Q_{n-1}(s,a) \right] \\ Q_n(s,a) &= Q_{n-1}(s,a) + \eta \left[ R(s,a) + \gamma R(s',a') + ... \gamma^2 R(s'',a'') + \gamma^{\tau-1} R(s^{\tau},a^{\tau}) - Q_{n-1}(s,a) \right] \\ Q_n(s,a) &= Q_{n-1}(s,a) + \eta \left[ R(s,a) + \gamma (R(s',a') + ... \gamma R(s'',a'') + \gamma^{\tau-2} R(s^{\tau},a^{\tau})) - Q_{n-1}(s,a) \right] \\ Q_n(s,a) &= Q_{n-1}(s,a) + \eta \left[ R(s,a) + \gamma (\mathbf{v}_{\tau}^{\mathbf{n},(s',a')}) - Q_{n-1}(s,a) \right] \\ Q_n(s,a) &= Q_{n-1}(s,a) + \eta \left[ R(s,a) + \gamma Q_{n-1}(s',a') - Q_{n-1}(s,a) \right] \end{split}$$



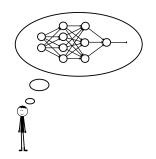
#### Model free toon



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## FUNCTION APPROXIMATION (1)

- ▶ There is usually some link between states
- ▶ We can train function approximators incrementally to model O(s, a)
- ▶ We now have  $Q(s, a; \theta)$ , where  $\theta$  are the parameters



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## FUNCTION APPROXIMATION (2)

- ▶ What are the links in states in Toon?
- ▶ Can we write down the Q-values in a more compact way?
- $\blacktriangleright$  Let's devise a tree to do this
- Examples include linear function approximators, neural networks, n-tuple networks
- ▶ Not easy to do, few convergence guarantees
  - $\blacktriangleright$  But with some effort, this works pretty well

# NEURAL NETWORKS AND FUNCTION APPROXIMATION

- Most common modern function approximation scheme is neural networks
- ► Can approximate almost any function
- ► We had a series of recent advances
- ► Go
- ► Atari

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More on neural networks
<ul> <li>▶ A function approximator loosely based on the brain</li> <li>▶ Main idea - a graph of neurons</li> <li>▶ Multiple layers</li> <li>▶ Of a certain type of neurons</li> <li>▶ Multiple types of training methods</li> </ul>
50 / 57  Introduction & Motivation Markov Decision Process (MDPs) Planning Model Free Reinforcement Learning C
Causality (bonus)
<ul> <li>▶ We often colliqually say "A is caused by B"</li> <li>▶ Can you discuss the meaning of this?</li> </ul>
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Introduction & Motivation Markov Decision Process (MDPs) Planning Model Free Reinforcement Learning C  What is the link?
<ul> <li>▶ Off-policy evaluation learning</li> <li>▶ Let's see an example</li> <li>▶ Features are colour of hair, height, smoking</li> <li>▶ Reward is -1000 (lung disease), 1 (healthy)</li> <li>▶ This would have been supervised learning if we knew the policy!</li> <li>▶ Let's see a possible example of data</li> <li>▶ Can you write down an example policy?</li> </ul>

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#### Introduction & Motivation Markov Decision Process (MDPs) Planning Model Free Reinforcement Learning

## Conclusion

### $\blacktriangleright$ RL is a massive topic

- $\blacktriangleright$  We have shown the tip of ice berg
- $\blacktriangleright$  Rabbit hole goes deep both on the application level and the theory level

## FURTHER STUDY (1)

- ► Tom Mitchell, Chapter 13
- ► David Silver's UCL Course: http://www0.cs.ucl.ac.uk/staff/D.Silver/web/Teaching.html
  - $\blacktriangleright$  Some ideas in these lecture notes taken from there
  - $\,\blacktriangleright\,$  Probably the best set of notes there is on the subject
  - ► Online at http://www.machinelearningtalks.com/tag/rl-course/
- ► Reinforcement Learning, by Richard S. Sutton and Andrew G. Barto
  - ► Classic book
  - $\blacktriangleright$  Excellent treatment of most subjects

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## FURTHER STUDY (2)

- ► Artificial Intelligence: A Modern Approach by Stuart J. Russell and Peter Norvig
  - $\blacktriangleright\,$  The Introductory A.I. Textbook
  - ► Chapters 16 and 21
- ► Algorithms for Reinfocement Learning by Csaba Szepesvari
  - ► Very "Mathematical", but a good resource that provides a very unified view of the field
- ► Reinforcement Learning: State-Of-The-Art by Marco Wiering (Editor), Martijn Van Otterlo (Editor)
  - ► Edited Volume

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