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Let  $S$  be a closed surface with a negatively curved Riemannian metric and consider its unit tangent bundle  $T^1S$ . The *geodesic flow* on  $T^1S$  is the flow  $\phi^t$  that takes the time-0 tangent of each unit-speed geodesic  $\gamma$  to its time- $t$  tangent at time  $t$ , i.e.  $\phi^t(\gamma'(0)) = \gamma'(t)$ . In particular, the orbits of the geodesic flow are in one-to-one correspondence with the geodesics on  $S$ .

From the general theory of *Anosov flows*, it is known that the geodesic flow admits a *Markov partition*. These can be thought of as directed graphs  $\Phi$  that ‘remember’ the dynamics of the flow. For example, the closed orbits of the flow are in correspondence with the cycles of  $\Phi$ . One can then attempt to study the closed geodesics on  $S$  by just studying such a graph  $\Phi$ .

However, one difficulty with this approach was that explicit examples of such Markov partitions were hard to come by. In a recent preprint, I reduced this barrier by constructing a Markov partition given any multicurve that cuts  $S$  up into  $n \geq 4$ -gons. The corresponding graph is determined by its projection in each  $n$ -gon, for which a recipe can be given. The picture on the left is such a projected graph for  $n = 9$ .