

Problem 1. Suppose that X is a discrete random variable with $P(X = 1) = \theta$ and $P(X = 2) = 1 - \theta$. Three independent observations of X are made: $x_1 = 1, x_2 = 2, x_3 = 2$.

- a. Find the method of moments estimate of θ .
- b. Find the MLE of θ .
- c. Find the asymptotic variance of MLE.

Problem 2. Consider an i.i.d. sample of random variables with density function

$$f(x|\sigma) = \frac{1}{2\sigma} \exp\left(-\frac{|x|}{\sigma}\right)$$

- a. Find the method of moments estimate of σ .
- b. Find the MLE of σ .
- c. Find the asymptotic variance of MLE.