

1. Suppose that  $y_i = \mu + \epsilon_i$ , where  $i = 1, \dots, n$  and the  $\epsilon_i$  are independent errors with mean and variance  $\sigma^2$ . Find the least squares estimate of  $\mu$ .

2. Find the least square estimate of  $\beta$  for fitting the line  $y = \beta x$  to points  $(x_i, y_i)$  where  $i = 1, \dots, n$ .

3. Suppose that we want to predict the value of a new observation,  $Y_0$  at  $x_0$ ,

$$Y_0 = \beta_0 + \beta_1 x_0 + \epsilon_0$$

by the estimate

$$\hat{Y}_0 = \hat{\beta}_0 + \hat{\beta}_1 x_0$$

- (a) Find the MSE of  $\hat{Y}_0$