

1. Let  $X \sim Geo(p)$ . Derive a likelihood ratio test of hypothesis  $H_0 : p = 1/2$  versus  $H_1 : p = 1/3$ .
2. Let  $X_1, \dots, X_n$  be i.i.d. random variables from a double exponential distribution with density  $f(x) = \frac{1}{2}\lambda \exp(-\lambda|x|)$ . Derive a likelihood ratio test of hypothesis  $H_0 : \lambda = \lambda_0$  versus  $H_1 : \lambda = \lambda_1$ , where  $\lambda_1 > \lambda_0$ .