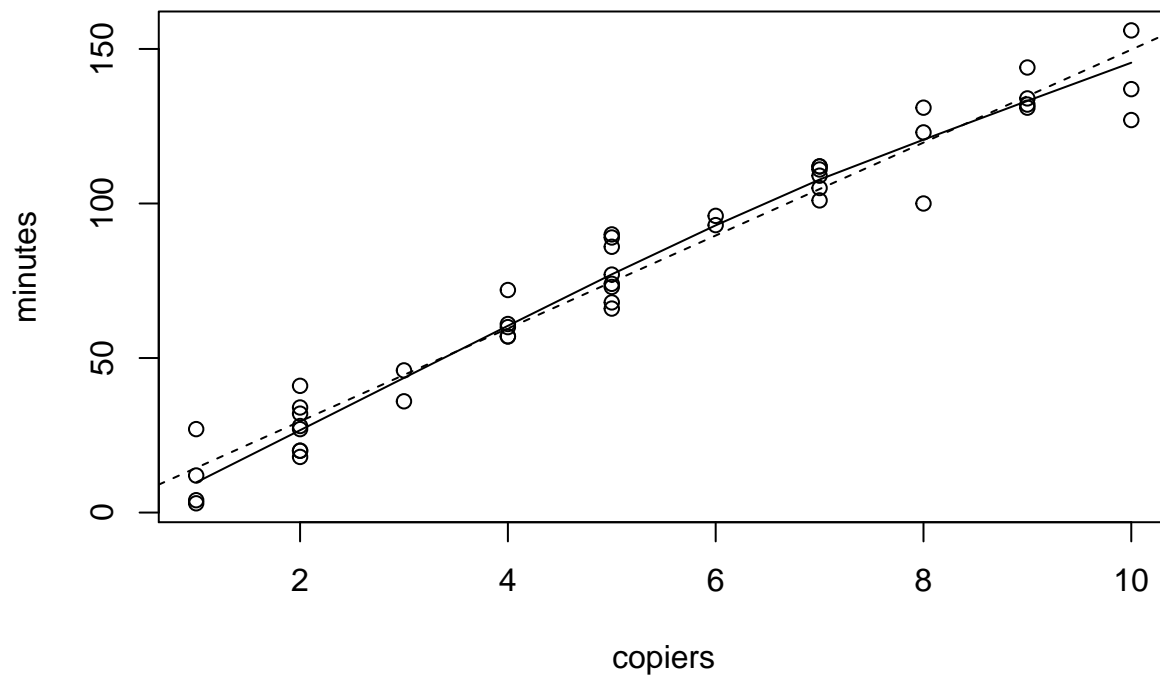


STAT GR5205 – Section 005 HW1 Bo Rong br2498

```
#1.
filename <- "~/Downloads/copier_maintenance.txt"
Data <- read.table(file=filename, header=T)
#(a)
plot(minutes ~ copiers, data=Data)
low.fit <- lowess(x=Data$copiers, y=Data$minutes)
lines(low.fit)

#The simple linear regression model seems appropriate, since average minutes
#of service time appears to be a linear function of number of copiers serviced.

#(b)
ls.fit <- lm(minutes ~ copiers, data=Data)
abline(ls.fit, lty=2)
```



```
summary(ls.fit)

##
## Call:
## lm(formula = minutes ~ copiers, data = Data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -22.7723  -3.7371   0.3334   6.3334  15.4039
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
##
```

```
## (Intercept)  -0.5802      2.8039  -0.207    0.837
## copiers      15.0352      0.4831  31.123   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.914 on 43 degrees of freedom
## Multiple R-squared:  0.9575, Adjusted R-squared:  0.9565
## F-statistic: 968.7 on 1 and 43 DF,  p-value: < 2.2e-16
```

*#Hence the regression line is $\hat{Y} = -0.5802 + 15.0352x$, the estimated regression function
#fit good to the data.*

#(c)The service time increases $b_1 = 15.0352$ minutes by each copier services.

#(d) $b_0 = -0.5802$ maybe the starting time, which is the time before works.

*#(e)estimate of the mean service time for calls with $x = 5$ copiers by
$\hat{Y} = -0.5802 + 15.0352(5) = 74.596$ minutes*

*#(f)predict of the service time for a single call with $x = 5$ copiers by
$\hat{Y} = -0.5802 + 15.0352(5) = 74.596$ minutes*

```
#(g)
e <- residuals(ls.fit)
e
```

```
##      1      2      3      4      5      6
## -9.4903394  0.4391645  1.4744125  11.5096606 -2.4550914 -12.7723238
##      7      8      9     10     11     12
## -6.5960836 14.4039164 -10.4550914  2.5096606  9.2629243  6.2276762
##     13     14     15     16     17     18
##  3.3686684 -8.5255875 12.4391645 -19.7018277  0.3334204 11.2981723
##     19     20     21     22     23     24
## -22.7723238 -2.5608355 -8.5960836 -3.6665796  4.3334204 -0.5960836
##     25     26     27     28     29     30
## -0.7370757  7.3334204 -11.4903394 -1.5960836  6.3334204  6.3686684
##     31     32     33     34     35     36
##  3.2981723 15.4039164 -9.4903394 -1.4903394 -11.4550914 -2.5608355
##     37     38     39     40     41     42
## 11.4039164 -2.7370757  7.3334204 12.5449086 -3.7370757  4.5096606
##     43     44     45
## -2.4903394  1.4391645  2.4039164
```

```
sum(e)
```

```
## [1] -1.176836e-14
```

*#sum(e)=-1.176836e-14 which is zero.The sum of squared residuals is the
#min value of quantity Q.*

```
#(h)Estimate variance(error) by the Residual standard error= 8.914 minutes.
```

```
#2.
```

```
#(a)
```

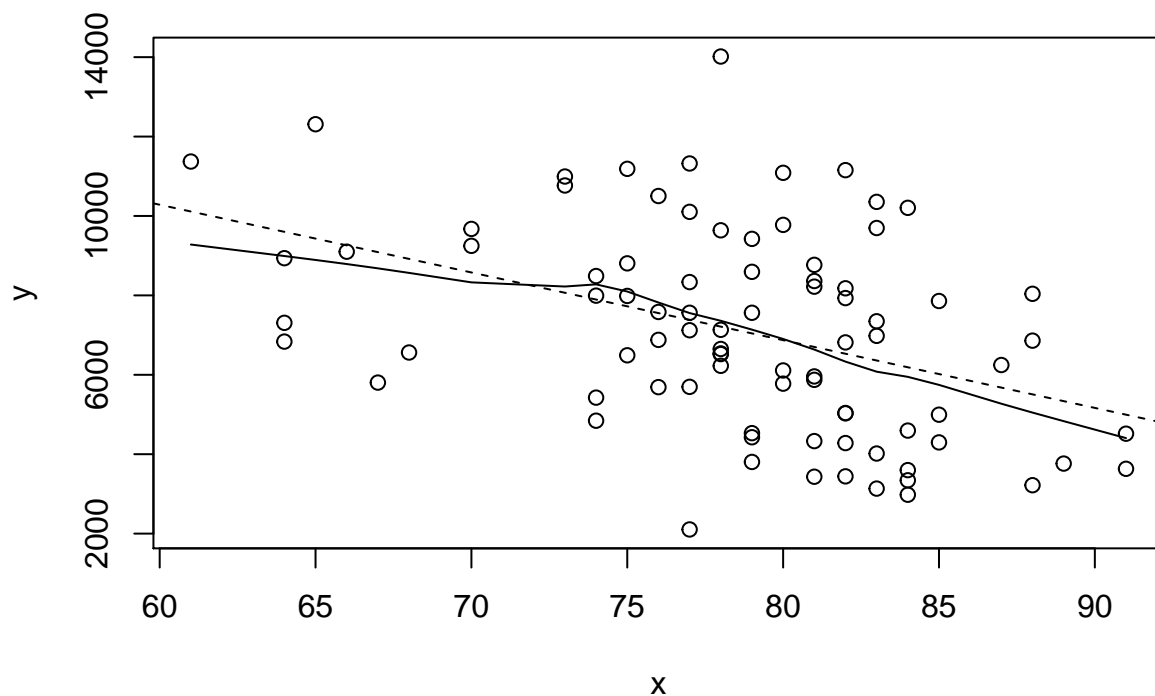
```
filename <- "~/Downloads/crime_rates.txt"
Data <- read.table(file=filename, header=T)
plot(y ~ x, data=Data)
low.fit <- lowess(x=Data$x, y=Data$y)
lines(low.fit)
```

```
#yes, the simple linear regression model seems appropriate for these data.
```

```
#Because the annual crime rate appears to be a linear function of the percentage of  
#individuals which has at least a high-school diploma.
```

```
#(b)
```

```
ls.fit <- lm(y ~ x, data=Data)
abline(ls.fit, lty=2)
```



```
summary(ls.fit)
```

```
##
```

```
## Call:
```

```
## lm(formula = y ~ x, data = Data)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max
```

```
## -5278.3 -1757.5  -210.5  1575.3  6803.3
```

```
##
```

```
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept) 20517.60    3277.64   6.260 1.67e-08 ***
## x           -170.58     41.57  -4.103 9.57e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2356 on 82 degrees of freedom
## Multiple R-squared:  0.1703, Adjusted R-squared:  0.1602
## F-statistic: 16.83 on 1 and 82 DF,  p-value: 9.571e-05

#regression line is  $\hat{Y} = 20517.60 - 170.58x$ 

#(c)
#(i) High-school graduation rates lower by 5 percentage points will have
#a higher crime rate by  $5(170.58) = 853$  crimes per 100,000.

#(ii) Estimation of the crime rate for a county with an 80% high-school
#graduation rate will be  $20517.60 - 170.58(80) = 6872$  crimes per 100,000.

#(iii)
Data[6,]
```

```
##      y  x
## 6 9100 66
```

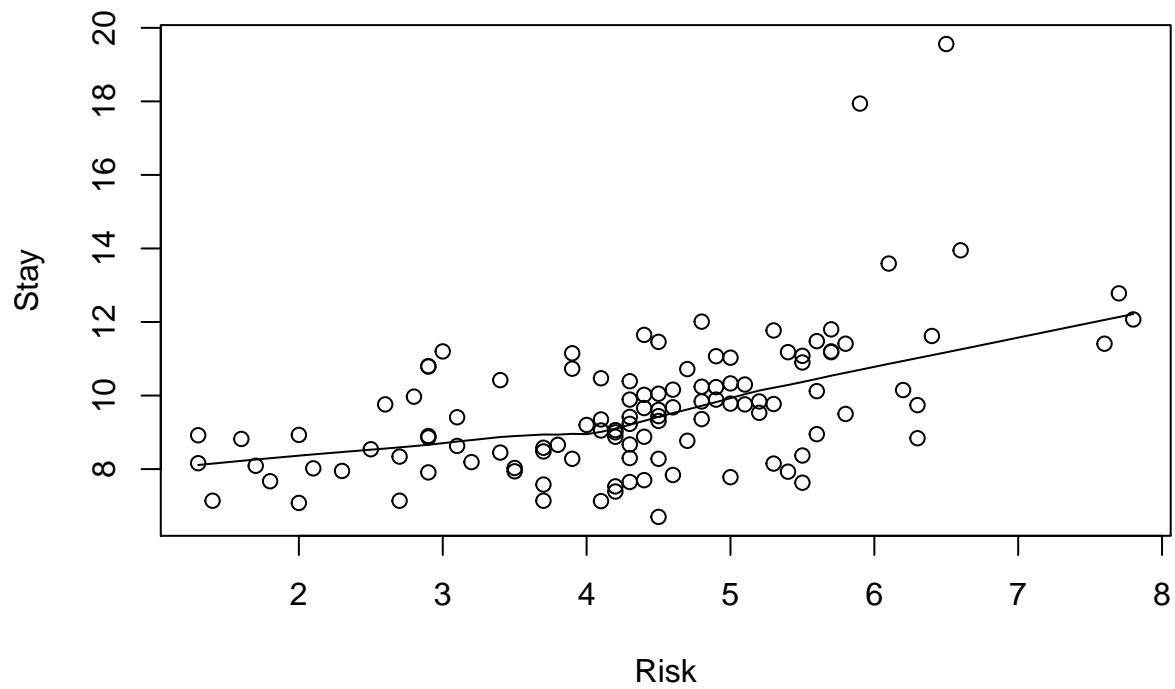
```
#So the random error term for the sixth county is  $e_6 = 9100 - [20517.60 - 170.58(66)]$ 
# = -159.64.

#(iv)
anova(ls.fit)
```

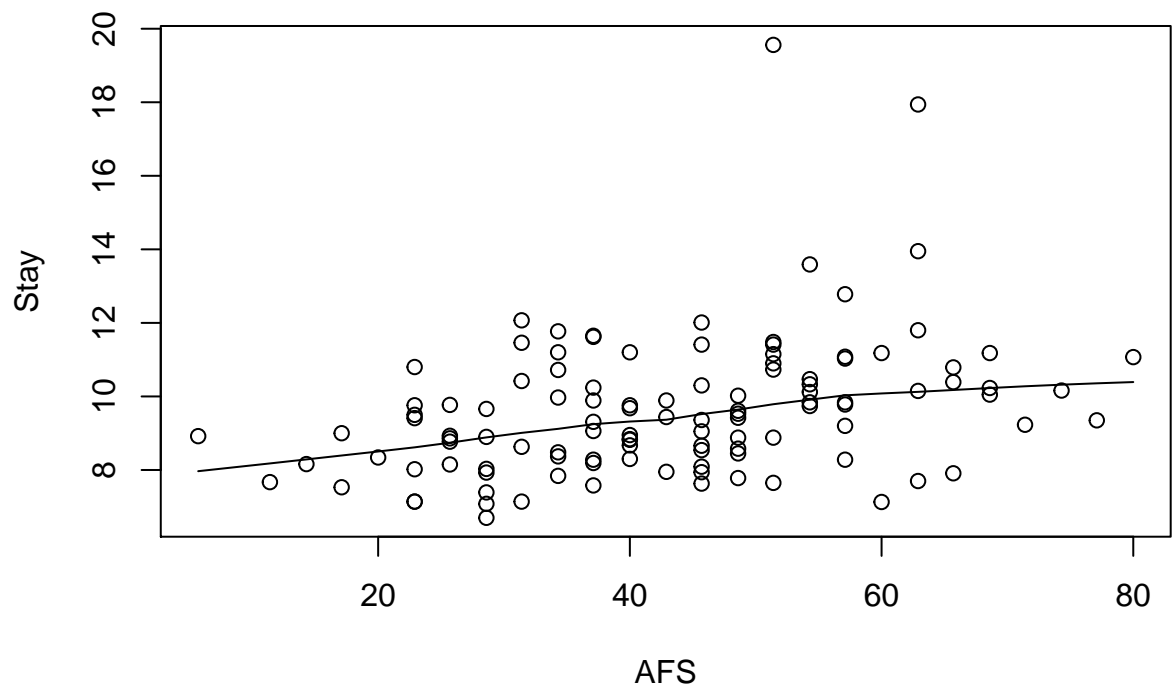
```
## Analysis of Variance Table
##
## Response: y
##           Df      Sum Sq  Mean Sq F value    Pr(>F)
## x           1  93462942  93462942   16.834 9.571e-05 ***
## Residuals  82  455273165   5552112
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
# the error term = MSE = 5,552,112.
```

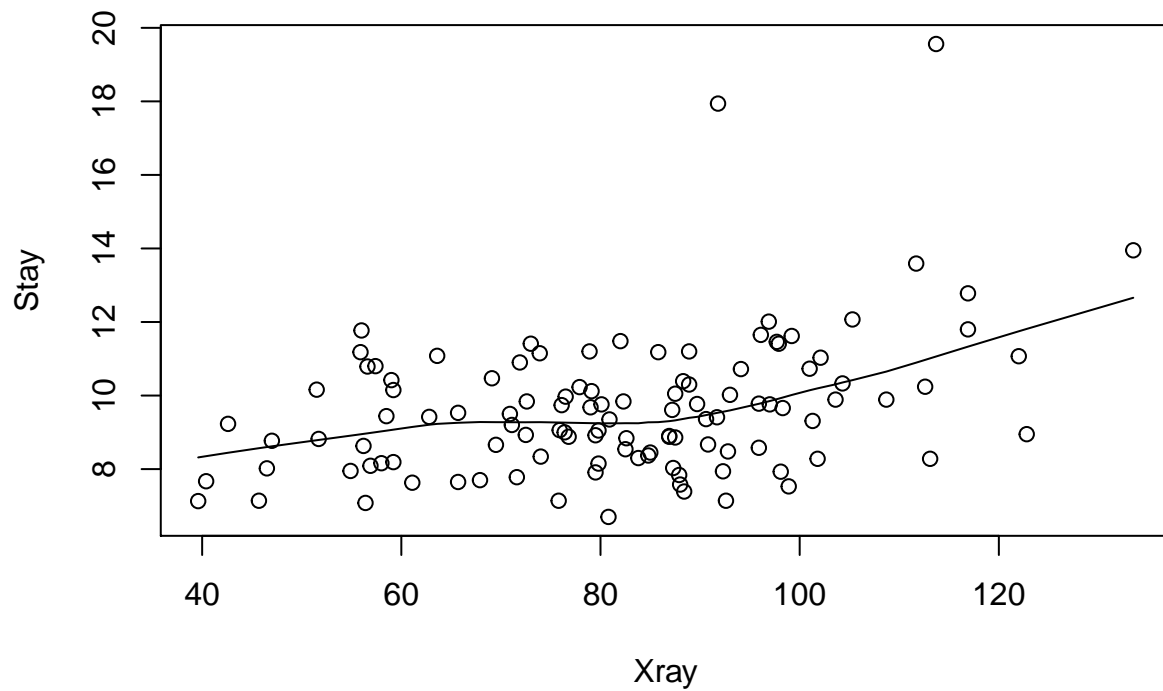
```
#3.
#(a)
filename <- "~/Downloads/SENIC.txt"
Data <- read.table(file=filename, header=T)
attach(Data)
plot(Risk, Stay)
lines(lowess(Risk, Stay))
```



```
plot(AFS, Stay)
lines(lowess(AFS, Stay))
```

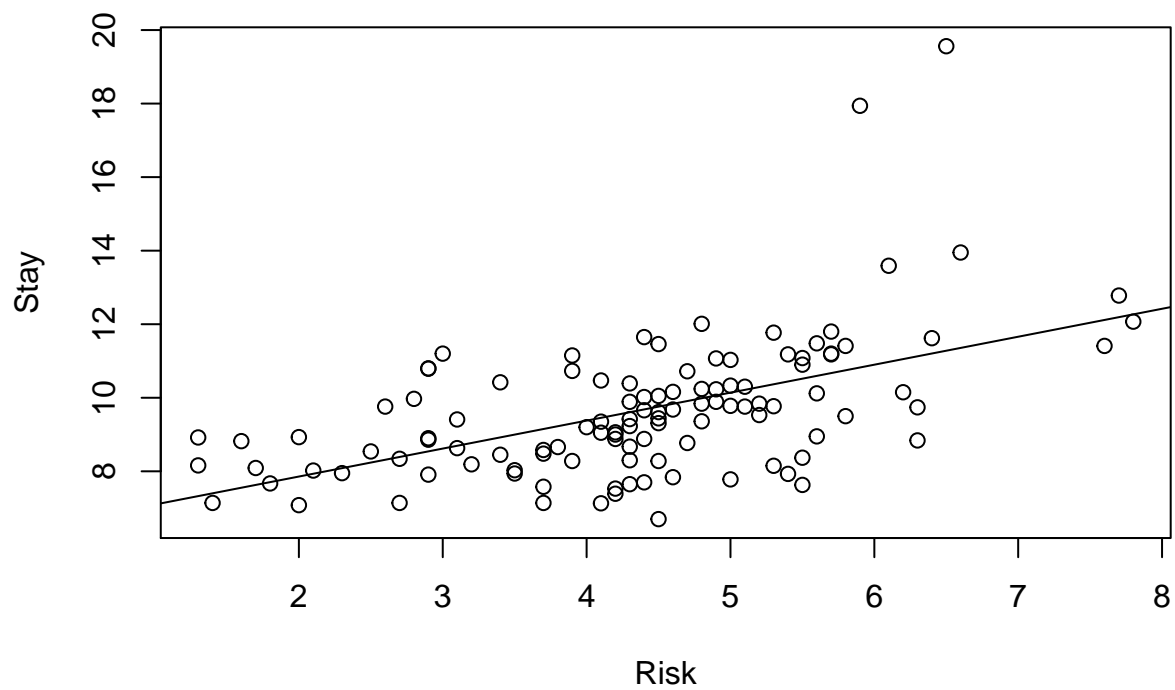


```
plot(Xray, Stay)
lines(lowess(Xray, Stay))
```

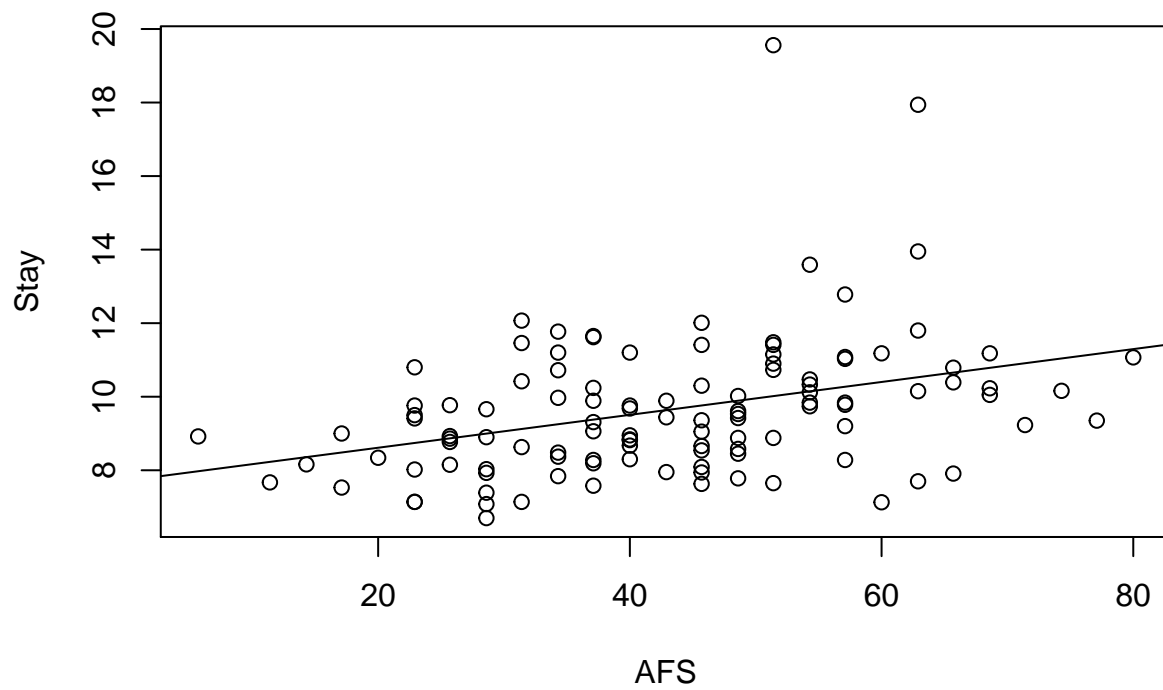


*#The mean function does appear linear in each case.we can see a "straight line"
#from bottom left to middle right going through the center of the points.*

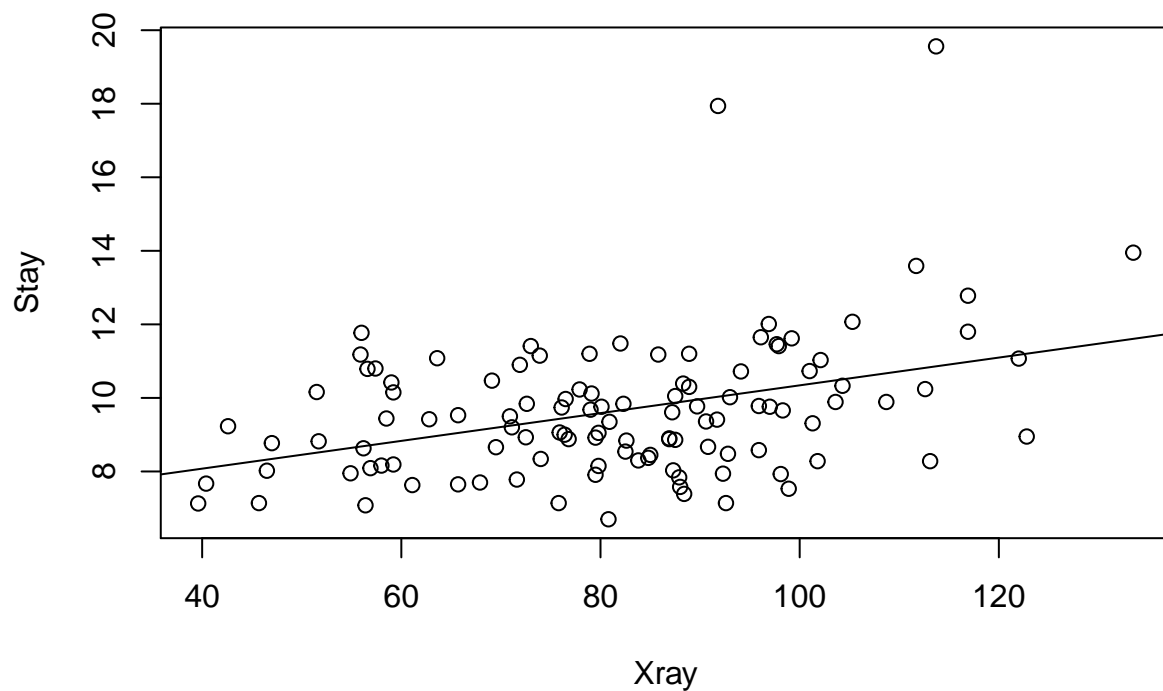
```
#(b)
plot(Stay ~ Risk)
abline(lm(Stay ~ Risk))
```



```
plot(Stay ~ AFS)
abline(lm(Stay ~ AFS))
```



```
plot(Stay ~ Xray)
abline(lm(Stay ~ Xray))
```



*#The simple linear regression model seems plausible in each case.
#we can see a "straight line" from bottom left to middle right going through*

```
#the center of the points.
```

```
#(c)
```

```
anova(lm(Stay ~ Risk))
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: Stay
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Risk         1  116.45  116.446   44.15 1.177e-09 ***
```

```
## Residuals 111  292.76    2.638
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
anova(lm(Stay ~ AFS))
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: Stay
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
## AFS          1   51.73   51.727  16.061 0.0001113 ***
```

```
## Residuals 111  357.48    3.221
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
anova(lm(Stay ~ Xray))
```

```
## Analysis of Variance Table
```

```
##
```

```
## Response: Stay
```

```
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Xray         1   59.86   59.864  19.021 2.906e-05 ***
```

```
## Residuals 111  349.35    3.147
```

```
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#MSE(Risk) = 2.638, MSE(AFS) = 3.221 and MSE(Xray) =3.147. Risk leads to
#the smallest variability around the fitted regression line.This result is
#apparent from plots in parts(a) and (b).
```