```
In [257...
           import numpy as np
           from scipy import signal
           a = np.arange(25).reshape(5, 5)
           b = np.arange(25).reshape(5, 5)
           v = np.arange(5)
           m = np.array([[1., 2.], [3., 4.]])
           n = np.array([[1., 2.], [3., 4.]])
           print(a)
          [[0 1 2 3 4]
           [5 6 7 8 9]
           [10 11 12 13 14]
           [15 16 17 18 19]
           [20 21 22 23 24]]
In [258...
           a.ndim
Out[258... 2
In [259...
           a.size
Out[259... 25
In [260...
           a.shape
Out[260... (5, 5)
In [261...
           (a.shape[1])
Out[261... 5
In [262...
          np.array([[1.,2.,3.], [4.,5.,6.]])
Out[262... array([[1., 2., 3.],
                 [4., 5., 6.]])
In [263...
           np.block([[1, 2], [3, 4]])
Out[263... array([[1, 2],
                 [3, 4]])
In [264...
           a[-1]
Out[264... array([20, 21, 22, 23, 24])
In [265...
           a[1, 4]
Out[265... 9
```

```
In [266...
          a[1]
Out[266... array([5, 6, 7, 8, 9])
In [267...
          a[0:5]
Out[267... array([[ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24]])
In [268...
          a[-5:]
Out[268... array([[ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24]])
In [269...
          a[0:3, 4:9]
Out[269... array([[ 4],
                [ 9],
                [14]])
In [270...
          a[np.ix_([1, 3, 4], [0, 2])]
Out[270... array([[ 5, 7],
                [15, 17],
                [20, 22]])
In [271...
          a[2:21:2,:]
Out[271... array([[10, 11, 12, 13, 14],
                [20, 21, 22, 23, 24]])
In [272...
          a[::2,:]
Out[272... array([[ 0, 1, 2, 3, 4],
                [10, 11, 12, 13, 14],
                [20, 21, 22, 23, 24]])
In [273...
          a[::-1,:]
Out[273... array([[20, 21, 22, 23, 24],
                [15, 16, 17, 18, 19],
                [10, 11, 12, 13, 14],
                [5, 6, 7, 8, 9],
                [ 0, 1, 2, 3, 4]])
In [274...
          a[np.r [:len(a),0]]
```

```
Out[274... array([[ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24],
                [0, 1, 2, 3, 4]])
In [275...
          a.transpose()
Out[275... array([[ 0, 5, 10, 15, 20],
                [ 1, 6, 11, 16, 21],
                [ 2, 7, 12, 17, 22],
                [ 3, 8, 13, 18, 23],
                      9, 14, 19, 24]])
In [276...
          a.conj().transpose()
Out[276... array([[ 0,
                      5, 10, 15, 20],
                [ 1,
                      6, 11, 16, 21],
                [ 2,
                     7, 12, 17, 22],
                [ 3, 8, 13, 18, 23],
                [ 4, 9, 14, 19, 24]])
In [277...
          a @ b
Out[277... array([[ 150, 160, 170, 180,
                                         190],
                [ 400, 435, 470, 505, 540],
                [ 650, 710, 770, 830, 890],
                [ 900, 985, 1070, 1155, 1240],
                [1150, 1260, 1370, 1480, 1590]])
In [278...
          a * b
                       1,
                             4,
                                  9, 16],
Out[278... array([[ 0,
                [ 25, 36, 49, 64, 81],
                [100, 121, 144, 169, 196],
                [225, 256, 289, 324, 361],
                [400, 441, 484, 529, 576]])
In [279... a / b
         <ipython-input-279-d8e10abd5ab6>:1: RuntimeWarning: invalid value encountered in
         true divide
           a / b
Out[279... array([[nan,
                                1., 1.],
                       1., 1.,
                      1., 1.,
                                1., 1.],
                [ 1.,
                      1., 1.,
                                1., 1.],
                [ 1.,
                [ 1., 1.,
                            1.,
                                 1., 1.],
                           1., 1., 1.]])
                [ 1., 1.,
In [280...
          a ** 3
                                   8,
                                         27,
                                                64],
Out[280... array([[
                     0,
                            1,
                  125,
                          216,
                                 343,
                                        512,
                                               7291,
                ſ
                [ 1000,
                        1331,
                                      2197, 2744],
                               1728,
```

```
[ 3375, 4096, 4913, 5832, 6859],
                 [ 8000, 9261, 10648, 12167, 13824]])
In [281...
          (a > 0.5)
Out[281... array([[False,
                          True,
                                 True,
                                         True,
                                                True],
                 [ True,
                                 True,
                          True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True ]])
In [282...
          np.nonzero(a > 0.5)
Out[282... (array([0, 0, 0, 0, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 4, 4, 4,
                  4, 4]),
           array([1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0, 1, 2,
                  3, 4]))
In [283...
          a[:,np.nonzero(v > 0.5)[0]]
                               4],
Out[283... array([[ 1, 2, 3,
                 [6, 7, 8, 9],
                 [11, 12, 13, 14],
                 [16, 17, 18, 19],
                 [21, 22, 23, 24]])
In [284...
          a[:, v.T > 0.5]
Out[284... array([[ 1, 2, 3, 4],
                 [6, 7, 8, 9],
                 [11, 12, 13, 14],
                 [16, 17, 18, 19],
                 [21, 22, 23, 24]])
In [285...
          a[a < 0.5] = 0
Out[285... array([[ 0, 1, 2, 3, 4],
                 [5, 6, 7, 8, 9],
                 [10, 11, 12, 13, 14],
                 [15, 16, 17, 18, 19],
                 [20, 21, 22, 23, 24]])
In [286...
          a * (a > 0.5)
Out[286... array([[ 0, 1, 2,
                               3, 4],
                 [5, 6, 7, 8, 9], [10, 11, 12, 13, 14],
                 [15, 16, 17, 18, 19],
                 [20, 21, 22, 23, 24]])
In [287...
          v[:] = 3
          v
Out[287... array([3, 3, 3, 3, 3])
```

```
b = a.copy()
In [288...
Out[288... array([[ 0, 1, 2, 3, 4],
                 [5, 6, 7, 8, 9],
                 [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                 [20, 21, 22, 23, 24]])
In [289...
          b = a[1, :].copy()
Out[289... array([5, 6, 7, 8, 9])
In [290...
          b = a.flatten()
Out[290... array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16,
                17, 18, 19, 20, 21, 22, 23, 24])
In [291...
          np.arange(1., 11.)
Out[291... array([ 1., 2., 3., 4., 5., 6., 7., 8., 9., 10.])
In [292...
          np.arange(10.)
Out[292... array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
In [293...
          np.arange(1.,11.)[:, np.newaxis]
Out[293... array([[ 1.],
                 [ 2.],
                 [ 3.],
                 [ 4.],
                 [ 5.],
                 [ 6.],
                 [ 7.],
                 [ 8.],
                 [ 9.],
                 [10.]]
In [294...
         np.zeros((3, 4))
Out[294... array([[0., 0., 0., 0.],
                [0., 0., 0., 0.],
                 [0., 0., 0., 0.]]
In [295...
          np.zeros((3, 4, 5))
Out[295... array([[[0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.]
                  [0., 0., 0., 0., 0.]
```

```
[[0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.]
                 [[0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.],
                  [0., 0., 0., 0., 0.]]])
In [296...
          np.ones((3, 4))
Out[296... array([[1., 1., 1., 1.],
                 [1., 1., 1., 1.],
                 [1., 1., 1., 1.]])
In [297...
          np.eye(3)
Out[297... array([[1., 0., 0.],
                 [0., 1., 0.],
                 [0., 0., 1.]])
In [298...
          np.diag(a)
Out[298... array([ 0, 6, 12, 18, 24])
In [299...
          np.diag(v, 0)
Out[299... array([[3, 0, 0, 0, 0],
                 [0, 3, 0, 0, 0],
                 [0, 0, 3, 0, 0],
                 [0, 0, 0, 3, 0],
                 [0, 0, 0, 0, 3]])
In [300...
          np.random.rand(3, 4)
Out[300... array([[0.36845515, 0.54825292, 0.88338353, 0.63177779],
                 [0.96784463, 0.40708092, 0.39760737, 0.89183071],
                 [0.44248143, 0.78498457, 0.73127013, 0.45526123]])
In [301...
          np.linspace(1,3,4)
Out[301... array([1.
                           , 1.66666667, 2.33333333, 3.
                                                                 ])
In [302...
          np.mgrid[0:9.,0:6.]
Out[302... array([[[0., 0., 0., 0., 0., 0.],
                  [1., 1., 1., 1., 1., 1.],
                  [2., 2., 2., 2., 2., 2.],
                  [3., 3., 3., 3., 3., 3.],
                  [4., 4., 4., 4., 4., 4.]
                  [5., 5., 5., 5., 5., 5.],
                  [6., 6., 6., 6., 6., 6.]
                  [7., 7., 7., 7., 7., 7.]
```

```
[8., 8., 8., 8., 8., 8.]],
                [[0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.],
                 [0., 1., 2., 3., 4., 5.]])
In [303...
          np.ix_(np.r_[0:9.],np.r_[0:6.])
Out[303... (array([[0.],
                 [1.],
                 [2.],
                 [3.],
                 [4.],
                 [5.],
                 [6.],
                 [7.],
                 [8.]]),
          array([[0., 1., 2., 3., 4., 5.]]))
In [304...
          np.meshgrid([1,2,4],[2,4,5])
Out[304... [array([[1, 2, 4],
                 [1, 2, 4],
                 [1, 2, 4]]),
          array([[2, 2, 2],
                 [4, 4, 4],
                 [5, 5, 5]])]
In [305...
          np.ix ([1,2,4],[2,4,5])
Out[305... (array([[1],
                 [2],
                 [4]]),
          array([[2, 4, 5]]))
In [306...
          np.tile(a, (3, 4))
Out[306... array([[ 0,
                      1,
                                                       4,
                                                                               0,
                          2,
                              3, 4, 0, 1, 2,
                                                  3,
                                                           0,
                                                               1,
                                                                   2, 3,
                                                                           4,
                              4],
                  1,
                      2,
                          3,
                              8, 9, 5, 6, 7, 8, 9, 5, 6, 7, 8, 9,
                [ 5,
                      6,
                         7,
                                                                              5,
                  6, 7, 8,
                              9],
                [10, 11, 12, 13, 14, 10, 11, 12, 13, 14, 10, 11, 12, 13, 14, 10,
                 11, 12, 13, 14],
                [15, 16, 17, 18, 19, 15, 16, 17, 18, 19, 15, 16, 17, 18, 19, 15,
                 16, 17, 18, 19],
                [20, 21, 22, 23, 24, 20, 21, 22, 23, 24, 20, 21, 22, 23, 24, 20,
                 21, 22, 23, 24],
                                  4, 0, 1, 2, 3, 4, 0, 1, 2, 3,
                [ 0, 1,
                         2, 3,
                                                                          4, 0,
                  1,
                     2,
                          3,
                              4],
                          7,
                                  9, 5, 6, 7, 8, 9, 5, 6, 7, 8,
                [ 5,
                      6,
                              8,
                                                                              5,
                      7,
                         8,
                              9],
                [10, 11, 12, 13, 14, 10, 11, 12, 13, 14, 10, 11, 12, 13, 14, 10,
                 11, 12, 13, 14],
                [15, 16, 17, 18, 19, 15, 16, 17, 18, 19, 15, 16, 17, 18, 19, 15,
```

```
16, 17, 18, 19],
                [20, 21, 22, 23, 24, 20, 21, 22, 23, 24, 20, 21, 22, 23, 24, 20,
                 21, 22, 23, 24],
                             3, 4, 0, 1, 2, 3, 4, 0, 1, 2, 3, 4, 0,
                [ 0, 1, 2,
                             4],
                      2,
                  1,
                          3,
                     6,
                         7,
                              8, 9, 5, 6, 7, 8, 9, 5, 6, 7, 8, 9, 5,
                [ 5,
                     7,
                         8, 9],
                [10, 11, 12, 13, 14, 10, 11, 12, 13, 14, 10, 11, 12, 13, 14, 10,
                11, 12, 13, 14],
                [15, 16, 17, 18, 19, 15, 16, 17, 18, 19, 15, 16, 17, 18, 19, 15,
                 16, 17, 18, 19],
                [20, 21, 22, 23, 24, 20, 21, 22, 23, 24, 20, 21, 22, 23, 24, 20,
                 21, 22, 23, 24]])
In [307...
          a = np.arange(25).reshape(5, 5)
          b = np.arange(25).reshape(5, 5)
          np.concatenate((a,b),1)
                                             2,
Out[307... array([[ 0, 1, 2,
                              3, 4, 0, 1,
                                                 3,
                                                      4],
                [5, 6, 7, 8, 9, 5, 6,
                                             7,
                                                 8,
                                                     9],
                [10, 11, 12, 13, 14, 10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19, 15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24, 20, 21, 22, 23, 24]])
In [308...
          np.concatenate((a,b))
Out[308... array([[ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24],
                [ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24]])
In [309...
          a.max()
Out[309... 24
In [310...
          a.max(0)
Out[310... array([20, 21, 22, 23, 24])
In [311...
          a.max(1)
Out[311... array([ 4, 9, 14, 19, 24])
In [312...
          np.maximum(a, b)
Out[312... array([[ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
```

```
[15, 16, 17, 18, 19],
                 [20, 21, 22, 23, 24]])
In [313...
          np.sqrt(v @ v)
Out[313... 6.708203932499369
In [314...
          np.logical_and(a,b)
Out[314... array([[False,
                          True,
                                 True,
                                         True,
                                                True],
                                 True,
                 [ True,
                          True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True]])
In [315...
         np.logical_or(a,b)
Out[315... array([[False,
                          True,
                                 True,
                                         True,
                                                True],
                 [ True,
                          True,
                                 True,
                                         True,
                                                True]])
In [316...
          a & b
Out[316... array([[ 0, 1, 2, 3, 4],
                 [5, 6, 7, 8, 9],
                 [10, 11, 12, 13, 14],
                 [15, 16, 17, 18, 19],
                 [20, 21, 22, 23, 24]])
In [317...
          a b
Out[317... array([[ 0, 1, 2, 3, 4],
                 [5, 6, 7, 8, 9],
                 [10, 11, 12, 13, 14],
                 [15, 16, 17, 18, 19],
                 [20, 21, 22, 23, 24]])
In [318...
          np.linalg.inv(m)
Out[318... array([[-2., 1.],
                [1.5, -0.5]
In [319...
          np.linalg.pinv(m)
Out[319... array([[-2., 1.],
                 [1.5, -0.5]
In [320...
          np.linalg.matrix rank(m)
Out[320... 2
```

```
In [321... | np.linalg.solve(m, n)
Out[321... array([[1.0000000e+00, 0.0000000e+00],
                [8.32667268e-17, 1.00000000e+00]])
In [322...
          np.linalg.svd(a)
Out[322... (array([[-0.06767881, -0.77163436, 0.63224391, 0.00167672, 0.01627349],
                 [-0.22699517, -0.49847085, -0.64277772, 0.40439987, 0.3511375],
                 [-0.38631153, -0.22530735, -0.29501495, -0.26831145, -0.80060923],
                 [-0.54562789, 0.04785615, -0.01061257, -0.68328362, 0.482712]
                 [-0.70494424, 0.32101965, 0.31616133, 0.54551847, -0.04951376]]),
          array([6.99085940e+01, 3.57609824e+00, 5.72246903e-15, 2.09124342e-16,
                 6.08024818e-17]),
          array([[-0.39024378, -0.41787354, -0.4455033 , -0.47313306, -0.50076282],
                 [ 0.66911119, 0.35409279, 0.03907438, -0.27594403, -0.59096243],
                 [0.37572717, 0.02608843, -0.58890396, -0.40336606, 0.59045442],
                 [-0.38884163, 0.47076134, 0.40132636, -0.65957023, 0.17632416],
                 [-0.32807206, 0.69116073, -0.54048985, 0.31978575, -0.14238457]]))
In [323...
          c = np.array([[1,-2j],[2j,5]])
          np.linalg.cholesky(c)
Out[323... array([[1.+0.j, 0.+0.j],
                [0.+2.j, 1.+0.j])
In [324...
          np.linalg.eig(a)
Out[324... (array([ 6.39116499e+01, -3.91164992e+00, 3.19626490e-15, -1.64396509e-15,
                  8.90756696e-17]),
          array([[-0.0851802 , 0.67779864, 0.06945307, -0.39148436, -0.10985832],
                 [-0.23825372, 0.36348873, 0.44032228, 0.290592, -0.03338055],
                 [-0.39132723, 0.04917881, -0.57200489, 0.01857127, 0.63352165],
                 [-0.54440074, -0.2651311, -0.45476933, 0.6570189, -0.72746836],
                 [-0.69747425, -0.57944101, 0.51699887, -0.5746978, 0.23718558]]))
In [325...
          np.linalg.qr(a)
Out[325... (array([[ 0.00000000e+00, -7.74596669e-01, 6.31373603e-01,
                  -3.43074273e-02, -1.37975813e-02],
                 [-1.82574186e-01, -5.16397779e-01, -6.00582802e-01,
                   4.65904120e-01, 3.49619292e-01],
                 [-3.65148372e-01, -2.58198890e-01, -3.50181388e-01,
                  -3.07929335e-01, -7.63251282e-01],
                 [-5.47722558e-01, -3.64316988e-17, -2.33832327e-02,
                  -6.44623979e-01, 5.32835012e-01],
                 [-7.30296743e-01, 2.58198890e-01, 3.42773819e-01,
                   5.20956622e-01, -1.05405441e-01]]),
          array([[-2.73861279e+01, -2.92118697e+01, -3.10376116e+01,
                  -3.28633535e+01, -3.46890953e+01],
                 [0.000000000e+00, -1.29099445e+00, -2.58198890e+00,
                  -3.87298335e+00, -5.16397779e+00],
                 [ 0.00000000e+00, 0.0000000e+00, 2.61397004e-15,
                   5.09829244e-15, 8.73506122e-15],
                 [ 0.00000000e+00, 0.0000000e+00, 0.0000000e+00,
                   1.86243709e-16, -1.70413110e-16],
                 [ 0.00000000e+00, 0.0000000e+00, 0.0000000e+00,
                   0.00000000e+00, -6.20597544e-16]]))
```

t2

```
In [326... | np.fft.fft(v)
Out[326... array([15.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j])
In [327...
          np.fft.ifft(v)
Out[327... array([3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j])
In [328...
          np.sort(a)
Out[328... array([[ 0, 1, 2, 3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24]])
In [329...
          np.sort(a, axis = 1)
Out[329... array([[ 0, 1, 2,
                              3,
                                  4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24]])
In [330...
          I = np.argsort(a[:, 0])
Out[330... array([0, 1, 2, 3, 4])
In [331...
          a[I,:]
Out[331... array([[ 0, 1, 2,
                              3, 4],
                [5, 6, 7, 8, 9],
                [10, 11, 12, 13, 14],
                [15, 16, 17, 18, 19],
                [20, 21, 22, 23, 24]])
In [332...
          x = np.linspace(0, 10, 20, endpoint=False)
          y = np.cos(-x**2/6.0)
          f = signal.resample(y, 100)
          signal.resample(y, 100)
                           , 1.23283311, 1.31727019, 1.27302765, 1.14740269,
Out[332... array([ 1.
                 0.99913207, 0.88078847, 0.82497964, 0.83806509, 0.90249922,
                 0.98614323, 1.05486
                                       , 1.08402435, 1.06536954, 1.00747904,
                 0.93050762, 0.85758366, 0.80620995, 0.78263328, 0.78081837,
                 0.78588726, 0.78033048,
                                           0.75048699, 0.69094819,
                                                                     0.60552319,
                 0.50478221, 0.40143727, 0.30548407, 0.22092394, 0.14511765,
                 0.0707372 , -0.01068719 , -0.10512733 , -0.21370903 , -0.33240564 ,
                -0.45366208, -0.56910426, -0.67215691, -0.75955883, -0.83131707,
                -0.88932657, -0.93540864, -0.9696874, -0.98998822, -0.9924354,
                -0.97288395, -0.92847886, -0.85863231, -0.76502853, -0.65074937,
                -0.51903563, -0.37236513, -0.21236454, -0.04065068, 0.13978552,
                 0.3233596 , 0.50154373, 0.66375109, 0.79927642, 0.89960584,
                 0.96017029, 0.98077748, 0.96447814, 0.91530208, 0.8358487,
```