

## ASTMA

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1. Bow - Bow, TF - IDF.

Doc 1: cat sat on the mat

Doc 2: dog sat on the mat

Doc 3: cat chased the dog.

Soln:

Step 1: Bow (Bag of words)

a) create vocabulary

["cat", "sat", "on", "the", "mat", "dog", "chased"]

b) count word frequencies

word	cat	sat	on	the	mat	dog	chased
Doc 1	1	1	1	1	1	0	0
Doc 2	0	1	1	1	1	1	0
Doc 3	1	0	0	1	0	1	1

c) Bow output:

The matrix is;

[[1, 1, 1, 1, 1, 1, 0, 0], [0, 1, 1, 1, 1, 1, 0], [1, 0, 0, 1, 0, 1, 1]]

Step 2: TF-IDF.

a) compute Term Frequency (TF)

TF = word F in doc / total words in doc.

$$TF(\text{cat}, \text{Doc 1}) = 1/5 = 0.2$$

$$TF(\text{dog}, \text{Doc 2}) = 1/5 = 0.2$$

$$TF(\text{sat}, \text{Doc 1}) = 1/5 = 0.2$$

$$TF(\text{sat}, \text{Doc 2}) = 1/5 = 0.2$$

$$TF(\text{on}, \text{Doc 1}) = 1/5 = 0.2$$

$$TF(\text{on}, \text{Doc 2}) = 1/5 = 0.2$$

$$TF(\text{the}, \text{Doc 1}) = 1/5 = 0.2$$

$$TF(\text{the}, \text{Doc 2}) = 1/5 = 0.2$$

$$TF(\text{mat}, \text{Doc 1}) = 1/5 = 0.2$$

$$TF(\text{mat}, \text{Doc 2}) = 1/5 = 0.2$$

$$TF(\text{cat}, \text{Doc 3}) = 1/4 = 0.25$$

$$TF(\text{chased}, \text{Doc 3}) = 0.25$$

$$TF(\text{the}, \text{Doc 3}) = 0.25$$

$$TF(\text{dog}, \text{Doc 3}) = 0.25$$

b)  $IDF = \log(\text{Total docs} / \text{docs containing the word})$   
 eg: cat appears 2 times in doc.

$$IDF(\text{cat}) = \log(3/2) = 0.176$$

$$IDF(\text{sat}) = \log(3/2) = 0.176$$

$$IDF(\text{on}) = \log(3/2) = 0.176$$

$$IDF(\text{the}) = \log(3/3) = 0$$

$$IDF(\text{mat}) = \log(3/2) = 0.176$$

$$IDF(\text{dog}) = \log(3/2) = 0.176$$

$$IDF(\text{chased}) = \log(3/1) = 0.477$$

c) Compute TF \* IDF.

$$TF-IDF = TF * IDF$$

$$\text{eg: } TF-IDF(\text{cat}, \text{Doc1}) = 0.2 * 0.176$$

$$TF-IDF(\text{sat}, \text{Doc1}) = 0.2 * 0.176$$

$$TF-IDF(\text{on}, \text{Doc1}) = 0.2 * 0.176$$

$$TF-IDF(\text{the}, \text{Doc1}) = 0.2 * 0$$

$$TF-IDF(\text{mat}, \text{Doc1}) = 0.2 * 0.176$$

$$TF-IDF(\text{dog}, \text{Doc2}) = 0.2 * 0.176$$

$$TF-IDF(\text{chased}, \text{Doc3}) = 0.25 * 0.477$$

d) TF-IDF output

word	cat	sat	on	the	mat	dog	chased.
Doc 1	0.0352	0.0352	0.0352	0	0.0352	0	0
Doc 2	0	0.0352	0.0352	0	0.0352	0.0352	0
Doc 3	<del>0.0352</del>	0	0	0	0	<del>0.0352</del>	<del>0.0352</del>
	0.044					0.044	0.1192

## 2. ACP problem (Average concept proportion)

HW: Laptop, Desktop, tab

SW: OS, Applications

NW: LAN, WAN, MAN, VRN

Soln:

Step 1: count the parent nodes - HW, SW, NW

Step 2: count the child node for each parent

HW  $\rightarrow 3$

SW  $\rightarrow 2$

NW  $\rightarrow 4$

Step 3: HW (3 children)  $= \frac{1}{3} = 0.33$

SW (2 children)  $= \frac{1}{2} = 0.5$

NW (4 children)  $= \frac{1}{4} = 0.25$

$< 0.5$  unevenly distributed  
 $> 0.5$  toward evenly distributed  
 $1 \rightarrow$  evenly distributed  
 (no need any modification)

Step 4: calculate ACP

$$\rightarrow \frac{0.33 + 0.5 + 0.25}{3} = 0.36$$

$$\Rightarrow 0.36 < 0.5$$

4. Distribution properties of / core / text mining operations.



3. calculate entropy and purity.

cluster	science	sports	politics
1	250	20	10
2	20	180	80
3	30	100	210
	<u>300</u>	<u>300</u>	<u>300</u>
			<u>900</u>

soln:  $entropy(D) = - \sum_{i=1}^k P(c_i) \log_2 P(c_i)$

$entropy_{total}(D) = \sum_{i=1}^k \frac{|D_i|}{|D|} \times entropy(D_i)$

$Purity(D_i) = \max_i (P(c_j))$

$Purity_{total}(D) = \sum_{i=1}^k \frac{|D_i|}{|D|} \times Purity(D_i)$

Probabilities;  
cluster

	science	sports	politics
1	250/280	20/280	10/280
2	20/280	180/280	80/280
3	30/340	100/340	210/340

→

cluster	s	s	P
1	0.893	0.071	0.036
2	0.071	0.643	0.286
3	0.088	0.294	0.618

$\therefore Purity(D_i) = \max(P_i)$

cluster 1 = 0.893

cluster 2 = 0.643

cluster 3 = 0.618

For cluster 1: (c1)

$$\text{Entropy}(c1) = -\sum P \log_2 P(c1)$$

$$\Rightarrow -\frac{250}{280} \log_2 \frac{250}{280} - \frac{20}{280} \log_2 \frac{20}{280} - \frac{10}{280} \log_2 \frac{10}{280}$$

$$\Rightarrow -0.893 (-0.163)$$

$$\Rightarrow 0.146 + 0.272 + 0.172$$

$$\Rightarrow 0.590$$

$$\text{Entropy}(c2) = -\frac{20}{280} \log_2 \frac{20}{280} - \frac{180}{280} \log_2 \frac{180}{280} - \frac{80}{280} \log_2 \frac{80}{280}$$

$$\Rightarrow 0.272 + 0.410 + 0.576$$

$$\Rightarrow 1.198$$

$$\text{Entropy}(c3) = -\frac{30}{340} \log_2 \frac{30}{340} - \frac{100}{340} \log_2 \frac{100}{340} - \frac{210}{340} \log_2 \frac{210}{340}$$

$$\Rightarrow 0.309 + 0.519 + 0.429$$

$$\Rightarrow 1.257$$

$$\text{Entropy}_{\text{total}} = 101 = 900$$

$$\text{Entropy}_{\text{total}}(D) = \frac{280}{900} \times 0.590 + \frac{280}{900} \times 1.198 + \frac{340}{900} \times 1.257$$

$$\Rightarrow 0.184 + 0.373 + 0.475$$

$$\Rightarrow 1.032$$

#### 4. Outlier detection

Z-score & IQR method.

A data pt is considered an outlier if its z-score exceeds a threshold (Eq:  $|z| > 3$ )

Data pt: 4, 8, 10, 14, 16, 18, 20, 22, 24, 28.

$$z = \frac{x - \mu}{\sigma}$$

$$\sigma = \sqrt{\frac{\sum (x - \mu)^2}{N}}, \quad \mu = \frac{\text{All add}}{N}$$

$$\mu = \frac{4 + 8 + 10 + 14 + 16 + 18 + 20 + 22 + 24 + 28}{10}$$

$$\mu = \frac{164}{10} = 16.4$$

$$\sigma = \sqrt{\frac{(4 - 16.4)^2 + (8 - 16.4)^2 + (10 - 16.4)^2 + (14 - 16.4)^2 + (16 - 16.4)^2 + (18 - 16.4)^2 + (20 - 16.4)^2 + (22 - 16.4)^2 + (24 - 16.4)^2 + (28 - 16.4)^2}{10}}$$

$$\sigma = \sqrt{\frac{153.76 + 70.56 + 40.96 + 5.76 + 2.56 + 12.96 + 31.36 + 57.76 + 134.56}{10}}$$

$$\sigma = \sqrt{\frac{510.24}{10}} = \sqrt{51.024} = 7.143$$

IQR (Inter Quartile range)

$Q_1$  = lower quartile = median of lower half of data

$$Q_1 = 10 \Rightarrow 25^{\text{th}} \text{ percentile} = \frac{(N+1) \times 25}{100} = \frac{11 \times 25}{100} = 2.75$$

$Q_3$  = upper quartile = median of upper half of data

$$Q_3 = 22 \Rightarrow 75^{\text{th}} \text{ percentile} = \frac{(N+1) \times 75}{100} = 8.75$$

$$IQR = Q_3 - Q_1 = 22 - 10 = 12$$

Any value below 10 and above 22 is considered an outlier.

Teacher's Signature:

$$\text{lower boundary} = Q1 - 1.5 \times IQR$$

$$= 10 - 1.5 \times 12$$

$$= 8$$

$$\text{upper boundary} = Q3 + 1.5 \times IQR$$

$$= 22 + 1.5 \times 12$$

$$= 40$$

Z-score: Data pts: [10, 12, 14, 18, 100]

Threshold = 3

$$\mu = \frac{10+12+14+18+100}{5} = \frac{154}{5} = 30.8$$

$$\sigma = \sqrt{\frac{\sum (x - \mu)^2}{N}}$$

$$= \sqrt{\frac{(10-30.8)^2 + (12-30.8)^2 + (14-30.8)^2 + (18-30.8)^2 + (100-30.8)^2}{5}}$$

$$= \sqrt{\quad} \Rightarrow 34.70$$

$x$	$z = \frac{x - \mu}{\sigma}$
10	-0.599
12	-0.542
14	-0.484
18	-0.369
100	1.99

$|z| > 3 \rightarrow$  External high value

$|z| < 3 \rightarrow$  External low value

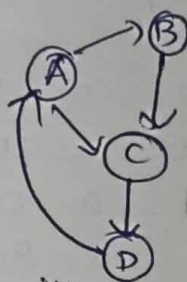
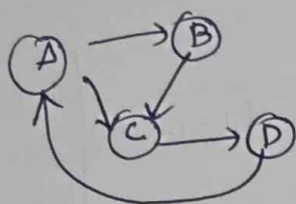
$|z| \leq 3 \rightarrow$  not outlier (within normal range)



5. Page rank.

To calculate the page rank for the directed graph with nodes A, B, C, D and edges A → B, A → C, B → C, C → D, D → A.

Soln:



a) Represent the graph as transition matrix probability of transitions from one-to-another node,

$$M = \begin{matrix} & \begin{matrix} A & B & C & D \end{matrix} \\ \begin{matrix} A \\ B \\ C \\ D \end{matrix} & \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1/2 & 0 & 0 & 0 \\ 1/2 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \end{matrix}$$

col-wise sum = 1  
matrix is stochastic

Max prob. is 1, No. of edges = 2, so 1/2

b) Initialize the page rank vector.

$$P^0 = \begin{bmatrix} 1/4 \\ 1/4 \\ 1/4 \\ 1/4 \end{bmatrix} \quad \text{total nodes} = 4 \Rightarrow 1/4$$

$$\Rightarrow \begin{bmatrix} 0.25 \\ 0.25 \\ 0.25 \\ 0.25 \end{bmatrix}$$

c) Applying damping factor (d)

$$\alpha \text{ (or) } d = 0.85 \text{ (constant)}$$

$$\frac{1}{2} \times 0.25$$

$$\frac{0.25}{2}$$

Teacher's Signature: \_\_\_\_\_

vector  $\vec{u}$ ; uniform distribution

Page rank formula becomes  $p^{(k+1)} = d \cdot M \cdot p^{(k)} + (1-d) \cdot \vec{u}$

$$v = \begin{bmatrix} 1/4 \\ 1/4 \\ 1/4 \\ 1/4 \end{bmatrix} \Rightarrow \begin{bmatrix} 0.25 \\ 0.25 \\ 0.25 \\ 0.25 \end{bmatrix}$$

$$p^{(k+1)} = 0.85 \times \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1/2 & 0 & 0 & 0 \\ 1/2 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \times \begin{bmatrix} 0.25 \\ 0.25 \\ 0.25 \\ 0.25 \end{bmatrix} + (1-0.85) \begin{bmatrix} 0.25 \\ 0.25 \\ 0.25 \\ 0.25 \end{bmatrix}$$

$$\Rightarrow 0.85 \begin{bmatrix} 0.25 \\ 0.125 \\ 0.375 \\ 0.25 \end{bmatrix} + (0.15) \begin{bmatrix} 0.25 \\ 0.25 \\ 0.25 \\ 0.25 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 0.213 \\ 0.106 \\ 0.319 \\ 0.213 \end{bmatrix} + \begin{bmatrix} 0.038 \\ 0.038 \\ 0.038 \\ 0.038 \end{bmatrix} \Rightarrow \begin{bmatrix} 0.251 \\ 0.144 \\ 0.357 \\ 0.251 \end{bmatrix}$$

$$p(1) = \begin{bmatrix} 0.25 \\ 0.144 \\ 0.35 \\ 0.25 \end{bmatrix}$$

$$p(2) = \begin{bmatrix} 0.25 \\ 0.14 \\ 0.26 \\ 0.34 \end{bmatrix}$$

$$p^{(k+1)} \Rightarrow p(2)$$

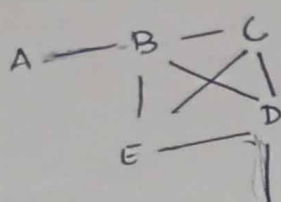
$$= 0.85 \times \begin{bmatrix} M \end{bmatrix} \times \begin{bmatrix} 0.25 \\ 0.14 \\ 0.26 \\ 0.25 \end{bmatrix} + (1-0.85) \begin{bmatrix} 0.25 \\ 0.25 \\ 0.25 \\ 0.25 \end{bmatrix}$$

# 6. k-core graph

A, B, C, D, E, F

edges: AB, BC, BE, BD, CD, CE, DE, DF

a) compute k-core collapse sequence for  $k=1, 2, 3, 4$ .



$k=1$   
 $k=2$   
 $k=3$   
 $k=4$

B, C, D, E.

B — C — D — E.

Removed nodes

Remaining nodes

subgraph

$k=1$

A, F

—

A, B, C, D, E, F

$k=2$

—

A, F

B, C, D, E

$k=3$

C, E

—

B, C, D, E

$k=4$

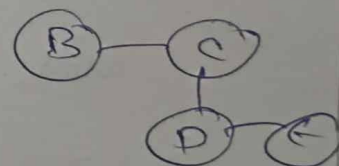
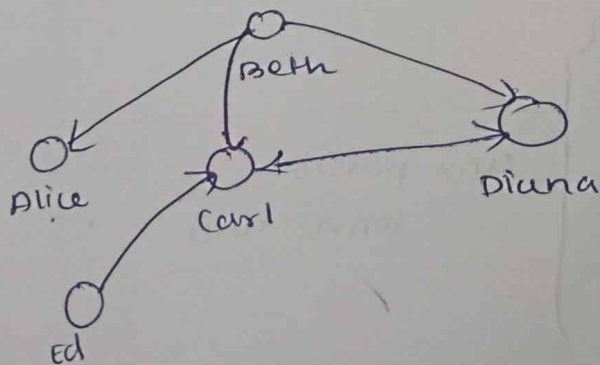
B, D

C, E

B, D

7. NW Analysis

Ego analysis (directed graph)



Ego NW Analysis for Alice

	Alice	Beth	Rowsum
Alice	0	1	1
Beth	1	0	1

Ego NW Analysis for Beth

	Beth	Alice	Carl	Diana	Rowsum
Beth	0	1	1	1	3
Alice	1	0	0	0	1
Carl	0	0	0	1	1
Diana	0	0	1	0	1

Ego for all.

Fred has no connections  $\rightarrow$  so independent8. whole NW analysis

Consider a NW with 4 nodes.

Node A	- 2	neighbors	with 1 connection
Node B	- 3	"	" 3 "
Node C	- 1	"	" 0 "
Node D	- 3	"	" 2 "

Soln:

Total possible  $\frac{n(n-1)}{2}$   $n \rightarrow$  neighbor

$$A \rightarrow \frac{2(2-1)}{2} = \frac{2(1)}{2} = 1$$

$$B \rightarrow \frac{3(3-1)}{2} = \frac{3(2)}{2} = 3$$

$$C \rightarrow \frac{1(1-1)}{2} = 0$$

$$D \rightarrow \frac{3(3-1)}{2} = 3$$

max possible connections



in: neighbors

A → 2

B → 3

C → 1

D → 3

out: among neighbors

A → 1

B → 3

C → 0

D → 2

Total connection

Max conn.

$$cc(A) = 1/1 = 1$$

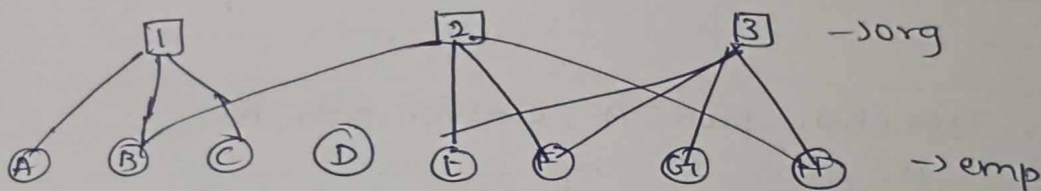
$$cc(B) = 3/3 = 1$$

$$cc(C) = 0/0 = 0$$

$$cc(D) = 2/3 = 0.67$$

Avg density:  $\frac{1+1+0+0.67}{4} = 0.667$

9. two mode NW analysis.



Adj matrix.

	1	2	3
A	1	0	0
B	1	1	0
C	1	0	0
D	0	0	0
E	0	1	1
F	0	1	1
G	0	0	1
H	0	1	1

density for 2 mode NW analysis

$$\Rightarrow \frac{L}{M \times N}$$

m → no. of nodes

n → no. of org.

$$\Rightarrow \frac{11}{3 \times 8} = \frac{11}{24}$$

11. G-test.

$$G\text{-test} = 2 \sum_{i=1}^n O_i \ln \left( \frac{O_i}{E_i} \right)$$

$$O = [8, 10, 12, 15, 7, 8]$$

$$E = [10, 10, 10, 10, 10, 10]$$

$$\alpha = 0.05$$

Step 1  $\rightarrow$  Cal  $\frac{O_i}{E_i}$  &  $O_i \ln \left( \frac{O_i}{E_i} \right)$

category ( $i$ )	$O_i$	$E_i$	$\left( \frac{O_i}{E_i} \right)$	$O_i \ln \left( \frac{O_i}{E_i} \right)$
1	8	10	0.8	-1.785
2	10	10	1	0
3	12	10	1.2	2.188
4	15	10	1.5	6.082
5	7	10	0.7	-2.497
6	8	10	0.8	-1.785

$$G = 2 \sum_{i=1}^n O_i \ln \left( \frac{O_i}{E_i} \right)$$

$$G = 2 \times (-1.785 + 2.188 + 6.082 + (-2.497) + (-1.785))$$

$$= 2 \times 2.20$$

$$= 4.40$$

$$\text{Degree of freedom} = df \Rightarrow k-1 = 6-1 = 5$$

$$\therefore p = 0.48$$

$$4.40 > 11.09$$

reject  $H_0$  (or) accept