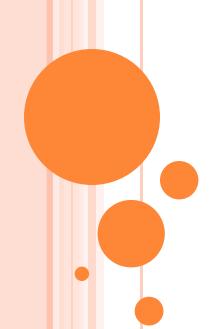


Basics of Data Structures and Algorithms

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Programming != Coding

- Programming

 Building a house
 - Requirements: purpose, input/output →需求為何、投入多少資金、產出什麼品質的房子
 - Analysis
 - o Bottom-up: small pieces to ultimate goal → 把每一面牆、每一塊 磚設計好,再想辦法拼起來
 - Top-down: ultimate goal to small pieces → 先考慮整體的需求,在 思考每一面牆、每一塊磚如何完成
 - Design: choices of data structures and algorithms → 建材和工法的 選定
 - Coding and refinement: actual implementation → 施工
 - Verification
 - o Proof (in math) → 確認是否符合設計圖,例如載重度或耐震度
 - Test and debug (on machines) → 工地現場的牢固度測試、監工等



From Coding to Programming

Comparison of DSA with "Intro to C"

	Intro to C	DSA
Requirements	*	*
Analysis & Design	*	***
Coding	***	***
Proof in Math	0	***
Test & Debugging	**	***

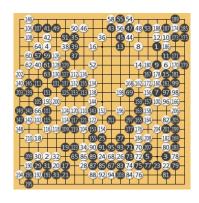


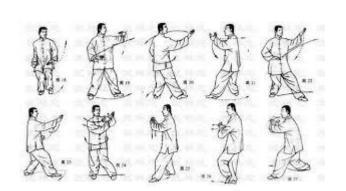
What Are Algorithms?

- o Algorithms can be viewed as "程式譜"
 - How to solve computation problems correctly and efficiently
- Similar terms
 - 食譜 (recipes)、樂譜 (sheet music)、劍譜、棋譜、拳譜
 - 臉譜、族譜、光譜、頻譜

Methods

Data, or example based









What Are Data Structures?

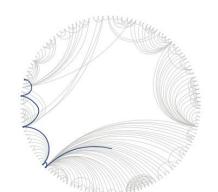
- Data structures can be viewed as "everything about data"
 - How to map the real world to the abstract representation?
 - How to use memory effectively?

Example

- Six Degrees of Separation (Stanley Milgram, 1960)
- Facebook users = 1.59 B, DOS=3.57 (link)



- 食譜 + 食材 = 菜 (Recipes + Ingredients = Dishes)
- 樂譜+樂器=音樂 (Sheet music + Instruments = Music)
- 劍譜+寶劍=天下無雙
- → Algorithms + Data Structures = Programs





Why Data Structures and Algorithms?

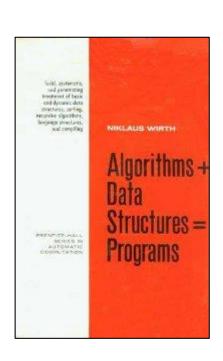
- A good program needs to leverage two types of resources on computers
 - Computing units: CPU, FPU, GPU, etc. → Time
 - Storage units: memory, disks, networks, etc. → Space
- Programs = Algorithms + Data Structures
 - Algorithms focus on computation issues, but needs to be accompanied by proper data structures
 - Data structures focus on storage management, but needs to be accompanied by proper algorithms

DSA helps you write better programs!



Algorithms & Data Structures

- Algorithms + Data Structures = Programs
 - A famous book published in 1976
 - The textbook for my DSA course
- o Algorithms (演算法)
- Data structures (資料結構)
 - How to arrange data? → Effective use of storage
- Trade-offs between computation and storage
 - You'll learn how to trade space with time, or vice versa.





About Algorithms

Quiz!

- Five basic criteria of algorithms (by Knuth)
 - Input: Zero or more quantities are externally supplied
 - Output: At least one quantity is produced
 - Definiteness: Each instruction is clear and unambiguous
 - Finiteness: The procedure terminates after a finite number of steps
 - Effectiveness: Each instruction is basic and feasible (do-able by computers)
- How to describe an algorithm
 - English: Description in a natural language
 - Graphic representation: Flow chart
 - Pseudo code: Program-like description in English
 - Programs: C/C++ combined with comments

FIVE CRITERIA OF 食譜

- 食材
 - 番茄、蛋、蔥、薑、太白 粉水、鹽、糖
- 食譜:番茄炒蛋
 - 蔥切花、薑切末備用。
 - 番茄去除蒂頭,劃十字刀, 下鍋汆燙後去皮。
 - 蛋液打匀,加少許鹽。
 - 番茄切成小塊備用。
 - 太白粉加水備用(1:3.5)。
 - 起油鍋爆香少許薑末,加入番茄、3大匙水、鹽、糖炒勻且湯汁稍微收乾。
 - 加入少許太白粉水勾芡。
 - 再加入蛋液輕輕翻炒。
 - 起鍋前灑上蔥花。

• Criteria

- Input
 - 食材
- Output
 - 菜
- Definiteness
 - 清楚的指令
- Finiteness
 - 一定可以做完
- Effectiveness
 - 可行的指令(電腦可完成)

FIVE CRITERIA OF ALGORITHMS

 Pseudo code for finding the index of the smallest number in an array: getMinPos()

```
getMinPos(integer array arr, integer len)
minPos <- 0
for i <- 1 to len-1 do
    if arr[i] smaller than arr[minPos] then
        minPos <- i
return minPos</pre>
```

Assignment

- Criteria
 - Input
 - An array
 - Output
 - Index of the smallest element in an array
 - Definiteness
 - Clear steps
 - Finiteness
 - Will terminate
 - Effectiveness
 - Achievable by computers



Pseudo Code vs. Real Code

Pseudo code:

```
getMinPos(integer array arr, integer len)
minPos <- 0
for i <- 1 to len-1 do
    if arr[i] smaller than arr[minPos] then
        minPos <- i
return minPos</pre>
```

Code in C++:

```
int getMinPos(int *arr, int len){
   int minPos=0;
   for (int i=1; i<len; i++) {
      if (arr[i]<arr[misPos])
            minPos=i;
   }
   return minPos;
}</pre>
```

- How to prove the correctness of getMinPos()
 - Claim: arr[minPos]<=arr[j] for j=0, 1, ..., len-1
 - Claim 2: After iteration i, arr[minPos]<=arr[j] for j=0, 1, ..., i
 - Proof by mathematical induction (數學歸納法)
 - Claim 2 holds when i=1
 - Assume claim 2 holds when i=k → Show that claim 2 holds when i=k+1.

Claim 2 is often called Invariance property of loops



Selection Sort

Animation

- Flash, YouTube, HTML
- Wiki about selection sort
- Pseudo code
 - Input: an integer array of length n
 - Output: an in-place sorted array
 - For i from 0 to n-1
 - Let s_{id} be the index of the smallest number from list[i] to list[n-1]
- Step 1 can be achieved by getMinPos().
- Step 2 can be done by the computer easily.



Sample Quiz for Selection Sort

• Please show each step of selection sort on the vector:

3 5 1 4 2 7 9 6 8



Correctness of Selection Sort

- Theorem
 - After the loop of i=q, for any j>q, we have
 - o list[0]<list[1]<list[2] ... < list[q] < list[j]</pre>
- Proof by mathematical induction
 - When q=0, the statement is true
 - Assume statement is true when q=t; then when q = t+1...