CSE 417T Introduction to Machine Learning

Lecture 22

Instructor: Chien-Ju (CJ) Ho

Logistics

Homework 5 is due Apr 19 (Tuesday)

- Exam 2 will be on April 28 (Thursday)
 - Will focus on the topics in the second half of the semester
 - Format / logistics will be similar with what we have in Exam 1
 - Timed exam (75 min) during lecture time in the classroom
 - Closed-book exam with 2 letter-size cheat sheets allowed (4 pages in total)
 - No format limitations (it can be typed, written, or a combination)
 - April 26 (Tuesday) will be a review lecture

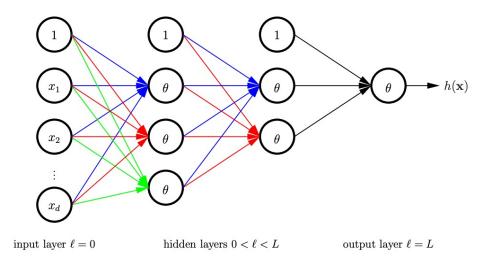
Recap

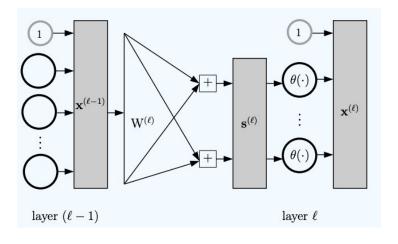
Neural Networks (NN)

- Notations:
 - $\ell = 0$ to L: layer
 - $d^{(\ell)}$: dimension of layer ℓ
 - $\vec{x}^{(\ell)}$: the nodes in layer ℓ
 - $w_{i,j}^{(\ell)}$: weights; characterize hypothesis in NN
 - $s_j^{(\ell)} = \sum_{i=0}^{d^{(\ell-1)}} w_{i,j}^{(\ell)} x_i^{(\ell-1)}$: linear signals
 - θ : activation function

•
$$x_j^{(\ell)} = \theta\left(s_j^{(\ell)}\right)$$

Feed-forward network





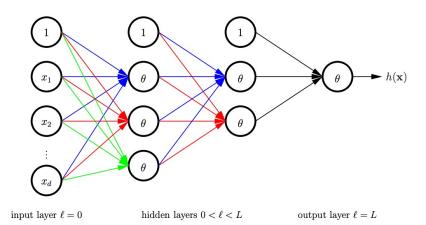
Forward Propagation and Backpropagation

- Evaluate $h(\vec{x})$ given h (characterized by $\{w_{i.i}^{(\ell)}\}$)
 - Forward propagation

$$\mathbf{x} = \mathbf{x}^{(0)} \xrightarrow{\mathrm{W}^{(1)}} \mathbf{s}^{(1)} \xrightarrow{\theta} \mathbf{x}^{(1)} \xrightarrow{\mathrm{W}^{(2)}} \mathbf{s}^{(2)} \xrightarrow{\theta} \mathbf{x}^{(2)} \cdots \xrightarrow{\mathrm{W}^{(L)}} \mathbf{s}^{(L)} \xrightarrow{\theta} \mathbf{x}^{(L)} = h(\mathbf{x}).$$

- Given D, learn the weights $W = \left\{ w_{i.i}^{(\ell)} \right\}$
 - Backpropagation
 - Initialize $w_{i,j}^{(\ell)}$ randomly
 - For t = 1 to T
 - Randomly pick a point from D (for stochastic gradient descent)

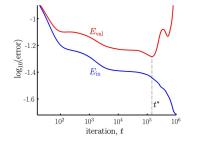
 - Forward propagation: Calculate all $x_i^{(\ell)}$ and $s_i^{(\ell)}$ Backward propagation: Calculate all $\delta_j^{(\ell)}$ Update the weights $w_{i,j}^{(\ell)} \leftarrow w_{i,j}^{(\ell)} \eta \delta_j^{(\ell)} x_i^{(\ell-1)}$
 - Return the weights



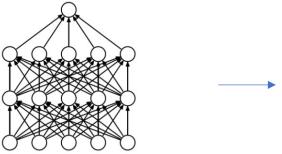
Regularizations in Neural Networks

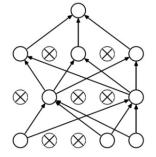
Weight-based regularization

Early stopping



Dropout





Adding noises





Today's Lecture

The notes are not intended to be comprehensive. They should be accompanied by lectures and/or textbook. Let me know if you spot errors.

Deep Learning

Neural networks with many layers

Single Hidden-Layer Neural Network

How do we write a hypothesis in a single-hidden layer NN mathematically?

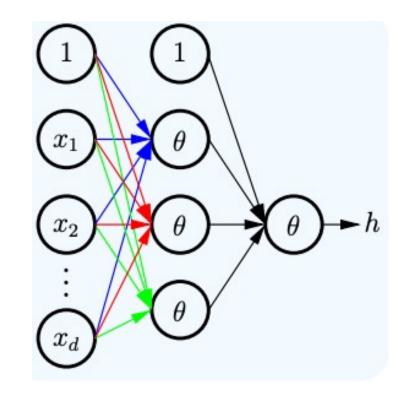
•
$$h(\vec{x}) = \theta \left(w_{0,1}^{(2)} + \sum_{j=1}^{d^{(1)}} w_{j,1}^{(2)} x_j^{(1)} \right)$$

 $= \theta \left(w_{0,1}^{(2)} + \sum_{j=1}^{d^{(1)}} w_{j,1}^{(2)} \theta \left(\sum_{i=0}^{d^{(0)}} w_{i,j}^{(1)} x_i^{(0)} \right) \right)$

- How do we write a linear model with nonlinear transform
 - $h(\vec{x}) = \theta(w_0 + \sum w_i \phi_i(\vec{x}))$
- How do we write a Kernel SVM hypothesis

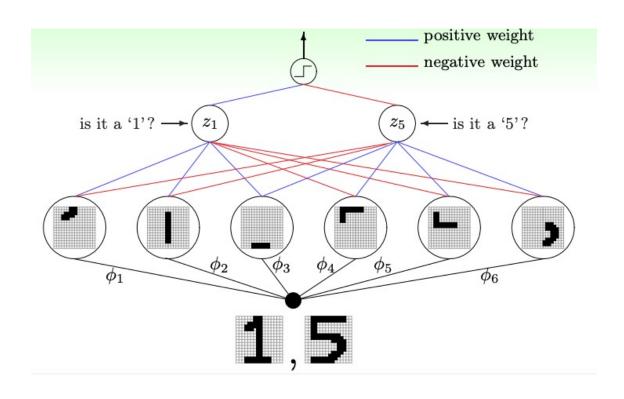
•
$$g(\vec{x}) = \theta \left(b^* + \sum_{\alpha_n^* > 0} \alpha_n^* y_n K(\vec{x}_n, \vec{x}) \right)$$

- Interpretation:
 - The hidden layer is like feature transform
 - Shallow learning vs. deep learning



Deep Neural Network

• "Shallow" neural network is powerful (universal approximation theorem holds with a single hidden layer). Why "deep" neural networks?



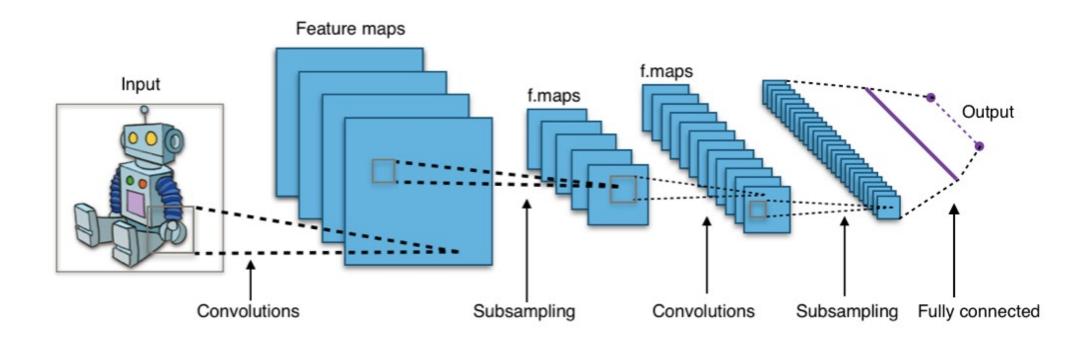
Each layer captures features of the previous layers.

We can use "raw data" (e.g., pixels of an image) as input. The hidden layer are extracting the features.

Design different network architectures to incorporate domain knowledge.

Convolutional Neural Networks (CNN)

Captures the localized properties of features hierarchically

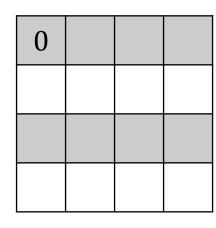


0	0	0	0	0	0
0	1	2	2	1	0
0	2	4	4	2	0
0	1	3	3	1	0
0	1	2	3	1	0
0	0	1	1	0	0

0	1	0
1	-4	1
0	1	0

0	0	0	0	0	0
0	1	2	2	1	0
0	2	4	4	2	0
0	1	3	3	1	0
0	1	2	3	1	0
0	0	1	1	0	0

0	1	0
1	-4	1
0	1	0



$$(0*0) + (0*1) + (0*0) + (0*1) + (1*-4) + (2*1) + (0*0) + (2*1) + (4*0) = 0$$

0	0	0	0	0	0
0	1	2	2	1	0
0	2	4	4	2	0
0	1	3	3	1	0
0	1	2	3	1	0
0	0	1	1	0	0

0	1	0
1	-4	1
0	1	0

0		

0	0	0	0	0	0
0	1	2	2	1	0
0	2	4	4	2	0
0	1	3	3	1	0
0	1	2	3	1	0
0	0	1	1	0	0

	0	1	0	
*	1	-4	1	=
	0	1	0	

0	-1	

$$(0*0) + (0*1) + (0*0) + (1*1) + (2*-4) + (2*1) + (2*0) + (4*1) + (4*0)$$

$$= -1$$

0	0	0	0	0	0
0	1	2	2	1	0
0	2	4	4	2	0
0	1	3	3	1	0
0	1	2	3	1	0
0	0	1	1	0	0

0	1	0
1	-4	1
0	1	0

0	-1	-1	0
-2	- 5	- 5	-2
2	-2	-1	3
-1	0	-5	0



Operation	Kernel ω	Image result g(x,y)
	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
	$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 0 & 0 \\ -1 & 0 & 1 \end{bmatrix}$	
	$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$	
	$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$	



Operation	Kernel ω	Image result g(x,y)
Identity	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
	$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 0 & 0 \\ -1 & 0 & 1 \end{bmatrix}$	
	$egin{bmatrix} 0 & 1 & 0 \ 1 & -4 & 1 \ 0 & 1 & 0 \end{bmatrix}$	
	$\begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$	



Operation	Kernel ω	Image result g(x,y)
Identity	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
	$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$	
	$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$	



Operation	Kernel ω	Image result g(x,y)
Identity	$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$	
Sharpen	$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$	
Box blur (normalized)	$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$	

Connection to Neural Networks

- Convolutions can be represented by a network structure
 - Nodes in the previous layer are only connected to "adjacent" nodes in the next layer.
 - Many of the weights have the same value.

0	0	0	0	0	0
0	1	2	2	1	0
0	2	4	4	2	0
0	1	3	3	1	0
0	1	2	3	1	0
0	0	1	1	0	0

0	1	0
1	-4	1
0	1	0

0	-1	-1	0
-2	- 5	5	-2
2	-2	-1	3
-1	0	5	0

Pooling Layers

Commonly used in convolutional neural networks.

A subsampling / down-sampling process:

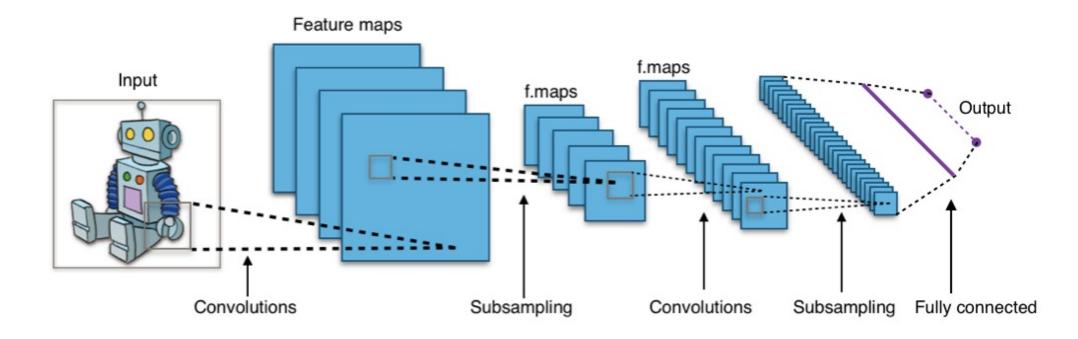
• Combines multiple adjacent nodes into a single node

0	-1	-1	0	 		
-2	-5	-5	-2	average	-2	-2
2	-2	2	3	pooling	0	0
-1	1	-5	0			

Reduce the dimensionality of input. More robust to noise.

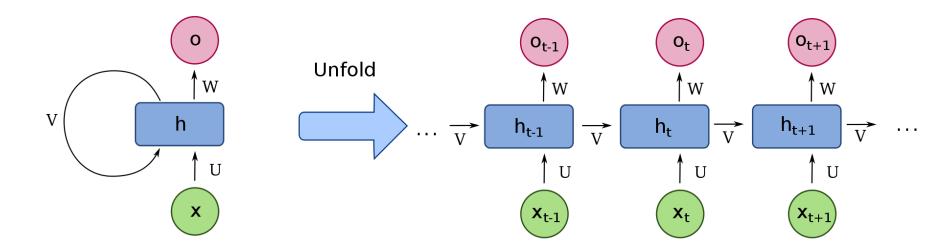
Convolutional Neural Networks (CNN)

- Captures the localized properties of features
 - Particularly suitable for computer vision (images)
 - Go (AlphaGo) is another famous application of CNN



Another Example Network Structure [Safe to Skip for the Exam]

- Recurrent Neural Network (RNN)
 - Aim to deal with time-series data, such as natural language processing
 - Using hidden layers to store temporal information
 - Allow previous outputs to be used as inputs and keep hidden states



Some Techniques in Improving Deep Learning

- Regularization to mitigate overfitting
 - Weight-based, early stopping, dropout, etc
- Incorporating domain knowledges
 - Network architectures (e.g., Convolutional Neural Nets)
- Improving computation with huge amount of data
 - Hardware architecture to improve parallel computation

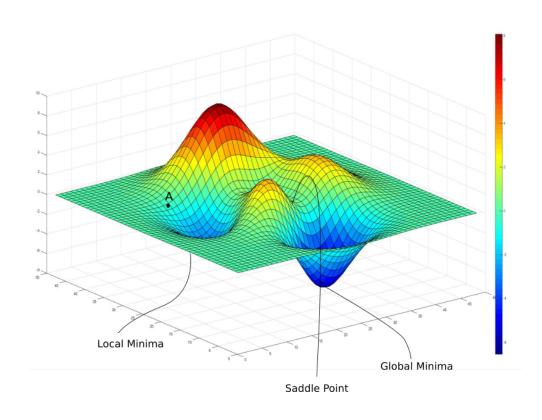
- Improving gradient-based optimization
 - Choosing better initialization points

Initialization

Why initialization matters in deep learning

- Error is nonconvex in NN
- Vanishing/exploding gradient problem

Error is Nonconvex in Neural Networks



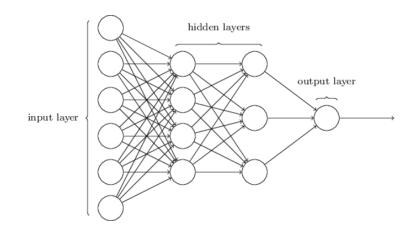
- We mostly adopt gradient-descent-style algorithms for optimization.
- No guarantee to converge to global optimal.
- Need to run it many times.
- Initialization matters.

Vanishing Gradient Problem

Backpropagation

•
$$\frac{\partial e_n(W)}{\partial w_{i,j}^{(\ell)}} = \delta_j^{(\ell)} x_i^{(\ell-1)}$$

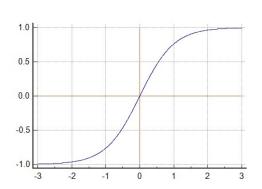
•
$$\delta_j^{(\ell)} = \theta' \left(s_j^{(\ell)} \right) \sum_{k=1}^{d^{(\ell+1)}} \delta_k^{(\ell+1)} w_{j,k}^{(\ell+1)}$$



• If we use activation function $\theta(s) = \tanh(s)$

•
$$\theta'(s) = 1 - \theta(s)^2 < 1$$

- In deep learning with a lot of layers,
 - the gradient might vanish
 - hard to update the early layers



Vanishing Gradient Problem

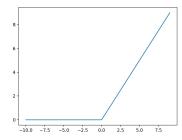
•
$$\delta_j^{(\ell)} = \theta' \left(s_j^{(\ell)} \right) \sum_{k=1}^{d^{(\ell+1)}} \delta_k^{(\ell+1)} w_{j,k}^{(\ell+1)}$$

• There is also a corresponding "exploding gradient problem"

- What can we do
 - Choose different activation functions
 - One common choice is Rectified Linear Unit (ReLU) and its variant

•
$$\theta(s) = \max(0, s)$$

- Choose better initialization
 - Many approaches



Weight Initialization

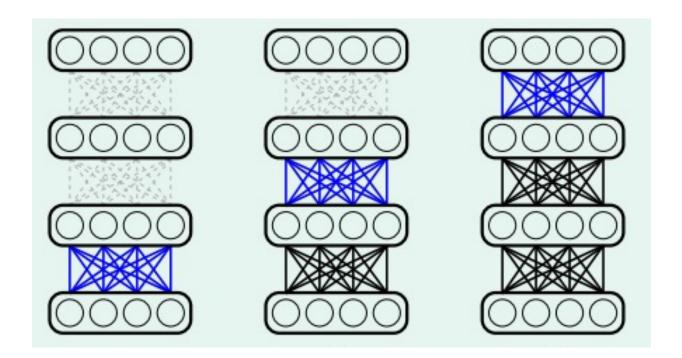
- Initializing weights to all 0 is a bad idea
 - Q6b of HW1
 - Hint: Look at the backpropagation formulation
- Randomly Initializing weights to regions so that vanishing/exploding gradients are less likely to happen
 - Activation-function dependent
 - e.g., Xavier initialization for tanh

$$\delta_{j}^{(\ell)} = \theta' \left(s_{j}^{(\ell)} \right) \sum_{k=1}^{d^{(\ell+1)}} \delta_{k}^{(\ell+1)} w_{j,k}^{(\ell+1)}$$

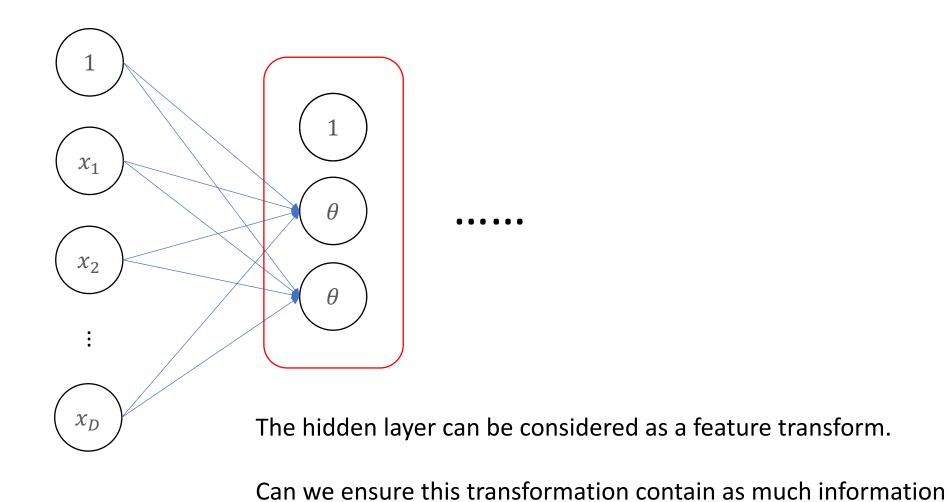
- Learning the initialization that might be closer to the optimal
 - E.g., using autoencoder

Initialization

- Hard to initialize the entire network well.
- Intuition: Initialize the weights layer by layer such that each layer preserves the properties of the previous layer.

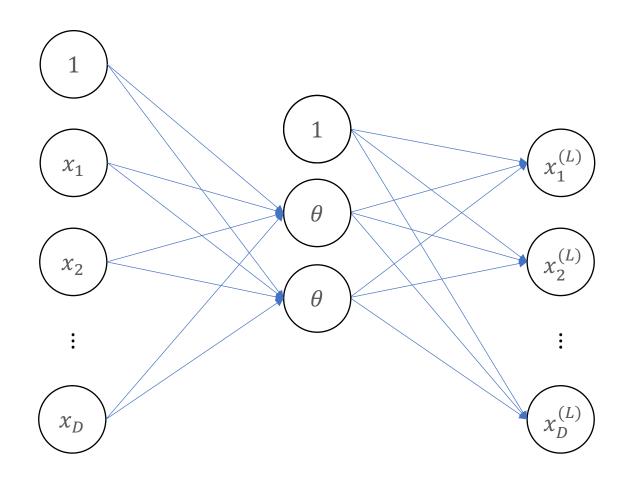


Autoencoders



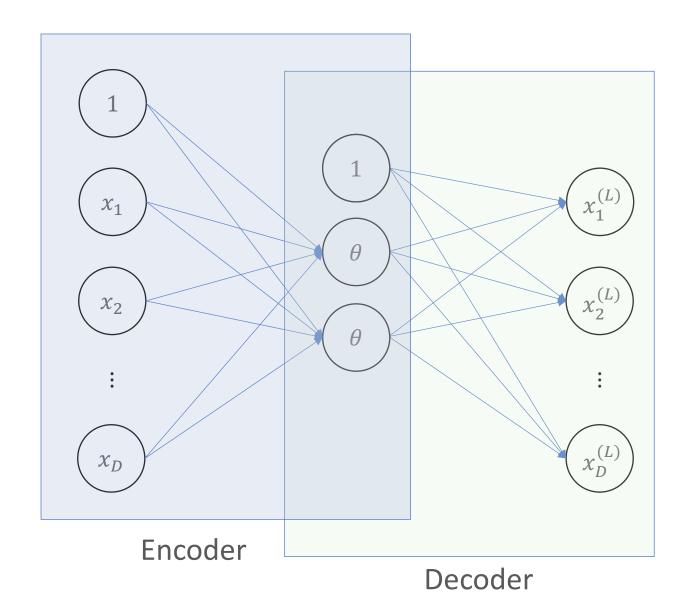
about the original input as possible?

Autoencoders

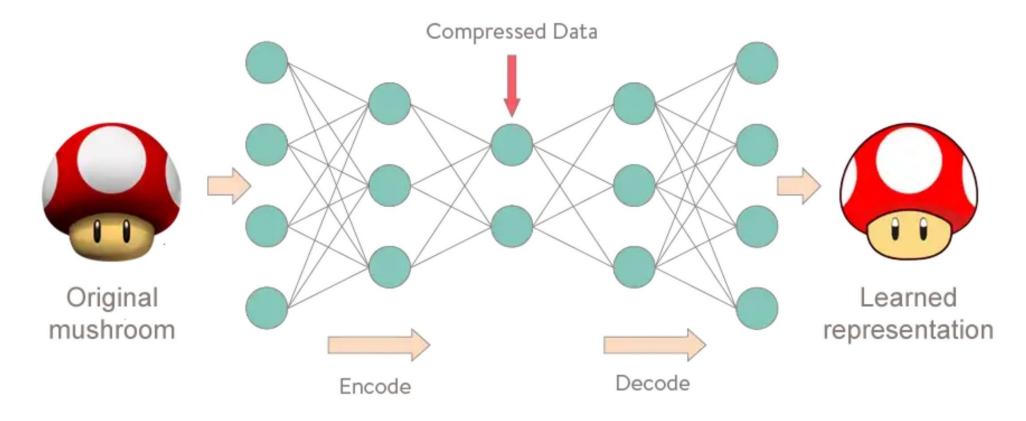


Minimize error of
$$\|\vec{x} - \overrightarrow{x^L}\|$$

Autoencoders



Autoencoder



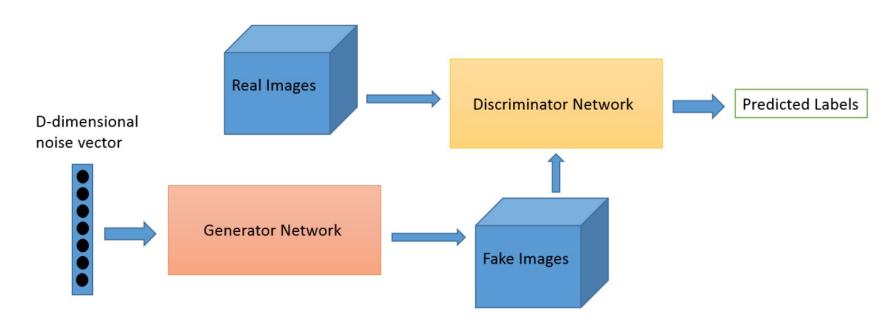
Unsupervised learning!

Cool Stuffs for Deep Learning

[Safe to Skip for the exam]

Generative Adversarial Nets (GAN)

- A Competition: Generator vs Discriminator
 - Discriminator wants to correctly classify the images (true images or not)
 - Generator wants to generate images that discriminator can't classify



[Safe to Skip for the Exam]



https://thisPersonDoesNotExist.com/

Style Transfer













- Informal intuitions:
 - Recall that we can treat hidden layers as feature transforms
 - Deep learning is learning representation of data
 - How to achieve style transfer:
 - Learn a content representation for an image using hidden layers
 - Learn a style representation for an image using hidden layers
 - Compute an image that jointly minimizes the distance from the content image's content representation and the style image's style representation
 - https://arxiv.org/pdf/1508.06576.pdf

A Quick Flashback to RBF

RBF Function

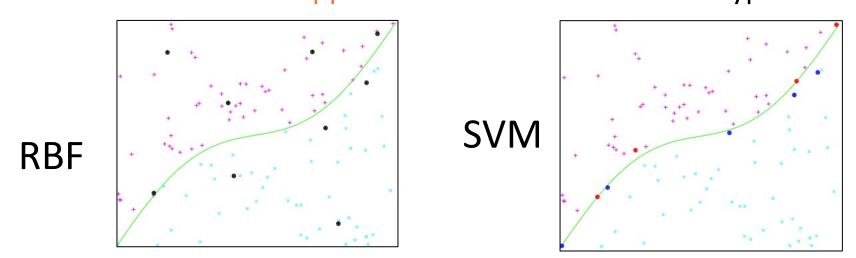
•
$$h(\vec{x}) = \sum_{k=1}^{K} w_k \, \phi\left(\frac{\|\vec{x} - \vec{\mu}_k\|}{r}\right)$$

- Connection to linear models
 - Parametric RBF is essentially linear model with nonlinear transformation
- Connection to nearest neighbor
 - Radial Basis Function is defined by "similarity
 - A prediction for a point is based on the "similarity" of the points to be predicted and other points

More Discussion on RBF

•
$$h(\vec{x}) = \sum_{k=1}^{K} w_k \, \phi\left(\frac{\|\vec{x} - \vec{\mu}_k\|}{r}\right)$$

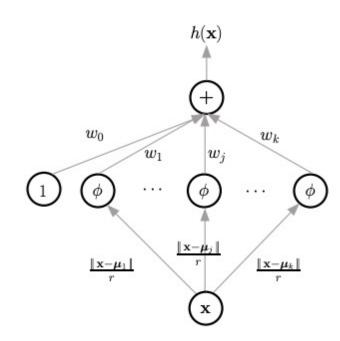
- Connection to SVM
 - Gaussian RBF Kernel: $g(\vec{x}) = sign(\sum_{\alpha_n^*>0} \alpha_n^* y_n K(\vec{x}_n, \vec{x}) + b^*))$
 - Use cluster centers or support vectors to characterize a hypothesis

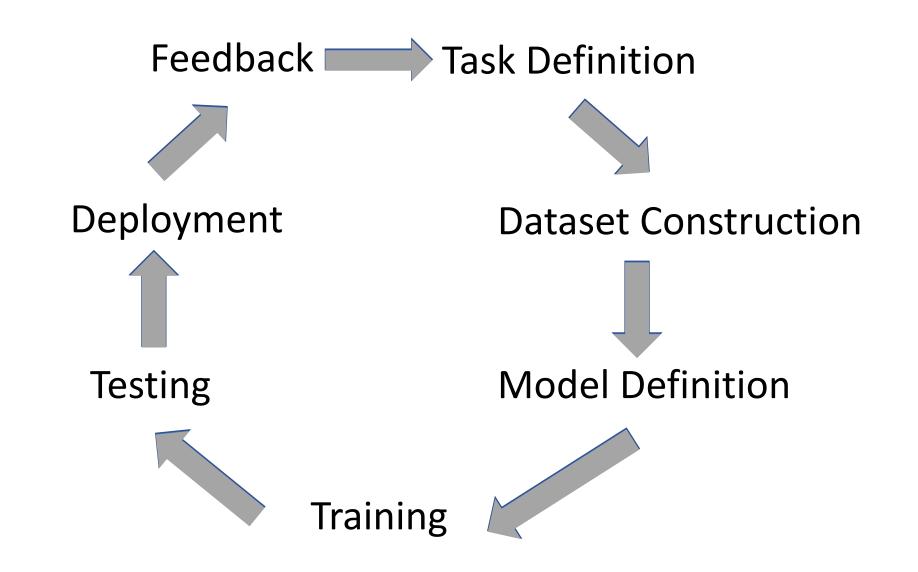


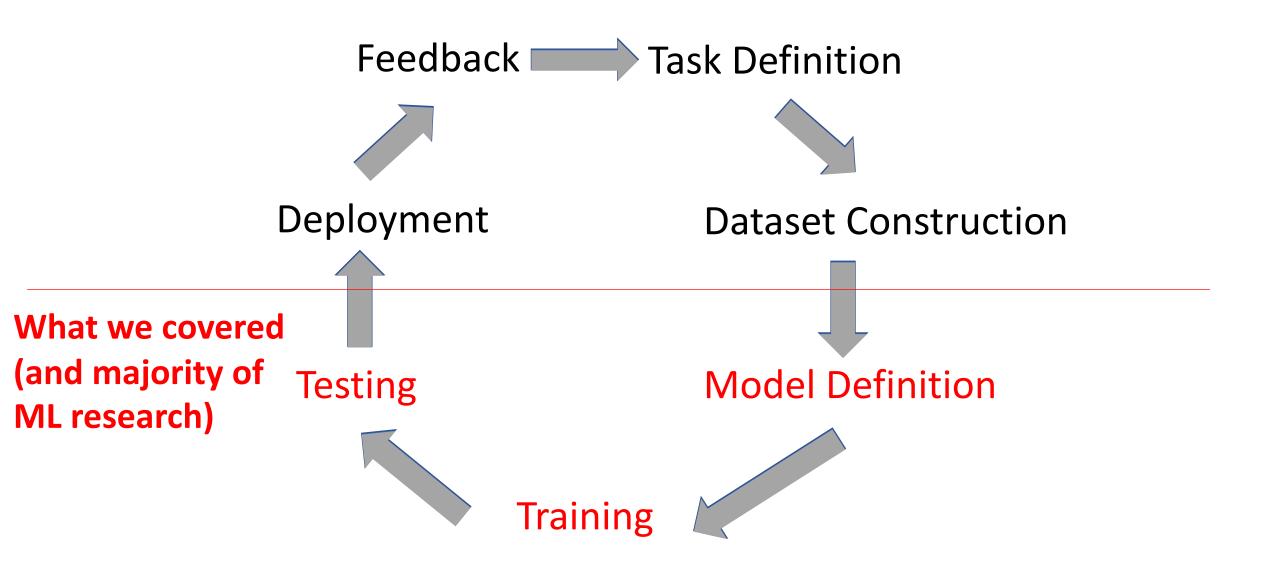
More Discussion on RBF

•
$$h(\vec{x}) = \sum_{k=1}^{K} w_k \, \phi\left(\frac{\|\vec{x} - \vec{\mu}_k\|}{r}\right)$$

- Connection to Neural Network
 - RBF can be graphically presented:
 - (Similar to SVM, it's a single-hidden layer NN)







To have "positive" impacts, we need to be careful in every stage

Feedback Task Definition



Deployment



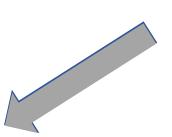
Dataset Construction

What we covered (and majority of ML research)

Testing

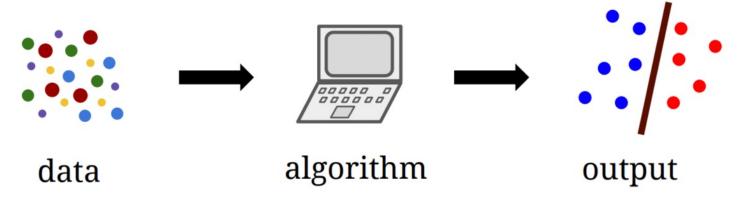


Model Definition



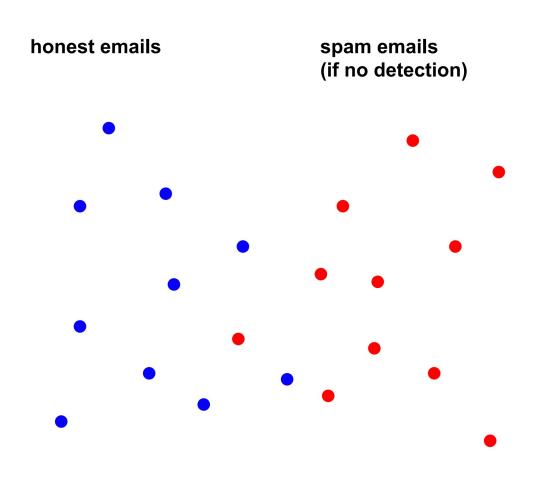
Supervised Learning

Standard setup of (supervised) machine learning

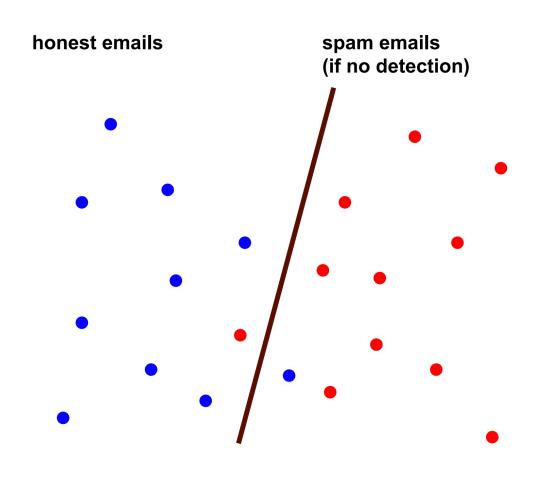


- Finding patterns from the given training datasets
- Use the pattern to make predictions on new testing data
- Fundamental assumption:
 - Training and testing data points are i.i.d. drawn from the same distribution

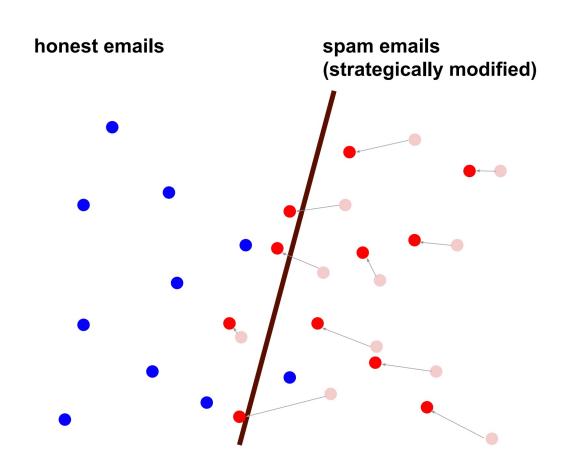
Example: Spam Filter



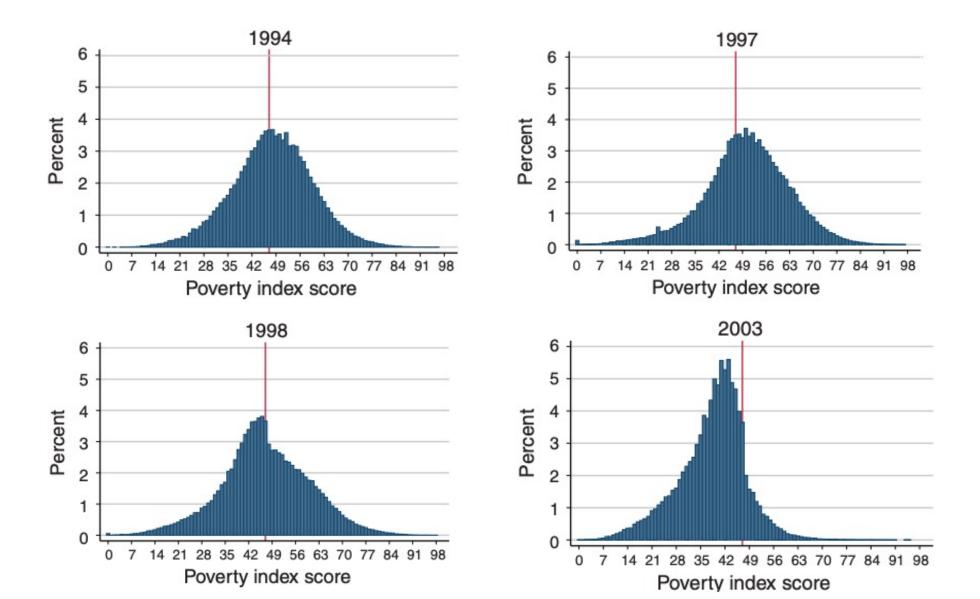
Example: Spam Filter



Example: Spam Filter



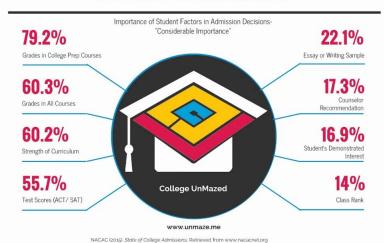
Social Program Eligibility [Camacho and Conover, 2012]

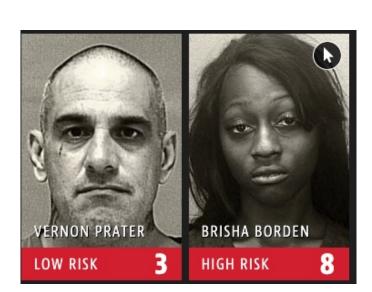


Goodhart's law:

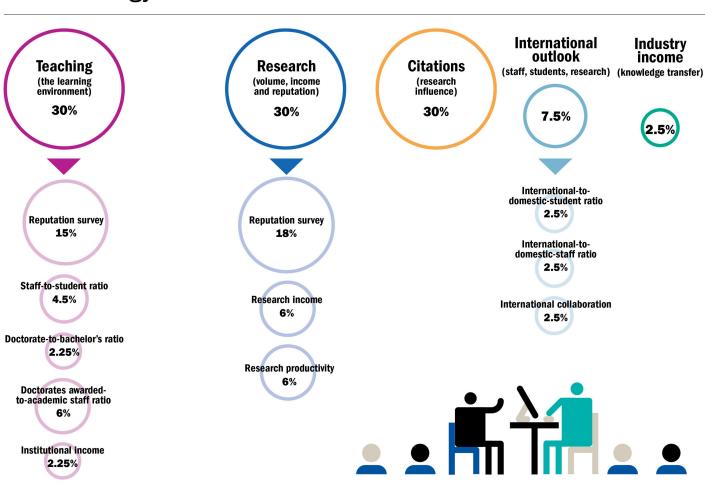
"If a measure becomes the public's goal, it is no longer a good measure."

COLLEGE ADMISSIONS





Methodology



Strategic Classification

