

CSE 417T

# Introduction to Machine Learning

Lecture 13

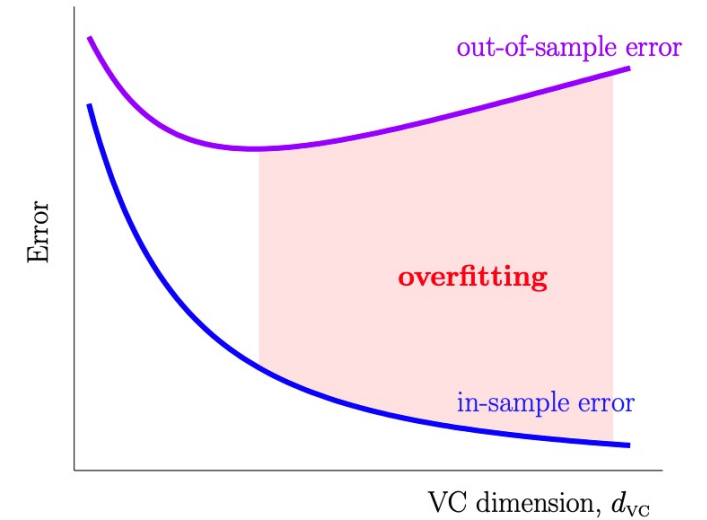
Instructor: Chien-Ju (CJ) Ho

- Homework 3: Due **Mar 19 (Friday)**. Keep track your late days
- Exam 1: **Mar 23 (Tuesday)**
  - Duration: 75+5 Minutes
  - Content: LFD Chapters 1 to 5
  - Time: By default, everyone is expected to take it during lecture time
    - Let me know **by this Friday (via private Piazza post)** if you can't do it during lecture time
  - Format: Gradescope online exam + turning on Zoom camera
    - A dummy exam is on Gradescope: Try file uploading and test various scenarios
  - Information access during exam:
    - Allowed: Textbook, slides, hardcopy materials (e.g., your own notes)
    - **Not allowed: search for information online during exam, talk to any other persons**
- Other notes
  - **Follow Piazza announcements**
  - I'll give some practice questions next week
  - Next Thursday lecture will be a review lecture

Recap

# Overfitting and Its Cures

- Overfitting
  - Fitting the data more than is warranted
  - Fitting the noise instead of the pattern of the data
  - Decreasing  $E_{in}$  but getting larger  $E_{out}$
  - When  $H$  is too strong, but  $N$  is not large enough
- Regularization
  - Intuition: Constraining  $H$  to make overfitting less likely to happen
- Validation
  - Intuition: Reserve data to estimate  $E_{out}$



# Regularization

- Constraining  $H$

- Example: Weight decay  $H(C) = \{h \in H_Q \text{ and } \vec{w}^T \vec{w} \leq C\}$
- Finding  $g \Rightarrow$  Constrained optimization

minimize  $E_{in}(\vec{w})$   
subject to  $\vec{w}^T \vec{w} \leq C$

- Defining augmented error

- $E_{aug}(h, \lambda, \Omega) = E_{in}(\vec{w}) + \frac{\lambda}{N} \Omega(h)$
- Finding  $g \Rightarrow$  Unconstrained optimization

minimize  $E_{in}(\vec{w}) + \frac{\lambda_c}{N} \vec{w}^T \vec{w}$

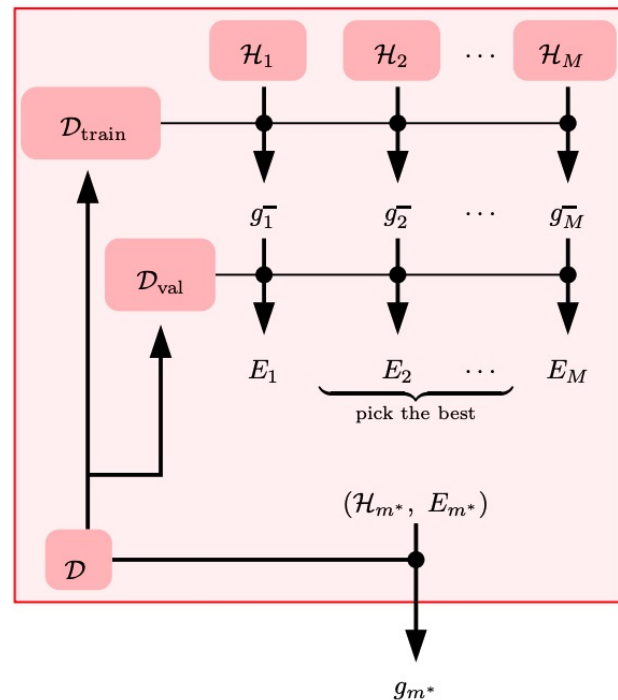
- The two interpretations are conceptually equivalent in a lot of cases.
- Understand the impacts of choosing  $\Omega$  and  $\lambda$

# Validations

- Reserving data to estimate  $E_{out}$

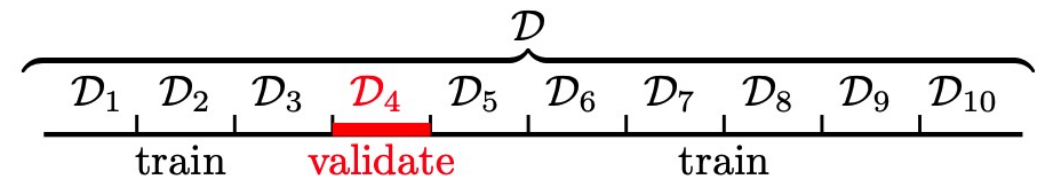
Note that the outlook comparisons are “in expectation”  
If you only get one “draw” of  $D_{train}, D_{val}, D_{test}$ ,  
you cannot say anything “for certain”

## Model Selection



|   | Outlook               | Relationship to $E_{out}$                  |
|---|-----------------------|--|
| $E_{in}$  | Incredibly optimistic | VC-bound                                   |
| $E_{val}$<br>(when used for<br>model selection) | Slightly optimistic   | Hoeffding's bound<br>(multiple hypotheses) |
| $E_{test}$                                      | Unbiased              | Hoeffding's bound<br>(single hypothesis)   |

- Cross Validation



# Today's Lecture

The notes are not intended to be comprehensive. They should be accompanied by lectures and/or textbook.  
Let me know if you spot errors.

# Three Learning Principles



Occam's Razor

Sampling Bias

Data Snooping

# Occam's Razor

The **simplest** model that fits the data is also the most **plausible**

# Sampling Bias

If the data is sampled in a **biased** way, learning will produce a similarly **biased** outcome.

# Credit card example

- Determine whether to approve credit cards given applicants' financial information
- Banks have lots of data:
  - Customer information
  - Whether they are good customers or not
- Are there any issues here?

|               |          |
|---------------|----------|
| age           | 32 years |
| gender        | male     |
| salary        | 40,000   |
| debt          | 26,000   |
| years in job  | 1 year   |
| years at home | 3 years  |
| ...           | ...      |

Approve for credit?

# Amazon scraps secret AI recruiting tool that showed bias against women

Jeffrey Dastin

8 MIN READ



The New York Times

## *Facial Recognition Is Accurate, if You're a White Guy*



By Steve Lohr

Feb. 9, 2018

SONIA PAUL

BACKCHANNEL 03.20.2017 12:00 AM

## Voice Is the Next Big Platform, Unless You Have an Accent

It's super funny that Alexa can't understand my mom — until we need Alexa to use the web, drive a car, and do pretty much anything else.

We will spend 1~2 lectures towards the end of the semester to talk about various ethical considerations of ML.

Occam's Razor

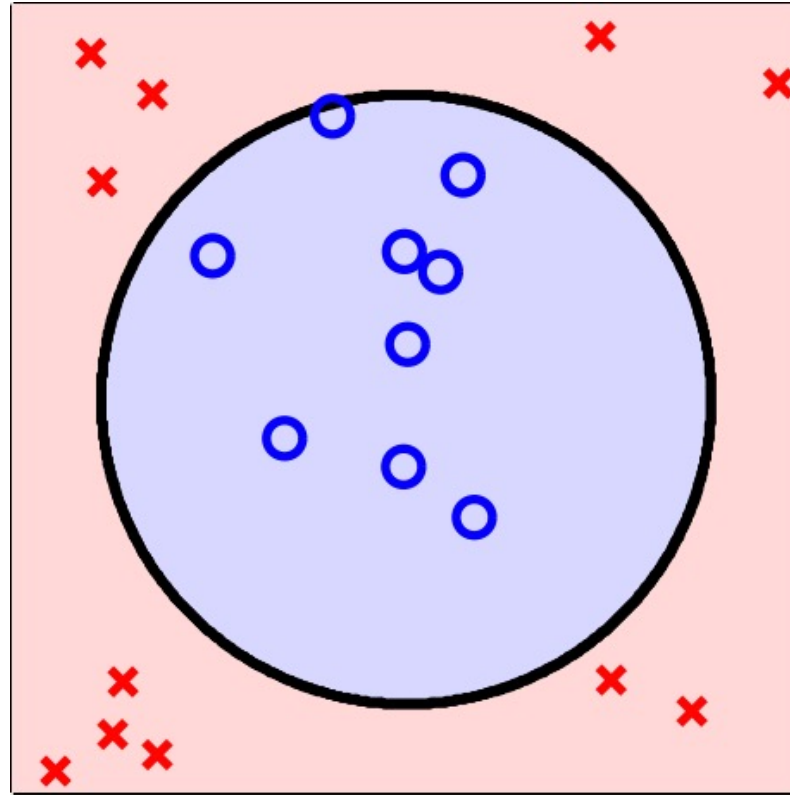
Sampling Bias

**Data Snooping**

# Data Snooping

If a data set has affected any step in the learning process, its ability to assess the outcome has been compromised.

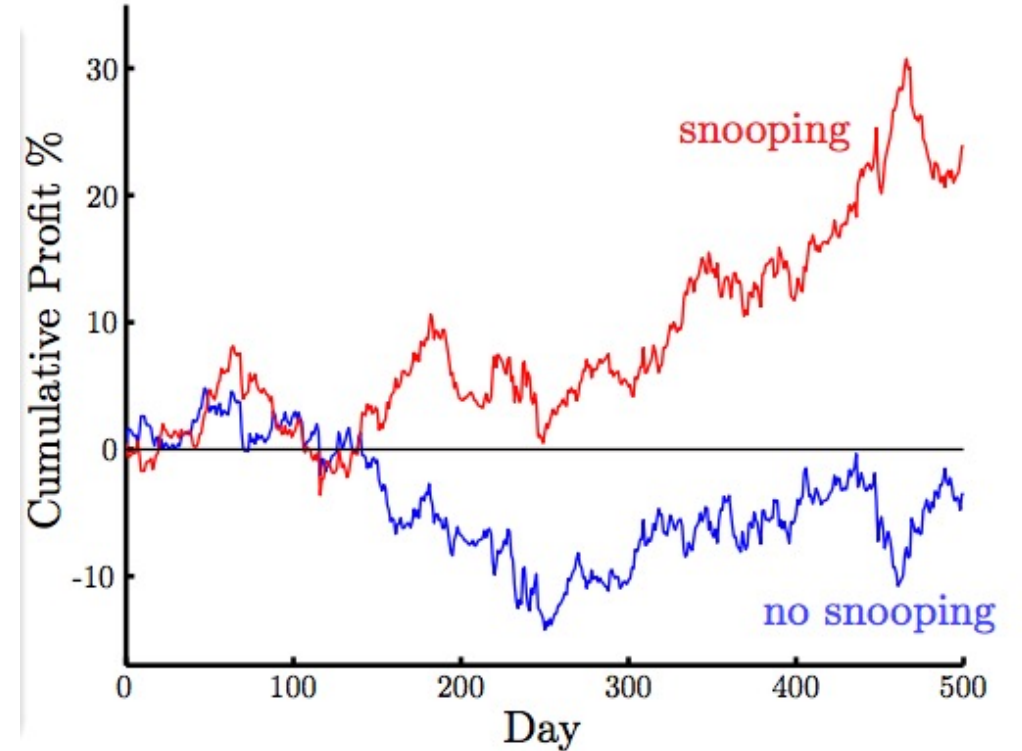
Shouldn't look at the data before selecting  $H$





# A Subtle Example

- Predict US Dollar vs. British Pound
  - $\vec{x}$ : the change for the previous 20 days
  - $y$ : the change in the 21th day
- Normalize data
- Split data  $D = D_{train} \cup D_{test}$
- Where does snooping happen?
  - The normalization “looks at”  $D_{test}$
- How should you perform normalization in Q1 of HW2?



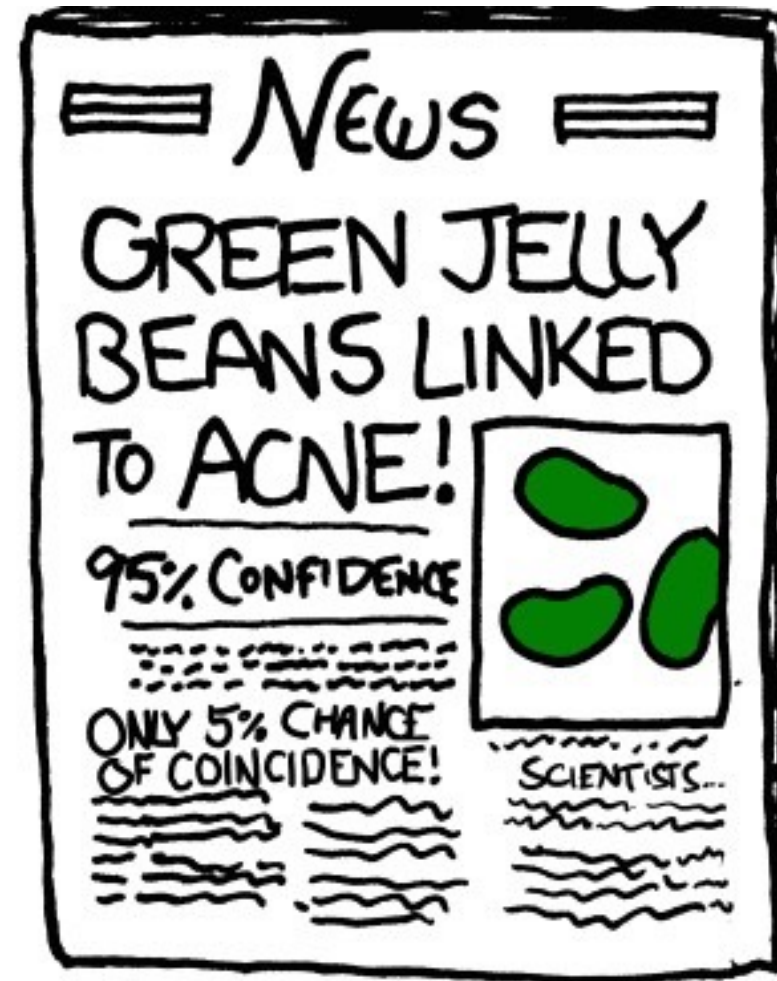
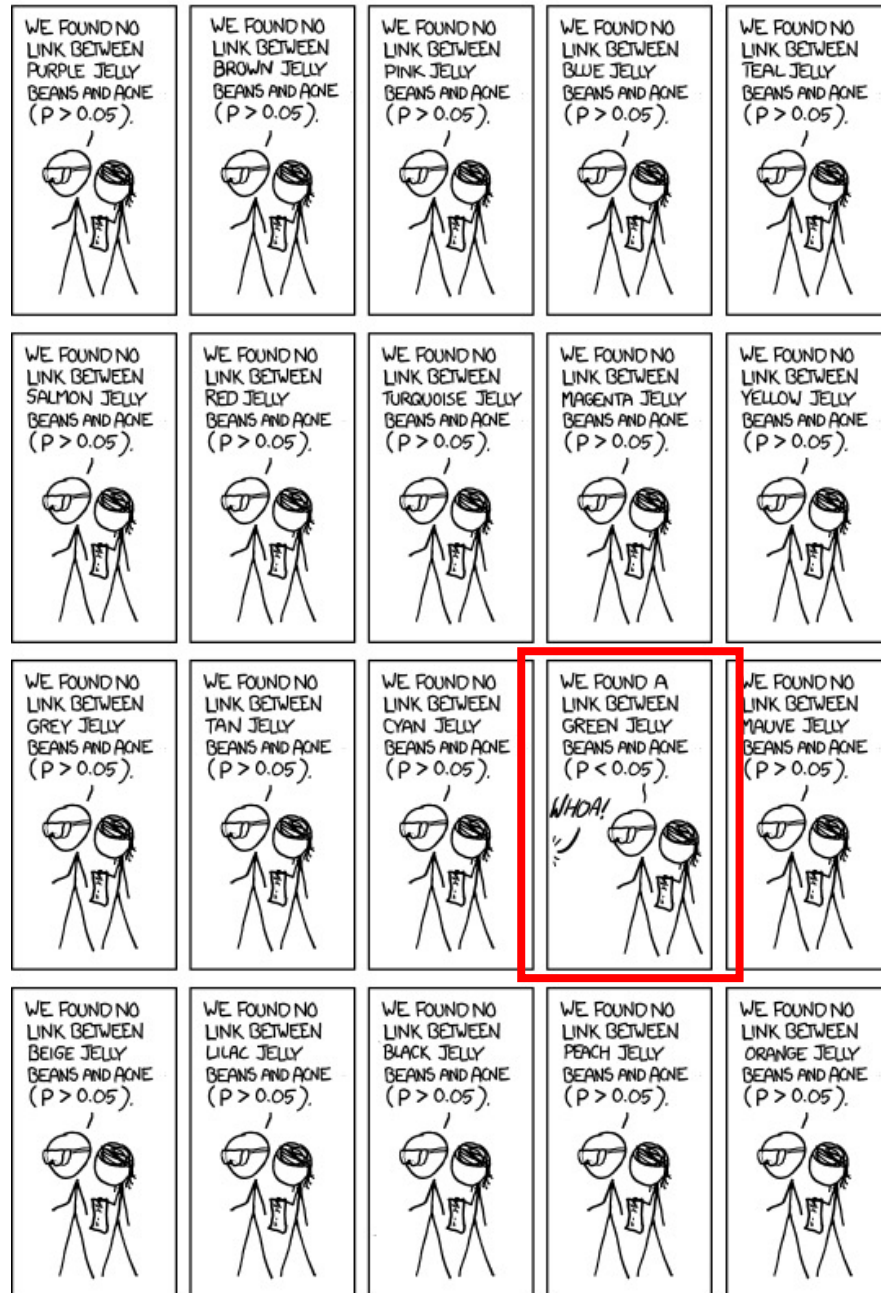
# Reuse of a Data Set

- Try one model after another **on the same data set**, you will eventually succeed.

“If you torture the data long enough, it will confess”

- VC dimension of the total learning models
- May even include what others tried (e.g., if you read their paper...)
- p-hacking...





# What Should We Do...

## Avoid data snooping

- Strict discipline
- E.g., be **honest** and lock the test data

## Account for data snooping

- Measure how much data is contaminated
- E.g., what we discussed in validation

Occam's Razor

Sampling Bias

Data Snooping

Content of Exam 1 Till Here

# Course Plan

- Foundations

- What's machine learning
- Feasibility of learning
- Generalization
- Linear models
- Non-linear transformations
- Overfitting and how to avoid it
  - Regularization
  - Validation

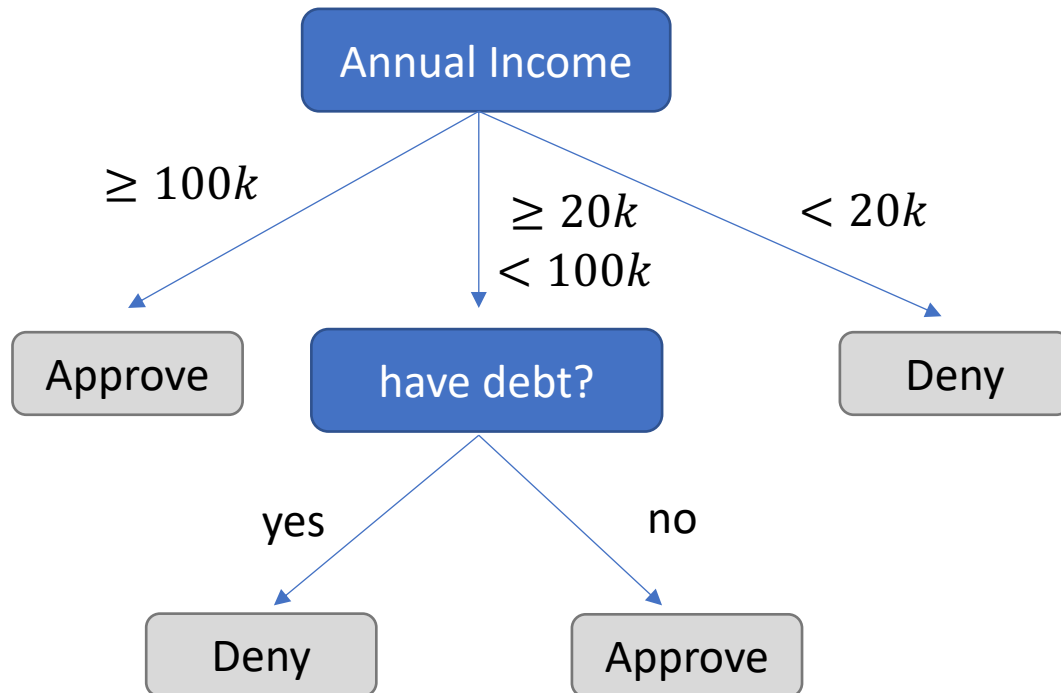
- Techniques

- Decision tree
- Ensemble learning
  - Bagging and random forest
  - Boosting and Adaboost
- Nearest neighbors
- Support vector machine
- Neural networks
- ...



# Decision Tree

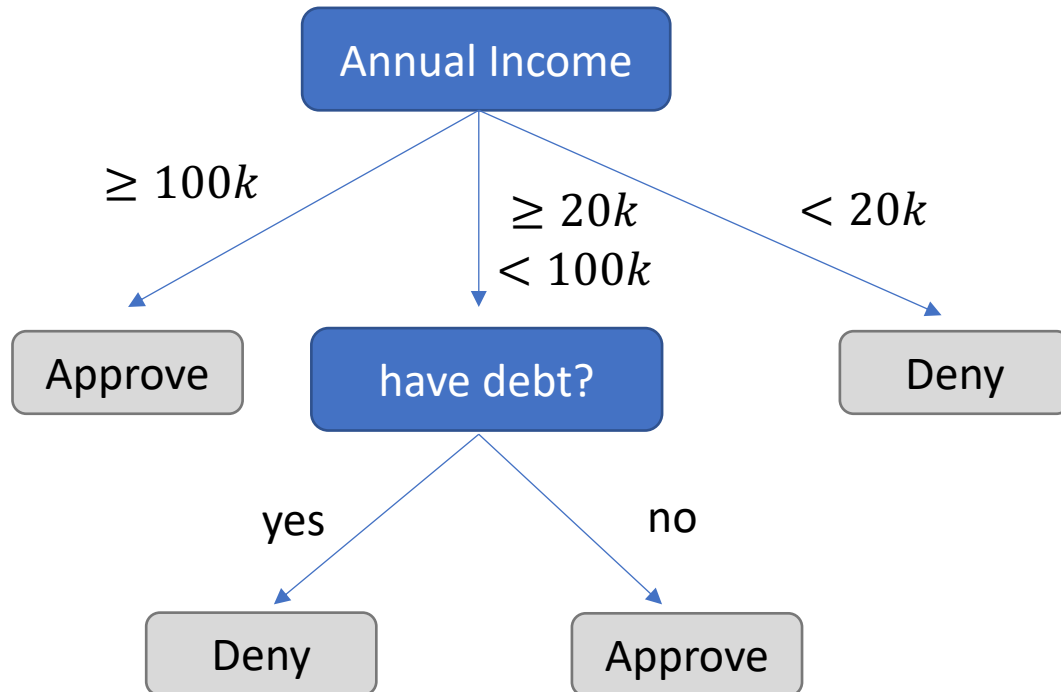
# Decision Tree Hypothesis



- $\vec{x} = (\text{annual income, have debt})$
- $y \in \{\text{approve, deny}\}$

Credit Card Approval Example

# Decision Tree Hypothesis



Credit Card Approval Example

- Pros
  - Easy to interpret (interpretability is getting attention and is important in some domains)
  - Can handle multi-type data (Numerical, categorical. ...)
  - Easy to implement (Bunch of if-else rules)
- Cons

# Decision Tree Hypothesis



Credit Card Approval Example

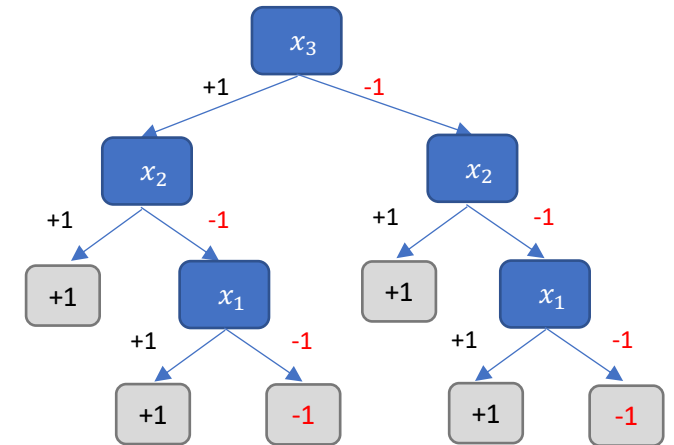
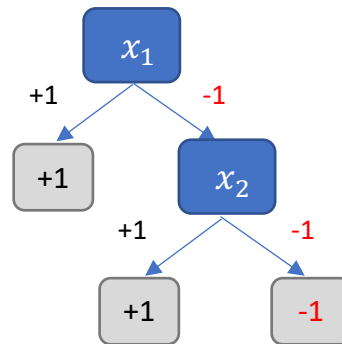
- Pros
  - Easy to interpret (interpretability is getting attention and is important in some domains)
  - Can handle multi-type data (Numerical, categorical. ...)
  - Easy to implement (Bunch of if-else rules)
- Cons
  - Generally speaking, bad generalization
  - VC dimension is infinity
  - High variance (small change of data leads to very different hypothesis)
  - Easily overfit
- Why we care?
  - One of the classical models
  - Building block for other models (e.g., random forest)

# Learning Decision Tree from Data

- Given dataset  $D$ , how to learn a decision tree hypothesis?
- Potential approach
  - Find  $g = \operatorname{argmin}_{h \in H} E_{in}(h)$

| $x_1$ | $x_2$ | $x_3$ | $y$ |
|-------|-------|-------|-----|
| +1    | +1    | +1    | +1  |
| +1    | +1    | -1    | +1  |
| +1    | -1    | +1    | +1  |
| +1    | -1    | -1    | +1  |
| -1    | +1    | +1    | +1  |
| -1    | +1    | -1    | +1  |
| -1    | -1    | +1    | -1  |
| -1    | -1    | -1    | -1  |

- Multiple decision trees with zero  $E_{in}$



Which one do you think might generalize better?

# Learning Decision Tree from Data

- Conceptual intuition to deal with overfitting
  - Regularization: **Constrain  $H$**
- Informally,

minimize  $E_{in}$   
subject to  $size(tree) \leq C$
- This optimization is generally computationally intractable.
- Most decision tree learning algorithms rely on **heuristics** to approximate the goal.

# Template of Greedy-Based Decision Tree Algorithm

- DecisionTreeLearn( $D$ ): Input a dataset  $D$ , output a decision tree hypothesis
  - Create a root node
  - If **termination conditions** are met
    - return a single node tree with **leaf prediction** based on  $D$
  - Else: Greedily find a feature  $A$  (assigned as root) to split according to **split criteria**
    - For each possible value  $v_i$  of  $A$ 
      - Let  $D_i$  be the dataset containing data with value  $v_i$  for feature  $A$
      - Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root
- Most decision tree learning algorithms follow this template, but with different choices of **heuristics**

# Example

DecisionTreeLearn( $D$ )

Create a root node

If **termination conditions** are met

return a single node tree with **leaf prediction** based on  $D$

Else: Greedily find a feature  $A$  (assigned as root) to split according to **split criteria**

For each possible value  $v_i$  of  $A$

Let  $D_i$  be the dataset containing data with value  $v_i$  for feature  $A$

Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root

Termination conditions not met  
Find a feature to split

| $x_1$ | $x_2$ | $x_3$ | $y$ |
|-------|-------|-------|-----|
| +1    | +1    | +1    | +1  |
| +1    | +1    | -1    | +1  |
| +1    | -1    | +1    | +1  |
| +1    | -1    | -1    | +1  |
| -1    | +1    | +1    | +1  |
| -1    | +1    | -1    | +1  |
| -1    | -1    | +1    | -1  |
| -1    | -1    | -1    | -1  |

DecisionTreeLearn

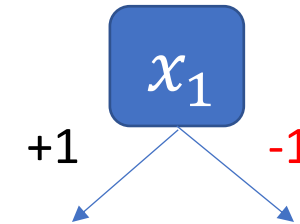


| $x_1$ | $x_2$ | $x_3$ | $y$ |
|-------|-------|-------|-----|
| +1    | +1    | +1    | +1  |
| +1    | +1    | -1    | +1  |
| +1    | -1    | +1    | +1  |
| +1    | -1    | -1    | +1  |

DecisionTreeLearn

terminate

Leaf prediction +1



| $x_1$ | $x_2$ | $x_3$ | $y$ |
|-------|-------|-------|-----|
| -1    | +1    | +1    | +1  |
| -1    | +1    | -1    | +1  |
| -1    | -1    | +1    | -1  |
| -1    | -1    | -1    | -1  |

DecisionTreeLearn

Don't terminate

Find next feature to split



# Example Heuristics

DecisionTreeLearn( $D$ )

Create a root node

If **termination conditions** are met

return a single node tree with **leaf prediction** based on  $D$

Else: Greedily find a feature  $A$  to split according to **split criteria**

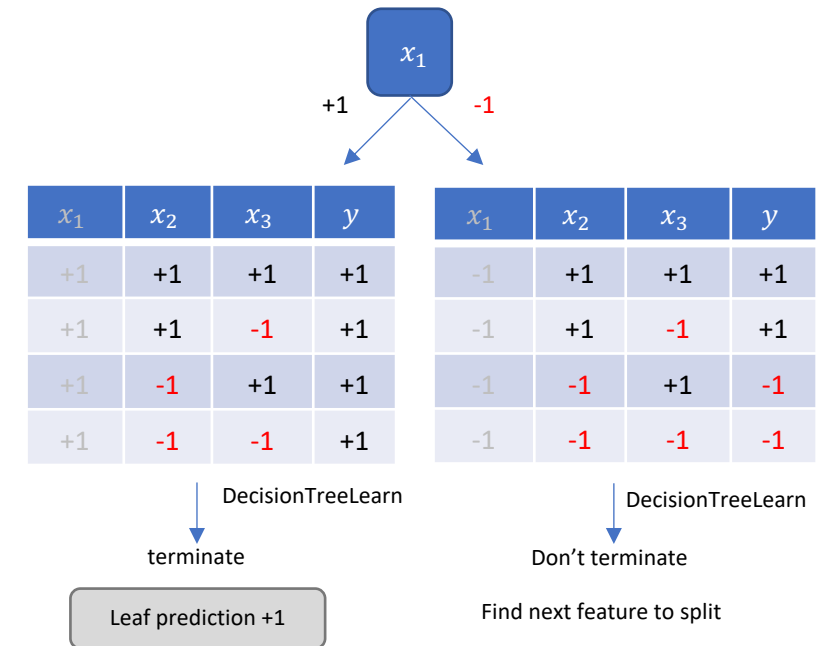
For each possible value  $v_i$  of  $A$

Let  $D_i$  be the dataset containing data with value  $v_i$  for feature  $A$

Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root

- **Termination conditions**

- When the dataset is empty
- When all labels are the same
- when all features are the same
- When the depth of the tree is too deep
- ...



- **Leaf predictions**

- Majority voting
- Average (for regression)
- ...

- **Split criteria?**

# Split Criteria

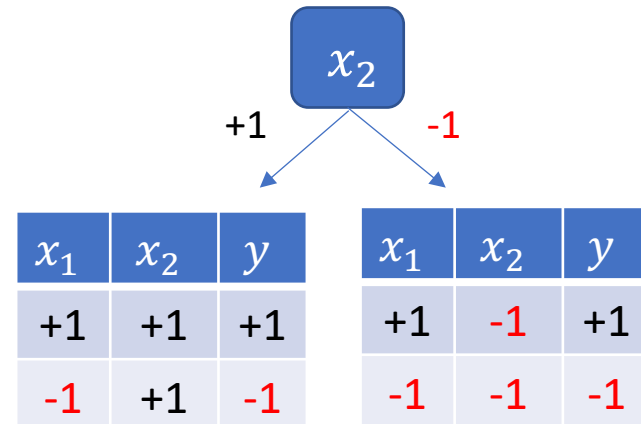
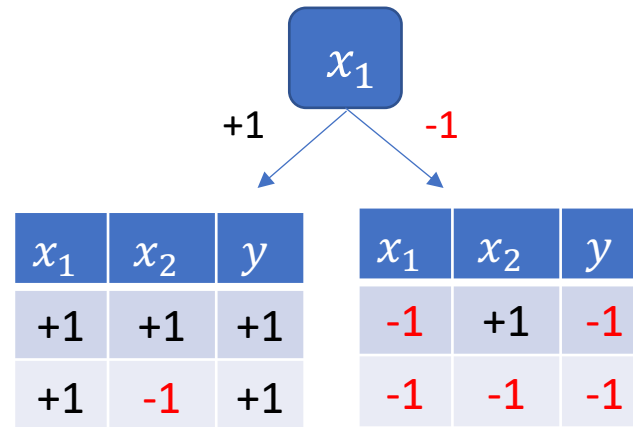
- Which feature would you choose to split?

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| +1    | +1    | +1  |
| +1    | -1    | +1  |
| -1    | +1    | -1  |
| -1    | -1    | -1  |

# Split Criteria

- Which feature would you choose to split?

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| +1    | +1    | +1  |
| +1    | -1    | +1  |
| -1    | +1    | -1  |
| -1    | -1    | -1  |



- Want the tree to be “smaller”
  - Intuition: choose the one that the labels are more “pure”
  - Example: choose the one maximizing **information gain** => **ID3 Algorithm**

# Brief Intro to Information Entropy

- Assume there are  $K$  possible labels
- Entropy:
  - $H(D) = \sum_{i=1}^K p_i \log_2 \frac{1}{p_i}$
  - $p_i$ : ratio of points with label  $i$  in the data

By definition

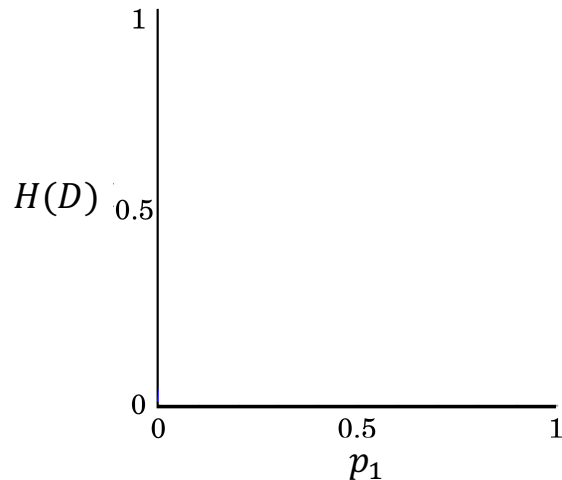
$$0 \log_2 \frac{1}{0} = 0; 1 \log_2 \frac{1}{1} = 0$$

# Brief Intro to Information Entropy

- Assume there are  $K$  possible labels
- Entropy:
  - $H(D) = \sum_{i=1}^K p_i \log_2 \frac{1}{p_i}$
  - $p_i$ : ratio of points with label  $i$  in the data
- Binary case with  $K = 2$

By definition

$$0 \log_2 \frac{1}{0} = 0; 1 \log_2 \frac{1}{1} = 0$$



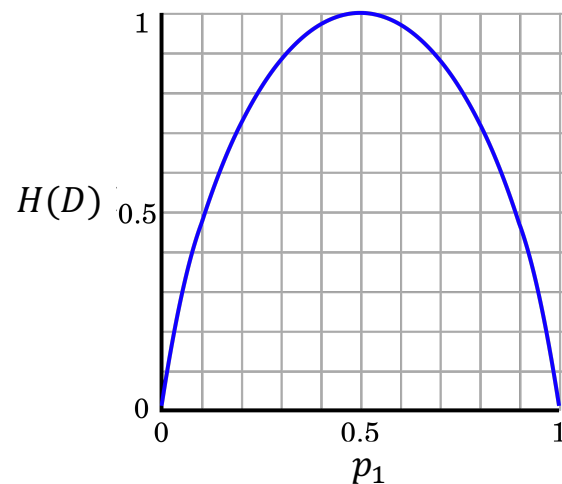
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- Assume there are  $K$  possible labels
- Entropy:
  - $H(D) = \sum_{i=1}^K p_i \log_2 \frac{1}{p_i}$
  - $p_i$ : ratio of points with label  $i$  in the data

By definition

$$0 \log_2 \frac{1}{0} = 0; 1 \log_2 \frac{1}{1} = 0$$

- Binary case with  $K = 2$



- Interpretations of entropy
  - Expected # bit to encode a distribution
- Higher entropy
  - data is less “pure”
- “pure” data => all labels are +1 or -1 => entropy = 0
- Want to choose splits that lead to pure data, i.e., lower entropy

# ID3: Using Information Gain as Selection Criteria

- Information gain of choosing feature  $A$  to split
  - $Gain(D, A) = H(D) - \sum_i \frac{|D_i|}{|D|} H(D_i)$  [The amount of decrease in entropy]
- ID3: Choose the split that maximize  $Gain(D, A)$

Notation:  
 $|D|$  is the number of points in  $D$

DecisionTreeLearn( $D$ )

Create a root node

If **termination conditions** are met

return a single node tree with **leaf prediction** based on  $D$

Else: Greedily find a feature  $A$  to split according to **split criteria**

For each possible value  $v_i$  of  $A$

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Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root

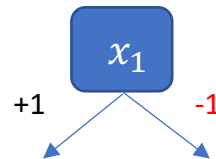
- ID3 termination conditions
  - If all labels are the same
  - If all features are the same
  - If dataset is empty
- ID3 leaf predictions
  - Most common labels (majority voting)
- ID3 split criteria
  - Information gain

# ID3: Using Information Gain as Selection Criteria

- Information gain of choosing feature  $A$  to split
  - $Gain(D, A) = H(D) - \sum_i \frac{|D_i|}{|D|} H(D_i)$
- ID3: Choose the split that maximize  $Gain(D, A)$

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| +1    | +1    | +1  |
| +1    | -1    | +1  |
| -1    | +1    | -1  |
| -1    | -1    | -1  |

$$H(D) = 0.5 \log_2 2 + 0.5 \log_2 2 = 1$$



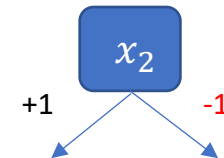
| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| +1    | +1    | +1  |
| +1    | -1    | +1  |

$$H(D_{x_1=1}) = 0$$

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| -1    | +1    | -1  |
| -1    | -1    | -1  |

$$H(D_{x_1=-1}) = 0$$

$$Gain(D, x_1) = 1$$



| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| +1    | +1    | +1  |
| -1    | +1    | -1  |

$$H(D_{x_2=1}) = 1$$

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| +1    | -1    | +1  |
| -1    | -1    | -1  |

$$H(D_{x_2=-1}) = 1$$

$$Gain(D, x_2) = 0$$

ID3 will choose  $x_1$  as the next split attribute



# Further Addressing Overfitting

- More Regularization (Constrain  $H$ )
  - Do not split leaves past a fixed depth
  - Do not split leaves with fewer than  $c$  labels
  - Do not split leaves where the maximal information gain is less than  $\tau$
- Pruning (removing leaves)
  - Evaluate each split using a validation set and compare the validation error with and without that split (replacing it with the most common label at that point)
  - Use statistical test to examine whether the split is “informative” (leads to different enough subtrees)

# More Discussions

- Real-valued features (continuous  $x$ )
  - Need to select threshold for branching
- Regression (continuous  $y$ )
  - Change leaf prediction: e.g., average instead of majority vote
  - Change measure for “purity” of data: e.g., squared error of data