# CSE 417T Introduction to Machine Learning

Lecture 12

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#### Logistics

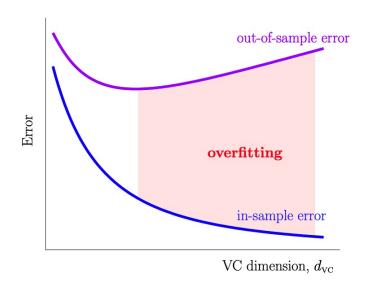
- Homework 2: Due Feb 24 (Thu)
- Homework 3: Due Mar 5 (Sat)
  - Keep track of your own late days
- Exam 1: Mar 10 (Thursday)
  - Topics: LFD Chapters 1 to 5
  - Covid-permitting
    - Timed exam (75 min) during lecture time in the classroom
    - Closed-book exam with 2 letter-size cheat sheets allowed (4 pages in total)
      - No format limitations (it can be typed, written, or a combination)
  - Mar 8 (Tuesday) will be a review lecture

## Recap

## Overfitting and Its Cures

#### Overfitting

- Fitting the data more than is warranted
- Fitting the noise instead of the pattern of the data
- Decreasing  $E_{in}$  but getting larger  $E_{out}$
- When *H* is too strong, but *N* is not large enough



#### Regularization

Intuition: Constrain H to make overfitting less likely to happen

#### Validation

• Intuition: Reserve data to estimate  $E_{out}$ 

### Regularization

- Constrain H
  - Example: Weight decay H(C) = {h ∈ H<sub>Q</sub> and w̄<sup>T</sup>w̄ ≤ C}
     Finding g => Constrained optimization

minimize  $E_{in}(\vec{w})$ subject to  $\overrightarrow{w}^T \overrightarrow{w} \leq C$ 

- Define augmented error
  - $E_{aug}(h, \lambda, \Omega) = E_{in}(\overrightarrow{w}) + \frac{\lambda}{N}\Omega(h)$
  - Finding g => Unconstrained optimization

minimize 
$$E_{in}(\overrightarrow{w}) + \frac{\lambda_C}{N} \overrightarrow{w}^T \overrightarrow{w}$$

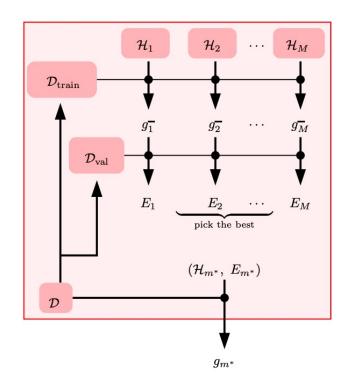
- The two interpretations are conceptually equivalent in a lot of cases.
- Understand the impacts of choosing  $\Omega$  and  $\lambda$

#### **Validations**

• Reserving data to estimate  $E_{out}$ 

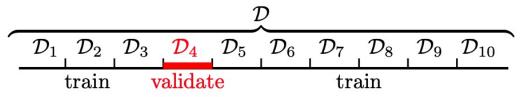
Note that the outlook comparisons are "in expectation" If you only get one "draw" of  $D_{train}$ ,  $D_{val}$ ,  $D_{test}$ , you cannot say anything "for certain"

#### **Model Selection**



	Outlook	Relationship to $E_{out}$
$E_{in}$	Incredibly optimistic	VC-bound
$E_{val}$ (when used for model selection)	Slightly optimistic	Hoeffding's bound (multiple hypotheses)
$E_{test}$	Unbiased	Hoeffding's bound (single hypothesis)

Cross Validation



## Today's Lecture

The notes are not intended to be comprehensive. They should be accompanied by lectures and/or textbook. Let me know if you spot errors.

## Three Learning Principles

Occam's Razor

Sampling Bias

Data Snooping

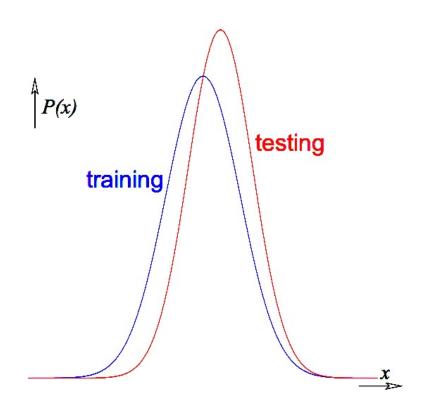
#### Occam's Razor

The simplest model that fits the data is also the most plausible

## Sampling Bias

If the data is sampled in a biased way, learning will produce a similarly biased outcome.

### What can we do if there are sampling biases

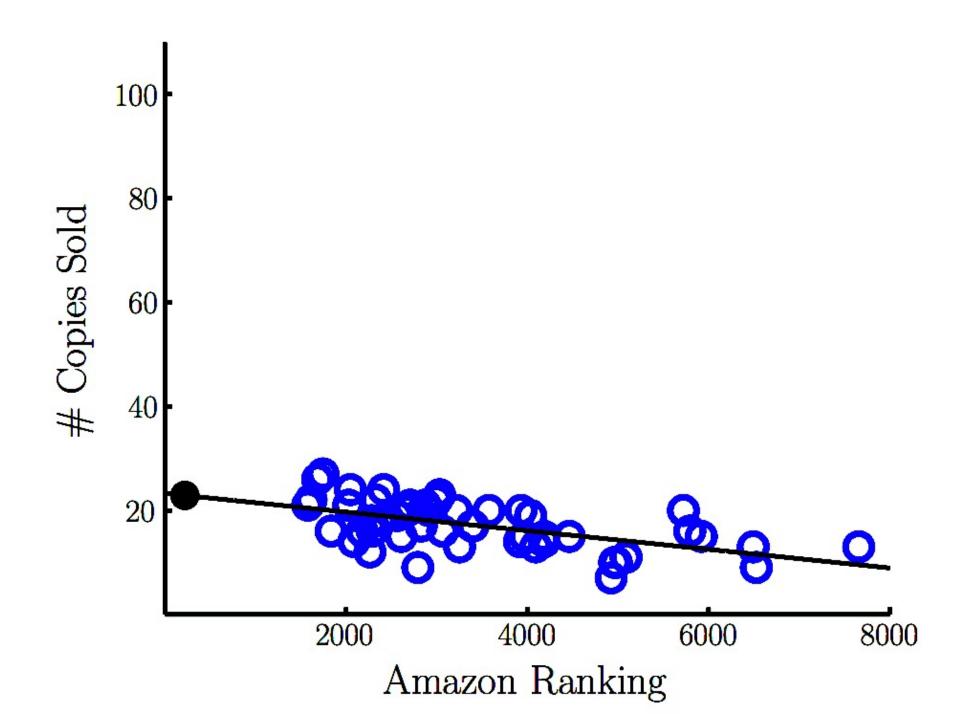


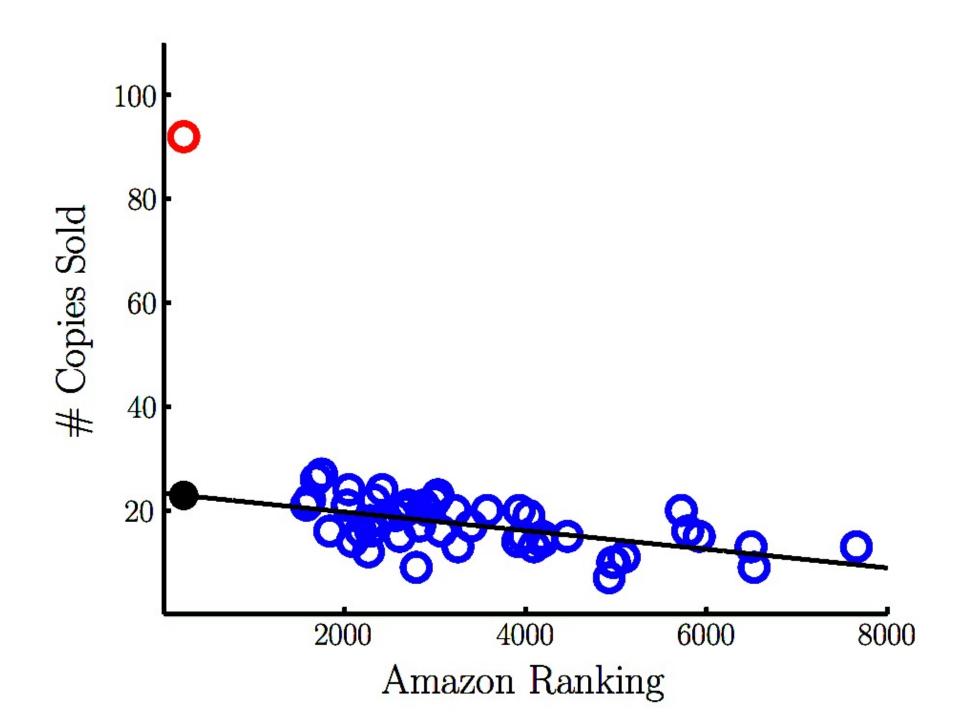
Make sure the training and test distributions are as close as possible...

- Example: importance weighting

Not always possible....

 If you don't have access to some region of points in training, but they appear in the testing distribution





### Credit card example

 Determine whether to approve credit cards given applicants' financial information

- Banks have lots of data:
  - Customer information
  - Whether they are good customers or not

Are there any issues here?

age	32 years
gender	male
salary	40,000
debt	26,000
years in job	1 year
years at home	3 years

Approve for credit?

## Amazon scraps secret AI recruiting tool that showed bias against women

Jeffrey Dastin

8 MIN READ

The New York Times

## Facial Recognition Is Accurate, if You're a White Guy



By Steve Lohr

Feb. 9, 2018



BACKCHANNEL 03.20.2017 12:00 AM

## Have an Accent

It's super funny that Alexa can't understand my mom — until we need Alexa to use the web, drive a car, and do pretty much anything else.

We will spend 1~2 lectures towards the end of the semester to talk about various ethical considerations of ML.

Occam's Razor

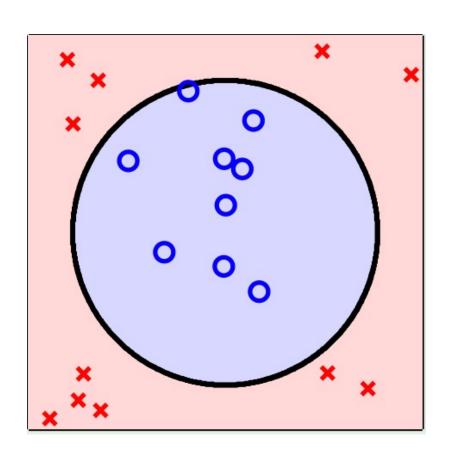
Sampling Bias

Data Snooping

### Data Snooping

If a data set has affected any step in the learning process, its ability to assess the outcome has been compromised.

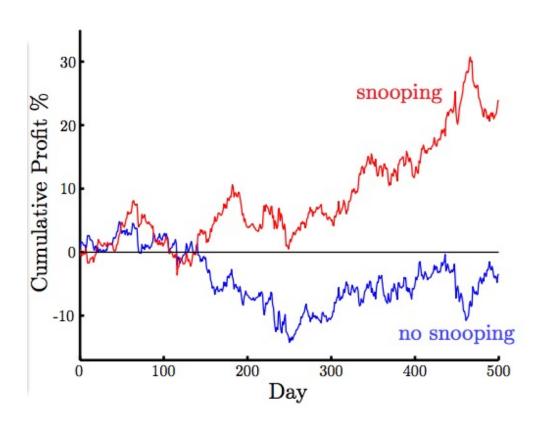
## Shouldn't look at the data before selecting H



## A Subtle Example

- Predict US Dollar vs. British Pound
  - $\vec{x}$ : the change for the previous 20 days
  - y: the change in the 21th day
- Normalize data
- Split data  $D = D_{train} \cup D_{test}$

- Where does snooping happen?
  - The normalization "looks at"  $D_{test}$



How should you perform normalization in Q1 of HW2?

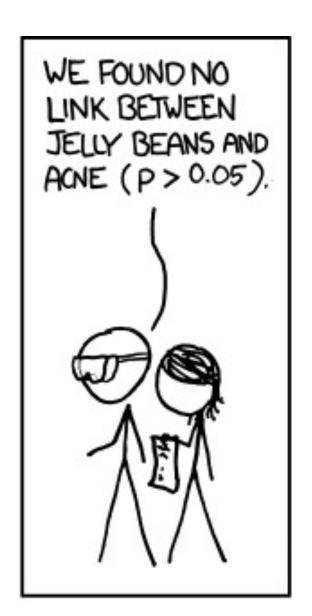
#### Reuse of a Data Set

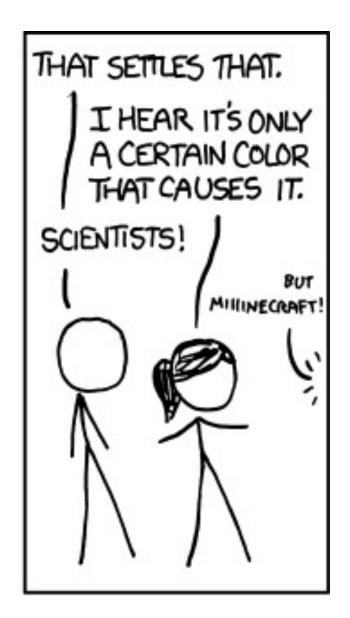
• Try one model after another **on the same data set**, you will eventually succeed.

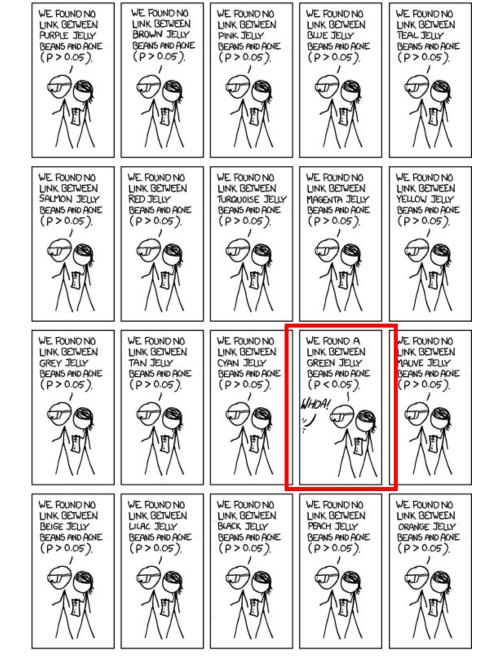
"If you torture the data long enough, it will confess"

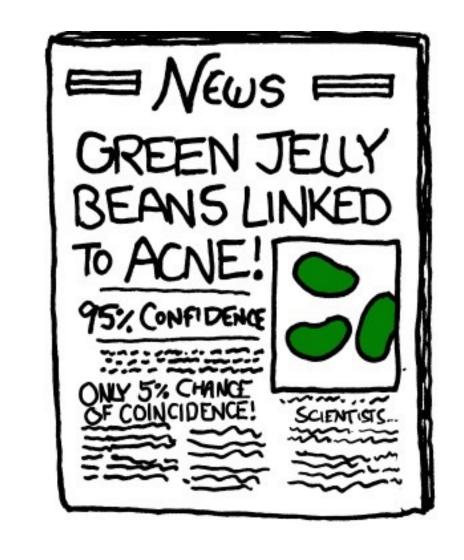
- VC dimension of the total learning models
- May even include what others tried (e.g., if you read their paper...)
- p-hacking...











#### What Should We Do...

#### Avoid data snooping

- Strict discipline
- E.g., be honest and lock the test data

#### Account for data snooping

- Measure how much data is contaminated
- E.g., what we discussed in validation

Occam's Razor

Sampling Bias

Data Snooping

## Content of Exam 1 Till Here

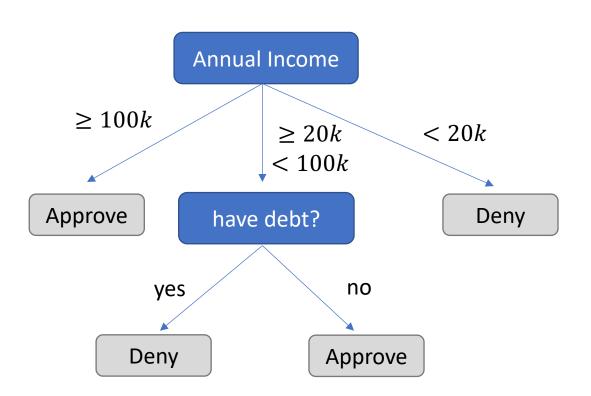
#### Course Plan

- Foundations
  - What's machine learning
  - Feasibility of learning
  - Generalization
  - Linear models
  - Non-linear transformations
  - Overfitting and how to avoid it
    - Regularization
    - Validation

- Techniques
  - Decision tree
  - Ensemble learning
    - Bagging and random forest
    - Boosting and Adaboost
  - Nearest neighbors
  - Support vector machine
  - Neural networks
  - •

## Decision Tree

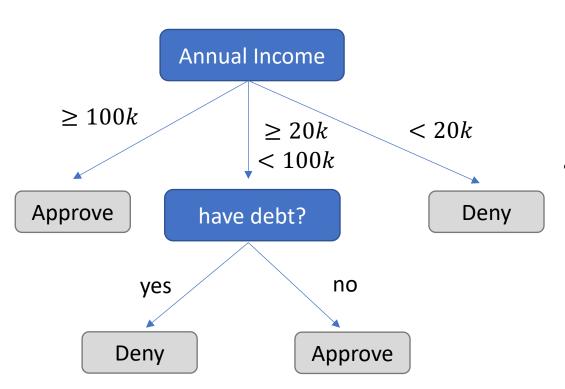
### Decision Tree <u>Hypothesis</u>



- $\vec{x}$  = (annual income, have debt)
- $y \in \{approve, deny\}$

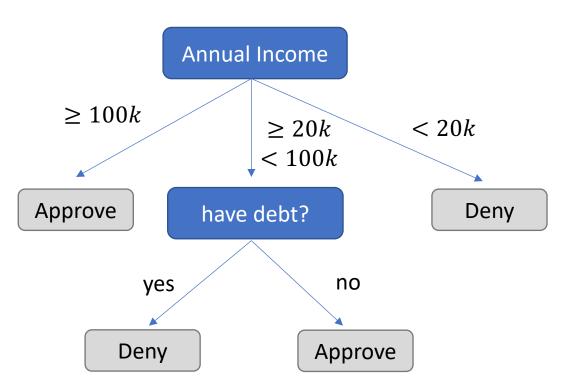
Credit Card Approval Example

## Decision Tree <u>Hypothesis</u>



- Pros
  - Easy to interpret (interpretability is getting attention and is important in many domains)
  - Can handle multi-type data (Numerical, categorical. ...)
  - Easy to implement (Bunch of if-else rules)
- Cons

### Decision Tree <u>Hypothesis</u>



Credit Card Approval Example

#### • Pros

- Easy to interpret (interpretability is getting attention and is important in some domains)
- Can handle multi-type data (Numerical, categorical. ...)
- Easy to implement (Bunch of if-else rules)

#### • Cons

- Generally speaking, bad generalization
- VC dimension is infinity
- High variance (small change of data leads to very different hypothesis)
- Easily overfit

#### Why we care?

- One of the classical models
- Building block for other models (e.g., random forest)

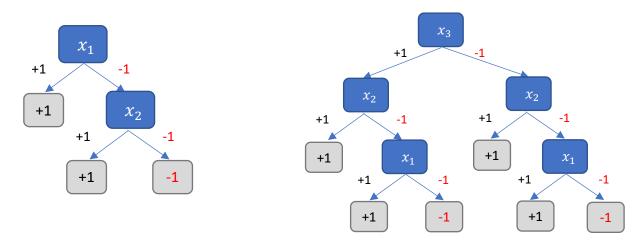
#### Learning Decision Tree from Data

• Given dataset *D*, how to learn a decision tree hypothesis?

$x_1$	$x_2$	$x_3$	у
+1	+1	+1	+1
+1	+1	-1	+1
+1	-1	+1	+1
+1	-1	-1	+1
-1	+1	+1	+1
-1	+1	-1	+1
-1	-1	+1	-1
-1	-1	-1	-1

- Potential approach
  - Find  $g = argmin_{h \in H} E_{in}(h)$

• Multiple decision trees with zero  $E_{in}$ 



#### Learning Decision Tree from Data

- Conceptual intuition to deal with overfitting
  - Regularization: Constrain H

Informally,

```
minimize E_{in} subject to size(tree) \leq C
```

- This optimization is generally computationally intractable.
- Most decision tree learning algorithms rely on *heuristics* to approximate the goal.

#### Template of Greedy-Based Decision Tree Algorithm

- DecisionTreeLearn(D): Input a dataset D, output a decision tree hypothesis
  - Create a root node
  - If termination conditions are met
    - return a single node tree with leaf prediction based on D
  - Else: Greedily find a feature A (assigned as root) to split according to split criteria
    - For each possible value  $v_i$  of A
      - Let  $D_i$  be the dataset containing data with value  $v_i$  for feature A
      - Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root
- Most decision tree learning algorithms follow this template, but with different choices of heuristics

## Example

$x_1$	$x_2$	$x_3$	у
+1	+1	+1	+1
+1	+1	-1	+1
+1	-1	+1	+1
+1	-1	-1	+1
-1	+1	+1	+1
-1	+1	-1	+1
-1	-1	+1	-1
-1	-1	-1	-1

DecisionTreeLearn(*D*)

Create a root node

If termination conditions are met

return a single node tree with leaf prediction based on D

Else: Greedily find a feature A (assigned as root) to split according to split criteria For each possible value  $v_i$  of A

Let  $D_i$  be the dataset containing data with value  $v_i$  for feature A Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root

Termination conditions not net Find a feature to split

+1 -1

DecisionTreeLearn

$x_1$	$x_2$	$x_3$	y
+1	+1	+1	+1
+1	+1	-1	+1
+1	-1	+1	+1
+1	-1	-1	+1

$x_1$	$x_2$	$x_3$	у
-1	+1	+1	+1
-1	+1	-1	+1
	-1	+1	-1
-1	-1	-1	-1

 ${\bf Decision Tree Learn}$ 

DecisionTreeLearn

terminate

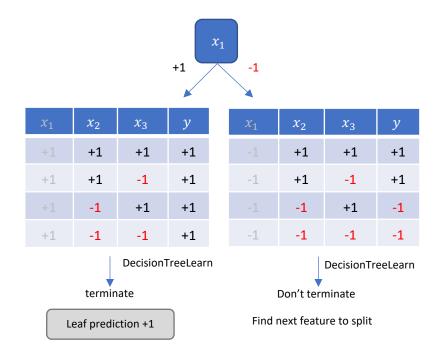
Don't terminate

Leaf prediction +1

Find next feature to split

#### Example Heuristics

DecisionTreeLearn(D)
Create a root node
If termination conditions are met
return a single node tree with leaf prediction based on DElse: Greedily find a feature A to split according to split criteria
For each possible value  $v_i$  of ALet  $D_i$  be the dataset containing data with value  $v_i$  for feature ACreate a subtree DecisionTreeLearn( $D_i$ ) that being the child of root



- Termination conditions
  - When the dataset is empty
  - When all labels are the same
  - when all features are the same
  - When the depth of the tree is too deep
  - ...

- Leaf predictions
  - Majority voting
  - Average (for regression)
  - ...
- Split criteria?

## Split Criteria

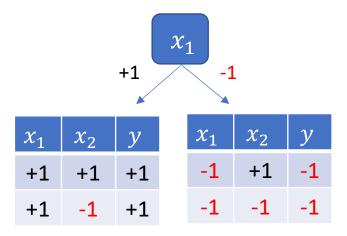
Which feature would you choose to split?

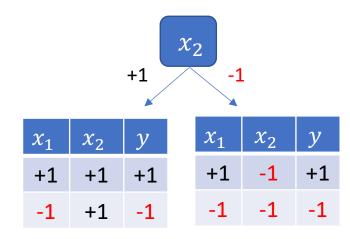
$x_1$	$x_2$	у
+1	+1	+1
+1	-1	+1
-1	+1	-1
-1	-1	-1

#### Split Criteria

Which feature would you choose to split?

$x_1$	$x_2$	у
+1	+1	+1
+1	-1	+1
-1	+1	-1
-1	-1	-1





- Want the tree to be "smaller"
  - Intuition: choose the one that the labels are more "pure"
  - Example: choose the one maximizing information gain => ID3 Algorithm

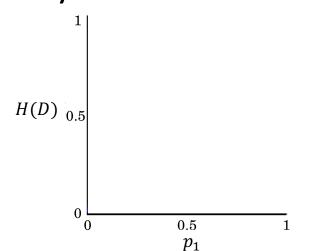
#### Brief Intro to Information Entropy

- Assume there are K possible labels
- Entropy:
  - $H(D) = \sum_{i=1}^{K} p_i \log_2 \frac{1}{p_i}$
  - $p_i$ : ratio of points with label i in the data

By definition  $0 \log_2 \frac{1}{0} = 0$ ;  $1 \log_2 \frac{1}{1} = 0$ 

#### Brief Intro to Information Entropy

- Assume there are K possible labels
- Entropy:
  - $H(D) = \sum_{i=1}^{K} p_i \log_2 \frac{1}{p_i}$
  - $p_i$ : ratio of points with label i in the data
- Binary case with K=2



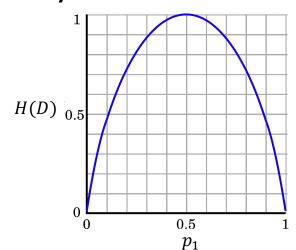
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#### Brief Intro to Information Entropy

- Assume there are K possible labels
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By definition  $0 \log_2 \frac{1}{0} = 0$ ;  $1 \log_2 \frac{1}{1} = 0$ 

• Binary case with K=2



- Interpretations of entropy
  - Expected # bit to encode a distribution
- Higher entropy
  - data is less "pure"
- "pure" data => all labels are +1 or -1 => entropy = 0
- Want to choose splits that lead to pure data, i.e., lower entropy

#### ID3: Using Information Gain as Selection Criteria

- Information gain of choosing feature A to split
  - $Gain(D,A) = H(D) \sum_i \frac{|D_i|}{|D|} H(D_i)$  [The amount of decrease in entropy]
- ID3: Choose the split that maximize Gain(D, A)

Notation: |D| is the number of points in D

#### DecisionTreeLearn(D)

Create a root node

If termination conditions are met

return a single node tree with leaf prediction based on D

Else: Greedily find a feature A to split according to split criteria For each possible value  $v_i$  of A

Let  $D_i$  be the dataset containing data with value  $v_i$  for feature A Create a subtree DecisionTreeLearn( $D_i$ ) that being the child of root

- ID3 termination conditions
  - If all labels are the same
  - If all features are the same
  - If dataset is empty
- ID3 leaf predictions
  - Most common labels (majority voting)
- ID3 split criteria
  - Information gain

### ID3: Using Information Gain as Selection Criteria

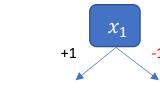
Information gain of choosing feature A to split

• 
$$Gain(D,A) = H(D) - \sum_{i} \frac{|D_i|}{|D|} H(D_i)$$

• ID3: Choose the split that maximize Gain(D, A)

$x_1$	$x_2$	у
+1	+1	+1
+1	-1	+1
-1	+1	-1
-1	-1	-1

$$H(D) = 0.5 \log_2 2 + 0.5 \log_2 2 = 1$$

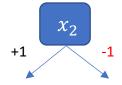


$x_1$	$x_2$	y
+1	+1	+1
+1	-1	+1

$$H(D_{x_1=1}) = 0 \quad H$$

$$H(D_{x_1=1}) = 0$$
  $H(D_{x_1=-1}) = 0$ 

$$Gain(D, x_1) = 1$$



$x_1$	$x_2$	y
+1	+1	+1
-1	+1	-1

$$H(D_{x_2=1})=1$$

$$\begin{array}{c|cccc} x_1 & x_2 & y \\ +1 & -1 & +1 \\ -1 & -1 & -1 \end{array}$$

$$H(D_{x_2=1}) = 1$$
  $H(D_{x_2=-1}) = 1$ 

$$Gain(D, x_2) = 0$$

#### Further Addressing Overfitting

- More Regularization (Constrain H)
  - Do not split leaves past a fixed depth
  - Do not split leaves with fewer than *c* labels
  - Do not split leaves where the maximal information gain is less than au
- Pruning (removing leaves)
  - Evaluate each split using a validation set and compare the validation error with and without that split (replacing it with the most common label at that point)
  - Use statistical test to examine whether the split is "informative" (leads to different enough subtrees)

#### More Discussions

- Real-valued features (continuous x)
  - Need to select threshold for branching

- Regression (continuous y)
  - Change leaf prediction: e.g., average instead of majority vote
  - Change measure for "purity" of data: e.g., squared error of data

# Ensemble Learning

The focus of the next two lectures

#### Ensemble Learning

- Assume we are given a set of learned hypothesis
  - $g_1, g_2, ..., g_M$
- What can we do?
  - Use validation to pick the best one
  - What if all of them are not good enough
- Can we aggregate them?

#### Is Aggregation a Good Idea?



 At a 1906 country fair, ~800 people participate in a contest to guess the weight of an ox.

 Reward is given to the person with the closest guess.

• The average guess is 1,197lbs. The true answer is 1,198lbs.

#### Is Aggregation a Good Idea?

- Maybe
  - If the hypothesis is "diverse", and "on average" they seem good
- Question:
  - How do we find a set of hypothesis that are diverse and "on average" good
  - How do we aggregate the set of hypothesis
- Ensemble learning (Next Two Lectures)
  - Bagging Random Forest
  - Boosting AdaBoost