# IS 604 Assignment 7

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#### 9.14

Use the Kolmogorov-Smirnov test to discover whether the distribution of location of accidents is uniformly distributed for the month of September.

To test for uniformity, our hypotheses are:

```
H_0: R_i \sim Uniform[0, 1]
H_A: R_i \sim Uniform[0, 1]
```

#### ## [1] 0.172

We will use table A.8 in the Discrete-Event System Simulation to test the critical value of D = 0.172 for the sample size N = 30.

For a significance level of  $\alpha = 0.10$  at N = 30,  $D_{0.10} = 0.22$ . Since our computed value of D = 0.172 is less than the critical value of  $D_{0.10} = 0.22$ , we do not reject the null hypothesis that the accidents are uniformly distributed.

### 9.17

The time required for 50 different employees to compute and record the number of hours worked during the week was measured, with the following results in minutes:

Use the chi-square test to test the hypothesis that these service times are exponentially distributed. Let the number of class intervals be k = 6. Use the level of significance  $\alpha = 0.05$ .

 $H_0 = exponentially\ distributed$   $H_A = not\ exponentially\ distributed$ 

Each interval will have equal probability p = 0.1666667. To find the enpoints of these intervals we must solve for the expression below where  $a_i$  is the endpoint of the i th interval.

$$a_i = -\frac{1}{\lambda}ln(1-ip), i = 0, 1, ...6$$

```
suppressWarnings(suppressMessages(library(knitr)))
lambda <- 1/mean(minutes)</pre>
p < -1/6
endpts <- c()
for (i in 0:6){
  endpts[i+1] \leftarrow log(1-(i*p))/-lambda
bins <- cut(minutes, breaks=endpts, labels=c("bin 1","bin 2","bin 3","bin 4"," bin 5"," bin 6"))
Oi <- summary(bins)
Ei <- rep(p*length(minutes),6)</pre>
fit <- ((0i-Ei)^2)/Ei
intervals <-c("[0,0.220)","[0.220,0.489)","[0.489,0.836)",
                "[0.836,1.325)","[1.325,2.161)","[2.161,inf)")
df <- data.frame("Class Intervals"=intervals,</pre>
                  "Observed Freq., Oi"=Oi,
                  "Expected Freq., Ei"=Ei,
                  "((Oi-Ei)^2)/Ei"=fit)
kable(df)
```

	Class.Intervals	Observed. Freq Oi	${\bf Expected.Freq..Ei}$	XOi.Ei2Ei
bin 1	[0,0.220)	8	8.333333	0.0133333
bin 2	[0.220, 0.489)	11	8.333333	0.8533333
bin 3	[0.489, 0.836)	9	8.333333	0.05333333
bin 4	[0.836, 1.325)	5	8.333333	1.3333333
bin 5	[1.325, 2.161)	10	8.333333	0.33333333
bin 6	[2.161, inf)	7	8.333333	0.2133333

Our value for  $\chi_0^2$  value is the sum of the right-most column, 2.8. At  $\alpha = 0.05$  and k - 1 = 5 degrees of freedom,  $\chi_{0.05,5}^2 = 11.1$ . Since  $\chi_0^2 < \chi_{0.05,5}^2$ , we do not reject the null hypothesis.