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# Particle Swarm Optimization: Algorithm and its Codes in MATLAB

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## Abstract

In this work, an algorithm for classical particle swarm optimization (PSO) has been discussed. Also, its codes in MATLAB environment have been included. The effectiveness of the algorithm has been analyzed with the help of an example of three variable optimization problem. Also, the convergence characteristic of the algorithm has been discussed.

*Keywords:* Algorithm, Codes, MATLAB, Particle swarm optimization, Program.

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## 1. Introduction

Particle swarm optimization is one of the most popular nature-inspired metaheuristic optimization algorithm developed by James Kennedy and Russell Eberhart in 1995 [1, 2]. Since its development, many variates have also been developed for solving practical issues related to optimization [3, 4, 5, 6, 7, 8, 9, 10]. Recently, PSO has emerged as a promising algorithm in solving various optimization problems in the field of science and engineering [11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25].

## 2. Particle Swarm Optimization: *Algorithm* [25]

Particle swarm optimization (PSO) is inspired by social and cooperative behavior displayed by various species to fill their needs in the search space. The algorithm is guided by personal experience (Pbest), overall experience (Gbest) and the present movement of the particles to decide their next positions in the search space. Further, the experiences are accelerated by two factors  $c_1$  and  $c_2$ , and two random numbers generated between  $[0, 1]$  whereas the present movement is multiplied by an inertia factor  $w$  varying between  $[w_{min}, w_{max}]$ .

The initial population (swarm) of size  $N$  and dimension  $D$  is denoted as  $\mathbf{X} = [\mathbf{X}_1, \mathbf{X}_2, \dots, \mathbf{X}_N]^T$ , where ' $T$ ' denotes the transpose operator. Each individual (particle)  $\mathbf{X}_i$  ( $i = 1, 2, \dots, N$ ) is given as  $\mathbf{X}_i = [X_{i,1}, X_{i,2}, \dots, X_{i,D}]$ . Also, the initial velocity of the population is denoted as  $\mathbf{V} = [\mathbf{V}_1, \mathbf{V}_2, \dots, \mathbf{V}_N]^T$ . Thus, the velocity of each particle  $\mathbf{X}_i$  ( $i = 1, 2, \dots, N$ ) is given as  $\mathbf{V}_i = [V_{i,1}, V_{i,2}, \dots, V_{i,D}]$ . The index  $i$  varies from 1 to  $N$  whereas the index  $j$  varies from 1 to  $D$ . The detailed algorithms of various methods are described below for completeness.

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$$V_{i,j}^{k+1} = w \times V_{i,j}^k + c_1 \times r_1 \times (Pbest_{i,j}^k - X_{i,j}^k) + c_2 \times r_2 \times (Gbest_j^k - X_{i,j}^k) \quad (1)$$

$$X_{i,j}^{k+1} = X_{i,j}^k + V_{i,j}^{k+1} \quad (2)$$

In eqn. (1)  $Pbest_{i,j}^k$  represents personal best  $j^{th}$  component of  $i^{th}$  individual, whereas  $Gbest_j^k$  represents  $j^{th}$  component of the best individual of population upto iteration  $k$ . Figure (1) shows the search mechanism of PSO in multidimensional search space.

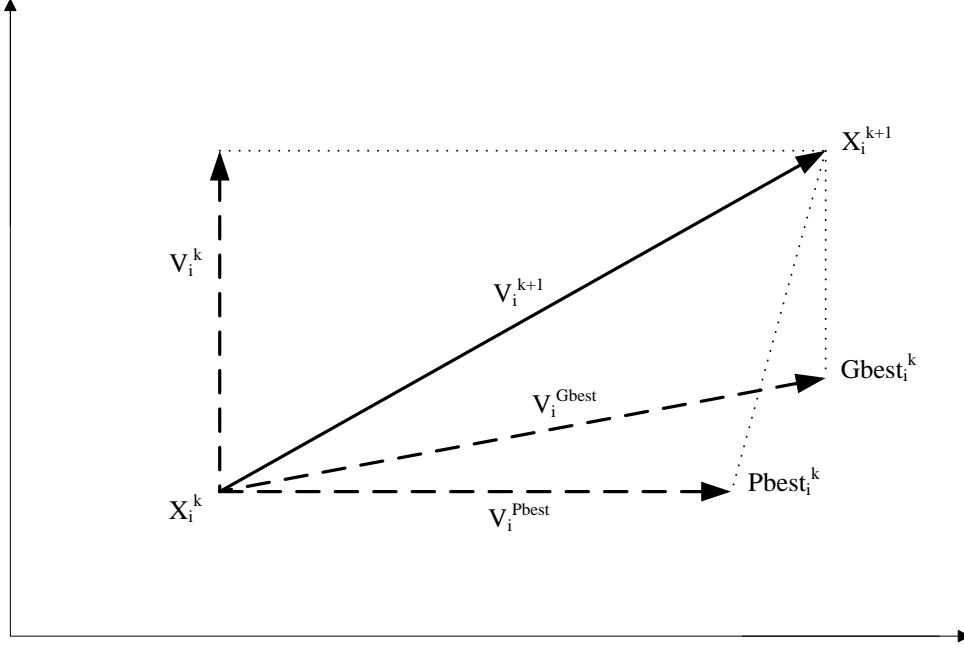


Figure 1: PSO search mechanism in multidimensional search space.

The different steps of PSO are as follows [25]:

1. Set parameter  $w_{min}$ ,  $w_{max}$ ,  $c_1$  and  $c_2$  of PSO
2. Initialize population of particles having positions  $\mathbf{X}$  and velocities  $\mathbf{V}$
3. Set iteration  $k = 1$
4. Calculate fitness of particles  $F_i^k = f(\mathbf{X}_i^k), \forall i$  and find the index of the best particle  $b$
5. Select  $\mathbf{Pbest}_i^k = \mathbf{X}_i^k, \forall i$  and  $\mathbf{Gbest}^k = \mathbf{X}_b^k$
6.  $w = w_{max} - k \times (w_{max} - w_{min}) / Maxite$
7. Update velocity and position of particles

$$V_{i,j}^{k+1} = w \times V_{i,j}^k + c_1 \times rand() \times (Pbest_{i,j}^k - X_{i,j}^k) + c_2 \times rand() \times (Gbest_j^k - X_{i,j}^k); \forall j \text{ and } \forall i$$

$$X_{i,j}^{k+1} = X_{i,j}^k + V_{i,j}^{k+1}; \forall j \text{ and } \forall i$$

8. Evaluate fitness  $F_i^{k+1} = f(\mathbf{X}_i^{k+1}), \forall i$  and find the index of the best particle  $b1$
9. Update Pbest of population  $\forall i$

$$\text{If } F_i^{k+1} < F_i^k \text{ then } \mathbf{Pbest}_i^{k+1} = \mathbf{X}_i^{k+1} \text{ else } \mathbf{Pbest}_i^{k+1} = \mathbf{Pbest}_i^k$$

10. Update Gbest of population

If  $F_{b1}^{k+1} < F_b^k$  then  $\mathbf{Gbest}^{k+1} = \mathbf{Pbest}_{b1}^{k+1}$  and set  $b = b1$  else  $\mathbf{Gbest}^{k+1} = \mathbf{Gbest}^k$

11. If  $k < \text{Maxite}$  then  $k = k + 1$  and goto step 6 else goto step 12

12. Print optimum solution as  $\mathbf{Gbest}^k$

The most commonly used parameters of PSO algorithm are considered as follows:

- Inertial weight: 0.9 to 0.4
- Acceleration factors ( $c_1$  and  $c_2$ ): 2 to 2.05
- Population size: 10 to 100
- Maximum iteration (Maxite): 500 to 10000
- Initial velocity: 10 % of position

A detailed flowchart of PSO considering the above steps is shown in Figure (2).

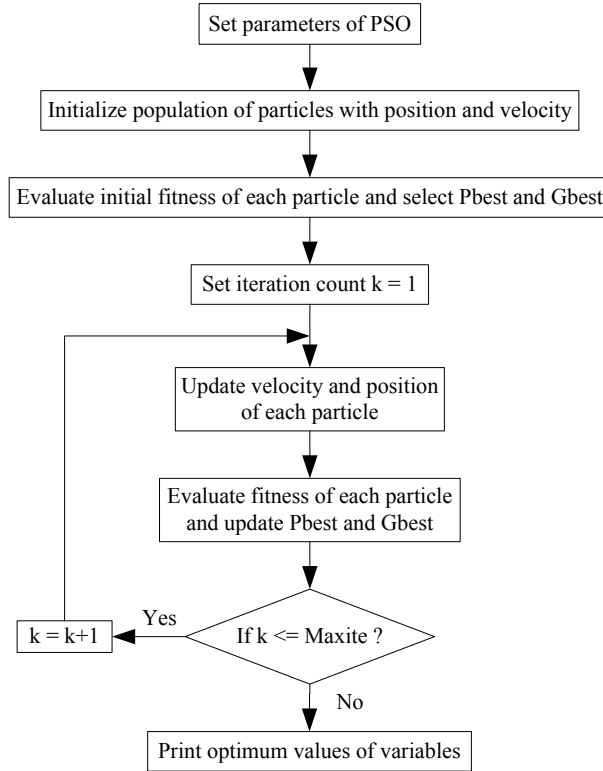


Figure 2: Flowchart of PSO.

### 3. Problem Formulation of Optimization Problem: An example

The objective function (OF) required here must be a minimization problem. Let us suppose that there is a problem defined below is need to be optimized. The OF is of minimization type subjected to inequality type constraints. The statement of the problem is as follows:

$$OF = \min [ 10 \times (1 - x(1))^2 + 20 \times (2 - x(2))^2 + 30 \times (3 - x(3))^2 ] \quad (3)$$

Subjected to

$$x(1) + x(2) + x(3) \leq 5 \quad (4)$$

$$x(1)^2 + 2 \times x(2) \leq x(3) \quad (5)$$

The optimum value of the  $OF$  (defined by Eq. 3) is 9.3941 at  $x(1) = 0.4377$ ,  $x(2) = 1.4569$  and  $x(3) = 3.1054$ . In the next section, MATLAB codes are developed for solving this problem.

#### 4. Particle Swarm Optimization: *Codes in MATLAB environment*

Two MATLAB script files (\*. m file) are needed to fully write the codes. In the first file, the objective function is defined, whereas in the second file, the main PSO program is developed [26].

Now, this problem will be solved by using the PSO algorithm. The objective function file and main program file can be written as follows:

##### 4.1. Objective function file

The problem defined in the last section can be expressed in MATLAB script file (\*.m) as follows:

```

1  function f=ofun(x)
2
3  -   c0=[];
4
5  -   % objective function (minimization)
6  -   of=10*(x(1)-1)^2+20*(x(2)-2)^2+30*(x(3)-3)^2;
7
8  -   % constraints (all constraints must be converted into <=0 type)
9  -   % if there is no constraints then comments all c0 lines below
10 -   c0(1)=x(1)+x(2)+x(3)-5;      % <=0 type constraints
11 -   c0(2)=x(1)^2+2*x(2)-x(3);    % <=0 type constraints
12
13 -   % defining penalty for each constraint
14 -   for i=1:length(c0)
15 -       if c0(i)>0
16 -           c(i)=1;
17 -       else
18 -           c(i)=0;
19 -       end
20 -   end
21
22 -   penalty=10000; % penalty on each constraint violation
23
24 -   f=of+penalty*sum(c); % fitness function

```

Save the above codes as ofun.m. The "ofun.m" file defines the problem discussed above. In main program file this function will be called again and again as per the requirement.

##### 4.2. Main program file

The main program file can be expressed as follows:

```

1 - tic
2 - clc
3 - clear all
4 - close all
5 - rng default
6
7 - LB=[0 0 0];           %lower bounds of variables
8 - UB=[10 10 10];       %upper bounds of variables
9
10 % pso parameters values
11 - m=3;                 % number of variables
12 - n=100;               % population size
13 - wmax=0.9;            % inertia weight
14 - wmin=0.4;            % inertia weight
15 - c1=2;                % acceleration factor
16 - c2=2;                % acceleration factor
17
18 % pso main program-----start
19 - maxite=1000;          % set maximum number of iteration
20 - maxrun=10;            % set maximum number of runs need to be
21 - for run=1:maxrun
22 -     run
23 -     % pso initialization-----start
24 -     for i=1:n
25 -         for j=1:m
26 -             x0(i,j)=round(LB(j)+rand()*(UB(j)-LB(j)));
27 -         end
28 -     end
29 -     x=x0;              % initial population
30 -     v=0.1*x0;          % initial velocity
31 -     for i=1:n
32 -         f0(i,1)=ofun(x0(i,:));
33 -     end
34 -     [fmin0,index0]=min(f0);
35 -     pbest=x0;           % initial pbest
36 -     gbest=x0(index0,:); % initial gbest
37 -     % pso initialization-----end
38
39     % pso algorithm-----start
40 -     ite=1;
41 -     tolerance=1;
42 -     while ite<=maxite && tolerance>10^-12
43
44 -         w=wmax-(wmax-wmin)*ite/maxite; % update inertial weight
45
46 -         % pso velocity updates
47 -         for i=1:n
48 -             for j=1:m
49 -                 v(i,j)=w*v(i,j)+c1*rand()*(pbest(i,j)-x(i,j))...
50 -                     +c2*rand()*(gbest(1,j)-x(i,j));
51 -             end
52 -         end
53
54 -         % pso position update
55 -         for i=1:n
56 -             for j=1:m
57 -                 x(i,j)=x(i,j)+v(i,j);
58 -             end
59 -         end
60

```

```

61 % handling boundary violations
62 for i=1:n
63     for j=1:m
64         if x(i,j)<LB(j)
65             x(i,j)=LB(j);
66         elseif x(i,j)>UB(j)
67             x(i,j)=UB(j);
68         end
69     end
70 end
71
72 % evaluating fitness
73 for i=1:n
74     f(i,1)=ofun(x(i,:));
75 end
76
77 % updating pbest and fitness
78 for i=1:n
79     if f(i,1)<f0(i,1)
80         pbest(i,:)=x(i,:);
81         f0(i,1)=f(i,1);
82     end
83 end
84
85 [fmin,index]=min(f0); % finding out the best particle
86 fffmin(ite,run)=fmin; % storing best fitness
87 fffite(run)=ite; % storing iteration count
88
89 % updating gbest and best fitness
90 if fmin<fmin0
91     gbest=pbest(index,:);
92     fmin0=fmin;
93 end
94
95 % calculating tolerance
96 if ite>100;
97     tolerance=abs(fffmin(ite-100,run)-fmin0);
98 end
99
100 % displaying iterative results
101 if ite==1
102     disp(sprintf('Iteration    Best particle    Objective fun'));
103 end
104 disp(sprintf('%8g    %8g    %8.4f',ite,index,fmin0));
105 ite=ite+1;
106 end
107 % pso algorithm-----end
108 gbest;
109 fvalue=10*(gbest(1)-1)^2+20*(gbest(2)-2)^2+30*(gbest(3)-3)^2;
110 fff(run)=fvalue;
111 rgbest(run,:)=gbest;
112 disp(sprintf('-----'));
113 end
114 % pso main program-----end
115 disp(sprintf('\n'));
116 disp(sprintf('*****'));
117 disp(sprintf('Final Results-----'));
118 [bestfun,bestrun]=min(fff)
119 best_variables=rgbest(bestrun,:)
120 disp(sprintf('*****'));

```

```

121 -   toc
122
123   % PSO convergence characteristic
124 -   plot(ffmin(1:ffite(bestrun),bestrun),'-k');
125 -   xlabel('Iteration');
126 -   ylabel('Fitness function value');
127 -   title('PSO convergence characteristic')
128 -   %#####

```

Subsections 4.1 and 4.2 represent the complete codes for PSO to solve the optimization problems defined in Section 3. Now, to solve the problem using PSO, it is only required to run the main program file developed in subsection 4.2. It is to be noted that the same codes are available in my older work [26] uploaded on the ResearchGate.

## 5. Particle Swarm Optimization: *Optimized results of the problem considered*

The snapshot of the optimized solution of the problem is shown in Figure 3. From this figure, it is observed that the best value of the objective function obtained after 10 independent runs is 9.3941. This value is obtained at  $x(1) = 0.4377$ ,  $x(2) = 1.4569$  and  $x(3) = 3.1054$ . Out of the 10 runs, 7<sup>th</sup> run gives this best results. The simulation total time taken is 22.9852 seconds. It is to be noted that the simulation time depends on computer configuration. Further, Figure 4 shows the convergence characteristic of PSO.

```

-----

*****
Final Results-----

bestfun =

    9.3941

bestrun =

     7

best_variables =

    0.4377    1.4569    3.1054

*****
Elapsed time is 22.985214 seconds.
fx >> |

```

Figure 3: Results displayed in command window of MATLAB.



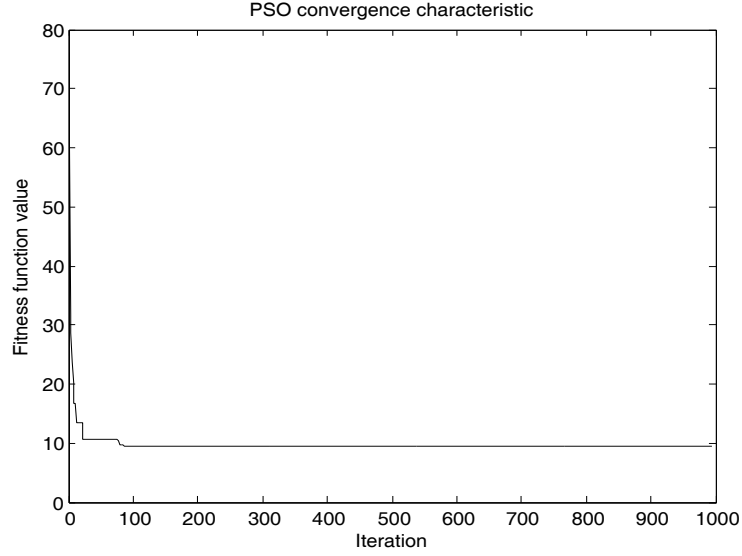


Figure 4: PSO convergence characteristic

## 6. Conclusion

In this paper, the concepts of particle swarm optimization have been discussed in a very simple way. Further, its algorithm has been developed. Also, PSO programming codes in MATLAB environment have been given and an example has been solved successfully which demonstrate the effectiveness of the algorithm. The following conclusions can be drawn from this work:

- (i) The MATLAB codes discussed here can be extended to solve any type of optimization problem of any size.
- (ii) Any equality constraint needs to convert into corresponding two inequality constraints.
- (iii) The codes discussed here are generalized for solving any optimization problem with inequality constraints of any size.

## Appendix

If  $X$  is a set of equality constraint need to be converted into a set inequality constraint , the following procedures need to be followed:

Equality constraint:

$$X = 0 \tag{6}$$

The corresponding set of inequality constraint can be represented as follows:

$$X \leq 0 \tag{7}$$

$$-X \leq 0 \tag{8}$$

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