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test 2 Discrete math

45%

1. direct proof

if n and m are odd

the $n \cdot m$ is odd

n and m are odd numbers

$$n = 2a + 1$$

$$m = 2b + 1$$

$$n \cdot m = (2a + 1)(2b + 1)$$

$$n \cdot m = 4ab + 2a + 2b + 1$$

$$n \cdot m = 2(2ab + a + b) + 1$$

So $2k + 1$ is an odd integer

$$n \cdot m = 2k + 1$$

$$k = 2ab + a + b$$

So $n \cdot m$ is odd.

suppose n & m
are odd Then
 \exists integers a & b
such that

-1

2. Suppose n is not an odd number
so ~~not~~ n is even

a) $n = 2k + 1$ why?

$$n^2 = 4k^2 + 4k + 1 = 4(k^2 + k) + 1$$

-1

So it is even

this gives that if n^2 is odd then n is odd.

b) Suppose n is even
and k is an integer

-3

$$n^2 = (2k + 1)^2$$

~~$$n^2 = 2(k+1)$$~~

~~$$n = (2k + 1)^2$$~~

~~$$n = 2(k+1)^2$$~~

~~$$n = (2k + 1)(2k + 1)$$~~

~~$$n = 2(k+1) \cdot 2(k+1)$$~~

Contradiction!

$$(k+1)(k+1)$$

$$k^2 + 4k + 4$$

Because the statement is false

$n^2 + 4$ is odd.

3. $n^2 + 2 \geq 2$ if $2 \leq n \leq 4$

suppose n is ~~odd~~ 3 ✓

$$3^2 + 2 \geq 2$$

$$9 + 2 \geq 2$$

$11 \geq 2$ this is true ✓

(-3)

~~so $n^2 + 2 \geq 2$ if the condition is $2 \leq n \leq 4$, I used a direct proof to prove it.~~

$$41 \quad n^2 + 2 \geq 2^n$$

2

$$s. \quad 3n^2 + n + 14$$

Case 1 Suppose n is even $n = 2k$

$$3(2k)^2 + 2k + 14 = 12k^2 + 2k + 14 = 2(6k^2 + k + 7)$$

Case 2 Suppose n is odd
 $n = 2k + 1$

So
 $3n^2 + n + 14$ is
even for all
integers n

$$3(2k+1)^2 + 2k+1 + 14 = 12k^2 + 12k + 3 + 2k + 1 + 14 = 12k^2 + 14k + 18$$

~~$$12k^2 + 14k + 18 = 2(6k^2 + 7k + 9)$$~~

~~$$12k^2 + 14k + 18 = 2(6k^2 + 7k + 9)$$~~

can't see
←

$$6. \quad 340 \bmod 12$$

$$\begin{array}{r} 28 \\ 12 \overline{) 340} \\ \underline{24} \\ 100 \\ \underline{96} \\ 4 \end{array}$$

$$340 \bmod 12 = 4$$

✓

$$b.) \quad -230 \bmod 25$$

$$\begin{array}{r} -9 \\ 25 \overline{) -230} \\ \underline{+225} \\ -5 \end{array}$$

$$-5 \equiv 20 \bmod 25$$

$$-230 \bmod 25 = -9$$

⊕

Q. 7.

$$x \cdot x \equiv -10 \pmod{7} -3$$

That's
not what the
question asked.
-3 are inverse
to -10 mod 7

$$\begin{array}{r} -1 \\ 7 \overline{) -10} \\ \underline{-7} \\ -3 \end{array} \checkmark$$

$$\frac{7}{x^2 + 10}$$

$$-3$$

$$\begin{array}{c} 5 \\ \textcircled{8} \end{array} ? \quad \begin{array}{c} 3 \\ \textcircled{9} \end{array} ? \quad \begin{array}{c} 6 \\ \textcircled{10} \end{array} ?$$

10 23 b, nur

$$\begin{array}{c}
 \begin{array}{c} \cancel{32} \\ \cancel{16} \end{array} \quad \frac{1}{2^4} \quad \frac{0}{2^3} \quad \frac{1}{2^2} \quad \frac{1}{2^1} \quad \frac{1}{2^0} \\
 16 \quad 8 \quad 4 \quad 2 \quad 1
 \end{array}$$

✓

$$\begin{array}{r}
 16 \overline{) 23} \\
 \underline{16} \\
 7
 \end{array}$$

$$\begin{array}{r}
 4 \overline{) 7} \\
 \underline{4} \\
 3
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 3} \\
 \underline{2} \\
 1
 \end{array}$$

12. 51751 as hexa decimal

$$51751 = CA27_{16}$$

$$\begin{array}{r}
 3234.4375 \\
 16 \overline{) 51751}
 \end{array}$$

$$\frac{C}{16^3} \quad \frac{A}{16^2} \quad \frac{2}{16^1} \quad \frac{7}{16^0}$$

$$\begin{aligned}
 3234.4375 - 3234 \\
 = 0.4375 \times 16 \\
 = 7
 \end{aligned}$$

I cannot see anything on this
page

13. (-3)

$(14) - 3$

15.

$$a) \quad \underline{26^6 \cdot 26^6 \cdot 10^6} = 9,54287566E22$$

$$= 9,542875666,000,000,000,000 \text{ combinations}$$

-3

b)

$$\underline{26} \quad \underline{26} \quad \underline{25} \quad \underline{24} \quad \underline{10} \quad \underline{9}$$

$$= 4,956,000 \text{ possible passwords}$$

16.

$$C(7, 3)$$

$$= \frac{7!}{3!(7-3)!} = \frac{7!}{3!4!} = \frac{7 \cdot 6 \cdot 5 \cdot 4 \cdot 3!}{3! \cdot 4 \cdot 8 \cdot 2 \cdot 8}$$

$$= 7 \cdot 5 = 35 \quad \checkmark$$

17) ? -3 18) ? -3 19) ? -3

20.

bag

5 cookies

first always

7 kinds

Chocolate

$$C(7+4-1, 4) \quad \checkmark$$

$$\frac{10!}{7! 4!}$$

$$\frac{10 \cdot 9 \cdot 8 \cdot 7}{7 \cdot 6 \cdot 5 \cdot 4}$$

$$\frac{2 \cdot 2 \cdot 1}{3 \cdot 2}$$

~~30~~
Combinations

21

a)

D # 1

$$\begin{array}{cccccc}
 1 & 2 & 3 & 4 & 5 & 6 \\
 \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6}
 \end{array}$$

D # 2

$$\begin{array}{cccccc}
 1 & 2 & 3 & 4 & 5 & 6 \\
 \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6}
 \end{array}$$

$$\begin{array}{cccc}
 \frac{1}{6} & \frac{1}{6} & \frac{2}{6} & \frac{3}{6} \\
 \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6}
 \end{array}$$

P(rolling at least ~ 4) is ?

b)

-4

$$P(1, 4) + P(2, 3) + P(4, 1) + P(3, 2)$$

$$\frac{1}{6} \cdot \frac{1}{6} + \frac{1}{6} \cdot \frac{1}{6} + \frac{1}{6} \cdot \frac{1}{6} + \frac{1}{6} \cdot \frac{1}{6}$$

$$\frac{1}{36} + \frac{1}{36} + \frac{1}{36} + \frac{1}{36} = \frac{4}{36} = \frac{2}{18} = \frac{1}{9}$$

$\left(\frac{1}{9}\right)$

✓

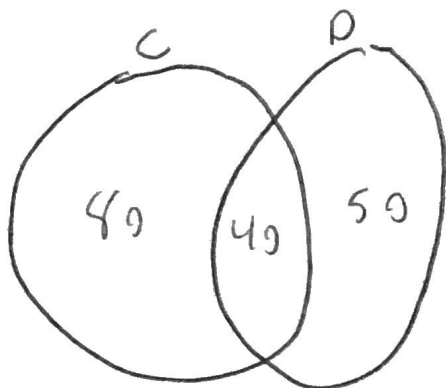
22.

200 people

120 coke

90 pepsi

40 both



$$80 + 40 + 50 = 170$$

$$\frac{170}{200} = \frac{17}{20}$$

✓

a) $P(\text{someone who likes coke and pepsi})$

$$\frac{17}{20} = 0.85$$

✓

b)

$$200 - 170 = 30$$

$$\frac{30}{200} = \frac{3}{20}$$

✓

$P(\text{picking someone that likes neither})$

$$\frac{3}{20} = 0.15$$

23.

a) the probability of having a boy is

~~$\left(\frac{1}{2} = 0.5\right)$~~ P

$\frac{2}{3}$

b) the probability of having a ~~boy~~ girl is

~~$\left(\frac{1}{2} = 0.5\right)$~~

$\frac{1}{3}$

(-2)

c) $\frac{B}{C_1} \frac{B}{C_2} / \frac{6}{C_1} \frac{6}{C_2} / \frac{B}{C_1} \frac{6}{C_2} / \frac{6}{C_1} \frac{B}{C_2}$

d) $\frac{B}{\text{Given}} \frac{B}{\text{Given}}$

$\frac{B}{\text{Given}} \frac{6}{\text{Given}}$

(-3)

P(having two boys) is

~~$\left(\frac{1}{2} = 0.5\right)$~~

266 H T

~~2~~ H, H, T, T, H, T

$$T, H = \frac{2}{4} \text{ chances}$$

When flipping
2 coins the probability = $\frac{1}{4}$

is ~~interpen~~ independent
because when you flip one coin

It does not ~~control~~ the outcome of
the second coin

