

Quiz Sec 8.1, 8.5, 9.1, 9.2

For the following relations in problems 1 and 2, determine if each is any of: reflexive, symmetric, transitive, or antisymmetric.

If a property holds, simply state that. If a property does *not* hold, give a counter example.

All relations  $R$  are on the set  $\{0, 1, 2, 3\}$

1.  $R = \{(0, 0), (1, 1), (1, 3), (3, 1), (3, 3)\}$

Reflexive?: \_\_\_\_\_

Symmetric?: \_\_\_\_\_

Anti-Symmetric?: \_\_\_\_\_

Transitive?: \_\_\_\_\_

2.  $R = \{(0, 0), (1, 1), (1, 3), (2, 2), (3, 3)\}$

Reflexive?: \_\_\_\_\_

Symmetric?: \_\_\_\_\_

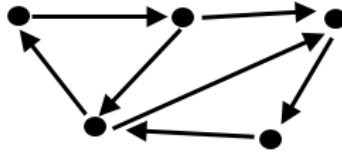
Anti-Symmetric?: \_\_\_\_\_

Transitive?: \_\_\_\_\_

3. For the following directed graphs, determine if each is Strongly Connected, Weakly Connected, or Neither. In each case, give your reasoning.

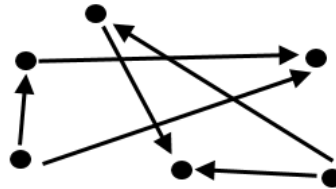
a)

\_\_\_\_\_



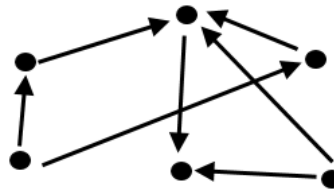
b)

\_\_\_\_\_

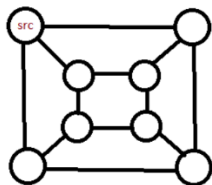


c)

\_\_\_\_\_



4. Draw  $K_7$ .
5. How many edges does the complete graph with 10 vertices have?
6. Is the graph below bipartite?



7. What is the sum of degrees in any graph?