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MACHINE ELEMENTS

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Project Report

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Design Problem

D_{bc} pulley diameter, mm

F_t tangential force, N

L service life, years

T working torque, N · mm

t working time, s

v_{bc} conveyor belt speed, m/s

δ_u error of speed ratio, %

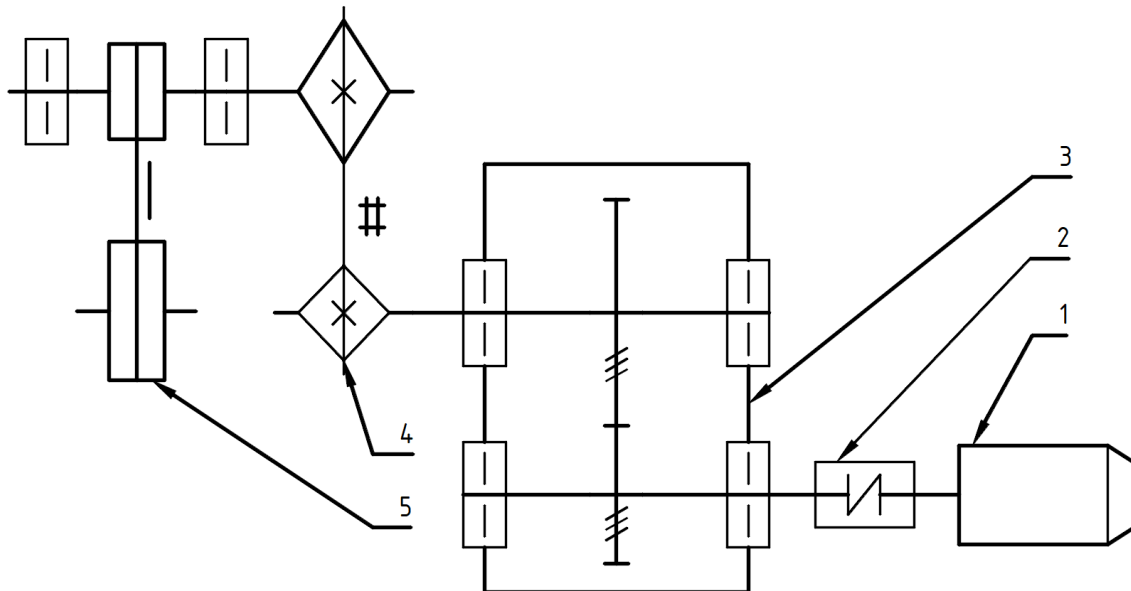


Figure 1: Mechanical transmission system of a belt conveyor

Given the mechanical transmission system in figure 1, determine the specifications for each machine element.

1. Electric motor
2. Elastic coupling
3. Gearbox
4. Chain drive
5. Belt conveyor

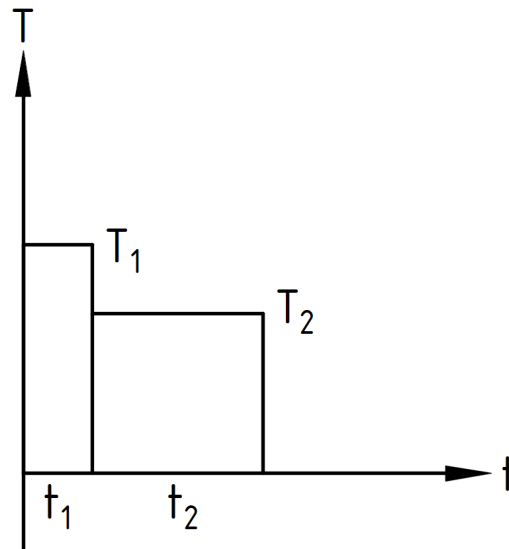


Figure 2: Input load diagram

Design parameters The chosen parameters are given in column 8:

- $F_t = 4500 \text{ (N)}$
- $v_{bc} = 3.05 \text{ (m/s)}$
- $D_{bc} = 500 \text{ (mm)}$
- $L = 4 \text{ (years)}$
- $T_1 = T \text{ (N} \cdot \text{mm)}, t_1 = 12 \text{ (s)}$
- $T_2 = 0.7T \text{ (N} \cdot \text{mm)}, t_2 = 60 \text{ (s)}$
- $\delta_u \leq \pm 5\%$

The machine works in one direction for 300 days, 2 shifts per day, 8 hours each and the load is low. Also, for the rest of this report, we will consider shaft 1 is the one connected to the electric motor, while shaft 2 is the connection between the chain drive and gearbox.

Chapter 1

Motor Design

1.1 Nomenclature

n_{bc}	rotational speed of belt conveyor, rpm	u_{hg}	transmission ratio of helical gear
n_{sh}	rotational speed of shaft, rpm	u_{sys}	transmission ratio of the system
P_m	maximum operating power of belt conveyor, kW	T_{motor}	motor torque, N · mm
P_{motor}	calculated motor power to drive the system, kW	T_{sh}	shaft torque, N · mm
P_{sh}	operating power of shaft, kW	η_b	bearing efficiency
P_w	operating power of the belt conveyor given a workload, kW	η_c	coupling efficiency
		η_{ch}	chain drive efficiency
		η_{hg}	helical gear efficiency
		η_{sys}	efficiency of the system
u_{ch}	transmission ratio of chain drive	1	shaft 1
		2	shaft 2

1.2 Calculate η_{sys}

From table (2.3):

$$\eta_c = 1$$

$$\eta_b = 0.99$$

$$\eta_{hg} = 0.96$$

$$\eta_{ch} = 0.95$$

$$\eta_{sys} = \eta_c \eta_b^3 \eta_{hg} \eta_{ch} \approx 0.88$$

1.3 Calculate P_{motor}

$$P_m = \frac{F_t v_{bc}}{1000} \approx 13.73 \text{ (kW)}$$

From equation (2.13) :

$$P_w = P_m \sqrt{\frac{\left(\frac{T_1}{T}\right)^2 t_1 + \left(\frac{T_2}{T}\right)^2 t_2}{t_1 + t_2}} \approx 10.41 \text{ (kW)}$$

$$P_{motor} = \frac{P_w}{\eta_{sys}} \approx 11.76 \text{ (kW)} < P_m$$

1.4 Calculate n_{motor}

$$n_{bc} = \frac{6 \times 10^4 v}{\pi D_{bc}} \approx 116.5 \text{ (rpm)}$$

$$u_{ch} = 5 \text{ (table (2.4))}$$

$$u_{hg} = 5 \text{ (table (2.4))}$$

$$u_{sys} = u_{ch} u_{hg} = 25$$

$$n_{motor} = u_{sys} n_{bc} \approx 2912.54 \text{ (rpm)}$$

1.5 Choose motor

To work normally, the maximum operating power of the chosen motor must be no smaller than both estimated P_{motor} and P_m . Since $P_{motor} < P_m$ for our case, the minimum operating power of choice is P_m . In similar fashion, its rotational speed must also be no smaller than estimated n_{motor} .

Thus, from table (P1.3), we choose motor 4A160M2Y3 which operates at 18.5 kW and 2930 rpm

$$\Rightarrow P_{motor} = 18.5 \text{ kW}, n_{motor} = 2930 \text{ (rpm)}$$

Recalculating u_{sys} with the new P_{motor} and n_{motor} , we obtain:

$$u_{sys} = \frac{n_{motor}}{n_{bc}} \approx 25.15$$

Assuming $u_{hg} = const$:

$$u_{ch} = \frac{u_{sys}}{u_{hg}} \approx 5.03$$

1.6 Calculate power, rotational speed and torque

Let us denote P_{sh1} , n_{sh1} and T_{sh1} be the transmitted power, rotational speed and torque onto shaft 1, respectively. Similarly, P_{sh2} , n_{sh2} and T_{sh2} will be the transmitted parameters onto shaft 2. These notations will be used throughout the next chapters.

1.6.1 Power

$$P_{ch} = P_m \approx 13.73 \text{ (kW)}$$

$$P_{sh2} = \frac{P_{ch}}{\eta_b \eta_{ch}} \approx 14.59 \text{ (kW)}$$

$$P_{sh1} = \frac{P_{sh2}}{\eta_b \eta_{hg}} \approx 15.35 \text{ (kW)}$$

1.6.2 Rotational speed

$$n_{sh1} = n_{motor} = 2930 \text{ (rpm)}$$

$$n_{sh2} = \frac{n_{sh1}}{u_{hg}} = 586 \text{ (rpm)}$$

1.6.3 Torque

$$T_{motor} = 9.55 \times 10^6 \frac{P_{motor}}{n_{motor}} \approx 60298.63 \text{ (N} \cdot \text{mm)}$$

$$T_{sh1} = 9.55 \times 10^6 \frac{P_{sh1}}{n_{sh1}} \approx 50047.56 \text{ (N} \cdot \text{mm)}$$

$$T_{sh2} = 9.55 \times 10^6 \frac{P_{sh2}}{n_{sh2}} \approx 237825.99 \text{ (N} \cdot \text{mm)}$$

In summary, we obtain the following table:

	Motor	Shaft 1	Shaft 2
P (kW)	18.5	14.59	15.35
u	5	5.03	
n (rpm)	2930	2930	586
T (N · mm)	60298.63	50047.56	237825.99

Table 1.1: System overall specifications

Chapter 2

Chain Drive Design

2.1 Nomenclature

$[i]$	permissible impact times per second	F_v	centrifugal force, N
		i	impact times per second
$[s]$	permissible safety factor	k	overall factor
$[P]$	permissible power, kW	k_0	arrangement of drive factor
a	center distance, mm	k_a	center distance and chain's length factor
a_{max}	maximum center distance, mm		
a_{min}	minimum center distance, mm	k_{bt}	lubrication factor
B	bush length, mm	k_c	rating factor
d	driving sprocket diameter, mm	k_d	dynamic loads factor
d_c	pin diameter, mm	k_{dc}	chain tension factor
F_0	sagging force, N	k_f	loosing factor
F_1	tight side tension force, N	k_n	coefficient of rotational speed
F_2	slack side tension force, N	k_x	chain weight factor
F_r	force on the shaft, N	k_z	coefficient of number of teeth
F_t	effective peripheral force, N		

n_{01}	experimental rotational speed, rpm	v	instantaneous velocity along the chain, m/s
n_{ch}	rotational speed of a sprocket, rpm	x	chain length in pitches, the number of links
P_t	calculated power, kW	x_c	an even number of links
p	pitch, mm	z	number of teeth of a sprocket
p_{max}	permissible sprocket pitch, mm	z_{max}	maximum number of teeth of the driven sprocket
Q	permissible load, N		
q	mass per meter of chain, kg/m	1	subscript for driving sprocket
s	safety factor	2	subscript for driven sprocket

2.2 Find p

Since the driving sprocket is connected to shaft 1, $n_1 = n_{sh2} = 586$ (rpm).

Find z Since z_1 and z_2 is preferably an odd number according to p.80:

$$z_1 = 29 - 2u_{ch} = 18.94 \approx 19$$

$$z_2 = u_{ch}z_1 = 95.57 \approx 97 \leq z_{max} = 120$$

Because $z_1 \geq 15$, we use table (5.8) and interpolation to approximate p_{max} .

Therefore, $p_{max} \approx 33.58$ (mm).

Find k Since $n_{ch} = 586 \approx 600$ (rpm), choose $n_{01} = 600$ (rpm), which is obtained from table (5.5). Then, we calculate k_z and k_n .

$$k_z = \frac{25}{z_1} \approx 1.32, k_n = \frac{n_{01}}{n_{ch}} \approx 1.02$$

Specifying the chain drive's working condition and ultizing table (5.6) , we find

out that $k_0 = k_a = k_{dc} = k_{bt} = 1$, $k_d = 1.25$, $k_c = 1.3$.

$$\Rightarrow k = k_0 k_a k_{dc} k_{bt} k_d k_c = 1.625$$

Find p From table (5.5):

$$P_t = P_{ch} k k_z k_n \approx 30.05 \text{ (kW)} \leq 42 \text{ (kW)} \Rightarrow [P] = 42 \text{ (kW)}$$

Using the table, we also get the other parameters:

$$p = 31.75 \text{ (mm)}, d_c = 9.55 \text{ (mm)}, B = 27.46 \text{ (mm)},$$

$$d_1 = \frac{p}{\sin \frac{z_1}{180^\circ}} \approx 192.9 \text{ (mm)}, d_2 = \frac{p}{\sin \frac{z_2}{180^\circ}} \approx 980.49 \text{ (mm)}$$

Having $p = 31.75 \text{ (mm)} \leq p_{\max} \approx 33.58 \text{ (mm)}$, we can safely choose the number of chains as 1, which is in agreement with the given figure. Hence, from table (5.2), we obtain the parameters in the section for 1 strand chain drive:

$$Q = 56.7 \times 10^3 \text{ (N)}, q = 2.6 \text{ (kg/m)}$$

By comparison to the conditions in the sub-table, the choice of B is satisfactory.

2.3 Find a , x_c , and i

Find x_c $a_{\min} = 30p = 952.5 \text{ (mm)}$, $a_{\max} = 50p = 1587.5 \text{ (mm)}$. Limiting the range of choice for a in $[a_{\min}, a_{\max}]$, we can approximate $a = 1000 \text{ (mm)}$.

$$x = \frac{2a}{p} + \frac{z_1 + z_2}{2} + \frac{(z_2 - z_1)^2 p}{4\pi^2 a} \approx 125.89 \Rightarrow x_c = 126$$

Find a From equation (5.13), we calculate a again with x_c :

$$a = \frac{p}{4} \left(x_c - \frac{z_2 + z_1}{2} + \sqrt{\left(x_c - \frac{z_2 + z_1}{2} \right)^2 - 2 \frac{(z_2 - z_1)^2}{\pi^2}} \right) - 0.003a \approx 998.98 \text{ (mm)}$$

Find i From table (5.9):

$$i = \frac{z_1 n_{sh2}}{15x} \approx 6 < [i] = 25$$

2.4 Strength of chain drive

For moderate workload, choose $k_d = 1.2$. Let the chain drive be angled 30° with respect to ground, we obtain $k_f = 4$.

$$v_1 = \frac{n_{ch} P_{z1}}{6 \times 10^4} \approx 5.89 \text{ (m/s)}$$

Find F_t, F_v, F_0 We also need to calculate F_t, F_v and F_0 :

$$F_t = \frac{10^3 P_{ch}}{v_1} \approx 2329.53 \text{ (N)}$$

$$F_v = q v_1^2 \approx 90.25 \text{ (N)}$$

$$F_0 = 9.81 \times 10^{-3} k_f q a \approx 101.92 \text{ (N)}$$

Validate s This value must be larger than the permissible safety factor to operate properly. From equation (5.15):

$$s = \frac{Q}{k_d F_t + F_0 + F_v} \approx 18.98 \geq [s] = 13.2, \text{ where } [s] \text{ is chosen from table (5.10).}$$

2.5 Force on shaft

From p.87:

$$F_2 = F_0 + F_v \approx 192.17 \text{ (N)}$$

$$F_1 = F_t + F_2 \approx 2521.7 \text{ (N)}$$

Choose $k_x = 1.15$ and follow equation (5.20) :

$$F_r = k_x F_t \approx 2678.96 \text{ (N)}$$

In summary, we have the following table:

	driving	driven
$[P]$ (kW)	42	
Q (N)	56700	
p (mm)	31.75	
i	6	
a (mm)	998.98	
z	19	97
d (mm)	192.9	980.49
d_c (mm)	9.55	
B (mm)	27.46	
v (m/s)	5.01	
u_{ch}	5	

Table 2.1: Chain drive specifications

Chapter 3

Gearbox Design (Helix gears)

3.1 Nomenclature

$[\sigma_H]$	permissible contact stress, MPa	F_a	axial force, N
$[\sigma_F]$	permissible bending stress, MPa	F_r	radial force, N
		F_t	tangential force, N
$[\sigma_H]_{max}$	permissible contact stress due to overload, MPa	H	surface roughness, HB
		K_d	coefficient of gear material
$[\sigma_F]_{max}$	permissible bending stress due to overload, MPa	K_F	load factor from bending stress
		K_{FC}	load placement factor
AG	accuracy grade of gear	K_{FL}	aging factor due to bending stress
a	center distance, mm		
b	face width, mm	K_{Fv}	factor of dynamic load from bending stress at meshing area
c	gear meshing rate		
d	pitch circle, mm	$K_{F\alpha}$	factor of load distribution from bending stress on gear teeth
d_a	addendum diameter, mm		
d_b	base diameter, mm	$K_{F\beta}$	factor of load distribution from bending stress on top land
d_f	deddendum diameter, mm		

K_H	load factor of contact stress	S_H	safety factor of contact stress
K_{HL}	aging factor due to contact stress	v	rotational velocity, m/s
K_{Hv}	factor of dynamic load from contact stress at meshing area	x	gear correction factor
$K_{H\alpha}$	factor of load distribution from contact stress on gear teeth	Y_F	tooth shape factor
$K_{H\beta}$	factor of load distribution from contact stress on top land	Y_β	helix angle factor
k_x	a coefficient	Y_ϵ	contact ratio factor
k_y	a coefficient	y	center displacement factor
m	transverse module, mm	z_H	contact surface's shape factor
m_F	root of fatigue curve in bending stress test	z_M	material's mechanical properties factor
m_H	root of fatigue curve in contact stress test	z_{min}	minimum number of teeth corresponding to β
m_n	normal module, mm	z_v	virtual number of teeth
N_{FE}	working cycle of equivalent tensile stress corresponding to $[\sigma_F]$	z_ϵ	meshing condition factor
N_{FO}	working cycle of bearing stress corresponding to $[\sigma_F]$	α	normal pressure angle, following Vietnam standard (TCVN 1065-71), i.e. $\alpha = 20^\circ$
N_{HE}	working cycle of equivalent tensile stress corresponding to $[\sigma_H]$	α_t	traverse pressure angle, $^\circ$
N_{HO}	working cycle of bearing stress corresponding to $[\sigma_H]$	ϵ_α	traverse contact ratio
S	length, mm	ϵ_β	face contact ratio
S_F	safety factor of bending stress	β	helix angle, $^\circ$
		β_b	base circle helix angle, $^\circ$
		ψ_{ba}	width to shaft distance ratio
		ψ_{bd}	face width factor
		σ_b	ultimate strength, MPa
		σ_{ch}	yield limit, MPa

σ_{Flim}^o	permissible bending stress	1	subscript for pinion
	corresponding to working cycle,	2	subscript for driven gear
MPa		w	subscript for variable value after
σ_{Hlim}^o	permissible contact stress		correction
	corresponding to working cycle,		
MPa			

3.2 Choose material

From table (6.1) , the material of choice for both gears is steel 40X with $S \leq 100$ (mm), HB250, $\sigma_b = 850$ (MPa), $\sigma_{ch} = 550$ (MPa).

Table (6.2) also gives $\sigma_{Hlim}^o = 2HB + 70$, $S_H = 1.1$, $\sigma_{Flim}^o = 1.8HB$, $S_F = 1.75$

Therefore, they have the same properties except for their surface roughness H .

For the pinion, $H_1 = HB250 \Rightarrow \sigma_{Hlim1}^o = 570$ (MPa), $\sigma_{Flim1}^o = 450$ (MPa)

For the driven gear, $H_2 = HB240 \Rightarrow \sigma_{Hlim2}^o = 550$ (MPa), $\sigma_{Flim2}^o = 432$ (MPa)

3.3 Calculate $[\sigma_H]$ and $[\sigma_F]$

3.3.1 Working cycle of bearing stress

Using equation (6.5) :

$$N_{HO1} = 30H_1^{2.4} = 17.07 \times 10^6 \text{ (cycles)}$$

$$N_{HO2} = 30H_2^{2.4} = 15.4749 \times 10^6 \text{ (cycles)}$$

3.3.2 Working cycle of equivalent tensile stress

Since $H_1, H_2 \leq HB350$, $m_H = 6$, $m_F = 6$.

Both gears meshed indefinitely, thus $c = 1$.

Applying equation (6.7) and T_1, T_2, t_1, t_2 in the initial parameters:

$$N_{HE1} = 60c \left[\left(\frac{T_1}{T} \right)^3 n_1 t_1 + \left(\frac{T_2}{T} \right)^3 n_2 t_2 \right] \approx 5.73 \times 10^6 \text{ cycles } (n_1 = n_2 = n_{sh1})$$

$$N_{HE2} = 60c \left[\left(\frac{T_1}{T} \right)^3 n_1 t_1 + \left(\frac{T_2}{T} \right)^3 n_2 t_2 \right] \approx 1.15 \times 10^6 \text{ cycles } (n_1 = n_2 = n_{sh2})$$

$$N_{FE1} = 60c \left[\left(\frac{T_1}{T} \right)^{m_F} n_1 t_1 + \left(\frac{T_2}{T} \right)^{m_F} n_2 t_2 \right] \approx 3.35 \times 10^6 \text{ cycles } (n_1 = n_2 = n_{sh1})$$

$$N_{FE2} = 60c \left[\left(\frac{T_1}{T} \right)^{m_F} n_1 t_1 + \left(\frac{T_2}{T} \right)^{m_F} n_2 t_2 \right] \approx 0.67 \times 10^6 \text{ cycles } (n_1 = n_2 = n_{sh2})$$

3.3.3 Aging factor

For steel, $N_{FO1} = N_{FO2} = 4 \times 10^6$ (MPa). Applying equations (6.3) and (6.4) yield:

$$K_{HL1} = \sqrt[m_H]{N_{HO1}/N_{HE1}} \approx 1.2$$

$$K_{HL2} = \sqrt[m_H]{N_{HO2}/N_{HE2}} \approx 1.54$$

$$K_{FL1} = \sqrt[m_F]{N_{FO1}/N_{FE1}} \approx 1.03$$

$$K_{FL2} = \sqrt[m_F]{N_{FO2}/N_{FE2}} \approx 1.35$$

3.3.4 Calculate $[\sigma_H]$ and $[\sigma_F]$

Since the motor works in one direction, $K_{FC} = 1$

$$[\sigma_{H1}] = \sigma_{Hlim1}^o K_{HL1}/S_{H1} \approx 621.61 \text{ (MPa)}$$

$$[\sigma_{H2}] = \sigma_{Hlim2}^o K_{HL2}/S_{H2} \approx 771.63 \text{ (MPa)}$$

$$[\sigma_{F1}] = \sigma_{Flim1}^o K_{FC1} K_{FL1}/S_{F1} \approx 264.85 \text{ (MPa)}$$

$$[\sigma_{F2}] = \sigma_{Flim2}^o K_{FC2} K_{FL2}/S_{F2} \approx 332.48 \text{ (MPa)}$$

The permissible contact stress due to overload must be lower than 1.25 times of either $[\sigma_{H1}]$ or $[\sigma_{H2}]$, whichever is smaller. For permissible bending stress, it is equal to either $[\sigma_{F1}]$ or $[\sigma_{F2}]$, whichever is larger:

$$[\sigma_H]_{max} = \frac{1}{2} ([\sigma_{H1}] + [\sigma_{H2}]) \approx 696.62 \text{ (MPa)} \leq 1.25[\sigma_H]_{min} = 1.25[\sigma_{H1}]$$

$$[\sigma_F]_{max} = [\sigma_{F2}] = 0.8\sigma_{ch} \approx 440 \text{ (MPa)}$$

3.4 Transmission Design

3.4.1 Determine basic parameters

Examine table (6.5) gives $K_a = 43$

Assuming symmetrical design, table (6.6) also gives $\psi_{ba} = 0.5$

$$\Rightarrow \psi_{bd} = 0.53\psi_{ba}(u_{hg} + 1) = 1.59$$

From table (6.7) , using interpolation, we approximate $K_{H\beta} \approx 1.108$, $K_{F\beta} \approx 1.2558$

Since the gear system only consists of involute gears and it is also a speed reducer gearbox, we estimate a using equation (6.15a) gives:

$$a = K_a(u_{hg} + 1) \sqrt[3]{\frac{T_{sh1}K_{H\beta}}{[\sigma_H]^2 u_{hg} \psi_{ba}}} \approx 91.94 \text{ (mm)}$$

According to SEV229-75 standard, we choose $a_w = 100 \text{ mm}$

3.4.2 Determine gear meshing parameters

Find m Applying equation (6.17) and choose m from table (6.8) :

$$m = (0.01 \div 0.02)a_w \approx (0.92 \div 1.84) \text{ (mm)} \Rightarrow m = 1.5 \text{ (mm)}$$

Find z_1, z_2, b_w Let $\beta = 15^\circ$. Combining equation (6.18) and (6.20), we come up with the formula to calculate z_1 . From the result, z_1 is rounded up to the nearest odd number (preferably a prime number).

$$z_1 = \frac{2a_w \cos \beta}{m(u_{hg} + 1)} \approx 19.73 \Rightarrow z_1 = 21$$

$$z_2 = u_{hg}z_1 = 105$$

$$\Rightarrow b_w = \psi_{ba}a_w = 50 \text{ (mm)}$$

Recalculate β There are 2 approaches for correction involving the change of either α or β . Because altering α leads to many other corrections (d_1 , d_2 and a), β will be used instead.

Since z_1 is rounded, we must find β to obtain the correct angle, ensuring that $\beta \in (8^\circ, 20^\circ)$. Using equation (6.32):

$$\beta = \arccos \frac{m(z_1 + z_2)}{2a_w} \approx 19.09^\circ$$

Find x_1, x_2 To find x_1 and x_2 , we will follow the calculation scheme provided in p.103. Since $\beta \approx 19.09^\circ \in (17, 21]$, $z_{min} = 15$, which leads to z_1 satisfying condition $z_1 \geq z_{min} + 2 > 10$, according to table (6.9). Combined with $u_{hg} = 5 \geq 3.5$, we obtain $x_1 = 0.3, x_2 = -0.3$, disregarding the calculation of y .

3.4.3 Other parameters

$$d_1 = d_{w1} = \frac{mz_1}{\cos \beta} \approx 33.33 \text{ (mm)}$$

$$d_{b1} = d_1 \cos \alpha \approx 31.32 \text{ (mm)}$$

$$d_2 = d_{w2} = \frac{mz_2}{\cos \beta} \approx 166.67 \text{ (mm)}$$

$$d_{b2} = d_2 \cos \alpha \approx 156.62 \text{ (mm)}$$

$$d_{a1} = d_1 + 2(1 + x_1)m \approx 37.23 \text{ (mm)}$$

$$\alpha_t = \alpha_{tw} = \arctan \frac{\tan \alpha}{\cos \beta} \approx 20.65^\circ$$

$$d_{a2} = d_2 + 2(1 + x_2)m \approx 168.77 \text{ (mm)}$$

$$v = \frac{\pi d_1 n_{sh1}}{6 \times 10^4} \approx 5 \text{ (m/s)}$$

$$d_{f1} = d_1 - (2.5 - 2x_1)m \approx 30.48 \text{ (mm)}$$

$$d_{f2} = d_2 - (2.5 - 2x_2)m \approx 162.02 \text{ (mm)}$$

3.4.4 Contact stress analysis

From section 6.3.3. in the text, contact stress applied on a gear surface must satisfy the condition below:

$$\sigma_H = z_M z_H z_\epsilon \sqrt{2T_{sh1} K_H \frac{u_{hg} + 1}{b_w u_{hg} d_{w1}^2}} \leq [\sigma_H]$$

Find z_M $z_M = 274$, according to table (6.5)

Find z_H $\beta_b = \arctan (\cos \alpha_t \tan \beta) \approx 17.94^\circ \Rightarrow z_H = \sqrt{2 \frac{\cos \beta_b}{\sin(2\alpha_t)}} \approx 1.7$

Find z_ϵ Obtaining z_ϵ through calculations:

$$\epsilon_\alpha = \frac{\sqrt{d_{a1}^2 - d_{b1}^2} + \sqrt{d_{a2}^2 - d_{b2}^2} - 2a_w \sin \alpha_t}{2\pi m \frac{\cos \alpha_t}{\cos \beta}} \approx 1.34$$

$$\epsilon_\beta = b_w \frac{\sin \beta}{m\pi} \approx 3.47 > 1 \Rightarrow z_\epsilon = \epsilon_\alpha^{-0.5} \approx 0.86$$

Find K_H We find K_H using equation $K_H = K_{H\beta} K_{H\alpha} K_{Hv}$

From table (6.13), $v \leq 6$ (m/s) \Rightarrow AG = 8

From table (P2.3), using interpolation, we approximate:

$$K_{Hv} \approx 1.05, K_{Fv} \approx 1.14$$

From table (6.14), using interpolation, we approximate:

$$K_{H\alpha} \approx 1.09, K_{F\alpha} \approx 1.27$$

$$\Rightarrow K_H \approx 1.27$$

Find σ_H After calculating $z_M, z_H, z_\epsilon, K_H$, we get the following result:

$$\sigma_H \approx 663.86 \text{ MPa} \leq [\sigma_H] \approx 696.62 \text{ MPa}$$

3.4.5 Bending stress analysis

For safety reasons, the following conditions must be met:

$$\sigma_{F1} = 2 \frac{T_{sh1} K_F Y_\epsilon Y_\beta Y_{F1}}{b_w d_{w1} m_n} \leq [\sigma_{F1}]$$

$$\sigma_{F2} = \frac{\sigma_{F1} Y_{F2}}{Y_{F1}} \leq [\sigma_{F2}]$$

Find Y_ϵ Knowing that $\epsilon_\alpha \approx 1.64$, we can calculate $Y_\epsilon = \epsilon_\alpha^{-1} \approx 0.75$

Find Y_β $Y_\beta = 1 - \frac{\beta}{140} \approx 0.86$

Find Y_F Using formula $z_v = z \cos^{-3}(\beta)$ and table (6.18):

$$z_{v1} = z_1 \cos^{-3}(\beta) \approx 24.88 \Rightarrow Y_{F1} \approx 3.6$$

$$z_{v2} = z_2 \cos^{-3}(\beta) \approx 124.42 \Rightarrow Y_{F2} \approx 3.64$$

Find K_F Using $K_{F\beta}$, $K_{F\alpha}$, K_{Fv} calculated from the sections above, we derive:

$$K_F = K_{F\beta} K_{F\alpha} K_{Fv} \approx 1.82$$

Find σ_F Since $m_n = m \cos \beta \approx 1.42$, substituting all the values, we find out that:

$$\sigma_{F1} \approx 179.07 \text{ (MPa)} \leq [\sigma_{F1}] \approx 264.85 \text{ (MPa)}$$

$$\sigma_{F2} \approx 181.06 \text{ (MPa)} \leq [\sigma_{F2}] \approx 332.48 \text{ (MPa)}$$

3.4.6 Force on shafts

$$F_t = \frac{2T_{sh1}}{d_1} \approx 3003.15 \text{ (N)}$$

$$F_r = F_t \tan \alpha_t \approx 1131.8 \text{ (N)}$$

$$F_a = F_t \tan \beta \approx 1039.35 \text{ (N)}$$

In summary, we have the following table:

	pinion	driving gear
H (HB)	250	240
$[\sigma_H]$ (MPa)	621.61	771.63
$[\sigma_F]$ (MPa)	264.85	332.48
$[\sigma_H]_{max}$ (MPa)	696.62	
$[\sigma_F]_{max}$ (MPa)	440	
σ_H (MPa)	621.61	771.63
σ_F (MPa)	179.07	181.06
σ_H (MPa)	663.86	
α_{tw} ($^\circ$)	20.65	
β ($^\circ$)	19.09	
a_w (mm)	100	
b_w (mm)	50	
m (mm)	1.5	
z	21	105
d (mm)	33.33	166.67
d_a (mm)	37.23	168.77
d_f (mm)	30.48	162.02
d_b (mm)	31.32	156.62
v (m/s)	5	
u_{hg}	5	

Table 3.1: Gearbox specifications

Chapter 4

Shaft Design

4.1 Nomenclature

$[\tau]$	permissible torsion, MPa	q	standardized coefficient of shaft diameter
r	position of applied force on the shaft, mm	b_O	rolling bearing width, mm
hr	tooth direction	l_m	hub diameter, mm
cb	role of gear on the shaft (active or passive)	k_1	distance between elements, mm
cq	rotational direction of the shaft	k_2	distance between bearing surface and inner walls of the gearbox, mm
σ_b	ultimate strength, MPa	k_3	distance between element surface and bearing lid, mm
σ_{ch}	yield limit, MPa	h_n	distance between bearing lid and bolt, mm
S	safety factor	T	torque on shaft
F_x	applied force, N	α_{tw}	meshing profile angle, °
F_t	tangential force, N	β	helix angle, °
F_r	radial force, N	$_1$	subscript for shaft 1
F_a	axial force, N	$_2$	subscript for shaft 2
a_w	shaft distance, mm		
d	shaft diameter, mm		
d_w	gear diameter, mm		
x	subscript for x-axis		

4.2 Choose material

For moderate load, we will use quenched steel 40X to design the shafts. From table 6.1, the specifications are as follows: $S \leq 100$ (mm), HB260, $\sigma_b = 850$ (MPa), $\sigma_{ch} = 550$ (MPa).

4.3 Transmission Design

4.3.1 Load on shafts

Applied forces from Gears

Following p.186, the subscript convention of the book will be used in this chapter. If a symbol has 2 numeric subscripts, the first one is the ordinal number of shafts while the second one is used for machine elements.

On shaft 1, the motor is labeled 1 and the pinion is labeled 2. On shaft 2, the driven gear is labeled 1 and the driving sprocket is labeled 2. Therefore, we obtain:

$$r_{12} = -d_{w12}/2 \approx -13.57 \text{ (mm)}, hr_{12} = +1, cb_{12} = +1, cq_1 = +1$$

$$r_{21} = +d_{w21}/2 \approx +67.84 \text{ (mm)}, hr_{21} = -1, cb_{21} = -1, cq_2 = -1$$

Find magnitude of F_t , F_r , F_a Using the results from the previous chapter:

$$\alpha_{tw} \approx 21.17^\circ, \beta = 20^\circ, d_{w12} \approx 27.14 \text{ (mm)}$$

$$\begin{cases} F_{t12} = F_{t21} = \frac{2T_{sh1}}{d_{w12}} \approx 2769.03 \text{ (N)} \\ F_{r12} = F_{r21} = \frac{F_{t12} \tan \alpha_{tw}}{\cos \beta} \approx 1141.36 \text{ (N)} \\ F_{a12} = F_{a21} = F_{t12} \tan \beta \approx 1007.84 \text{ (N)} \end{cases}$$

Find direction of F_t , F_r , F_a Following the sign convention, we obtain the forces:

$$\begin{cases} F_{x12} = \frac{r_{12}}{|r_{12}|} c q_1 c b_{12} F_{t12} \approx -2769.03 \text{ (N)} \\ F_{y12} = -\frac{r_{12}}{|r_{12}|} \frac{\tan \alpha_{tw}}{\cos \beta} F_{t12} \approx 1141.36 \text{ (N)} \\ F_{z12} = c q_1 c b_{12} h r_{12} F_{t12} \tan \beta \approx 1007.84 \text{ (N)} \end{cases}$$

$$\begin{cases} F_{x21} = \frac{r_{21}}{|r_{21}|} c q_2 c b_{21} F_{t21} \approx 2769.03 \text{ (N)} \\ F_{y21} = -\frac{r_{21}}{|r_{21}|} \frac{\tan \alpha_{tw}}{\cos \beta} F_{t21} \approx -1141.36 \text{ (N)} \\ F_{z21} = c q_2 c b_{21} h r_{21} F_{t21} \tan \beta \approx -1007.84 \text{ (N)} \end{cases}$$

Applied forces from Chain drives

Assuming the angle between x-axis and F_r is 210° and $F_r \approx 2539.28 \text{ (N)}$ (chapter 2), we get the direction of F_r on shaft 2:

$$\begin{cases} F_{x22} = F_{r22} \cos 210^\circ \approx -1269.64 \text{ (N)} \\ F_{y22} = F_{r22} \sin 210^\circ \approx -2199.08 \text{ (N)} \end{cases}$$

4.3.2 Preliminary calculations

Since shaft 1 receives input torque T_{sh1} and shaft 2 produces output torque T_{sh2} , $[\tau_1] = 15 \text{ (MPa)}$ and $[\tau_2] = 30 \text{ (MPa)}$. Using equation (10.9), we can approximate d_1 and d_2 :

$$d_1 \geq \sqrt[3]{\frac{T_{sh1}}{0.2[\tau_1]}} \approx 23.22 \text{ (mm)} \Rightarrow d_1 = 25 \text{ (mm)}$$

$$d_2 \geq \sqrt[3]{\frac{T_{sh2}}{0.2[\tau_2]}} \approx 30.99 \text{ (mm)} \Rightarrow d_2 = 35 \text{ (mm)}$$

4.3.3 Identify the distance between bearings and applied forces

In this section, we will find all the parameters in Figure 4.1. However, if a parameter has 2 numeric subscripts, the first one will denote the ordinal number

of shafts.

From table (10.2), we can estimate b_O . On shaft 1, $b_{O1} = 15$ (mm). On shaft 2, $b_{O2} = 21$ (mm). Using equation (10.10), the gear hubs are $l_{m13} = l_{m12} = 1.5d_1 \approx 34.83$ (mm), $l_{m23} = l_{m22} = 1.5d_2 \approx 46.48$ (mm) (l_{m22} is the chain hub)

From table (10.3), we choose $k_1 = 10$ (mm), $k_2 = 8$ (mm), $k_3 = 15$ (mm), $h_n = 18$ (mm). This parameters apply for both shafts in the system.

Table (10.4) introduce the formulas for several types of gearbox. Since our system only concerns about 1-level gear reducer, the formulas below are used:

On shaft 1:

$$l_{12} = -l_{c12} = -[0.5(l_{m12} + b_{O1}) + k_3 + h_n] \approx -57.92 \text{ (mm)}$$

$$l_{13} = 0.5(l_{m13} + b_{O1}) + k_1 + k_2 \approx 42.92 \text{ (mm)}$$

$$l_{11} = 2l_{13} \approx 85.83 \text{ (mm)}$$

On shaft 2:

$$l_{22} = -l_{c22} = -[0.5(l_{m22} + b_{O2}) + k_3 + h_n] \approx -66.74 \text{ (mm)}$$

$$l_{23} = 0.5(l_{m23} + b_{O2}) + k_1 + k_2 \approx 51.74 \text{ (mm)}$$

$$l_{21} = 2l_{23} \approx 103.48 \text{ (mm)}$$

4.3.4 Determine shaft diameters and lengths

From the diagram, we derive the reaction forces at A_1 , A_2 , B_1 , B_2 , which are R_{A1x} , R_{A1y} , R_{B1x} , R_{B1y} , R_{A2x} , R_{A2y} , R_{B2x} , R_{B2y} . Using equilibrium conditions:

$$\begin{cases} \sum_i \mathbf{F}_i = 0 \\ \sum_i \mathbf{r}_i \times \mathbf{F}_i = 0 \end{cases}$$

We obtain the results as follows:

From the reaction forces, we can easily draw shear force-bending moment diagram

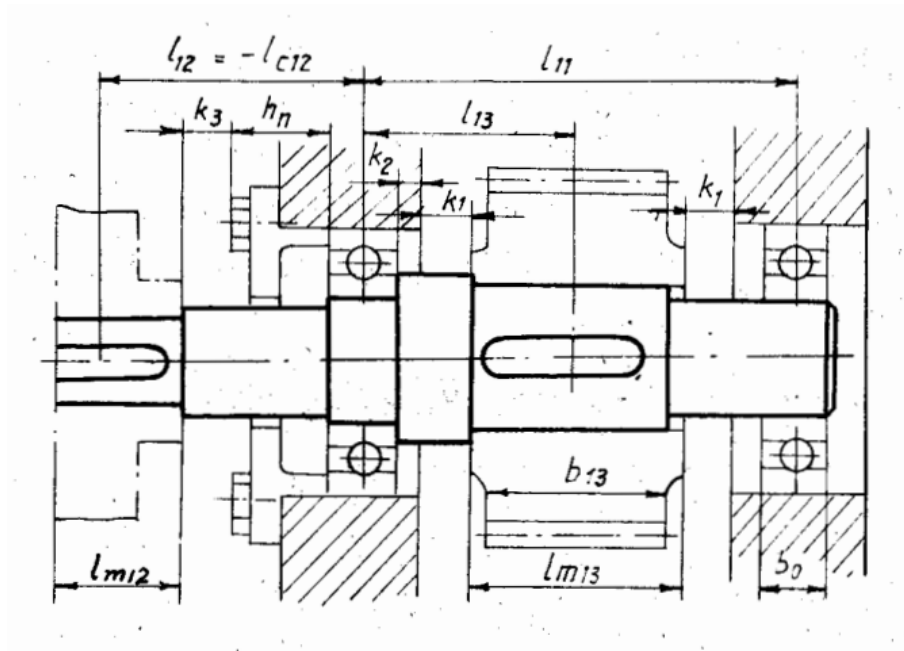


Figure 4.1: Shaft design and its dimensions

$$\left\{ \begin{array}{l} R_{A1x} \approx 1384.51 \text{ (N)} \\ R_{A1y} \approx -570.68 \text{ (N)} \\ R_{B1x} \approx 1384.51 \text{ (N)} \\ R_{B1y} \approx -570.68 \text{ (N)} \end{array} \right. \quad \left\{ \begin{array}{l} R_{A2x} \approx 703.98 \text{ (N)} \\ R_{A2y} \approx 4188.06 \text{ (N)} \\ R_{B2x} \approx -2203.37 \text{ (N)} \\ R_{B2y} \approx -847.62 \text{ (N)} \end{array} \right.$$

for both shafts on 2 major planes (xOz) and (yOz).

From equation (10.15), we calculate the total bending moment at point C_2 , A_2 , D_2 , B_2 , A_1 , D_1 , B_1 , C_1

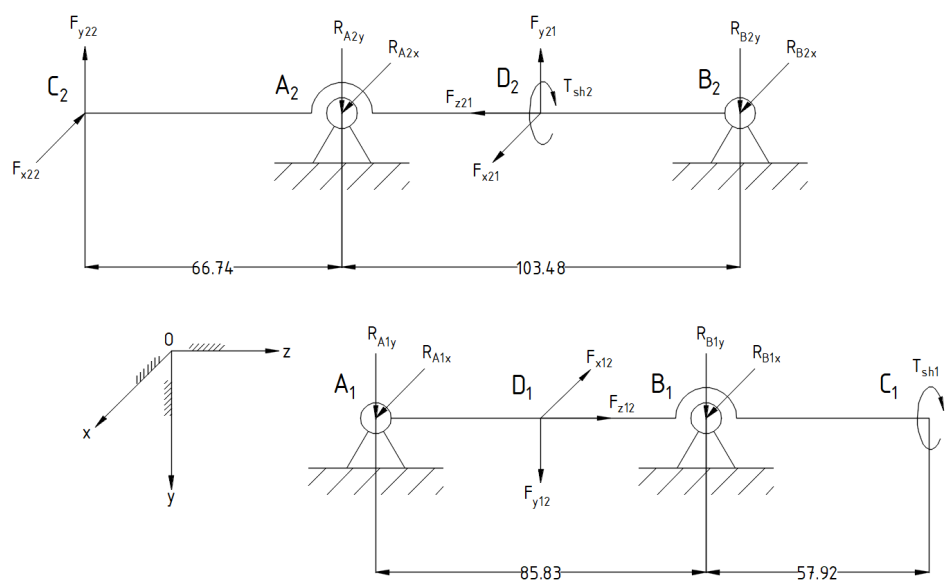


Figure 4.2: Force analysis of shafts

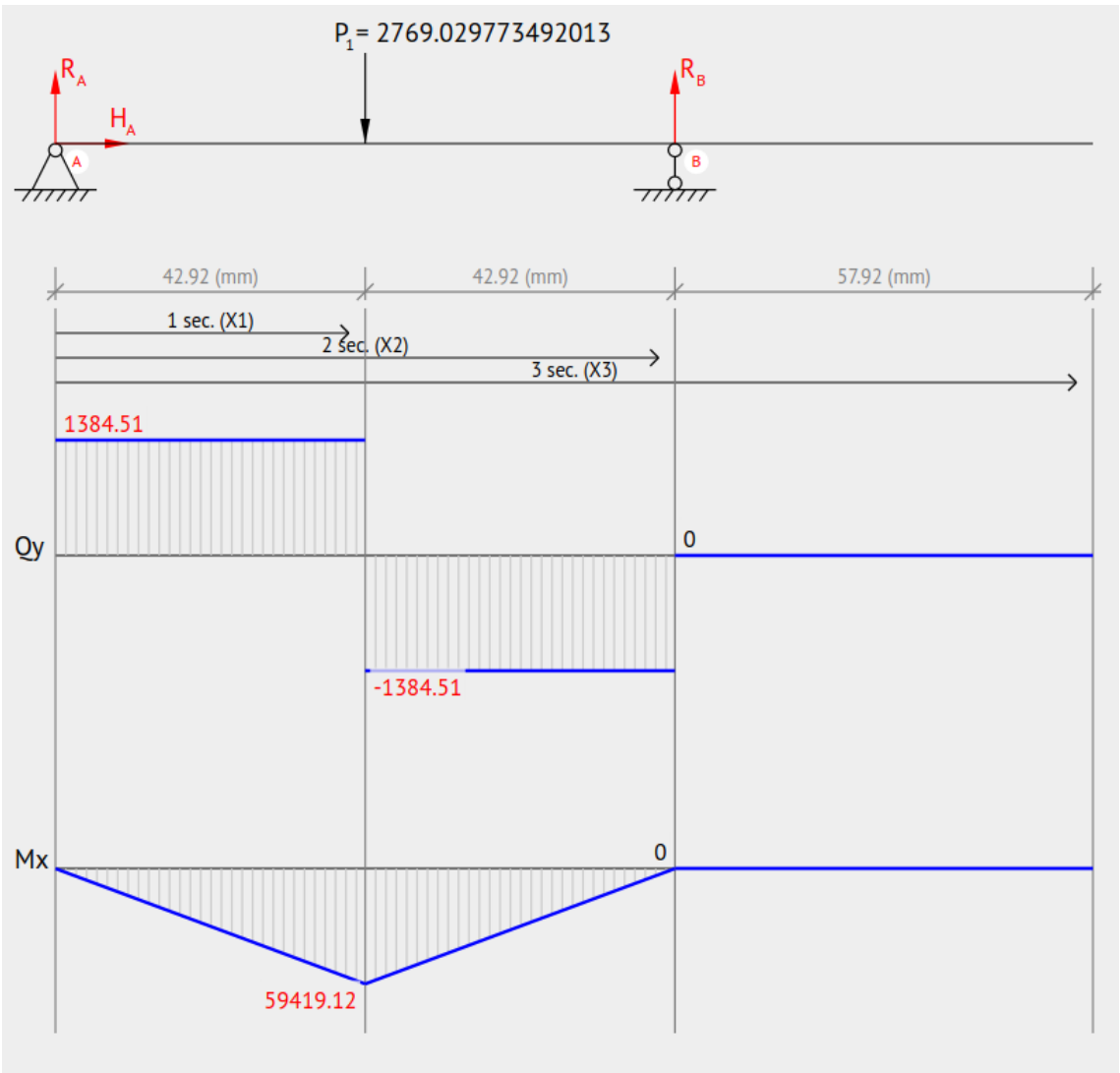


Figure 4.3: Shear force - Bending moment diagram on (xOz) of shaft 1

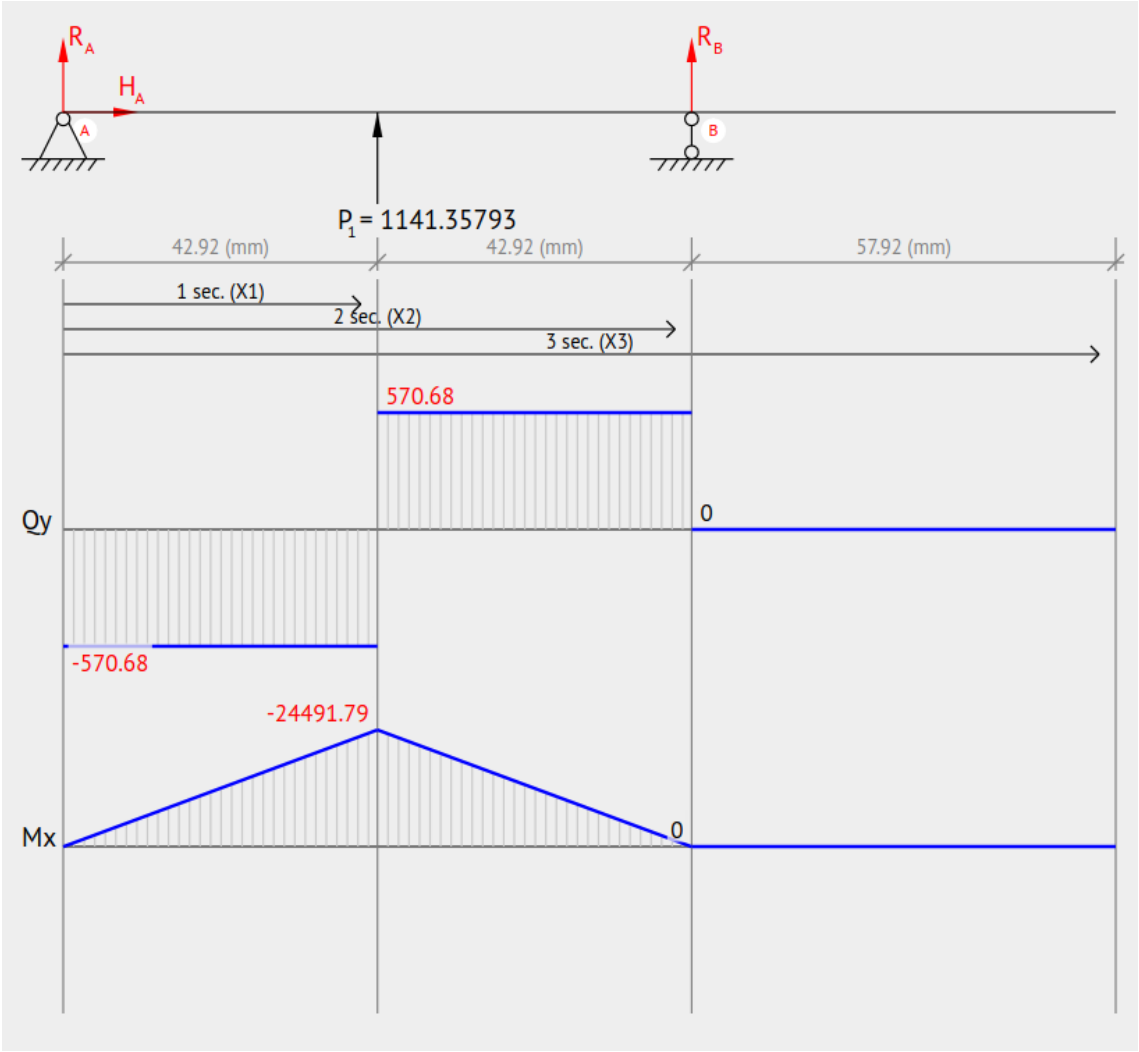


Figure 4.4: Shear force - bending moment diagram on (yOz) of shaft 1

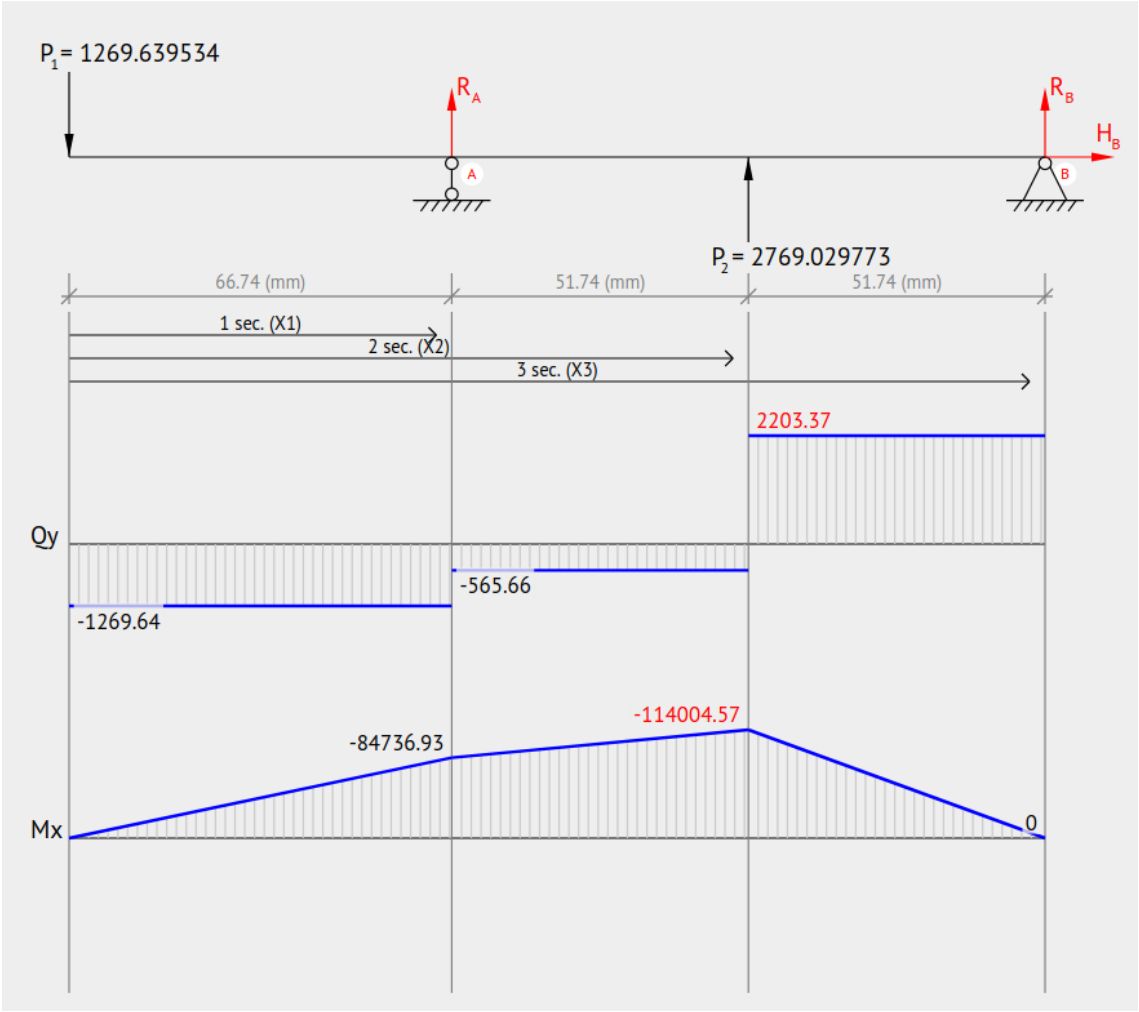


Figure 4.5: Shear force - Bending moment diagram on (xOz) of shaft 2

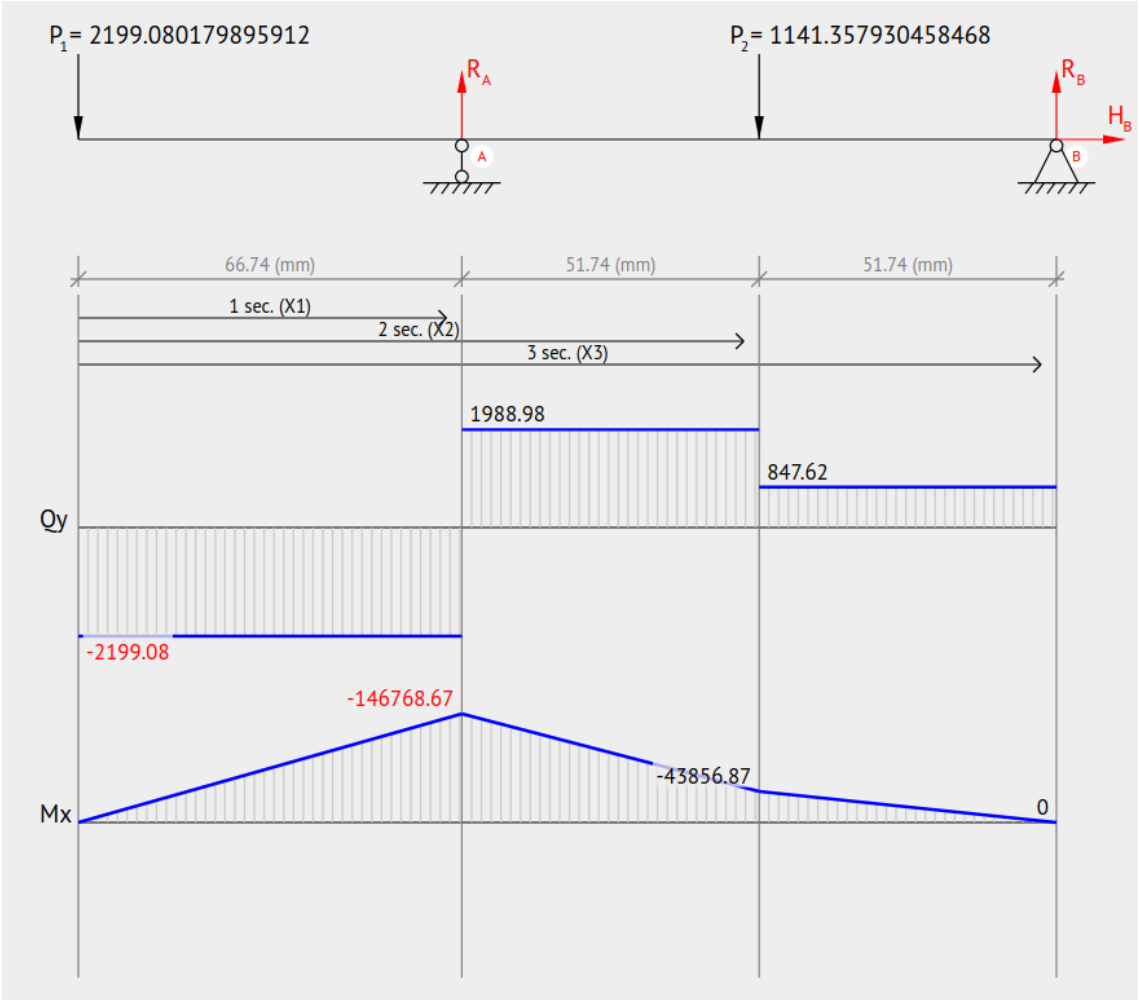


Figure 4.6: Shear force - Bending moment diagram on (yOz) of shaft 2