

### HCM University of Technology Fluid Mechanics CI2003

### Assignment

Submitted To: Le Van Duc PhD Fluid Mechanics Department Submitted By: Nguyen Quy Khoi

# **Contents**

1	Properties of Fluids	4
2	Pressure and Fluid Statics	Ç

# **List of Tables**

# **List of Figures**

2.1	Differential manometer	9
2.2	Rotating rectangular valve	10

### **Chapter 1**

## **Properties of Fluids**

#### Q1.1

A steel vessel of 1% increase in volume when the pressure is increased by 70 MPa. At standard condition (pressure P = 101.3 KPa), the vessel is filled with m = 450 kg of water ( $\rho = 1000$  kg/m<sup>3</sup>). Given bulk modulus of elasticity,  $\kappa = 2.06 \times 10^9$  Pa. Compute the mass of water to add into the vessel to increase the pressure to 70 MPa.

Ans:  

$$V = \frac{m}{\rho} = \frac{450}{1000} = 0.45 \text{ (m}^3\text{)}$$

$$\kappa = -V \frac{dP}{dV}$$

$$\Rightarrow dm = \rho dV = -\rho V \frac{dP}{\kappa}$$

$$= -1000 \times 0.45 \times \frac{101.3 \times 10^3 - 70 \times 10^6}{2.06 \times 10^9} = 15.27 \text{ (kg)}$$

#### Q1.2

Determine the change in volume of  $V_i=3\,\mathrm{m}^3$  of air when the pressure increases from  $P_i=100\,\mathrm{kPa}$  to  $P_f=500\,\mathrm{kPa}$ . Air is at  $T=23\,\mathrm{^{\circ}C}$  (assume ideal gas)

#### Ans:

Assume isothermal condition: 
$$P_i V_i = P_f V_f$$
  

$$\Rightarrow \Delta V = V_f - V_i = \frac{P_i V_i}{P_f} - V_i = \frac{100 \times 3}{500} - 3 = -2.4 \text{ (m}^3)$$

#### Q1.3

They compress the air into a vessel having volume,  $V_1 = 0.3 \,\mathrm{m}^3$  under pressure  $P_1 = 100 \,\mathrm{at}$ . After a period of leakage, the air pressure in the vessel is lowered to  $P_2 = 90 \,\mathrm{at}$ . Regardless of the deformation of the vessel, determine the volume of air that is leaked during that period (corresponding to the atmospheric pressure, 1 atm), if the constant temperature and atmospheric pressure are considered to be at 1 at.

#### Ans:

For ideal gas, 
$$\kappa = P_2 = -V_1 \frac{dP}{dV}$$
  

$$\Rightarrow dV = -\frac{V_1}{P_2} dP = -\frac{0.3}{90} (90 - 100 - 1) = -0.0367 \text{ (m}^3)$$

#### Q1.4

A diameter piston  $d=50\,\mathrm{mm}$  moves evenly in a cylinder  $D=50.1\,\mathrm{mm}$ . Determine the decrease in force acting on the piston (as a percentage) when the speed decreases by 5%.

#### Ans:

Assume constant speed: 
$$\frac{\Delta V}{V_1} = -5\%$$
  
We also have  $\tau = \frac{F}{A} = \mu \frac{du}{dy} = \mu \frac{V}{l} \Rightarrow \frac{F_1}{V_1} = \frac{F_2}{V_2} = \mu \frac{A}{l}$   
From the relation:  $\frac{\Delta F}{F_1} = \frac{\Delta V}{V_1} = -5\%$ 

#### Q1.5

A machine axis having diameter, D = 75 mm, with uniform movement with V = 0.1 m/s under the force, F = 100 N. The lubricating layer thickness, l in

the bearing is l = 0.07 mm. Length of bearing L = 200 mm. Determine oil dynamic viscosity.

#### Ans:

$$A = (D + 2l)\pi \times L = (75 + 2 \times 0.07)\pi \times 200 = 47211.85 \text{ (mm}^3) = 4.72 \times 10^{-5} \text{ (m}^3)$$

$$\tau = \frac{F}{A} = \mu \frac{V}{l} \Rightarrow \mu = \frac{F}{A} \frac{l}{V} = \frac{100}{4.72 \times 10^{-5}} \times \frac{0.07 \times 10^{-3}}{0.1} = 1.483 \text{ (kg/m} \cdot \text{s)}$$

#### Q1.6

A thin layer of Newton liquid with specific weight  $\gamma$ , dynamic viscosity  $\mu$  and thickness t flows on a plane inclined at an angle  $\alpha$ . The upper surface is exposed to the air. Assuming no friction between liquid and air. Find the expression of u(y). Can u consider as a linear function of y?

#### Ans:

The force exerting on the center of gravity of the liquid is

$$F = \gamma V \sin \alpha$$

Both contact surfaces

#### 01.9

Determine the frictional force at the inner wall of a water supply pipe segment at T = 20 °C, radius R = 80 mm = 0.08 m, L = 10 m. The velocity at the points on the pipe cross-section varies according to the following:

$$u(r) = 0.5 \left( 1 - \frac{r^2}{R^2} \right)$$

where r is the radius of considered point.

#### Ans

From table at 
$$T = 20 \,^{\circ}\text{C} \Rightarrow \mu = 1.002 \times 10^{-3} \, (\text{kg/m} \cdot \text{s})$$
  
 $A = 2\pi R L = 2\pi \times 0.08 \times 10 = 5.03 \, (\text{m}^2)$   
 $F = \tau A = \mu \frac{du}{dr} A = \mu \frac{(-2)R}{R^2} A$   
 $= 1.002 \times 10^{-3} \times \frac{(-2) \times 0.08}{0.08^2} \times 5.03 = -0.126 \, (\text{N})$ 

#### Q1.10

Determine the gauge pressure inside a water drop of diameter  $d=2 \,\mathrm{mm}=0.002 \,\mathrm{m}$ . The temperature of water is  $T=25\,^{\circ}\mathrm{C}$ .

#### Ans:

From table at 
$$T = 25 \,^{\circ}\text{C} \Rightarrow \sigma_s = 0.072 \,(\text{N/m})$$
  
 $P_g = \Delta P_{droplet} = \frac{2\sigma_s}{d/2} = \frac{2 \times 0.072}{0.002/2} = 144 \,(\text{Pa})$ 

#### Q1.11

A gas has a molar mass of R = 32 kg/mol under a pressure condition of P = 5 at = 490332.5 Pa, a temperature of  $T = 30 \,^{\circ}\text{C}$ 

- 1. Determine the gas density.
- 2. Determine the density of this gas if P = const, while temperature drops to  $T_f = 15$  °C.
- 3. Determine the density of this gas if holding T = const, while the pressure drops to  $P_f = 2$  at.

#### Ans:

1. 
$$P = \rho RT \Rightarrow \rho = \frac{P}{RT} = \frac{32}{490332.5 \times (30 + 273)} = 0.215 \times 10^{-6} \text{ (kg/m}^3)$$

2. adiabatic condition

$$\rho T = \rho_f T_f \Rightarrow \rho_f = \frac{\rho T}{T_f} = \frac{0.215 \times 10^{-6} \times (30 + 273)}{15 + 273} = 0.226 \times 10^{-6} \text{ (kg/m}^3)$$

3. isothermal condition

$$\frac{P}{\rho} = \frac{P_f}{\rho_f} \Rightarrow \rho_f = \frac{\rho P_f}{P} = \frac{0.215 \times 10^{-6} \times 2}{5} = 0.086 \times 10^{-6} \text{ (kg/m}^3)$$

#### Q1.12

A liquid is compressed in a cylinder, the water initially has a volume of  $V_o = 41$  at normal pressure,  $P_o = 1$  at = 98066.5 Pa. The pressure in the cylinder increases to  $p_1 = 6$  at, the water volume decreases by 1 cm<sup>3</sup>.

- 1. Compute the bulk modulus of elasticity of water.
- 2. If the pressure in the cylinder increases to 20 at, calculate the volume of water  $V_f$  in the cylinder.
- 3. Calculate the pressure in the cylinder, if the volume of the water is reduced by 0.1%.

#### Ans:

1. 
$$\kappa = -V_o \frac{dP}{dV} = -4 \times 10^{-3} \times \frac{6 \times 98066.5}{(-1) \times 10^{-6}} = 2.36 \times 10^9 \text{ (Pa)}$$

2. Cylinder increase pressure to 20 at  $\Rightarrow dV = V_f - 4 \times 10^{-3} = \frac{-20}{6} = -3.33 \text{ (cm}^3\text{)} = -3.33 \times 10^{-3} \text{ (l)}$  $\Rightarrow V_f = 3.997 \text{ (l)}$ 

3. 
$$dP = P_f - P_o = -\kappa \times \frac{dV}{V_o} = -2.36 \times 10^9 \times \frac{(-0.1)}{100} = 2.36 \times 10^6 \text{ (Pa)}$$
  
 $\Rightarrow P_f = 2.458 \text{ (MPa)}$ 

#### Q1.13

The air moving through a narrow tube into a water tank forms a stream of bubbles d=3 mm in diameter. Calculate the difference between air pressure in the narrowed section and surrounding water pressure. Give the surface tension of water  $\sigma_s = 0.0728 \,\mathrm{N/m}$ .

#### Ans:

### **Chapter 2**

### **Pressure and Fluid Statics**

#### Q2.1

A differential manometer consists of a U-shaped pipe of diameter d, connecting two cylinders of diameter D, the instrument being filled with two insoluble liquids of specific gravity  $\gamma_1$  and  $\gamma_2$ . When the pressure difference,  $\Delta p = p_1 - p_2 = 0$ , the interface between two liquids is at position 0 on the scale.

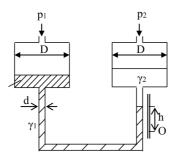


Figure 2.1: Differential manometer

1. Determine the relationship between  $\Delta p$  and the displacement of the interface between the two fluids, h. Given d = 5 mm, D = 50 mm,  $\gamma_1 = 8530 \,\mathrm{N/m^3}$ ,  $\gamma_2 = 8140 \,\mathrm{N/m^3}$ ,  $h = 280 \,\mathrm{mm}$ .

2. With the given  $\Delta p$ , how many times h will decrease, if d = D = 5 mm.

#### Ans:

Let  $h_1, h_2$  be the height of the liquid from O on the left and right pipe, respectively.

The relation between  $P_1$  and  $P_2$  is described according to the formula:

$$\frac{D^2}{d^2}p_1 = p_2\frac{D^2}{d^2} + \gamma_2(h_2 - h) - \gamma_1(h_1 - h)$$

Rearranging the equation yields:

$$h = \frac{D^2}{d^2} \Delta p + \gamma_1 h_1 - \gamma_2 h_2$$
$$\gamma_1 - \gamma_2$$

#### Q2.2

A rectangular valve length b rotates about the horizontal axis at point A. Neglecting valve thickness, determine the minimum weight G of the gate based on the parameters  $h1, h2, h3, \rho, b$  and g such that the system is balanced. Use figure 2.2 to solve the problem.

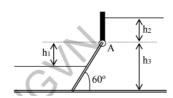


Figure 2.2: Rotating rectangular valve