# VIETNAM NATIONAL UNIVERSITY HO CHI MINH CITY HCM UNIVERSITY OF TECHNOLOGY FACULTY OF MECHANICAL ENGINEERING - MECHATRONICS DEPARTMENT



#### ENGINEERING INTERNSHIP REPORT

# **Air Compressor Modeling using MATLAB**

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In particular, I would like to thank Dr. Nguyen Tan Tien, who wholeheartedly guided and helped me complete this internship report topic.

Finally, I also would like to thank my teammates, Nguyen Dang Hung and Nguyen Khanh Trung and the seniors at DCSELab for their help and support.

At the same time, the school has given me the opportunity to practice where I love, let me step into real life to apply the knowledge that my teachers have taught. Through this internship, I realize many new and useful things in the preliminary design of practical machines to help me in my future work.

Due to my lack of knowledge and experience regarding the modeling skills, this report is very likely be prone to mistakes. I am looking forward to your response for future improvements.

## **Chapter 1**

# **Overview of the Company**

### 1.1 History of the Organization

DCSELab (National key Laboratory of Digital Control and System Engineering), founded on 04/08/2003 under Decision number 590/QD/DHQG/TCCB of Vietnam National Unversity Ho Chi Minh City. It is an independent organization which has a status of legal person; conducts technological advancement on its own accord based on the Regulation for developing and functioning of National key Laboratory.



Figure 1.1: DCSELab main entrance

### 1.2 Working Objectives

Experimenting, designing, installing, maintaining and transferring equipment (hardware and software) regarding digital control, system engineering; mechatronics, telecommunication, information technology, automation and industrial process.

## 1.3 The Organizational Structure

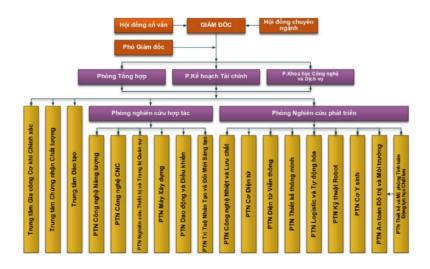


Figure 1.2: The organizational structure of DCSELab

# Chapter 2

# **Internship tasks**

### 2.1 Problem

At the moment, the light duty air compressor market mainly use electricity as the power source, which can be inconvenient at remote locations where power grid is difficult to reach. To solve this problem, we will analyze and model a V-twin air compressor with a compression end and a combustion end. The model is programmed using  $MATLAB^{\otimes}$  R2019a.

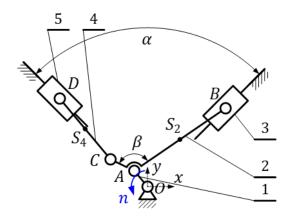


Figure 2.1: Mechanism of the air compressor

2 Internship tasks

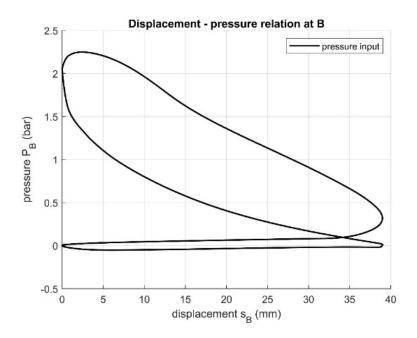


Figure 2.2: Pressure graph at link 3 (not to scale)

## 2.2 Parameters

Piston lift	$H_C = 39 \mathrm{mm}$
V-angle	$\alpha = 90^{\circ}$
Connecting rod dimensions	$\frac{l_{AB}}{l_{OA}} = 5.372, l_{AC} = 25mm, \beta = 120^{\circ}$
Crankshaft 1 weight	$m_1 = 1.6262 \mathrm{kg}$
Center of gravity of link 1	$S_1 \equiv O$
Moment of inertia of link 1	$J_{s1} = 0.0045585 \mathrm{kg \cdot m^2}$
Connecting rod 2 weight	$m_2 = 0.29597 \mathrm{kg}$
Center of gravity of link 2	$l_{AS2} = l_{S2B}$
Moment of inertia of link 2	$J_{S2} = 0.004874 \mathrm{kg \cdot m^2}$
Connecting rod 4 weight	$m_2 = 0.13865 \mathrm{kg}$
Center of gravity of link 4	$l_{CS4} = l_{S4D}$
Moment of inertia of link 4	$J_{S4} = 0.00011121 \mathrm{kg} \cdot \mathrm{m}^2$
Piston weight	$m_3 = m_5 = 0.33513 \mathrm{kg}$
Center of gravity of link 3 and 5	$S_3 \equiv B, S_5 \equiv D$
Piston crown area	$A = 0.01 \text{ m}^2$
Maximum operating pressure (The graphs given in figure 2.2 and	$p_{max} = 23  \text{bar}$
2.3)	
Allowable tolerance factor	$\delta = 1/80$
Average rotational velocity	$n_1 = 500 \mathrm{rpm}$
Valve lift (trapezoidal acceleration)	$s_0 = 2 \mathrm{mm}$
Early opening and late closing of combustion end	25°
Early opening of compression end	$40^{\circ}$
Pressure angle of cam follower	$\alpha_2 = 6^{\circ}$
Periodic angles	$\phi_{rise} = \phi_{fall},  \phi_{rise,comb} = 5^{\circ},$ $\phi_{rise,comp} = 20^{\circ}$

2.3 Objectives 9

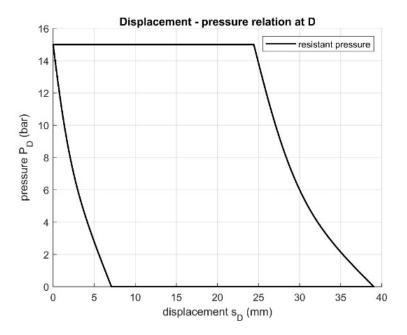


Figure 2.3: Pressure graph at link 5 (not to scale)

### 2.3 Objectives

- 1. Mechanism synthesis [1]
- 2. Kinematic analysis of the mechanism
- 3. Force analysis of the mechanism
- 4. Identify energy relation and calculate the flywheel weight
- 5. Combining the motion
- 6. Model cam mechanism for compression piston

### 2.4 Displacement analysis

#### **Position of** A

$$\vec{r}_A = \begin{bmatrix} x_A \\ y_A \\ 0 \end{bmatrix} = \begin{bmatrix} l_{OA}\cos\phi \\ l_{OA}\sin\phi \\ 0 \end{bmatrix}$$
 (2.1)

where  $\phi = \widehat{xOA}$ 

Position of B

$$\begin{cases} (x_A - x_B)^2 + (y_A - y_B)^2 &= l_{AB}^2 \\ \frac{y_B}{x_B} &= \tan x \widehat{OB} \end{cases}$$
 (2.2)

Solve equation (2.2) yields 2 positions  $B_1$ ,  $B_2$ . Combining with condition  $x_B$ ,  $y_B > 0$  to find the correct solution.

$$\vec{r}_B = \left[ \begin{array}{c} x_B \\ y_B \\ 0 \end{array} \right]$$

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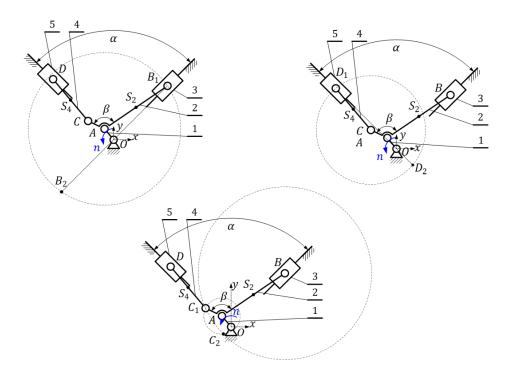


Figure 2.4: Position analysis of B, C and D

#### Position of C

$$\begin{cases} (x_A - x_C)^2 + (y_A - y_C)^2 &= l_{AC}^2 \\ (x_B - x_C)^2 + (y_B - y_C)^2 &= l_{BC}^2 \end{cases}$$
 (2.3)

Solve equation (2.3) yields 2 sets of positions  $C_1$ ,  $C_2$ , one of which is the correct solution. This can be programmed using MATLAB® to try both sets.

$$\vec{r}_C = \left[ \begin{array}{c} x_C \\ y_C \\ 0 \end{array} \right]$$

Position of D

$$\begin{cases} (x_C - x_D)^2 + (y_C - y_D)^2 &= l_{CD}^2 \\ \frac{y_D}{x_D} &= \tan \widehat{xOD} \end{cases}$$
 (2.4)

Solve equation (2.4) yields 2 positions  $D_1, D_2$ . Combining with condition  $x_D < 0, y_D > 0$  to find the correct solution.

$$\vec{r}_D = \left[ \begin{array}{c} x_D \\ y_D \\ 0 \end{array} \right]$$

Using MATLAB® to plot the positions of the mechanism in figure 2.5

### 2.5 Velocity and Acceleration analysis

With the analytical solutions of the points A, B, C, D, we can easily find the corresponding velocities and accelerations using derivative with respect to time t. Also, we need to remember that  $\phi(t)$  is a time-dependent variable.

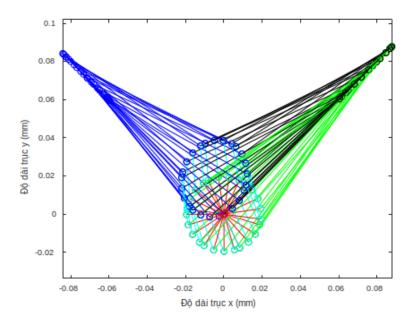


Figure 2.5: Locus of the mechanism using MATLAB®

#### 2.5.1 Velocity analysis

#### Velocity of A

$$\vec{v}_A = \dot{\vec{r}}_A = \frac{d\vec{r}_A}{dt} \tag{2.5}$$

where  $\phi = \widehat{xOA}$ 

#### Velocity of B

$$\vec{v}_B = \dot{\vec{r}}_B = \frac{d\vec{r}_B}{dt} = \vec{v}_A + \vec{\omega}_2 \times (\vec{r}_B - \vec{r}_A)$$
 (2.6)

From equation (2.6), we solve analytically for  $\vec{\omega}_2$ 

$$\vec{\omega}_2 = \left[ \begin{array}{c} 0 \\ 0 \\ \omega_2 \end{array} \right]$$

Velocity of C

$$\vec{v}_C = \dot{\vec{r}}_C = \frac{d\vec{r}_C}{dt} \tag{2.7}$$

#### Velocity of D

$$\vec{v}_D = \dot{\vec{r}}_D = \frac{d\vec{r}_D}{dt} = \vec{v}_C + \vec{\omega}_4 \times (\vec{r}_D - \vec{r}_C)$$
 (2.8)

From equation (2.8), we solve analytically for  $\vec{\omega}_4$ 

$$\vec{\omega}_4 = \left[ \begin{array}{c} 0 \\ 0 \\ \omega_4 \end{array} \right]$$

Using MATLAB® to plot the velocity graph of the mechanism in figure 2.6 [2].

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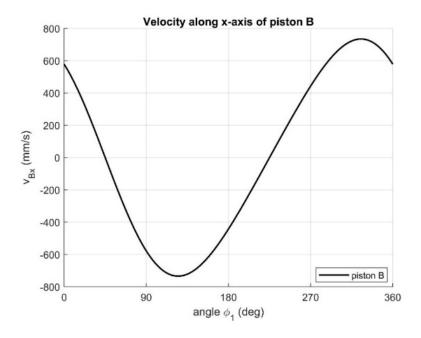


Figure 2.6: Velocity of link 3

#### 2.5.2 Acceleration analysis

Acceleration of A

$$\vec{a}_A = \dot{\vec{v}}_A = \frac{d\vec{v}_A}{dt} \tag{2.9}$$

where  $\phi = \widehat{xOA}$ 

**Acceleration of** *B* 

$$\vec{a}_B = \dot{\vec{v}}_B = \frac{d\vec{v}_B}{dt}$$

$$\vec{\alpha}_2 = \frac{d\vec{\omega}_2}{dt}$$
(2.10)

Acceleration of C

$$\vec{a}_C = \dot{\vec{v}}_C = \frac{d\vec{v}_C}{dt} \tag{2.11}$$

Acceleration of D

$$\vec{a}_D = \dot{\vec{v}}_D = \frac{d\vec{v}_D}{dt}$$

$$\vec{\alpha}_4 = \frac{d\vec{\omega}_4}{dt}$$
(2.12)

Using MATLAB® to plot the acceleration graph of the mechanism in figures 2.7

### 2.6 Force analysis

To find the reaction forces, we separate the links and solve the D'Alembert equations analytically. Position and acceleration equations of the links, located at their centers of gravity:

$$\vec{r}_{S1} = \vec{0}, \vec{r}_{S2} = \frac{\vec{r}_A + \vec{r}_B}{2}, \vec{r}_{S4} = \frac{\vec{r}_D + \vec{r}_C}{2}$$
 (2.13)

2.6 Force analysis

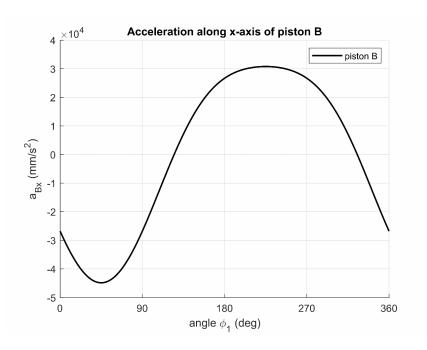


Figure 2.7: Acceleration of link 3

$$\vec{a}_{S1} = \vec{0}, \vec{a}_{S2} = \frac{\vec{a}_A + \vec{a}_B}{2}, \vec{a}_{S4} = \frac{\vec{a}_D + \vec{a}_C}{2}$$
 (2.14)

The equations for 5 links are systemized as follows:

Link 5

$$\begin{cases}
\vec{Q}_5 + \vec{F}_{45} + \vec{P}_D + \vec{R}_{05} &= m_5 \vec{a}_5 \\
|\vec{R}_{05x}| &= |\vec{R}_{05y}|
\end{cases} (\vec{a}_5 = \vec{a}_D) \tag{2.15}$$

Link 4

$$\begin{cases}
\vec{Q}_4 + \vec{F}_{24} + \vec{F}_{54} &= m_4 \vec{a}_{S4} & (\vec{F}_{54} = -\vec{F}_{45}) \\
(\vec{r}_D - \vec{r}_{S4}) \times \vec{F}_{54} + (\vec{r}_C - \vec{r}_{S4}) \times \vec{F}_{24} &= J_{S4} \vec{\alpha}_4
\end{cases}$$
(2.16)

Link 3

$$\begin{cases}
\vec{Q}_3 + \vec{F}_{23} + \vec{P}_B + \vec{R}_{03} &= m_3 \vec{a}_3 \\
|\vec{R}_{03x}| &= -|\vec{R}_{03y}|
\end{cases}$$
(2.17)

Link 2

$$\begin{cases}
\vec{Q}_2 + \vec{F}_{12} + \vec{F}_{42} &= m_2 \vec{a}_{S2} \\
(\vec{r}_C - \vec{r}_{S2}) \times \vec{F}_{42} + (\vec{r}_B - \vec{r}_{S2}) \times \vec{F}_{32} + (\vec{r}_A - \vec{r}_{S2}) \times \vec{F}_{12} &= J_{S2} \vec{\alpha}_2
\end{cases} (2.18)$$

where  $\vec{F}_{42} = -\vec{F}_{24}$ ,  $\vec{F}_{32} = -\vec{F}_{23}$ 

Link 1

$$\begin{cases} \vec{Q}_1 + \vec{F}_{21} + \vec{R}_{01} &= m_1 \vec{a}_{S1} \\ \vec{r}_A \times \vec{F}_{21} + \vec{M}_{cb} &= 0 \end{cases}$$
 (2.19)

Solving for system of equations from (2.13) to (2.19) by rearranging them into matrix form, we obtain  $\vec{F}_{45}$ ,  $\vec{R}_{05}$ ,  $\vec{F}_{24}$ ,  $\vec{F}_{23}$ ,  $\vec{F}_{12}$ ,  $\vec{R}_{01}$ ,  $\vec{R}_{02}$ . Using MATLAB® to plot the reaction force  $\vec{F}_{23}$ ,  $\vec{R}_{03}$  of the mechanism in figures 2.9 and 2.10

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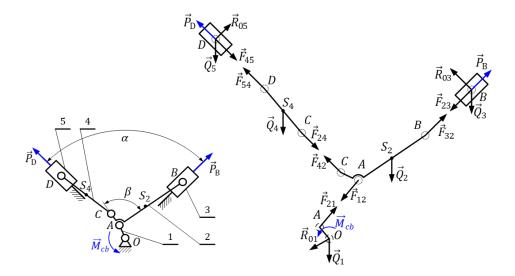


Figure 2.8: Force analysis of the mechanism

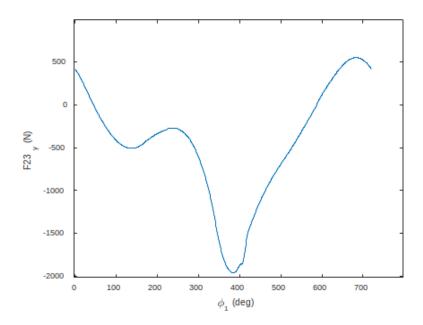


Figure 2.9: Reaction force  $\vec{F}_{23}$  along y axis

2.6 Force analysis

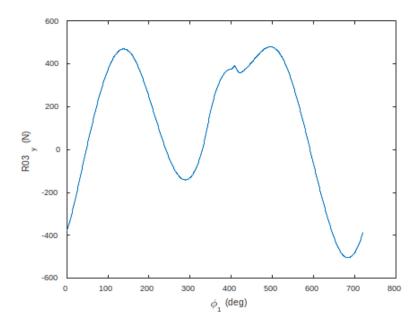


Figure 2.10: Reaction force  $\vec{R}_{03}$  along y axis

2 Internship tasks

### 2.7 Energy relation analysis

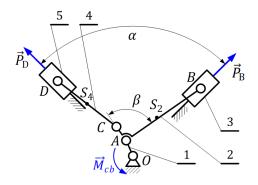


Figure 2.11: Pressure on both ends of the system

The energy relation of the machine must satisfy the condition such that the motion of the system is regulated after each cycle. To put it another way, the dynamic work is offset by the resistance work:

$$M_c(0) = M_d(0)$$
  
 $M_c(2\pi) = M_d(2\pi)$  (2.20)

Let us choose the driving link as the equivalent link of the system:  $\omega_{tt} = \omega_1$ .

#### 2.7.1 Find equivalent dynamic moment and dynamic work

From the displacement - pressure relation graph (figure 2.2), we convert it to the external force acting on the system  $F_B(\phi) = P_B(\phi)A$  in a cycle (each displacement data corresponds to a specific position and angle  $\phi(t)$  of the system).

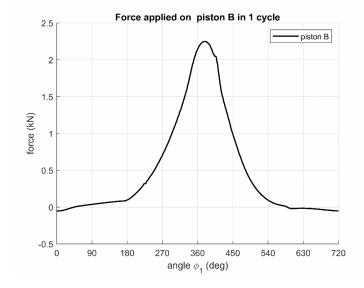


Figure 2.12: Force applied on piston 3 corresponding to angle of crankshaft 1

The equivalent dynamic moment on link 1 is calculated as:

$$M_d(\phi) = \frac{1}{\omega_1} \left( \vec{F}_B \cdot \vec{v}_B + \vec{Q}_2 \cdot \vec{v}_{S2} + \vec{Q}_4 \cdot \vec{v}_{S4} + \vec{Q}_3 \cdot \vec{v}_B + \vec{Q}_5 \cdot \vec{v}_D \right)$$
(2.21)

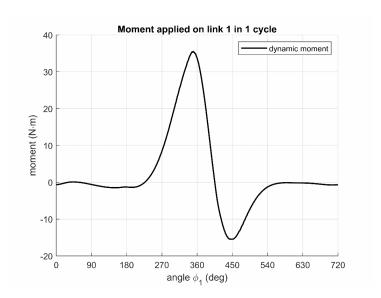


Figure 2.13: Equivalent dynamic moment applied on crankshaft 1

From the moment, we integrate to obtain the dynamic work:

$$A_d(\phi) = \int_{\phi_i}^{\phi_f} M_d d\phi \tag{2.22}$$

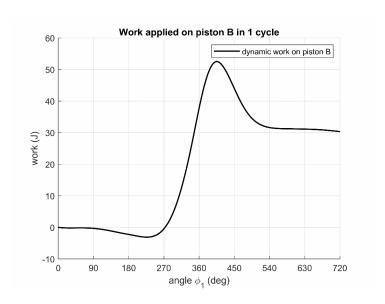


Figure 2.14: Dynamic work of the system in 1 cycle

#### 2.7.2 Find equivalent resistant moment and resistant work

From the displacement - pressure relation graph (figure 2.3), we convert it to the external force acting on the system  $F_D(\phi) = P_D(\phi)A$  in a cycle (each displacement data corresponds to a specific position and angle  $\phi(t)$  of the system).

The equivalent resistant moment on link 1 is calculated as:

$$M_c(\phi) = \frac{1}{\omega_1} \vec{F}_D \cdot \vec{v}_D \tag{2.23}$$

2 Internship tasks

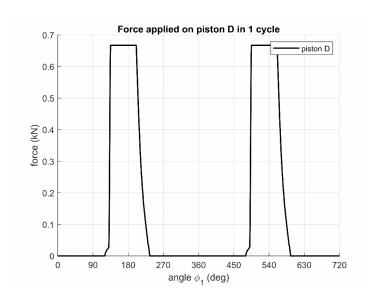


Figure 2.15: Force applied on piston 3 corresponding to angle of crankshaft 1

From the moment, we integrate to obtain the resistant work:

$$A_c(\phi) = \int_{\phi_i}^{\phi_f} M_c d\phi \tag{2.24}$$

However, the value of  $M_c$  in equation 2.23 still does not satisfy condition (2.20). To compensate for this, we multiply the force  $F_D$  by a ratio  $\frac{A_d}{A_c}$  and recalculate  $M_c$ ,  $A_c$ :

$$F_{D,new}(\phi) = \frac{A_d}{A_c} F_D$$

$$M_{c,new}(\phi) = \frac{1}{\omega_1} \vec{F}_{D,new} \cdot \vec{v}_D$$

$$A_{c,new}(\phi) = \int_{\phi_i}^{\phi_f} M_{c,new} d\phi$$
(2.25)

We then obtain the figure of equivalent resistant moment and work:

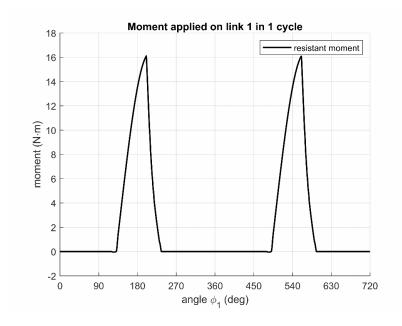


Figure 2.16: Equivalent resistant moment applied on crankshaft 1

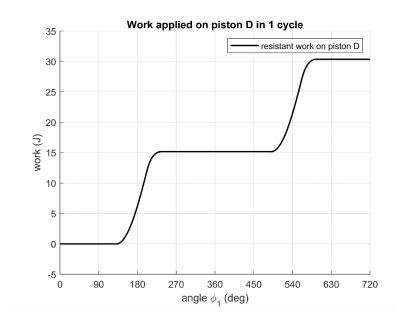


Figure 2.17: Resistant work of the system in 1 cycle

Combining the 2 figures 2.14 and 2.17, we obtain the works applied onto the system in 1 cycle:

### 2.8 Find the energy equation and calculate the flywheel weight

Since the crankshaft is chosen to be the equivalent link, we obtain the equivalent moment of inertia as follows:

$$J(\phi) = J_1 + J_2 \left(\frac{\omega_2}{\omega_1}\right)^2 + m_2 \left(\frac{v_{S2}}{\omega_1}\right)^2 + m_3 \left(\frac{v_B}{\omega_1}\right)^2 + J_4 \left(\frac{\omega_4}{\omega_1}\right)^2 + m_5 \left(\frac{v_D}{\omega_1}\right)^2$$
(2.26)

where  $m_k, \omega_k, v_k$  are the weight, rotational speed and instantaneous speed at point k respectively.

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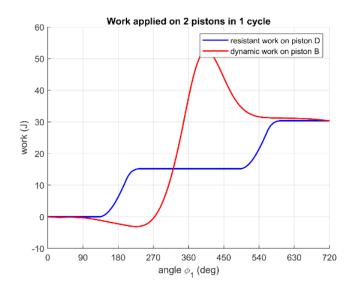


Figure 2.18: Resistant and dynamic moment of the system in 1 cycle

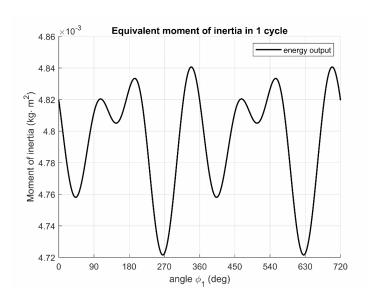


Figure 2.19: Equivalent moment of inertia of the system

Then, we calculate the total energy output of the system:

$$E(\phi) = \Delta E + E_0 = (A_c + A_d) + \frac{1}{2} J_0 \omega_1^2$$
 (2.27)

where  $\Delta E$  is the total equivalent work and  $J_0 = J(0)$ 

From the equivalent energy equation  $E(\phi)$  and moment of inertia  $J(\phi)$  we plot the graph of E(J)

From figure 2.21 we draw 2 tangent lines at the boundaries. Let the slope of the lower tangent line be  $\psi_{min}$  and the upper one be  $\psi_{max}$ . The slope of the lines at calculated numerically as follows:

$$\psi_{min} = \frac{\mu_E \omega_1^2}{2\mu_J} \left( 1 - \frac{[\delta]}{2} \right)^2$$

$$\psi_{max} = \frac{\mu_E \omega_1^2}{2\mu_J} \left( 1 + \frac{[\delta]}{2} \right)^2$$
(2.28)

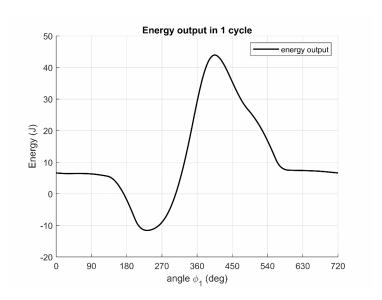


Figure 2.20: Energy output of the system in 1 cycle

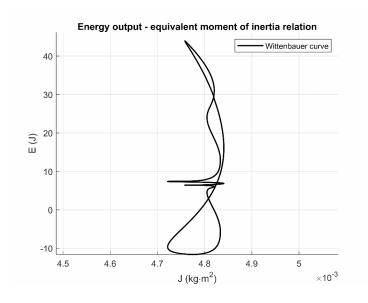


Figure 2.21: Equivalent moment of inertia - energy output relations

where

 $[\delta] = 1/80$  is given above

 $\mu_E = \mu_J = 1$  are the scale of the figure (MATLAB® or similar programs always understands these values as 1)

The lines cross the ordinate E(J) at a, b respectively. We then derive the equations describing these lines and draw them in figure 2.21:

$$y_{min} = \psi_{min}x + a$$
  

$$y_{max} = \psi_{max}x + b$$
(2.29)

Calculating the moment of inertia of the flywheel using:

$$J_d = \frac{\mu_J ab}{\psi_{max} - \psi_{min}} \tag{2.30}$$

Programming with MATLAB®, we estimate  $J_d = 1.63 \text{ kg} \cdot \text{m}^2$ . Assuming the cross section area is  $100 \text{ cm}^2$ , the weight of the flywheel will be about 16.3 g.

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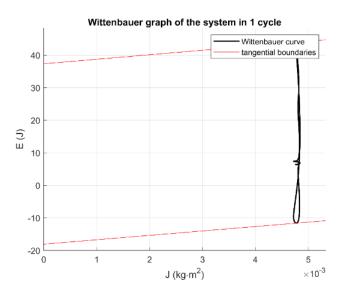


Figure 2.22: Wittenbauer curve with tangent boundaries

## 2.9 Combining motion of the system

From the given parameters, we derive the following table:

Van xả B	an xả B ĐÓNG MỞ					ĐÓNG					
Cam hút B		9	$ ho_{g\grave{a}n}$				$arphi_{ exttt{d}i+xa+v\grave{e}}$			$arphi_{g  ext{ \^{a}}n}$	
Van hút B		Đ	ÓN	NG			ΜỞ			ÐÓNG	
Piston B	NŐ	j		XÅ	HÚT		NÉN	NÉN			
Khâu dẫn	101.55 μ	40		281.55		25 36	461.55	48	0 25	641.55	720
Piston D			ΗÚ	jΤ	NÉN				HÚT		
Van hút D			I	MỞ	ÐÓ		ĐÓNG		ΜỞ		
Van xả D		·	:	ĐÓNG		ΜỞ			ĐÓNG		

Figure 2.23: Timing chart of the system

#### 2.10 Cam mechanism

#### 2.10.1 Tasks

- Modeling 4 cams for 4 valves, 2 of which are intake-outtake of the combustion end, and the remaining are for the compression end.
- The intake cams are identical.
- The outtake cams are identical.

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#### 2.10.2 Cam profile determination

For combustion ends, we will find the rise, dwell, fall of the motion:

$$\phi_{rise,comb} + \phi_{dwell,comb} + \phi_{fall,comb} = \frac{230^{\circ}}{2} = 115^{\circ}$$

$$\Rightarrow \begin{cases} \phi_{rise,comb} = 55^{\circ} \\ \phi_{dwell,comb} = 5^{\circ} \\ \phi_{fall,comb} = 55^{\circ} \end{cases}$$

Knowing the angles of each interval and the form of acceleration (modified trapezoidal), we can integrate to find velocity and displacement of the cam follower. For vibration safety, jerk is included using derivative with respect to  $\phi(t)$ 

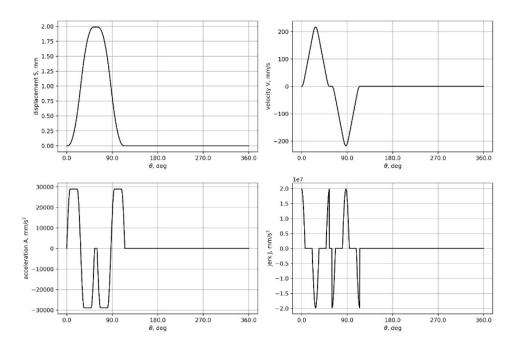


Figure 2.24: Displacement, velocity, acceleration and jerk of the cam follower

For flat faced follower, the pressure angle is constant. This leads to the condition of convex cam profile  $R_0 + Y + \frac{dY^2}{d\phi} > 0$  or:

$$R_0 > h_{max} \tag{2.31}$$

where  $h_{max}$  is the minimum value of the sum  $Y + \frac{dY^2}{d\phi}$ .

From the figure,  $h_{max} = 9.096$  mm. Then, arbitrarily choose  $R_0 = 12$  mm to satisfy the condition (2.31).

From the pressure angle  $\alpha_2 = 6^\circ$ , we use superposition to create an equivalent cam profile, namely  $Y = Y \cos \alpha_2$ . Then, apply the following formula to find cam profile:

$$\begin{cases} u = (R_0 + Y)\sin\phi + Y'\cos\phi \\ v = (R_0 + Y)\cos\phi - Y'\sin\phi \end{cases}$$
 (2.32)

where  $\phi(t) = \widehat{xOA}$ ; u, v are the position of cam along x, y-axes respectively; Y, Y' are the displacement and velocity of the cam follower as shown in figure 2.24.

Using MATLAB®, we plot the cam profile numerically. Applying this process to the compression end, we also plot the cam profile in figure 2.28:

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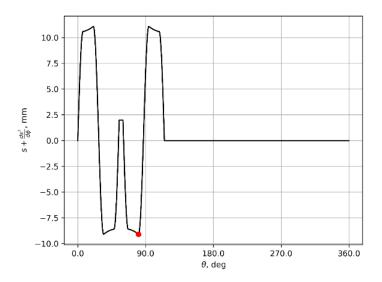


Figure 2.25: Displacement - acceleration diagram of the cam

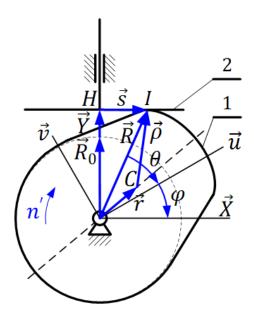


Figure 2.26: Position vectors of the cam

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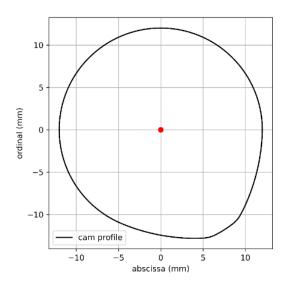


Figure 2.27: Cam profile of the combustion end

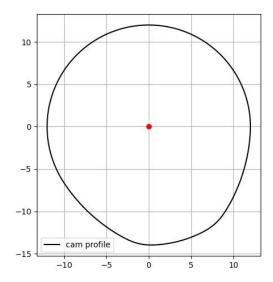


Figure 2.28: Cam profile of the compression end

# **Chapter 3**

# **Summary and Conclusions**

During the internship, I had a chance to get acquainted with a new working environment. I have accumulated experience in industry knowledge as well as experience skills above.

I was trained in problem solving skills in many stages, trying to complete the job in the shortest time, boldly exchanging and sharing knowledge. At the same time, it also fosters a lot of knowledge about graphic software as well as programming skills to solve the problems learned in school but professionally and saves more time.

Shortcomings: the skill is not mature which still takes a long time to execute; the ability to think and propose design plans is limited due to the lack of practical experience and in-depth knowledge.

Solution: practice more software skills, add additional specialized knowledge that is lacking.

# **Bibliography**

- [1] Khac Liem Lai. Huong dan thiet ke mon hoc nguyen ly may. Service Education School HCMC, 1984.
- [2] Dan B Marghitu. Mechanisms and robots analysis with MATLAB. Dordrecht Springer, 2009.