Notes on Mutect2

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I. MUTECT2

Here we describe the command-line program `Mutect2` itself, which takes us from aligned reads to unfiltered, annotated variant calls. Code block 1 shows how to invoke `Mutect2` using the gatk launch script.

Listing 1: Mutect2 command

```
gatk Mutect2 -R reference.fasta \
   -L intervals.interval_list \
   -I tumor1.bam \
   # Mutect2 may input more tumor samples from the same individual
   [-I tumor2.bam -I tumor3.bam . . .]  \
   # Mutect may input matched normals from the same individual
   [-I normal1.bam -I normal2.bam . . .]  \
   -O unfiltered.vcf
```

A. Additional modes

The command above encompasses tumor-only, tumor-normal, and multiple-tumor somatic variant calling.

B. Finding Active Regions

`Mutect2` triages sites based on their pileup at a single base locus. If there is sufficient evidence of variation `Mutect2` proceeds with local reassembly and realignment. As in the downstream parts of `Mutect2` we seek a likelihood ratio between the existence and non-existence of an alt allele. Instead of obtaining read likelihoods via Pair-HMM, we assign each base a likelihood. For substitutions we can simply use the base quality. For indels we assign a heuristic effective quality that increases with length. Supposing we have an effective quality for each element in the read pileup we can now estimate the likelihoods of no variation and of a true alt allele with allele fraction f. Let $\mathcal{R}$ and $\mathcal{A}$ denote the sets of ref and alt reads. The likelihood of no variation is the likelihood that every alt read was in error. Letting ϵ_i be the error probability of pileup element i we have:

$$L(\text{no variation}) = \prod_{i \in \mathcal{R}} (1 - \epsilon_i) \prod_{j \in \mathcal{A}} \epsilon_j \approx \prod_{j \in \mathcal{A}} \epsilon_j \tag{1}$$

$$L(f) = \prod_{i \in \mathcal{R}} [(1-f)(1-\epsilon_i) + f\epsilon_i] \prod_{j \in \mathcal{A}} [f(1-\epsilon_j) + (1-f)\epsilon_j] \approx (1-f)^{N_{\text{ref}}} \prod_{j \in \mathcal{A}} [f(1-\epsilon_j) + (1-f)\epsilon_j], \tag{2}$$

where the approximations amount to giving ref reads infinite quality, which speeds the computation, and we let $N_{\text{ref}} = |\mathcal{R}|$. This is equivalent to the following model in which we give the nth alt read a latent indicator z_j which equals 1 when the read is an error:

$$P(\text{reads}, f, \mathbf{z}) = (1-f)^{N_{\text{ref}}} \prod_{n=1}^{N_{\text{alt}}} [(1-f)\epsilon_n]^{z_n} [f(1-\epsilon_n)]^{1-z_n} \tag{3}$$

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We approximate the model evidence $L(f) = \sum_{\mathbf{z}} \int df P(\text{reads}, f, \mathbf{z})$ via a mean field variational Bayes approximation in which we factorize the full data likelihood as $P(\text{reads}, f, \mathbf{z}) \approx q(f)q(\mathbf{z}) = q(f) \prod_n q(z_n)$[1]. For simplicity and speed, we will not iteratively compute $q(f)$. Rather, we use the fact that z_n is almost always 0 to see, by inspection, that

$$q(f) \approx \text{Beta}(f|\alpha, \beta), \quad \alpha = N_{\text{alt}} + 1, \beta = N_{\text{ref}} + 1. \tag{4}$$

Here the "+1"s come from the pseudocounts of a flat prior on f. Then, following the usual recipe of averaging the log likelihood with respect to f and re-exponentiating, we find

$$q(z_n) = \text{Bernoulli}(z_n|\gamma_n), \quad \gamma_n = \frac{\rho \epsilon_n}{\rho \epsilon_n + \tau(1 - \epsilon_n)}, \tag{5}$$

where $\ln \rho \equiv E_{q(f)}\left[\ln(1 - f)\right] = \psi(\beta) - \psi(\alpha + \beta)$ and $\ln \tau \equiv E_{q(f)}\left[\ln f\right] = \psi(\alpha) - \psi(\alpha + \beta)$. Then, Equation 10.3 of Bishop gives us the variational lower bound on $L(f)$:

$$L(f) \approx E_q\left[\ln P(\text{reads}, f, \mathbf{z})\right] + \text{entropy}[q(f)] + \sum_n \text{entropy}[q(z_n)] \tag{6}$$

$$= H(\alpha, \beta) + N_{\text{ref}} \ln \rho + \sum_n \left[\gamma_n \ln(\rho \epsilon_n) + (1 - \gamma_n)\ln(\tau(1 - \epsilon_n)) + H(\gamma_n)\right], \tag{7}$$

where $H(\alpha, \beta)$ and $H(\gamma)$ are Beta and Bernoulli entropies. We summarize these steps in the following algorithm:

1: Record the base qualities, hence the error probabilities ϵ_n of each alt read.
2: $\alpha = N_{\text{alt}} + 1$, $\beta = N_{\text{ref}} + 1$
3: $\rho = \exp\left(\psi(\beta) - \psi(\alpha + \beta)\right)$, $\tau = \exp\left(\psi(\alpha) - \psi(\alpha + \beta)\right)$.
4: $\gamma_n = \rho \epsilon_n / \left[\rho \epsilon_n + \tau(1 - \epsilon_n)\right]$
5: $L(f) \approx H(\alpha, \beta) + N_{\text{ref}} \ln \rho + \sum_n \left[\gamma_n \ln(\rho \epsilon_n) + (1 - \gamma_n)\ln(\tau(1 - \epsilon_n)) + H(\gamma_n)\right]$

To get the log odds we subtract the log likelihood, $\sum_n \ln \epsilon_n$, from $L(f)$.

C. Local Assembly, Pair-HMM, and Realignment

These topics, which are common to `Mutect2` and HaplotypeCaller, are discussed in docs/local_assembly.pdf, docs/pair_hmm.pdf, and docs/variants_from_haplotypes.pdf in the gatk git repository. As a black box, whenever the evidence in the previous section suffices to trigger local assembly and realignment, we end up at each candidate variant site with one read-vs-allele log likelihood matrix ℓ for each sample, where ℓ_{ra} is the log probability of sequencing read r given its base qualities and given that read r is derived from a molecule exhibiting allele a. [2]

D. Somatic Likelihoods Model

We have a set of potential somatic alleles and read-allele likelihoods $\ell_{ra} \equiv P(\text{read } r | \text{allele } a)$. We don't know which alleles are real somatic alleles and so we must compute, for each subset $\mathbb{A}$ of alleles, the likelihood that the reads come from $\mathbb{A}$. A simple model for this likelihood is as follows: each read r is associated with a latent indicator vector $\mathbf{z}_r$ with one-hot encoding $z_{ra} = 1$ iff read r came from allele $a \in \mathbb{A}$. The conditional probabilities of reads given alleles is ℓ_{ra}. There is a latent vector $\mathbf{f}$ of allele fractions such that f_a is the allele fraction of allele a, that is, the prior probability that any given read comes from allele a. Giving $\mathbf{f}$ a Dirichlet prior, we have a full-model likelihood

$$P(\mathbb{R}, \mathbf{z}, \mathbf{f}|\mathbb{A}) = P(\mathbf{f})P(\mathbf{z}|\mathbf{f})P(\mathbb{R}|\mathbf{z}, \mathbb{A}) = \text{Dir}(\mathbf{f}|\boldsymbol{\alpha}) \prod_a \prod_r (f_a \ell_{ra})^{z_{ra}}. \tag{8}$$

We want to marginalize the latent variables to obtain the evidence $P(\mathbb{R}|\mathbb{A})$, which we make tractable via a mean-field approximation $P(\mathbb{R}, \mathbf{z}, \mathbf{f}|\mathbb{A}) \approx q(\mathbf{z})q(\mathbf{f})$, which is exact in two limits. First, if there are many reads, each allele is

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[1] The latter step is an induced factorization – once f and $\mathbf{z}$ are decoupled, then the different z_n become independent as well.

[2] Technically, pair-HMM produces a read-vs-*haplotype* likelihood matrix, which is then "marginalized" to produce a set of read-vs-allele likelihood matrices. In the future, `Mutect2` may operate directly on this read-vs-haplotype matrix in order to exploit the biological fact that there are only a few haplotypes in any region.

associated with many reads and therefore the Law of Large Numbers causes $\mathbf{f}$ and $\mathbf{z}$ to become uncorrelated. Second, if the allele assignments of reads are obvious $\mathbf{z}_r$ is effectively determinate, hence uncorrelated with $\mathbf{f}$. In the variational Bayesian mean-field formalism we have

$$q(\mathbf{f}) \propto E_{q(\mathbf{z})}\left[P(\mathbb{R}, \mathbf{z}, \mathbf{f}|\mathbb{A})\right] \propto \mathrm{Dir}(\mathbf{f}|\boldsymbol{\alpha} + \sum_r \bar{\mathbf{z}}_r) \equiv \mathrm{Dir}(\mathbf{f}|\boldsymbol{\beta}), \quad \boldsymbol{\beta} = \boldsymbol{\alpha} + \sum_r \bar{\mathbf{z}}_r \tag{9}$$

$$q(\mathbf{z}_r) \propto E_{q(\mathbf{f})}\left[P(\mathbb{R}, \mathbf{z}, \mathbf{f}|\mathbb{A})\right] \propto \prod_a \left(\tilde{f}_a \ell_{ra}\right)^{z_{ra}}, \tag{10}$$

where, with ψ denoting the digamma function, the moments

$$\bar{z}_{ra} = E_{q(\mathbf{z})}\left[z_{ra}\right] = \frac{\tilde{f}_a \ell_{ra}}{\sum_{a'} \tilde{f}_{a'} \ell_{ra'}} \tag{11}$$

$$\ln \tilde{f}_a = E_{q(\mathbf{f})}[\ln f_a] = \psi(\beta_a) - \psi(\sum_{a'} \beta_{a'}) \tag{12}$$

are easily obtained from the categorical distribution $q(\mathbf{z})$ and the Dirichlet distribution $q(\mathbf{f})$[3] We initialize $\bar{z}_{ra} = 1$ if a is the most likely allele for read r, 0 otherwise and iterate Equations 9 and 10 until convergence. Having obtained the mean fields of $q(\mathbf{z})$ and $q(\mathbf{f})$, we use the variational approximation (Bishop's Eq 10.3) to the model evidence:

$$\ln P(\mathbb{R}|\mathbb{A}) \approx E_q\left[\ln P(\mathbb{R}, \mathbf{z}, \mathbf{f}|\mathbb{A})\right] - E_q\left[\ln q(\mathbf{z})\right] - E_q\left[\ln q(\mathbf{f})\right]. \tag{13}$$

The terms in Eq 13 all involve the standard moments mentioned above, so after a bit of algebraic cancellation we obtain

$$\ln P(\mathbb{R}|\mathbb{A}) \approx g(\boldsymbol{\alpha}) - g(\boldsymbol{\beta}) + \sum_{ra} \bar{z}_{ra} \left(\ln \ell_{ra} - \ln \bar{z}_{ra}\right), \tag{14}$$

where we define g to be the Dirichlet distribution log normalization:

$$\ln \Gamma(\sum_a \omega_a) - \sum_a \ln \Gamma(\omega_a). \tag{15}$$

We now have the model evidence for allele subset $\mathbb{A}$. This lets us choose which alleles are true somatic variants. It also lets us make calls on somatic loss of heterozygosity events. Furthermore, instead of reporting max-likelihood allele fractions as before, we may emit the parameters of the Dirichlet posterior $q(\mathbf{f})$, which encode both the maximum likelihood allele fractions and their uncertainty.

II. FILTERING

Here we describe the command line tool FilterMutectCalls

A. Filtering Architecture

1. Filtering False Discovery Rate

Let $p_1 \leq p_2 \leq ... \leq p_n$ denote ordered posterior probabilities that given variants are sequencing artifacts. Suppose we filter variants for which $p_i > p_j$ for some index j; that is, we keep the first j variants as PASS and filter the rest. Then the expected number of false positives is

$$\mathbb{E}[\mathrm{FP}(j)] = \sum_{i=1}^{j} p_i \tag{16}$$

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[3] Note that we didn't *impose* this in any way. It simply falls out of the mean field equations.
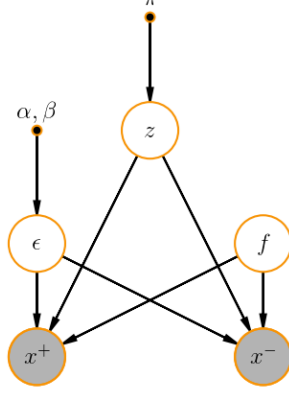
FIG. 1: The probabilistic graphical model for the strand artifact model

And the expected false positive rate is

$$\mathbb{E}[\text{FPR}(j)] = \frac{1}{j}\sum_{i=1}^{j} p_i \tag{17}$$

We choose the threshold so as to maximize the number of variants to let through while keeping the false positive rate below $\delta \in [0, 1]$. In other words, we solve for

$$j^* = \text{argmax}_j \mathbb{E}[\text{FPR}(j)] = \frac{1}{j}\sum_{i=1}^{j} p_i \tag{18}$$

under the constraint $\mathbb{E}[\text{FPR}(j)] < \delta$. We can prove by induction that $\mathbb{E}[\text{FPR}(j)]$ is monotonically increasing in j. Thus we test $\mathbb{E}[\text{FPR}(j)]$ for $j = 1, \cdots, k$, where k is the smallest integer such that $\mathbb{E}[\text{FPR}(\text{k})] > \delta$, and set $j^* = k-1$.

B. Hard Filters

C. Strand Artifact Model

The strand artifact filter detects sequencing artifacts in which the evidence for the alt allele consists entirely of forward strand reads alone or reverse strand reads alone. We must detect this while taking into account the fact that at some loci, such as near the end of an exome target, *all* reads are biased towards one direction, and therefore a bias towards a particular strand among alt reads is no cause for alarm.

Let $z \in \{z_+, z_-, z_o\}$ be a latent random variable with 1-hot encoding that represents the artifact state of a suspected variant i.e. $z_+ = 1$ for a forward strand artifact, $z_- = 1$ for a reverse artifact, and $z_o = 1$ otherwise. At each locus, let $a_\pm$ be the number of forward $(+)$ or reverse $(-)$ strand alt reads and let $n_\pm$ be the total depth for each strand. By modeling $a+_\pm$ relative to $n_\pm$ we account for inherent strand bias due to, for example, reads falling at the end of an exome target and do not confuse it for an artifact. Let f be the allele fraction of true variation in case $z_o = 1$. Let ϵ be the strand bias error rate and let θ be the non-strand-biased error rate. We will ignore the case in which significant strand bias coincides with real variation, first because this is exceedingly rare and ignoring it has a negligible effect on the parameters of our model, and secondly because such variants should be considered true positives.

The conditional distributions of our model are binomial

$$a_+|\epsilon, \theta, f, z_+ = 1 \sim \text{Bin}(a_+|n_+, \epsilon) \tag{19}$$
$$a_+|\epsilon, \theta, f, z_- = 1 \sim \text{Bin}(a_+|n_+, \theta) \tag{20}$$
$$a_+|\epsilon, \theta, f, z_o = 1 \sim \text{Bin}(a_+|n_+, f), \tag{21}$$

and similarly for a_-. Putting beta priors on ϵ, θ, and f, with parameters $(\alpha_\epsilon, \beta_\epsilon)$, $(\alpha_\theta, \beta_\theta)$, and (α_f, β_f) and marginalizing latent parameters we obtain likelihoods

$$P(a_+, a_-|z_\pm = 1) = \text{BetaBinom}(a_\pm|n_\pm, \alpha_\epsilon, \beta_\epsilon)\text{BetaBinom}(a_\mp|n_\mp, \alpha_\theta, \beta_\theta) \tag{22}$$

$$P(a_+, a_-|z_o = 1) = \int_0^1 \text{Beta}(f|\alpha_f, \beta_f)\text{Binom}(a_+|n_+, f)\text{Binom}(a_-|n_-, f) \tag{23}$$

$$= \frac{\binom{n_+}{a_+}\binom{n_-}{a_-}}{\binom{n_+ + n_-}{a_+ + a_-}}\text{BetaBinom}(a_+ + a_-|n_+ + n_-, \alpha_f, \beta_f) \tag{24}$$

Finally, we let $\pi/2$ be the prior probability of a forward or reverse strand artifact. From the above equations it is straightforward to calculate the posterior probability of z and to learn π iteratively via the EM algorithm. It is somewhat more complicated to learn $(\alpha_\epsilon, \beta_\epsilon)$ and $(\alpha_\theta, \beta_\theta)$, so we treat these as fixed hyperparameters. We use a flat prior $\alpha_f = \beta_f = 1$ for the true allele fraction.

D. Germline Filter

Suppose we have detected an allele such that its (somatic) likelihood in the tumor is ℓ_t and its (diploid) likelihood in the normal is ℓ_n[4]. By convention, both of these are relative to a likelihood of 1 for the allele *not* to be found. If we have no matched normal, $\ell_n = 1$. Suppose we also have the population allele frequency f of this allele. Then the prior probabilities for the normal to be heterozygous and homozygous alt for the allele are $2f(1 - f)$ and f^2 and the prior probability for the normal genotype not to contain the allele is $(1 - f)^2$. Finally, suppose that the prior for this allele to arise as a somatic variant is π.

We can determine the posterior probability that the variant exists in the normal genotype by calculating the unnormalized probabilities of four possibilities:

1. The variant exists in the tumor and the normal as a germline het. This has unnormalized probability $2f(1 - f)\ell_n\ell_t(1 - \pi)$.

2. The variant exists in the tumor and the normal as a germline hom alt. This has unnormalized probability $f^2\ell_n\ell_t(1 - \pi)$.

3. The variant exists in the tumor but not the normal. This has unnormalized probability $(1 - f)^2\ell_t\pi$.

We exclude possibilities in which the variant does not exist in the tumor sample because we really want the conditional probability that the variant is germline given that it would otherwise be called.

Normalizing, we obtain the following posterior probability that an allele is a germline variant:

$$P(\text{germline}) = \frac{(1) + (2)}{(1) + (2) + (3)} = \frac{\left(2f(1 - f) + f^2\right)\ell_n\ell_t(1 - \pi)}{\left(2f(1 - f) + f^2\right)\ell_n\ell_t(1 - \pi) + \ell_t(1 - f)^2\pi}. \tag{25}$$

The above equation, in which the factors of ℓ_t could cancel if we wished, is not quite right. The tumor likelihood ℓ_t is the probability of the tumor data given that the allele exists in the tumor *as a somatic variant*. If the allele is in the tumor as a germline het we must modify ℓ_t to account for the fact that the allele fraction is determined by the ploidy – it must be either f_g or $1 - f_g$ with equal probability, where f_g is the minor allele fraction of germline hets. It would be awkward to recalculate the tumor likelihood with the allele frequency constrained to these two values[5], but we can estimate a correction factor as follows: assuming that the posterior on the allele fraction in the somatic likelihoods model is fairly tight, the likelihood of a alt reads out of n total reads is $\binom{n}{a}(1 - f_t)^{n-a}f^a$, where f_t is the tumor alt allele fraction. That is, our sophisticated model that marginalizes over f_t reduces to something more naive. If the variant is a germline event, the likelihood becomes $\frac{1}{2}\binom{n}{a}\left[(1 - f_g)^{n-a}f_g^a + f_g^{n-a}(1 - f_g)^a\right]$. Thus, in case (1) we have $\ell_t \rightarrow \chi\ell_t$, where

$$\chi = \frac{1}{2}\frac{(1 - f_g)^{n-a}f_g^a + f_g^{n-a}(1 - f_g)^a}{(1 - f_t)^{n-a}f_t^a}. \tag{26}$$

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[4] This is the total likelihood for het and hom alt in the normal.
[5] The model could easily accommodate this change, but the likelihoods are long gone from memory once the germline computation occurs.

For germline hom alts, both the tumor and normal allele fractions will be similarly large, so to decent approximation we don't have to modify ℓ_t. Of course, this only applies if the allele fraction is large. Rather than try to model the count of ref reads within a germline hom alt site, we simply set a threshold of allele fraction 0.9, so that in case (2) $\ell_t \to \mathrm{I}[f_t > 0.9]\ell_t$. and the corrected germline probability is

$$P(\text{germline}) = \frac{(1) + (2)}{(1) + (2) + (3)} = \frac{\left(2f(1-f)\chi + \mathrm{I}[f_t > 0.9]f^2\right)\ell_n(1-\pi)}{\left(2f(1-f)\chi + \mathrm{I}[f_t > 0.9]f^2\right)\ell_n(1-\pi) + (1-f)^2\pi}. \tag{27}$$

To filter, we set a threshold on this posterior probability.

So far we have assumed that the population allele frequency f is known, which is the case if it is found in our germline resource, such as gnomAD. If f is not known we must make a reasonable guess as follows. Suppose the prior distribution on f is $\mathrm{Beta}(\alpha, \beta)$. The mean $\alpha/(\alpha+\beta)$ of this prior is the average human heterozygosity $\theta \approx 10^{-3}$, so we have $\beta \approx \alpha/\theta$. We need one more constraint to determine α and β, and since we are concerned with imputing f when f is small we use a condition based on rare variants. Specifically, the number of variant alleles n at some site in a germline resource with $N/2$ samples, hence N chromosomes, is given by $f \sim \mathrm{Beta}(\alpha, \beta), n \sim \mathrm{Binom}(N, f)$. That is, $n \sim \mathrm{BetaBinom}(\alpha, \beta, N)$. The probability of a site being non-variant in every sample is then $P(n = 0) = \mathrm{BetaBinom}(0|\alpha, \beta, N)$, which we equate to the empirical proportion of non-variant sites in our resource, about $7/8$ for exonic sites in gnomAD. Solving, we obtain approximately $\alpha = 0.01, \beta = 10$ for gnomAD. Now, given that some allele found by `Mutect2` is not in the resource, the posterior on f is $\mathrm{Beta}(\alpha, \beta + N)$, the mean of which is, since $\beta << N$, about α/N. By default, `Mutect2` uses this value.

E. Contamination Filter

Suppose our tumor bam has contamination fraction α and that at some site we have a alt reads out of d total reads. Suppose further that the alt allele has population allele frequency f. We will compute a simple estimate of the posterior probability that these alt reads came from a contaminating sample and not from a true somatic variant. Let π be the prior probability of somatic variation as above. Our crude model for the alt count distribution of somatic variation is a uniform distribution. That is, we assume that any value of a from 0 to d is equally likely. Then the likelihood of the data given a true somatic variant is

$$P(a|\text{somatic}) = \frac{1}{d+1}. \tag{28}$$

We consider two models of contamination. If there are multiple contaminants we approximate each contaminant read as independent. Then the probability of any given read being an alt contaminant read is αf, so we have

$$P(a|\text{many contaminant}) = \mathrm{Binom}(a|d, \alpha f). \tag{29}$$

If there is a single contaminating sample it is heterozygous with probability $2f(1-f)$ and homozygous for the alt with probability f^2, in which cases fractions $\alpha/2$ and α of all reads to be alt contaminants. The contaminant is homozygous for the ref with probability $(1-f)^2$, which yields no alt reads. Thus

$$P(a|\text{one contaminant}) = 2f(1-f)\mathrm{Binom}(a|d, \alpha/2) + f^2\mathrm{Binom}(a|d, \alpha) + (1-f)^2\mathrm{I}[a = 0]. \tag{30}$$

We take the likelihood $P(a|\text{contamination})$ to be the maximum of these, which admittedly is not quite rigorous. Usually one will be overwhelmingly larger than the other, however, so it's a decent approximation. Our posterior probability of contamination is then

$$P(\text{contamination}|a) = \frac{P(a, \text{contamination})}{P(a, \text{contamination}) + P(a, \text{somatic})} = \frac{(1-\pi)P(a|\text{contamination})}{(1-\pi)P(a|\text{contamination}) + \pi P(a|\text{somatic})} \tag{31}$$

We filter by setting a threshold on this posterior probability.

F. Summary of Mutect2 filters

`Mutect2` emits candidate variants with a set of annotations. After that `FilterMutectCalls` produces filtered calls by subjecting these variants to a series of hard filters that reject sites if some annotation is out of an allowable range. Here are the command line arguments that control these filters, along with the annotations they relate to.

- `tumor-lod` is the minimum likelihood of an allele as determined by the somatic likelihoods model required to pass.

- `max-events-in-region` is the maximum allowable number of called variants co-occurring in a single assembly region. If the number of called variants exceeds this they will all be filtered.

- `unique-alt-read-count` is the minimum number of unique (start position, fragment length) pairs required to make a call. This count is a proxy for the number of unique molecules (as opposed to PCR duplicates) supporting an allele. Normally PCR duplicates are marked and filtered by the GATK engine, but in UMI-aware calling this may not be the case, hence the need for this filter.

- `max-alt-allele-count` is the maximum allowable number of alt alleles at a site. By default only biallelic variants pass the filter.

- `max-germline-posterior` is the maximum posterior probability, as determined by the above germline probability model, that a variant is a germline event.

- `normal-artifact-lod` is the maximum acceptable likelihood of an allele in the normal *by the somatic likelihoods model*. This is different from the normal likelihood that goes into the germline model, which makes a diploid assumption. Here we compute the normal likelihood as if it were a tumor in order to detect artifacts.

- `max-strand-artifact-probability` is the posterior probability of a strand artifact, as determined by the model described above, required to apply the strand artifact filter. This is necessary but not sufficient – we also require the estimated max a posteriori allele fraction to be less than `min-strand-artifact-allele-fraction`. The second condition prevents filtering real variants that also have significant strand bias, i.e. a true variant that *also* has some artifactual reads.

- `min-median-base-quality` is the minimum median base quality of bases supporting a SNV.

- `min-median-mapping-quality` is the minimum median mapping quality of reads supporting an allele.

- `max-median-fragment-length-difference` is the maximum difference between the median fragment lengths reads supporting alt and reference alleles. Note that fragment length is based on where paired reads are mapped, not the actual physical fragment length.

- `min-median-read-position` is the minimum median length of bases supporting an allele from the closest end of the read. Indels positions are measured by the end farthest from the end of the read.

- If `FilterMutectCalls` is passed a `contamination-table` from `CalculateContamination` it will filter alleles with allele fraction less than the whole-bam contamination in the table[6].

Additionally, there are two unadjustable filters. the panel of normals filter removes all alleles at a site belonging to the panel of normals, which is a vcf of blacklisted artifact sites. It can be disabled by not passing a panel of normals to `Mutect2`. There is also an STR contraction filter which removes variants that are the deletion of a single repeat unit of an STR when this repeat unit contains more than one base. This filter can be disabled with the argument `-XA TandemRepeat` which turns off the `TandemRepeat` annotation.

Here for convenience is a table of `Mutect2` filters with their corresponding annotations specified by the `-A` argument[7], vcf keys for these annotations, and command line arguments controlling filtering thresholds.

III. READ ORIENTATION ARTIFACT FILTER

The read orientation artifact, also known as the orientation bias artifact, arises due to a chemical change in the nucleotide during library prep that results in, for example, G base-paring with A. This kind of artifact has a clear signature (e.g. C to A SNP that occurs predominantly for the middle C in the DNA sequence CCG), and it's single-stranded in nature. Downstream, this artifact manifests as low allele fraction SNPs whose evidence for the alt allele consists almost entirely F1R2 reads or F2R1 reads. A read pair is F1R2 (forward 1st, reverse 2nd) if the sequence of

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[6] This should be made more sophisticated by integrating the possibility of contamination into the germline model.

[7] Most of these are default annotations and do not need to be invoked explicitly.

Filter	Annotation	Key	Argument
t_lod	-	TLOD	tumor_lod
clustered_events	-	ECNT	max-events-in-region
duplicate_evidence	UniqueAltReadCount	UNIQ_ALT_READ_COUNT	unique-alt-read-count
multiallelic	-	-	max-alt-alleles-count
germline_risk	-	P_GERMLINE	max-germline-posterior
artifact_in_normal	-	N_ART_LOD	normal-artifact-lod
strand_artifact	StrandArtifact	SA_POST_PROB, SA_MAX_AF	max-strand-artifact-probability
base_quality	BaseQuality	MBQ	min-median-base-quality
mapping_quality	MappingQuality	MMQ	min-median-mapping-quality
fragment_length	FragmentLength	MFRL	max-median-fragment-length-difference
read_position	ReadPosition	MPOS	min-median-read-position
panel_of_normals	-	IN_PON	panel-of-normals
contamination	-	-	contamination-table
str_contraction	TandemRepeat	RU, RPA	-

bases in Read 1 maps to the forward strand of the reference (F1), and the sequence of Read 2 to the reverse strand of the reference (R2). F2R1 is defined similarly.

Without loss of generality, suppose that the reference context at locus i is ACT. Let $\mathbf{z}_i$ denote the genotype at locus i with the one-hot encoding $z_{ik} = 1$ iff the genotype of locus i is k, where the possible genotypes are

$$z_i \in \{\text{F1R2}_A, \text{F1R2}_G, \text{F1R2}_T, \text{F2R1}_A, \text{F2R1}_G, \text{F2R1}_T, \text{Hom Ref}, \text{Germline Het}, \text{Somatic Het}, \text{Hom Var}\}$$

$z_i = \text{F1R2}_A$ denotes that at locus i we have an artifact in which the evidence for alt allele A consists entirely of reads in the F1R2 orientation. The remaining artifact states are defined analogously. Let π denote the prior probabilities of the $\mathbf{z}_i$ under the reference context ACT. Then we have

$$P(\mathbf{z}_i) = \prod_k \pi_k^{z_{ik}} \tag{32}$$

The number of alt reads at a locus depends on the genotype z_i. Let n_i and m_i denote the total depth and alt depth at locus i, respectively. The conditional distribution of m_i is

$$P(m_i|z_{ik} = 1) = \text{BetaBinomial}(m_i|n_i, \alpha_k, \beta_k) \tag{33}$$

where α_k and β_k are fixed hyperparameters for genotype z_k. When the site's genotype indicates in m_i alt reads we expect a heavily skewed distribution of F1R2 reads. This is captured in the conditional distribution of F1R2 alt reads. Let c_i denote the number of F1R2 reads among the m_i alt reads at locus i. Then we have

$$P(c_i|m_i, z_{ik} = 1) = \text{BetaBinomial}(c_i|m_i, \alpha_k', \beta_k') \tag{34}$$

We learn the prior artifact probabilities π based on the observed values of n_i, m_i, c_i for each of N loci using the EM algorithm. In the E-step, we compute the posterior probabilities of $\mathbf{z}_i$ for $i = 1...N$. The joint probabilities of $\mathbf{z}$ factorizes over i, thus the posteriors over $\mathbf{z}$ are independent across loci.

$$P(z_{ik} = 1|m_i, c_i) \propto P(z_{ik} = 1, m_i, c_i) = \pi_k \text{BetaBinomial}(m_i|n_i, \alpha_k, \beta_k)\text{BetaBinomial}(c_i|m_i, \alpha_k', \beta_k') \tag{35}$$

In the M-step we maximize the expectation of the log complete-data likelihood with respect to π. The log complete data likelihood is given as

$$\ln P(\mathbf{z}, \mathbf{m}, \mathbf{c}) = \sum_i \sum_k z_{ik} \left(\ln \pi_k + \ln \text{BetaBinomial}(m_i|n_i, \alpha_k, \beta_k) + \ln \text{BetaBinomial}(c_i|m_i, \alpha_k', \beta_k') \right) \tag{36}$$

Maximizing the log likelihood under the constraint $\sum_k \pi_k = 1$ gives us

$$\pi_k = \frac{N_k}{N} \tag{37}$$

where $N_k = \sum_i P(z_{ik}|m_i, c_i)$ is the effective count of loci with genotype k. We alternate E-step and M-step until convergence. We then use the learned prior genotype probabilities to compute the posterior artifact probabilities of variants in a vcf. The filtering threshold is set such that the false discovery rate doesn't exceed a specified value, as described below.

IV. RELATED GATK TOOLS

The Broad somatics SNVs and indels pipeline involves several GATK tools besides `Mutect2` and FilterMutectCalls. We describe them here.

A. Calculating Contamination

Below, we present the GATK's fast, simple, and accurate method for calculating the contamination of a sample. This methods does not require a matched normal, makes no assumptions about the number of contaminating samples, and remains accurate even when the sample has a lot of copy number variation.

The inputs to our tool are a bam file and a vcf of common variants – for example ExAC, gnomAD, or 1000 Genomes – with their allele frequencies. The basic idea, which comes from ContEst[8] by Kristian Cibulskis and others in the Broad Institute Cancer Genome Analysis group, is simply to count ref reads at hom alt sites and subtract the number of ref reads expected from sequencing error to obtain the number of ref reads contaminating these hom alt sites. Finally, we use the allele frequencies to account for the fact that some contaminating reads have the alt allele. The only subtlety is in distinguishing hom alt sites from loss of heterozygosity events, which we describe below.

Suppose we have a set $\mathbb{H}$ of SNPs at which our sample is homozygous for the alternate allele. Let N_{ref} be the total number of ref reads at these sites. We can decompose N_{ref} as follows:

$$N_{\mathrm{ref}} = N_{\mathrm{ref}}^{\mathrm{error}} + N_{\mathrm{ref}}^{\mathrm{contamination}}, \tag{38}$$

where $N_{\mathrm{ref}}^{\mathrm{error}}$ and $N_{\mathrm{ref}}^{\mathrm{contamination}}$ are as the number of ref reads due to error and contamination, respectively. We can obtain N_{ref} by counting reads, and we estimate $N_{\mathrm{ref}}^{\mathrm{error}}$ as follows. Suppose, WLOG, that the ref allele is A and the alt is C. Then, assuming that all substitution errors are equally likely, $N_{\mathrm{ref}}^{\mathrm{error}}$ is approximately half the number of Gs and Ts. This is, of course, not a perfect assumption for any one site, but on average over all the sites in $\mathbb{H}$ it is very good.

Next we take the expectation of both sides of Equation 39 to obtain

$$\langle N_{\mathrm{ref}} - N_{\mathrm{ref}}^{\mathrm{error}} \rangle = \left\langle \sum_{s \in \mathbb{H}} \text{number of contaminant ref reads at } s \right\rangle \tag{39}$$

$$= \sum_{s \in \mathbb{H}} \langle \text{number of contaminant ref reads at } s \rangle \tag{40}$$

$$= \sum_{s \in \mathbb{H}} \langle \text{number of contaminant reads at } s \times \text{ref fraction of contaminant reads at } s \rangle \tag{41}$$

$$= \sum_{s \in \mathbb{H}} \langle \text{number of contaminant reads at } s \rangle \times \langle \text{ref fraction of contaminant reads at } s \rangle \tag{42}$$

where we have used the linearity of the expectation and the independence of the total number of contaminant reads with the fraction of contaminant reads that are ref. The expectation of the total number of contaminant reads is the depth d_s at site s times the contamination, which we denote by χ. The expected fraction of contaminant reads that are ref is one minus the alt allele frequency f_s. Crucially, this fact is independent of how many contaminating samples there are. Thus we have

$$\langle N_{\mathrm{ref}} - N_{\mathrm{ref}}^{\mathrm{error}} \rangle = \chi \sum_{s \in \mathbb{H}} d_s(1 - f_s) \tag{43}$$

and obtain the estimate

$$\hat{\chi} \approx \frac{N_{\mathrm{ref}} - N_{\mathrm{ref}}^{\mathrm{error}}}{\sum_{s \in \mathbb{H}} d_s(1 - f_s)} \tag{44}$$

Let us now roughly estimate the error bars on this result. The main source of randomness is the stochasticity in the number of contaminating ref reads. Although the nature of this randomness depends on the number of contaminants,

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[8] ContEst: estimating cross-contamination of human samples in next-generation sequencing data, *Bioinformatics* **27**, 2601 (2011)

the most variable case, hence an upper bound, is that of a single haploid contaminant, since at each site the only possibilities are the extremes of all contaminant reads being ref or all being alt. In this case, the contribution to the numerator of Eq. 45 from site s is the random variable $X_s Z_s$, where $X_s \sim \text{Binom}(d_s, \chi)$ is the number of contaminant reads at s and Z_s is a binary indicator for whether the contaminant reads are ref, with $P(Z_s = 1) = 1 - f_s$. X and Z are independent, so we can work out the variance of XZ as:

$$
\text{var}(XZ) = E[X^2 Z^2] - E[XZ]^2 \tag{45}
$$
$$
= (1 - f_s)E[X^2] - (1 - f_s)^2 E[X]^2 \tag{46}
$$
$$
= (1 - f_s)\left(\text{var}(X) + E[X]^2\right) - (1 - f_s)^2 E[X]^2 \tag{47}
$$
$$
= (1 - f_s)d_s\chi(1 - \chi) + f_s(1 - f_s)d_s^2\chi^2 \tag{48}
$$

And therefore the standard error on $\hat{\chi}$ comes out to the square root of the sum of these per-site variances, divided by the denominator of Eq. 45, that is,

$$
\text{std}(\hat{\chi}) = \frac{\sqrt{\sum_s \left[(1 - f_s)d_s\hat{\chi}(1 - \hat{\chi}) + f_s(1 - f_s)d_s^2\hat{\chi}^2\right]}}{\sum_s d_s(1 - f_s)} \tag{49}
$$

It remains to describe how we determine which sites are hom alt. The fundamental challenge here is that in cancer samples loss of heterozygosity may cause het sites to look like hom alt sites. Our strategy is to partition the genome into allelic copy-number segments, then infer the minor allele fraction of those segments. We segment the genome just as in GATK CNV, using a kernel segmenter with a Gaussian kernel computed on the alt fraction. A nonlinear kernel is important because each segment is multimodal, with peaks for hom ref, alt minor het, alt major het, and hom alt.

We then perform maximum likelihood estimation MLE on a model with learned parameters μ, the local minor allele fraction for each segment, χ, the contamination, and a constant base error rate parameter ϵ determined by counting reads that are neither the ref nor primary alt base at biallelic SNPs as described above. The model likelihood is

$$
P(\{a\}|\{f\}, \chi, \{d\}) = \prod_{\text{segments } n} \prod_{\text{sites } s} \sum_{\text{genotype } g} P(g|f_s)\text{Binom}(a_s|d_s, (1 - \chi)\phi(g, \mu_n, \epsilon) + \chi f_s) \tag{50}
$$

where a_s and d_s are the alt and total read counts at site s, allelic CNV genotypes g run over hom ref, alt minor, alt major, and hom alt with priors $P(\text{hom ref}) = (1 - f_s)^2$, $P(\text{alt minor}) = P(\text{alt major}) = f_s(1 - f_s)$, and $P(\text{homalt} = f^2$. $\phi(g, \mu, \epsilon)$ is the alt allele fraction of the uncontaminated sample: $\phi(\text{hom ref}) = \epsilon$, $\phi(\text{alt minor}) = \mu$, $\phi(\text{alt major}) = 1 - \mu$, $\phi(\text{hom alt}) = 1 - \epsilon$. The binomial is the weighted average of the uncontaminated sample and sample reads drawn independently from allele frequency f. This is inconsistent with a single diploid contaminant sample, or indeed with any finite number of contaminants, which is why we do not the the MLE estimate in the final output of the tool. The model also assumes that the uncontaminated and contaminating samples have the same overall depth distribution at each site, which is inconsistent with any differences in copy-number. We perform the MLE by brute force, alternately maximizing with respect to χ with μ fixed and vice versa. In order to make the solution more robust, we exclude segments with low μ from the maximization over χ by taking the highest possible threshold (up to 0.5, of course) for μ that retains at least $1/4$ of all sites.

Once we have learned the parameters of this model, we can easily infer the posterior probabilities of hom alt genotypes. We take every site with a posterior probability greater than 0.5. In order to make the result more reliable against CNVs, we again impose a threshold on segment minor allele fraction and apply the above formula only to hom alt sites in these segments. This time, however, we choose the highest possible threshold such that the estimated relative error is less than 0.2.

Finally, we note that the same calculation can be reversed by using alt reads in hom ref sites as the signal and replacing f by $1 - f$ everywhere above. We use the estimate from hom refs as a backup when the hom alt estimate has too great an error, as can occur in the case of targeted panels with few sites. We do not use this as our primary estimate because it is much more affected by uncertainty in the population allele frequencies and is thus susceptible to systematic bias.

B. Proposed tumor in normal estimation tool

Note: the following notes are just a proposal for which no GATK tool yet exists. A popular tool is DeTiN[9] by Amaro Taylor-Weiner and others at the Broad Institute Cancer Genome Analysis group.

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[9] DeTiN: overcoming tumor-in-normal contamination, *Nature Methods* **15**, 531 (2018)

Similar to the spirit of CalculateContamination, the fraction of tumor reads in the normal bam is a single number with a large amount of evidence and is probably well-estimated by simple descriptive statistics rather than a full-fledged probabilistic model. It shouldn't be much more complicated than finding somatic variants and comparing their signal in the normal sample to that in the tumor.

We propose the following steps to obtain our input of confident somatic SNVs:

- Run `Mutect2` with the `--genotype-germline-sites` argument to obtain a preliminary list of somatic SNVs, including those that look like germline variants due to tumor-in-normal contamination. For the sake of speed, we could implement a pileup-based mode in which we skip reassembly and equate read likelihoods with base qualities. This would allow us to obtain variant annotations using the existing architecture of `Mutect2` and therefore to filter calls with no new code.

- Run FilterMutectCalls. With default settings this eliminates the great majority of sequencing artifacts. To eliminate even more we could increase the log odds threshold slightly, essentially requiring a slightly larger alt allele count. Normally we don't do this because it sacrifices some sensitivity, but for our purposes here a 10 or 20 percent loss of sensitivity is perfectly acceptable as long as we are left with enough SNVs for our estimate. It would also make sense to be especially stringent with variants that have any significant population allele frequency in gnomAD, as well as possible mapping errors. Thus we might also run FilterAlignmentArtifacts with strict parameters.

- Reconsider all variants that are filtered only by the germline and/or normal artifact filters. Those that have enough read counts in the normal that we conclude they are germline variants, as opposed to tumor in normal contamination, should remain filtered.

The above steps are all very reliable, so at this point we can assume we have a collection of confident biallelic somatic SNVs that are hom ref in the germline. Similar to CalculateContamination, we can now estimate the number of alt reads in the normal at these sites:

$$\text{alt in normal} \approx \sum_{\text{sites}} (\text{depth in normal}) \times (\text{alt fraction in tumor}) \times (\text{tumor in normal fraction}) \tag{51}$$

Hence we estimate

$$\text{tumor in normal fraction} \approx \frac{\text{total number of alt reads in normal at somatic SNV sites}}{\sum_{\text{somatic SNV sites}} (\text{depth in normal}) \times (\text{alt fraction in tumor})} \tag{52}$$

We could also iterate this process as in CalculateContamination: first get an initial guess of the tumor-in-normal fraction, then use the initial guess to improve our "un-filtering" in the third step above.