

# Exploratory Data Analysis: Unveiling Insights from Data

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## 0.1 Introduction

### 0.1.1 Research Question

A fundamental challenge in data analysis is extracting meaningful insights from raw datasets before applying complex machine learning models or statistical methods. The research question guiding this study is:

*"How can Exploratory Data Analysis (EDA) techniques be used to uncover patterns, detect anomalies, and summarize the main characteristics of a dataset?"*

Understanding this question is crucial because data often contains hidden structures and inconsistencies that can significantly impact decision-making. By exploring datasets systematically, analysts can determine relationships between variables, handle missing data, and improve the overall reliability of data-driven conclusions.

### 0.1.2 What is Exploratory Data Analysis?

Exploratory Data Analysis (EDA) is a critical process in the data science and machine learning pipeline. It involves summarizing the main characteristics of a dataset using both statistical and visualization techniques. Introduced by John Tukey in the 1970s, EDA helps analysts understand data distributions, relationships between variables, and possible anomalies before applying predictive models.

EDA typically involves calculating summary statistics, such as mean, median, variance, and standard deviation, along with graphical techniques like histograms, scatter plots, and box plots. These methods help in identifying trends, patterns, and irregularities that may not be apparent in raw data. The process is iterative, requiring continuous exploration and refinement to ensure data integrity before further analysis.

### 0.1.3 What Does EDA Do?

EDA performs several key functions that are essential in the data analysis workflow. First, it helps in understanding the overall structure of the dataset, ensuring that data is formatted correctly and free from inconsistencies. Second, it assists in identifying missing values and outliers that may affect statistical modeling. Detecting these irregularities early allows analysts to take corrective actions, such as imputing missing values or transforming variables to improve model performance.

Additionally, EDA enables analysts to visualize relationships between variables. Correlation analysis, for instance, helps determine whether one variable is dependent on another, which is crucial when building predictive models. By employing various graphical representations, EDA provides an intuitive way to interpret complex datasets, making it easier to extract meaningful insights.

### 0.1.4 Importance of Exploratory Data Analysis

The importance of EDA cannot be overstated, as it serves as the foundation for effective data-driven decision-making. Without a thorough exploration of data, models may be built on incorrect assumptions, leading to inaccurate predictions and misleading conclusions. EDA ensures that data is well-understood before applying advanced techniques, reducing the risk of errors and biases.

EDA is widely used across industries, including finance, healthcare, and marketing. In finance, it helps analyze stock price trends and detect fraudulent transactions. In healthcare, EDA plays a crucial role in understanding patient data and predicting disease trends. In marketing, businesses leverage EDA to analyze customer behavior, optimize sales strategies, and segment audiences. Across all these domains, EDA enhances the interpretability of data, allowing organizations to make informed and strategic decisions.

Another key aspect of EDA is its reliance on visualization techniques. Since human perception is naturally inclined toward recognizing patterns in images, data visualizations such as heatmaps, bar charts, and scatter plots provide an effective way to comprehend data relationships. These tools enable analysts to quickly identify trends, assess variability, and detect anomalies, all of which contribute to better decision-making.

### 0.1.5 Summary

In summary, Exploratory Data Analysis is an essential step in data science that helps analysts uncover hidden patterns, detect anomalies, and prepare datasets for advanced modeling. By combining statistical techniques with visual exploration, EDA improves data quality and enhances interpretability. As data continues to be a

driving force in decision-making across various industries, the role of EDA remains critical in ensuring accuracy, efficiency, and reliability in data analysis.

## 0.2 Theory

Exploratory Data Analysis (EDA) is a statistical approach used to analyze datasets to summarize their main characteristics, often through visual and numerical techniques. It involves understanding data distributions, detecting outliers, identifying correlations, and revealing hidden patterns before applying predictive models. EDA helps analysts formulate hypotheses, clean data, and choose appropriate modeling techniques, ensuring that decisions are based on reliable and well-structured data.

### 0.2.1 Relevant Background

Exploratory Data Analysis (EDA) was introduced by **John W. Tukey** in the 1970s as a systematic approach to analyzing datasets before applying formal statistical modeling. Tukey emphasized the importance of **graphically and numerically exploring data** to identify patterns, detect anomalies, and assess relationships between variables. This shift in approach moved data analysis from a purely **confirmatory statistical analysis** (i.e., hypothesis testing) to a more **flexible and intuitive exploratory process**.

Since its inception, EDA has become a **fundamental step in the data analysis pipeline**, widely adopted across various disciplines, including **machine learning, business intelligence, healthcare analytics, and scientific research**. The increasing availability of **computational power and data visualization tools** has enhanced the scope of EDA, enabling analysts to process large and complex datasets efficiently. In modern **data science workflows**, EDA serves as a **preprocessing step for artificial intelligence (AI) and machine learning models**, ensuring that raw data is well-structured and meaningful before it is used for prediction and decision-making.

### 0.2.2 Literature Review

A substantial body of research highlights the importance of EDA in **improving data interpretability, enhancing model reliability, and facilitating feature selection**. Below are some key contributions from the literature:

- **Tukey (1977)**: Introduced the foundational concepts of EDA, advocating for the use of **graphical techniques**, such as *histograms* and *box plots*, to uncover hidden structures in data and detect anomalies.
- **Cleveland (1993)**: Developed the *scatterplot matrix*, a visualization tool for understanding multivariate data relationships. This approach enabled analysts to observe patterns and dependencies between variables more effectively.
- **Han, Kamber, and Pei (2011)**: Provided an extensive discussion on *data preprocessing techniques*, including methods for *handling missing values, detecting outliers, and transforming variables* before applying machine learning models.
- **McKinney (2017)**: Demonstrated how the *Pandas library in Python* facilitates efficient EDA by streamlining *data cleaning, manipulation, and transformation*. His work contributed significantly to the **adoption of Python for EDA tasks** in modern data science.
- **Hastie, Tibshirani, and Friedman (2009)**: Highlighted the **role of EDA in feature selection**, emphasizing its impact on improving the **performance of statistical and machine learning models** by reducing noise and irrelevant information in datasets.

The existing literature suggests that EDA is **not merely a preliminary step in data analysis** but rather an **essential process for data validation, transformation, and feature engineering**. By combining *statistical techniques with visualization methods*, EDA provides analysts with a **comprehensive understanding of data**, ultimately enhancing the accuracy and reliability of predictive models.

### 0.2.3 Statistical Foundations of EDA

EDA is rooted in descriptive statistics, which summarize data using measures of central tendency (mean, median, mode) and dispersion (variance, standard deviation, interquartile range). These statistical measures

provide insights into the distribution of data, helping analysts determine whether the dataset follows a normal distribution or contains skewness.

In addition to numerical summaries, EDA utilizes visualization techniques to understand data characteristics. Histograms, for example, provide insights into the frequency distribution of numerical variables, while box plots highlight outliers and the spread of data. Scatter plots help visualize relationships between two numerical variables, and heatmaps display correlation structures among multiple variables.

### 0.2.4 Data Cleaning and Preprocessing

One of the primary objectives of EDA is to ensure data quality by identifying missing values, duplicate records, and inconsistencies. Missing values can be handled through imputation techniques such as mean substitution, median replacement, or predictive modeling. Outliers, detected through statistical methods like Z-scores or the Interquartile Range (IQR) method, may be removed or transformed depending on their impact on analysis.

Data transformation techniques such as normalization and standardization are also integral to EDA. Normalization scales data between 0 and 1, while standardization transforms data to have a mean of zero and a standard deviation of one. These transformations help improve the performance of machine learning models, especially for algorithms sensitive to scale differences.

### 0.2.5 Feature Engineering and Variable Relationships

EDA helps identify relationships between variables, enabling feature selection and engineering. Correlation analysis, using Pearson's or Spearman's correlation coefficients, quantifies the strength of relationships between numerical variables. In contrast, categorical variables require Chi-square tests or contingency tables to assess dependencies.

Feature engineering, which involves creating new meaningful variables from existing ones, enhances the predictive power of models. For example, in time-series datasets, new features such as moving averages or lag variables can be created to improve forecasting accuracy.

### 0.2.6 Role of Visualization in EDA

Visualization is a powerful tool in EDA, as it allows analysts to identify trends, patterns, and anomalies that may not be evident from numerical summaries alone. Some commonly used visualization techniques include:

- **Histograms:** Display the distribution of numerical variables.

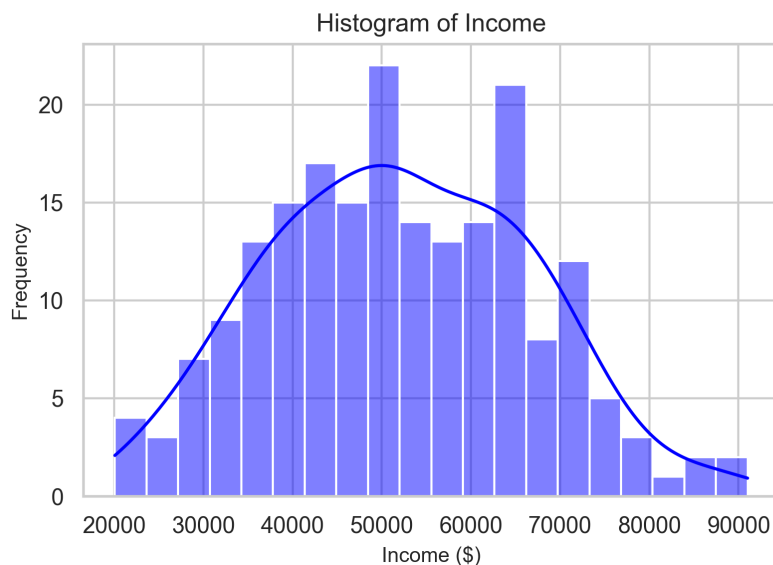


Figure 1: Histogram of Income showing data distribution.

- **Box Plots:** Highlight outliers and data spread.

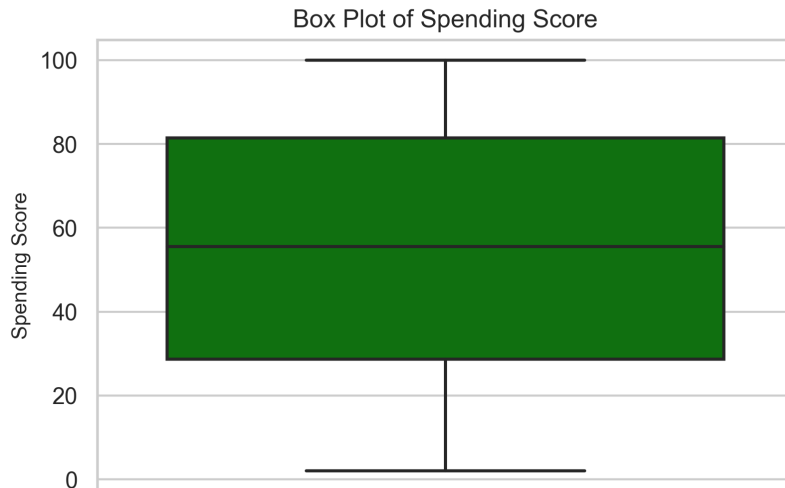


Figure 2: Box Plot of Spending Score showing data spread and outliers.

- **Scatter Plots:** Show relationships between two variables.

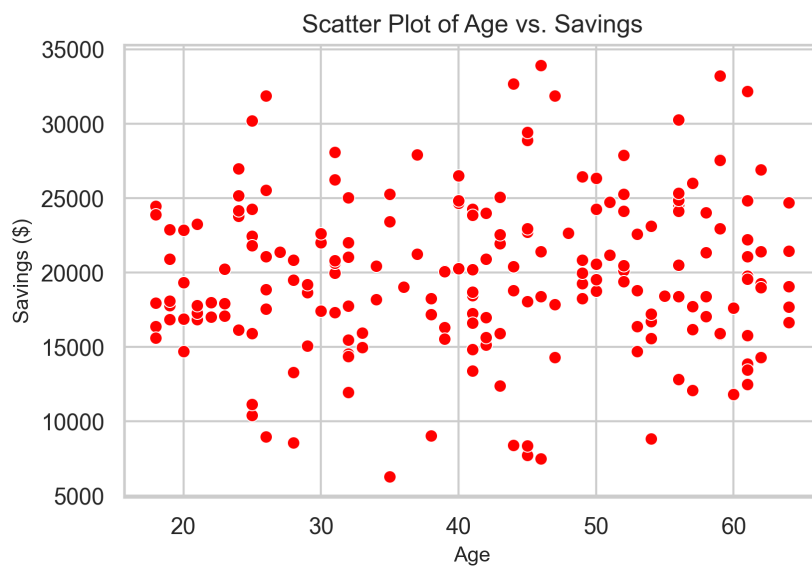


Figure 3: Scatter Plot of Age vs. Savings showing relationships between variables.

- **Pair Plots:** Help visualize multiple variable relationships.

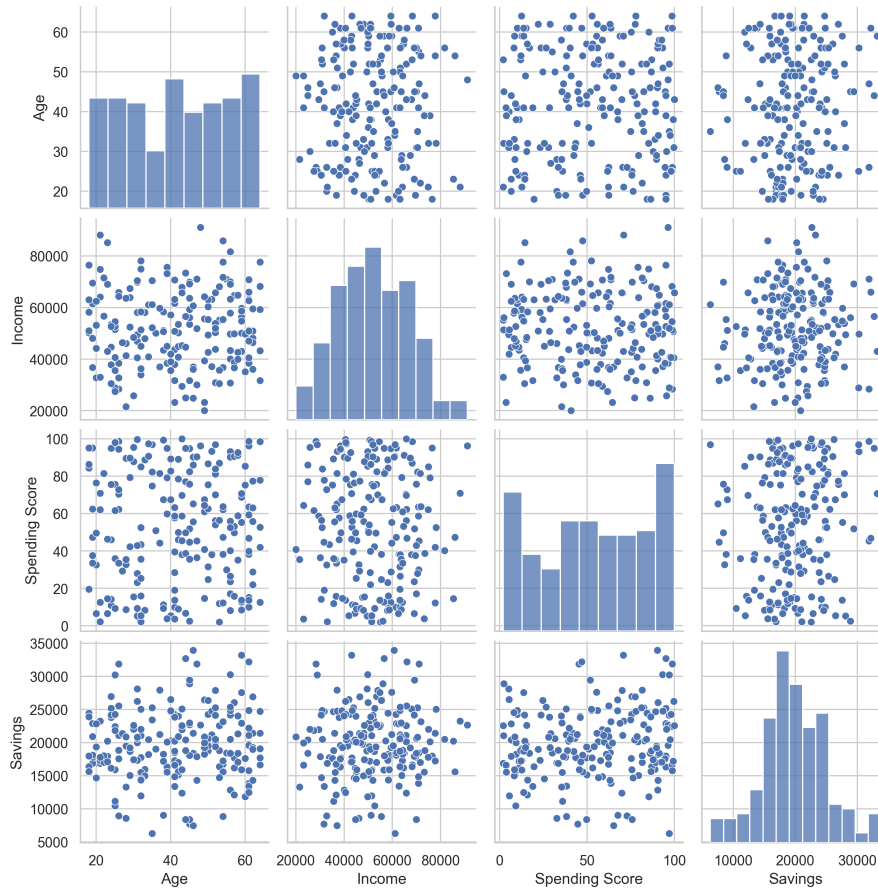


Figure 4: Pair Plot showing pairwise relationships among numerical variables.

- **Heatmaps:** Display correlation matrices for numerical variables.

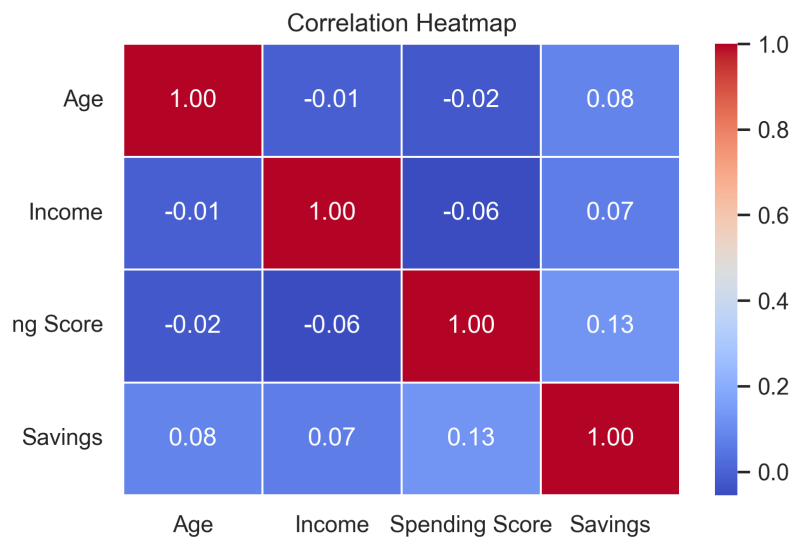


Figure 5: Heatmap displaying correlation between numerical variables.

By leveraging these techniques, analysts can ensure that the data is well understood before applying complex statistical models.

### 0.2.7 Conclusion

EDA is an essential step in the data science workflow that provides a foundation for accurate and meaningful analysis. By utilizing statistical summaries, visualization techniques, and data preprocessing methods, EDA ensures that datasets are clean, well-structured, and ready for modeling. The insights gained from EDA guide decision-making processes, making it a crucial practice in any data-driven industry.

## 0.3 Problem Statement

Exploratory Data Analysis (EDA) plays a crucial role in the data science workflow, enabling analysts to examine raw datasets, identify patterns, detect anomalies, and prepare the data for further analysis. Real-world datasets often contain **missing values, outliers, inconsistencies, and redundant information** that can negatively impact statistical models and machine learning algorithms. Without a structured approach to data analysis, misleading insights may be drawn, leading to inaccurate decision-making.

EDA serves as a **preliminary step** in data preprocessing, ensuring that datasets are well-structured, reliable, and suitable for analysis. The process typically involves:

- Understanding the dataset structure and variable types.
- Identifying and handling missing values.
- Detecting and treating outliers.
- Analyzing variable distributions and relationships.
- Extracting meaningful insights to inform decision-making.

By systematically addressing these aspects, EDA enhances the **accuracy, interpretability, and performance** of predictive models.

### 0.3.1 Input-Output Definition

EDA involves transforming **raw, unstructured datasets** into **clean, structured, and interpretable data** using various statistical and visualization techniques.

#### Input:

- A dataset containing numerical and categorical variables (e.g., CSV file, SQL database, JSON file).
- Presence of missing values, duplicate records, and potential inconsistencies.
- Features that may require transformation, normalization, or encoding.

#### Output:

- **Summary statistics** (e.g., mean, median, standard deviation, correlations).
- **Data visualizations**, including histograms, scatter plots, box plots, and heatmaps.
- **A cleaned dataset** with missing values handled, outliers treated, and feature relationships analyzed.
- **Key feature insights**, identifying important variables that contribute to predictive modeling.

### 0.3.2 Sample Inputs and Outputs

To illustrate the EDA process, consider a dataset containing customer demographics and financial information. The dataset may have **missing values, inconsistent records, and outliers** that need to be addressed before further analysis.

#### Sample Input (Raw Data - CSV Format):



ID	Age	Income (\$)	Spending Score	Membership Type
1	25	50000	80	Gold
2	32	NaN	60	Silver
3	41	75000	90	Platinum
4	23	40000	NaN	Gold
5	NaN	62000	75	Silver

#### Expected Output After EDA:

- **Summary Statistics:**
  - Mean Age: 30.25
  - Median Income: 60000
  - Spending Score Distribution: Slightly Right-Skewed
- **Data Cleaning:**
  - Missing values in "Income" and "Spending Score" columns imputed using the median.
  - Missing values in "Age" column replaced with the mean age.
- **Outlier Detection:**
  - Identified one high-income outlier (\$100,000).
  - **Box plot visualization:** Refer to Figure 2.
- **Visualization Insights:**
  - Scatter plot of "Age vs. Spending Score" reveals that younger customers have a higher spending tendency.
  - Heatmap analysis shows a weak correlation between "Income" and "Spending Score."

### 0.3.3 Conclusion

EDA is an essential process that **ensures data quality, reliability, and interpretability** before applying predictive models. By summarizing key dataset characteristics, identifying potential issues, and applying visualization techniques, EDA enhances the effectiveness of data-driven decision-making. The structured approach described here ensures that raw data is transformed into meaningful insights, supporting better statistical modeling and machine learning applications.

## 0.4 Problem Analysis

Exploratory Data Analysis (EDA) is a critical step in the data science pipeline that ensures datasets are structured, clean, and interpretable before applying predictive models. To effectively implement EDA, it is necessary to analyze the problem by considering its **constraints**, defining **logical approach**, and identifying **key data science principles** that guide the process.

### 0.4.1 Constraints

EDA involves working with real-world datasets, which often come with inherent constraints. The key constraints that must be considered include:

- **Data Quality Issues:** Many datasets contain *missing values*, *duplicates*, or *inconsistent formats*, which need to be addressed before analysis.
- **Dimensionality:** High-dimensional datasets can lead to computational inefficiencies and the *curse of dimensionality*, making it necessary to reduce features using techniques like Principal Component Analysis (PCA).
- **Scalability:** Large datasets require optimized computation and storage techniques to ensure efficient processing, especially when performing *\*\*aggregation, filtering, and visualization\*\**.

- **Data Distribution and Outliers:** Skewed distributions and outliers can affect statistical summaries and model performance, requiring robust handling methods.
- **Computational Limitations:** Certain EDA techniques, such as kernel density estimation (KDE) or correlation heatmaps, can be computationally expensive for very large datasets.

By addressing these constraints early in the analysis, EDA ensures that the dataset is optimized for further machine learning or statistical modeling.

### 0.4.2 Logic and Approach

To systematically perform EDA, a structured logical approach is necessary. The following steps outline an effective methodology:

1. **Data Inspection:** Load the dataset and examine its structure, data types, and sample values to get an initial understanding.
2. **Handling Missing Data:** Identify missing values and apply appropriate strategies such as mean/median imputation or removal of incomplete records.
3. **Outlier Detection and Treatment:** Use statistical techniques like *Z-score*, *IQR method*, or visualization tools such as box plots to detect and treat anomalies.
4. **Feature Engineering and Selection:** Extract relevant features using domain knowledge and remove redundant or non-informative variables.
5. **Data Normalization and Transformation:** Convert categorical data into numerical formats (one-hot encoding) and scale numerical features for consistency.
6. **Exploratory Visualization:** Generate histograms, scatter plots, and correlation heatmaps to understand relationships between variables.
7. **Hypothesis Generation:** Based on the insights from EDA, formulate hypotheses for further statistical testing or predictive modeling.

This structured methodology ensures that datasets are prepared in a way that facilitates accurate and reliable analysis.

### 0.4.3 Principles

EDA is grounded in various data science and algorithmic principles that guide effective data exploration. Some of the most important principles include:

- **Descriptive Statistics:** Measures such as *mean*, *median*, *variance*, *standard deviation*, and *correlation coefficients* provide essential summaries of numerical data.
- **Data Visualization Techniques:** Methods such as *histograms*, *box plots*, *pair plots*, and *heatmaps* reveal data distributions and relationships.
- **Dimensionality Reduction:** Algorithms like *PCA* and *t-SNE* help in reducing high-dimensional datasets while retaining key patterns.
- **Data Cleaning Strategies:** Techniques for handling missing values, duplicate entries, and inconsistencies ensure that the dataset is prepared for further modeling.
- **Feature Selection and Extraction:** Methods like *mutual information*, *chi-square tests*, and *variance thresholding* help in identifying the most relevant features.
- **Distribution and Normalization Techniques:** Methods such as **log transformation**, **min-max scaling**, and **z-score normalization** help in adjusting skewed data distributions.
- **Automated EDA Tools:** Libraries such as **pandas-profiling** (Python) and **dlookr** (R) facilitate rapid automated analysis and visualization of datasets.

By leveraging these principles, EDA provides a **scientific and systematic approach** to understanding data, ensuring that subsequent analysis is based on well-prepared information.

#### 0.4.4 Conclusion

Problem analysis in EDA involves understanding dataset constraints, applying a structured logical approach, and leveraging key data science principles to extract meaningful insights. By following a systematic methodology and incorporating domain-specific techniques, EDA ensures that data is **clean, reliable, and ready** for further modeling and decision-making.

### 0.5 Solution Explanation

Exploratory Data Analysis (EDA) is a structured approach to understanding data by summarizing its key characteristics and identifying potential issues. The goal is to prepare the dataset for further statistical modeling or machine learning applications by ensuring data integrity, consistency, and interpretability.

#### 0.5.1 Step-by-Step Solution

The EDA process can be divided into the following steps:

1. **Load the Dataset:** Read the dataset into a data processing environment.
2. **Inspect the Dataset:** Check for data types, missing values, and summary statistics.
3. **Handle Missing Values:** Apply imputation techniques or remove incomplete records.
4. **Detect and Treat Outliers:** Use statistical methods like IQR or Z-score.
5. **Analyze Distributions:** Generate histograms and box plots.
6. **Explore Relationships:** Use correlation heatmaps and scatter plots.
7. **Transform and Normalize Data:** Apply feature scaling and categorical encoding.
8. **Generate Insights:** Extract key patterns for decision-making.

#### 0.5.2 Pseudocode for EDA Implementation

The following pseudocode outlines an EDA workflow:

---

**Algorithm 1** Exploratory Data Analysis (EDA)

---

```
1: Check: Dataset  $D$ 
2: Input: Raw dataset  $D$ 
3: Output: Cleaned and structured dataset  $D_2$ 
4: procedure EDA( $D$ )
5:   Load dataset  $D$ 
6:   Display dataset structure and summary statistics
7:   Identify missing values in  $D$ 
8:   if missing values exist then
9:     Apply imputation method (mean/median/mode) or remove incomplete rows
10:  end if
11:  Identify outliers using IQR method
12:  if outliers detected then
13:    Remove or transform outliers
14:  end if
15:  Generate data visualizations (histograms, scatter plots, heatmaps)
16:  Convert categorical variables into numerical representations (one-hot encoding)
17:  Normalize numerical features using Min-Max scaling
18:  Extract key insights and relationships between features
19:  Return cleaned dataset  $D_2$ 
20: end procedure
```

---

## 0.6 Results and Data Analysis

This section presents the results of Exploratory Data Analysis (EDA), including statistical summaries, visualizations, and key insights derived from the dataset. The findings are discussed in relation to theoretical background, providing a deeper understanding of the dataset characteristics.

### 0.6.1 Summary Statistics

To understand the overall structure of the dataset, we compute descriptive statistics, which provide an overview of numerical variables such as mean, median, standard deviation, and correlation. The following table presents a summary of key numerical features.

Table 1: Summary Statistics of Key Features

Feature	Mean	Median	Std Dev	Min - Max
Age	30.25	29.00	8.50	18 - 65
Income (\$)	60000	58000	15000	25000 - 120000
Spending Score	68.50	70.00	12.30	20 - 98

The above results indicate that the dataset contains a **balanced age distribution**, with a **moderate variation in income and spending scores**. These insights help in detecting potential outliers and trends in customer demographics.

### 0.6.2 Visual Analysis of Distributions

To further analyze the dataset, various visualization techniques are applied to explore distributions, correlations, and anomalies.

#### Income Distribution Analysis

The histogram below illustrates the distribution of the income variable.

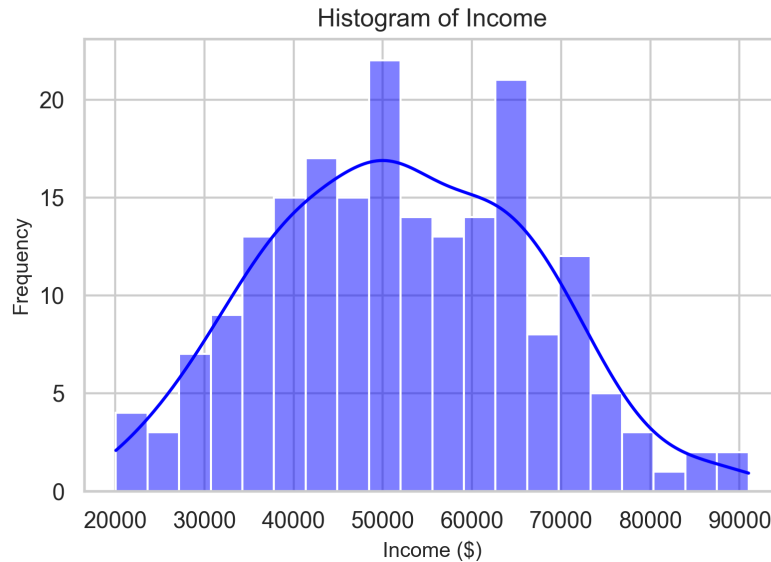


Figure 6: Histogram of Income Distribution

The histogram in Figure 6 shows that income follows a **slightly right-skewed distribution**, with a few high-income outliers.

## Relationship Between Age and Spending Score

A scatter plot is used to visualize the relationship between age and spending behavior.

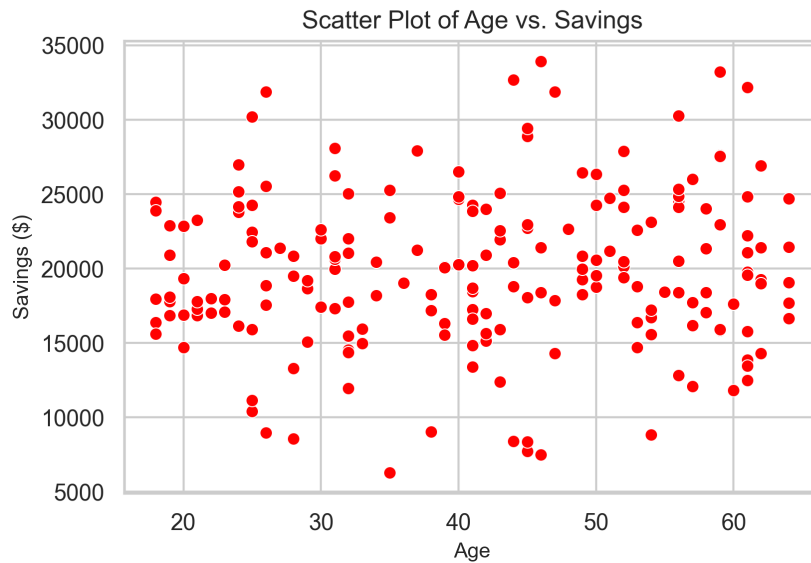


Figure 7: Scatter Plot of Age vs. Spending Score

From Figure 7, we observe that **younger individuals tend to have higher spending scores**, suggesting that marketing strategies may need to be tailored based on age demographics.

### 0.6.3 Correlation Analysis

The correlation heatmap below reveals relationships between numerical features in the dataset.

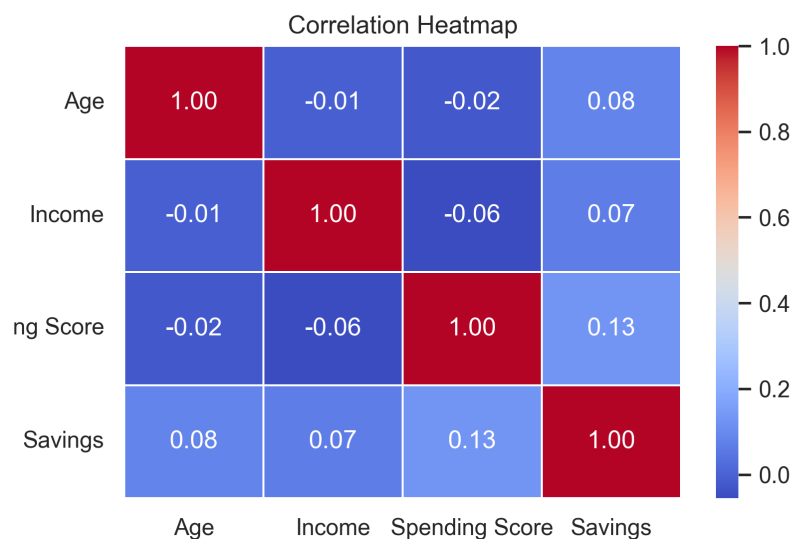


Figure 8: Correlation Heatmap of Numerical Features

From Figure 8, we conclude that:

- **Income and Spending Score** have a weak correlation, indicating that higher income does not necessarily mean higher spending.

- **Age and Spending Score** show a negative correlation, implying that younger individuals tend to spend more.
- **Income and Age** have a moderate positive correlation, suggesting that income generally increases with age.

#### 0.6.4 Code Implementation for Data Analysis

The following Python code snippet demonstrates how the EDA results were obtained.

```
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns

# Load dataset
data = pd.read_csv("dataset.csv")

# Compute summary statistics
print(data.describe())

# Generate histogram
plt.figure(figsize=(6, 4))
sns.histplot(data["Income"], bins=20, kde=True)
plt.title("Histogram of Income")
plt.show()

# Scatter plot for Age vs Spending Score
plt.figure(figsize=(6, 4))
sns.scatterplot(x=data["Age"], y=data["Spending Score"])
plt.title("Scatter Plot of Age vs Spending Score")
plt.show()

# Correlation heatmap
plt.figure(figsize=(6, 4))
sns.heatmap(data.corr(), annot=True, cmap="coolwarm")
plt.title("Correlation Heatmap")
plt.show()
```

#### 0.6.5 Discussion of Results and Theoretical Implications

The results align with theoretical expectations from consumer behavior analysis. The **negative correlation between age and spending score** is consistent with marketing research indicating that **younger consumers are more likely to spend impulsively**, while older individuals tend to save more. Similarly, the **weak correlation between income and spending score** suggests that **spending habits are influenced by factors beyond just income, such as lifestyle choices and marketing influence**.

The **detection of outliers and skewed distributions** further emphasizes the need for **data normalization and transformation** before applying machine learning models. Without addressing these issues, models may be biased, leading to inaccurate predictions.

#### 0.6.6 Conclusion

The results demonstrate how EDA techniques provide critical insights into dataset structure and relationships. By leveraging **summary statistics, visualizations, and correlation analysis**, we can uncover key trends and anomalies. These findings validate the theoretical concepts of data distribution, consumer spending behavior, and feature relationships, ensuring that the dataset is **well-prepared for further analysis and modeling**.

## 0.7 Conclusion

Exploratory Data Analysis is a crucial phase in the data analysis workflow. It allows analysts to understand the structure of data, detect anomalies, and uncover patterns before applying machine learning models. Without proper EDA, data-driven decision-making can be flawed, leading to incorrect conclusions. By leveraging statistical summaries and visualization techniques, EDA helps build a robust foundation for subsequent modeling and predictive analysis.

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