

Tutorial 7

Everyone who loves someone who loves them back is happy.
 Mary loves Everyone.
 There is someone who loves Mary.

$$\forall x \exists y \text{ loves}(x, y) \wedge \text{loves}(y, x) \Rightarrow \text{Happy}(x)$$

$$\forall x \text{ loves}(\text{Mary}, x)$$

$$\exists y \text{ loves}(\text{Mary}, y)$$

$$\forall x \exists y \neg (\text{loves}(x, y) \wedge \text{loves}(y, x)) \vee \text{Happy}(x)$$

$$\forall x \text{ loves}(\text{Mary}, x)$$

$$\exists y \text{ loves}(y, \text{Mary})$$

$$\forall x \text{ others}(y) \neg (\text{loves}(x, \text{others}(y)) \wedge \text{loves}(\text{others}(y), x))$$

$$\vee \text{Happy}(x)$$

$$\forall x \text{ loves}(\text{Mary}, x)$$

$$\text{others}(y) \text{ loves}(\text{others}(y), \text{Mary})$$

$$\forall x \text{ others}(y) (\neg \text{loves}(x, \text{others}(y)) \vee \text{loves}(\text{others}(y), x))$$

$$\vee \text{Happy}(x)$$

- 1.1) $\neg \text{loves}(x, \text{others}(y)) \vee \neg \text{loves}(\text{others}(y), x)$
- 1.2) $\text{Happy}(x)$
- 2) ~~loves~~ $\text{loves}(\text{Mary}, x)$
- 3) $\text{loves}(\text{others}(y), \text{Mary})$

9-11

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classmate

Date

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Happy (Mangy)

100.3

~~Happy Mangy~~

~~loves (Mangy, other)~~