

CSO PRACTICAL NO-1

BASICS OF R SOFTWARE

- i) R is a software for data analysis and statistical computing.
 - ii) It is a software by which effective data handling outcome storage is possible
 - iii) It is capable of graphical display
 - iv) It's a full software
 $+,-,*,,|, \text{abs}, \text{sqrt}$
- Q1. $\alpha^2 + |-5| + 4 \times 5 + 6/5$

$$\text{Code: } \alpha^2 + \text{abs}(-5) + 4 * 5 + 6/5 \\ \Rightarrow 30.2$$

Q2. $x = 20$

$$y = 2x$$

$$z = x + y$$

Find \sqrt{z}

Code: $x = 20$

$$y = 2 * x$$

$$z = x + y$$

$$\text{sqrt}(z)$$

7.445701

$$Q3) x=10, y=15, z=5$$

040

$$\begin{aligned} & \text{1) } x+y+z \\ &= x+y+z \\ &= 30 \end{aligned}$$

$$\begin{aligned} & \text{2) } \sqrt{xyz} \\ &= \sqrt{x \cdot y \cdot z} \\ &= \sqrt{10 \cdot 15 \cdot 5} \\ &= \sqrt{750} \\ &= 27.38613 \end{aligned}$$

$$\begin{aligned} & \text{3) } x \cdot y \cdot z \\ &= x \cdot y \cdot z \\ &= 750 \end{aligned}$$

$$\begin{aligned} & \text{4) } \lceil \text{round}(\sqrt{xyz}) \rceil \\ &= \lceil \text{round}(a) \rceil \\ &= 27 \end{aligned}$$

Q4) A vector in R software is defined by C

$$1) x = c(2, 3, 5, 7)^T$$

$$\Rightarrow x$$

$$\Rightarrow [1] 2 \quad 3 \quad 5 \quad 7$$

$$2) x = c(2, 3, 5, 7)^T c(2, 3)$$

$$\Rightarrow x$$

$$\Rightarrow [1] 4 \quad 27 \quad 25 \quad 543$$

$$3) a = c(1, 2, 3, 4, 5, 6)^T c(2, 3, 4)$$

$$\Rightarrow a$$

$$\Rightarrow [1] 1 \quad 8 \quad 81 \quad 16 \quad 125 \quad 1296$$

$$4) c(2, 23, 1, 4)^* 3$$

$$\Rightarrow [1] 63 \quad 69 \quad 3 \quad 12$$

$$5) c(2, 23, 1, 4)^* c(-2, -3, -5, -7)$$

$$\Rightarrow [1] -42 \quad -69 \quad -51 \quad -28$$

Q40

$$6) c(2, 3, 5, 7) + c(-2, -3, -1, 0)$$

$$\Rightarrow [1] \quad 0 \quad 0 \quad 4 \quad 7$$

$$7) c(2, 3, 5, 7)/2$$

$$\Rightarrow 1.0 \quad 1.5 \quad 2.5 \quad 3.5$$

Q5) Find the sum, product, sqrt of sum & p10 d10 for the given value.

$$4, 9, 2, 5, 7, 8, 3, 6, 15, 12, 10, 9, 8, 13, 14$$

Code :-

$i = c(4, 9, 2, 5, 7, 8, 3, 6, 15, 12, 10, 9, 8, 13, 14)$	OUTPUT
$s = sum(i)$	
$p = pmod(i)$	$[1] 125$
s	$[1] 8.559323e+12$
p	$[1] 11.18034$
$sqrt(s)$	$[1] 292.5632$
$sqrt(p)$	

Q6) Find the sum, pmod, max, min, value of $x = c(2, 8, 9, 7, 6)^{1/2}$

$sum(x)$	$max(x)$	$pmod(x)$	$min(x)$
$\Rightarrow [1] 53$	$[1] 11$	$[1] 665280$	$[1] 2$

* Matrix : $x = matrix(nrow=4, ncol=2, data=c(1, 2, 3, 4, 5, 6))$

041

a<- matrix(nrow=3, ncol=3, data=r(4,5,6,7,8,9,1,4,0,2))
b<- matrix(nrow=3, ncol=3, data=c(6,4,5,11,12,18,9,7,4))

$\Rightarrow a + b$

$a \neq b$

$b \neq 3$

$$\begin{matrix} [1,1] & [1,2] & [1,3] & [1,1] & [1,2] & [1,3] & [1,1] & [1,2] & [1,3] \\ [1,1] & 10 & 18 & 13 & 11 & 8 & 14 & 8 & 18 & 33 & 27 \\ [1,2] & 9 & 20 & 7 & 21 & 10 & 16 & 0 & 12 & 36 & 21 \\ [1,3] & 11 & 27 & 6 & 31 & 12 & 18 & 4 & 15 & 54 & 12 \end{matrix}$$

$\rightarrow a \neq b$

$$\begin{matrix} [1,1] & [1,2] & [1,3] \\ [1,1] & 24 & 77 & 36 \\ [1,2] & 20 & 96 & 0 \\ [1,3] & 30 & 162 & 8 \end{matrix}$$

M

IPO

PRACTICAL NO - 2.1

* Binomial Distribution

n = total no of trials

p = P(success)

q = P(failure)

s_1 = no of success out of n

$$P[X] = {}^n C_x \ p^x q^{n-x}$$

$$E[X] = np$$

$$V(X) = npq$$

dbinom(x, n, p)

$$n \neq p$$

$$n \neq p \neq q$$

pbinom(x, n, p)

* EXERCISE :-

Q1) Toss a coin 10 times $P(\text{heads}) = 0.5$ let X be the no. of heads

Find the probability
of seven heads

i) four heads

ii) Atleast six heads

iv) Almost four heads

v) No heads

vi) All heads

output

$$\gamma^n = 10$$

$$\gamma^P = 0.6$$

$$\gamma^q = 0.4$$

$$\gamma^a = \text{dbinom}(7, n, P)$$

$$\gamma^a$$

$$[1] 0.2149908$$

$$\gamma^b = \text{dbinom}(4, n, P)$$

$$\gamma^b$$

$$[1] 0.1114767$$

$$\gamma^c = 1 - \text{pbunom}(6, n, P)$$

$$\gamma^c$$

$$[1] 0.3822806$$

$$\gamma^d = \text{pbunom}(4, n, P)$$

$$\gamma^d$$

$$[1] 0.1662386$$

$$\gamma^e = \text{dbinom}(0, n, P)$$

PM

$$\gamma^e$$

$$[1] 0.0001048576$$

$$\gamma^f = \text{dbinom}(10, n, P)$$

$$\gamma^f$$

$$[1] 0.006046618$$

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PRACTICAL NO : 2.2

* Binomial Distribution

- Q2) Suppose there are 10 MCQ's in an ENGLISH paper. Each question has 5 answers out of which only one is correct. Find the probability of having i) 4 correct answers.
ii) atmost 4 correct answers.
iii) atleast 8 correct answers.
- Q3) Find the complete binomial distribution when $p = 0.1$
- Q4) Find the probability of exactly 10 success out of 100 trials with $p = 0.1$
- Q5) 'X' follows binomial distribution with $n=12$ & $p = 0.25$:
Find i) $P(X \leq 5)$
ii) $P(X \geq 7)$
iii) $P(5 \leq X \leq 7)$
- Q6) There are 10 members in a committee. Probability of any member attending a meeting is 0.9 . What is the probability that 7 or more members will present?
- Q7) A sales man has a 20% chance of

sell to a customer. On a typical day he'll meet 46 customers. What minimum no of sells will make with 88% probability

Q2) for $n=10, p=0.6$. Find the binomial probability that & plot the graphs of part b c d.

* formula :-

* Probability of atmost x values:

$$P(X \leq x) = \text{ptbinom}(x, n, p)$$

* Probability of atleast x values

$$P(X \geq x) = 1 - \text{ptbinom}(x, n, p)$$

* If ' x' is unknown and the probability is given as P , to find $\text{qbinom}(P, n, p)$

Q2)

$$\rightarrow n = 12$$

$$\rightarrow p = 1/5$$

$$\rightarrow P$$

$$[1] 0.2$$

$$\rightarrow n$$

$$[1] 12$$

$$i) > \text{dtbinom}(4, n, p)$$

$$[1] 0.1328756$$

$$ii) > \text{ptbinom}(4, n, p)$$

$$[1] 0.927445$$

$$iii) > 1 - \text{ptbinom}(2, n, p)$$

$$[1] 0.4416543$$

$$iv) > n = 5$$

$$\rightarrow p = 0.1$$

$$> \text{dtbinom}(0, n, p)$$

$$[1] 0.59049$$

$$> \text{dtbinom}(1, n, p)$$

$$[1] 0.32805$$

$$> \text{dtbinom}(2, n, p)$$

$$[1] 0.1077$$

~~$$> \text{dtbinom}(2, n, p)$$~~

~~$$[1] 0.0081$$~~

~~$$> \text{dtbinom}(4, n, p)$$~~

~~$$[1] 0.00045$$~~

~~$$> \text{dtbinom}(5, n, p)$$~~

~~$$[1] 1e-05$$~~

Q4)

$$\rightarrow x = 10$$

$$\rightarrow n = 100$$

$$\rightarrow p = 0.1$$

$$> \text{dtbinom}(x, n, p)$$

$$[1] 0.131863$$

Q5) > $n = 12$

$$\rightarrow p = 0.25$$

$$> \text{ptbinom}(5, n, p)$$

$$[1] 0.9455978$$

$$> 1 - \text{ptbinom}(17, n, p)$$

$$[1] 0.00278151$$

$$> \text{dtbinom}(16, n, p)$$

$$[1] 0.0010945$$

APC

(06) > n = 10

> p = 0.9

> 1 - pbinom(6, n, p)

[1] 0.9872048

(07) > n = 30

> p = 0.2

> p1 = 0.88

> qbeta(p1, n, q)

[1] 9

(08) > n = 10

> p = 0.6

> M = 0:n

> bp = dtbnom(M, n, p)

> bp

[1] 0.0001048576 0.0015728640 0.0106168320 0.047467378
0.111476734

[6] 0.2006551248 0.2508226560 0.2149708480 0.1209373820

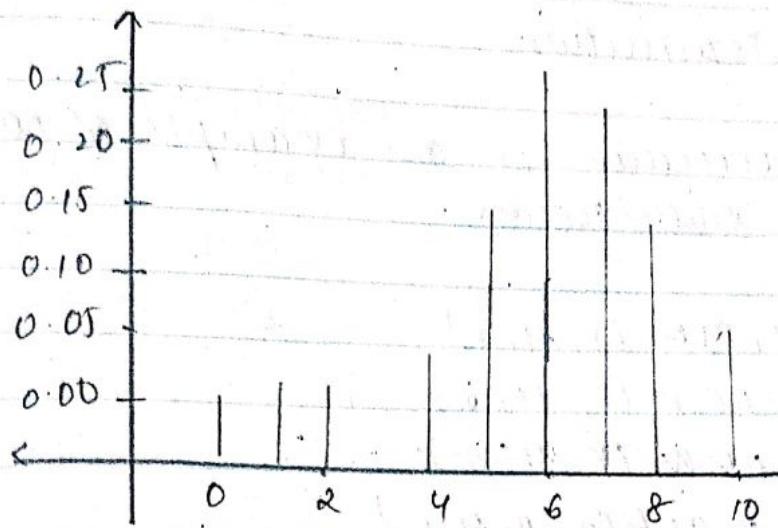
[11] 0.0060466176

> d = data.frame ("x.value" = x, probatuity" = bp)

> d

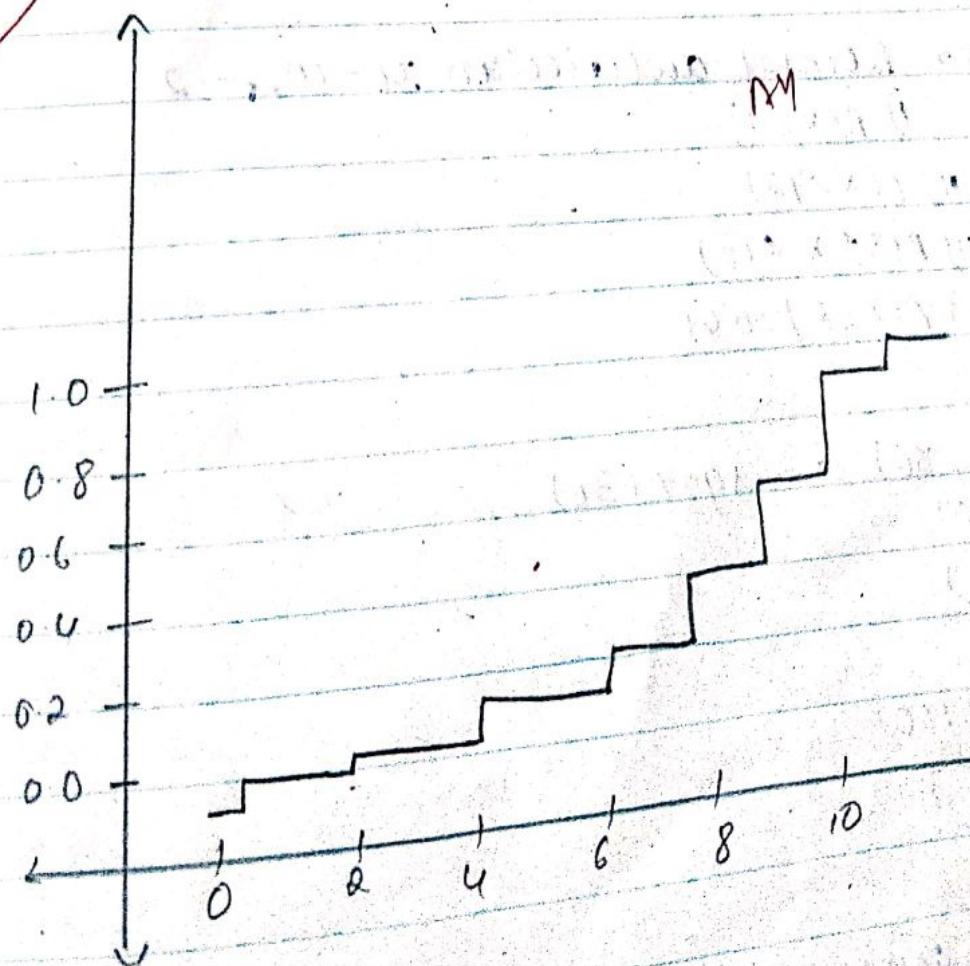
	x.value	probatuity
1	0	0.0001048576
2	1	0.0015728640
3	2	0.0106168320
4	3	0.0474673780
5	4	0.1114767360
6	5	0.2006581248
7	6	0.2508226560
8	7	0.2149908480
9	8	0.1209325300
10	9	0.006046617600

$\gamma \text{plot}(x, bp_1, "h")$



$\gamma cp = \text{polyom}(x, bp_1)$

$\gamma \text{plot}(x, cp, "s")$



PRACTICAL NO:-3

check the following are p.m.f or not?

	1	2	3	4	5
$p(x)$	0.2	0.5	0.5	0.4	0.4

	10	20	30	40	50
$p(x)$	0.3	0.2	0.3	0.1	0.1

	0	1	2	3	4
$p(x)$	0.4	0.2	0.3	0.2	0.1

Solutions

It is not a p.m.f since it does not satisfy the first condition.

All values of $p(x)$ are more than zero and less than one, 1st condⁿ is satisfied.

$$\text{Also, } \sum p(x) = p(10) + p(20) + p(30) + p(40) + p(50) \\ = 0.3 + 0.2 + 0.3 + 0.1 + 0.1$$

$$\therefore = 1$$

∴ 2nd condition is also satisfied

∴ we can say it is a p.m.f

$$\text{prob} = (0.3, 0.2, 0.3, 0.1, 0.1)$$

$$\text{prob} = 0.3 \quad 0.2 \quad 0.3 \quad 0.1 \quad 0.1$$

$$[1] \quad 0.3 \quad 0.2 \quad 0.3 \quad 0.1 \quad 0.1$$

$$\therefore \text{sum of prob} > 1$$

iii) \rightarrow since all the values of $P(x)$ are more than zero & less than one than first condition is satisfied.

Also,

$$\begin{aligned}\sum P(x) &= P(0) + P(1) + P(2) + P(3) + P(4) \\ &= 0.4 + 0.2 + 0.3 + 0.2 + 0.1 \\ &= 1.2\end{aligned}$$

still, 2nd condition is not satisfied
since the value is greater than 1.

Hence, it is not a p.m.f

Q2) Following is a p.m.f of X

x	1	2	3	4	5
$P(x)$	0.1	0.15	0.2	0.3	0.25

Find mean & variance of ' X '.

x	$P(x)$	$xP(x)$	$x^2P(x)$
1	0.1	0.1	0.1
2	0.15	0.30	0.60
3	0.2	0.6	1.8
4	0.3	1.2	4.8
5	0.25	1.25	6.25

$$E(X) = 3.45 \quad E(x^2) = 13.55$$

$$\text{Mean} = E(X) = \sum xP(x) = 3.45$$

$$\begin{aligned}\text{Var} &= V(X) = \sum x^2P(x) - [E(X)]^2 \\ &= 13.55 - (3.45)^2 \\ &= 1.6475\end{aligned}$$

011
7 $x = C(1, 2, 3, 4, 5)$
7 $p_{prob} = C(0.1, 0.15, 0.2, 0.3, 0.25)$

7 $a = x * prob$

7 $\text{sum}(a)$

[1] 13.45

7 $b = x * a$

7 $\text{sum}(b)$

[1] 13.55

7 $\text{var} = 13.55 - (13.45^2)$

[1] 1.06475

Q3. find mean & variance of x

x p(x)

5 0.1

10 0.3

15 0.2

20 0.25

25 0.15

7 $x = C(5, 10, 15, 20, 25)$

7 $p_{prob} = C(0.1, 0.3, 0.2, 0.25, 0.15)$

7 $a = x * prob$

7 $\text{sum}(a)$

[1] 15.25

7 $b = x * a$

7 $\text{sum}(b)$

[1] 27.25

7 $\text{var} = \text{sum}(b) - (\text{sum}(a)^2)$

7 var

Q4) Find C.D.F of the following P.M.F and draw the graph of C.D.F

x	1	2	3	4
$P(x)$	0.4	0.3	0.2	0.1

$$\geq x = \{1, 2, 3, 4\}$$

$$\geq \text{prob } x = \{0.4, 0.3, 0.2, 0.1\}$$

$$\geq a = \text{sum}(\text{prob } x)$$

$$\geq a$$

$$\{1, 0.4, 0.7, 0.9, 1.0\}$$

$$F(x) = 0 \quad x < 1$$

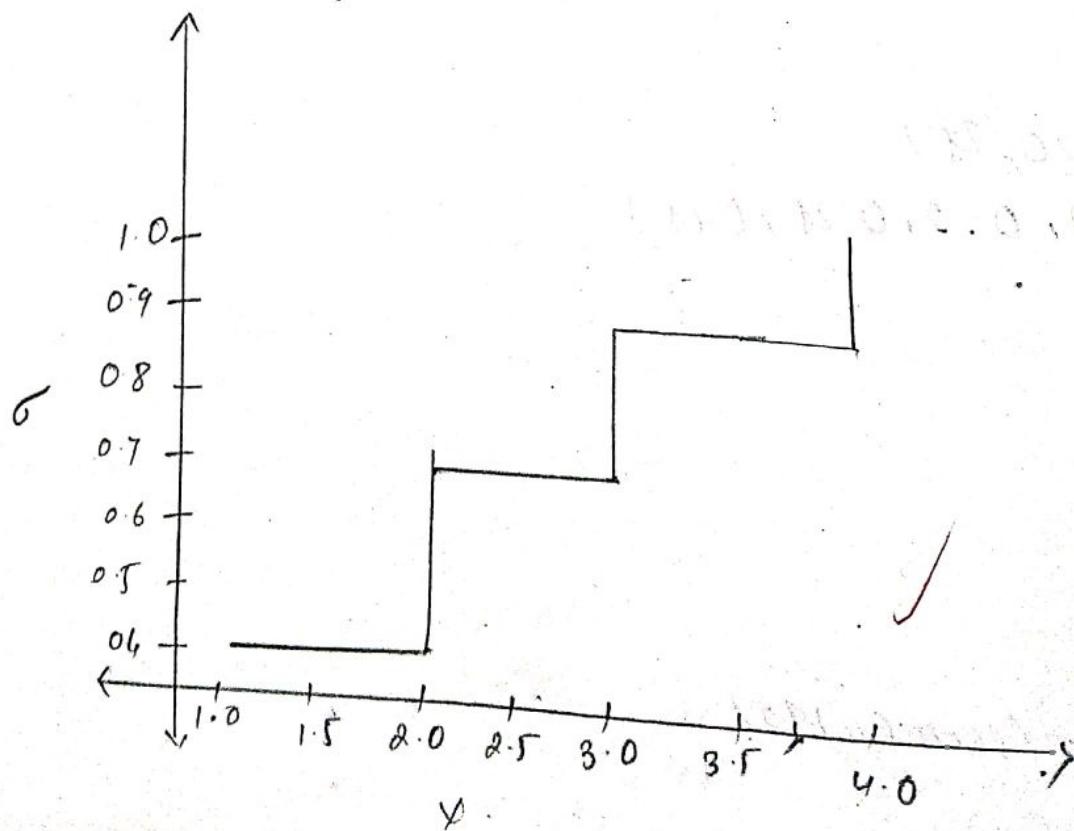
$$= 0.4 \quad 1 \leq x < 2$$

$$= 0.7 \quad 2 \leq x < 3$$

$$= 0.9 \quad 3 \leq x < 4$$

$$= 1.0 \quad x \geq 4$$

Plot $(x, F(x))$



04/11)	x	0	2	4	6	8
	$f(x)$	0.2	0.3	0.2	0.2	0.1

$$\gamma x = c(0, 2, 4, 6, 8)$$

$$\gamma \text{prob} = c(0.2, 0.3, 0.2, 0.2, 0.1)$$

$$\gamma a = \text{cumsum}(\text{prob}x)$$

$$\gamma 9$$

$$[1] 0.2 \quad 0.5 \quad 0.7 \quad 0.9 \quad 1.0$$

$$P(x) = 0.2 \quad x < 0$$

$$= 0.2 \quad 0 \leq x < 2$$

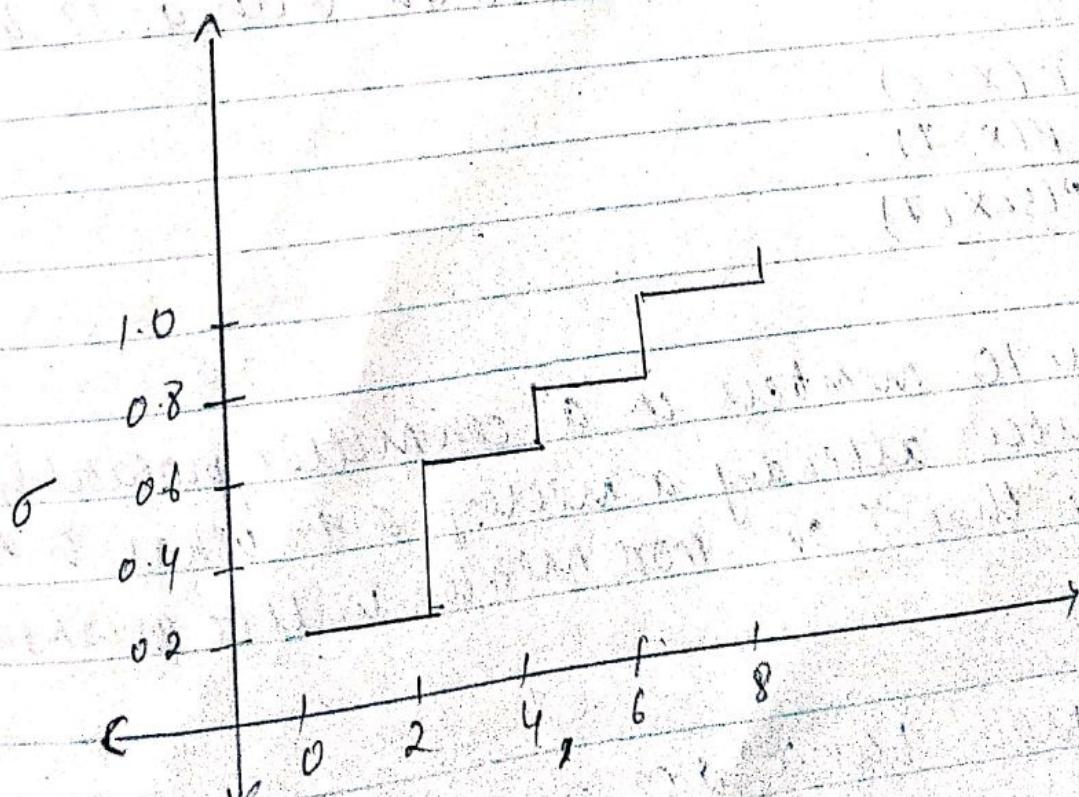
$$= 0.5 \quad 2 \leq x < 4$$

$$= 0.7 \quad 4 \leq x < 6$$

$$= 0.9 \quad 6 \leq x < 8$$

$$= 1.0 \quad x \geq 8$$

plot(x, q, "s")



Q4) PRACTICAL - NO 4

$$P(X=x) = {}^n \text{C}_x p^x q^{n-x}$$

[$n=8, p=0.6, q=0.4$] - given

$$\text{v) } P(X=7) = {}^8 \text{C}_7 (0.6)^7 (0.4)^1 \\ = {}^8 \text{C}_7 \times 0.2799 \times 0.4 \\ = 8 \times 0.2799 \times 0.4 = 0.08957$$

$$\text{ii) } P(X \leq 3) = P(0) + P(1) + P(2) + P(3) \\ = {}^8 \text{C}_0 (0.6)^0 (0.4)^8 + {}^8 \text{C}_1 (0.6)^1 (0.4)^7 \\ + {}^8 \text{C}_2 (0.6)^2 (0.4)^6 + {}^8 \text{C}_3 (0.6)^3 (0.4)^5 \\ = 1 \times 0.0006536 + 8 \times 0.6 \times 0.0016384 \\ + 28 \times 0.36 \times 0.004096 \\ + 56 \times 0.216 \times 0.01024 \\ = 0.1736704$$

$$\text{iii) } P(X=2 \text{ or } 3) = P(2) + P(3) \\ = {}^8 \text{C}_2 (0.6)^2 (0.4)^6 + {}^8 \text{C}_3 (0.6)^3 (0.4)^5 \\ = 28 \times 0.36 \times 0.004096 + 56 \times 0.216 \times 0.01024 \\ = 0.04128768 + 0.12386304 \\ = 0.16515012$$

PRACTICAL NO-9

Normal Distribution

* Normal Distribution

Normal distribution is an example of continuous probability distribution.

i) $p(x=x) = \text{dnorm}(x, \mu, \sigma)$

ii) $p(x \leq x) = \text{pnorm}(x, \mu, \sigma)$

iii) $p(x > x) = 1 - \text{pnorm}(x, \mu, \sigma)$

iv) $p(x \leq k) = \text{pnorm}(k, \mu, \sigma)$

v) To generate a random sample of size n
 $\text{rnorm}(n, \mu, \sigma)$

ii) x follows normal distribution $\mu=10, \sigma^2=2$

to find :- i) $p(x \leq 7)$

ii) $p(x > 12)$

iii) $p(5 \leq x \leq 12)$

iv) $p(x < k) = 0.4$

iii) $x \sim N(100, 36) \sigma = \sqrt{36}$

i) $p(x \leq 110)$

ii) $p(x > 105)$

iii) $p(x \leq 92)$

iv) $p(95 \leq x \leq 110)$

v) $p(x < k) = 0.9$

iii) $x \sim N(10, 3)$ generate a 10 random sample. find sample, mean, median, variance & SD

solution ij pnorm(7, 10, 2)

[1] 0.0668072

> cat ("P(XL=7) u=" "p")

p(XL=7) u = 0.0668072

> p2 = 1 - pnorm(10, 10, 2)

> cat ("P(X>12) u=", p2)

p(X>12) u = 0.158653

> p3 = p2 - pnorm(15, 10, 2)

> cat ("P(5<=XL=12) u=", p3)

p(5<=XL=12) u = 0.1524456

> k = qnorm(10.4, 10, 2)

> cat ("P(XLK) = 0.4, K u=", k)

p(XLK) = 0.4, K u = 9.493306

iii) X=rnorm(10, 10, 3)

> X

[1] 9.195412 11.360665 5.331607 17.160876 11.912200

9.372691 12.436043 13.810705 10.908016 13.367803

> am = mean(X)

> am

[1] 11.48346

> m1 = median(X)

> m1

[1] 11.62647

> n = 10

> varainc = (n-1) * var(X)/n

> varainc

[1] 9.018713

> sd = sqrt(variance)

> sd

[1] 5.003117

840.

$$\text{ii) } \gamma_{P1} = \text{pnorm}(110, 100, 6)$$

$$[1] 0.9522096 \\ \gamma_{\text{cat}} ("p(x_L=110) v = "p1)$$

$$p(x_L=110)v = 0.95220967$$

$$\gamma_{P2} = 1 - \text{pnorm}(105, 100, 6)$$

$$\gamma_{\text{cat}} ("p(x > 105) v = "p2)$$

$$p(x > 105) v = 0.20232847$$

$$\gamma_{P3} = \text{pnorm}(92, 100, 6)$$

$$\gamma_{\text{cat}} ("p(x_L=92) v = "p3)$$

$$p(x_L=92) v = 0.091211227$$

$$\gamma_{P4} = \text{pnorm}(110, 100, 6) - \text{pnorm}(95, 100, 6)$$

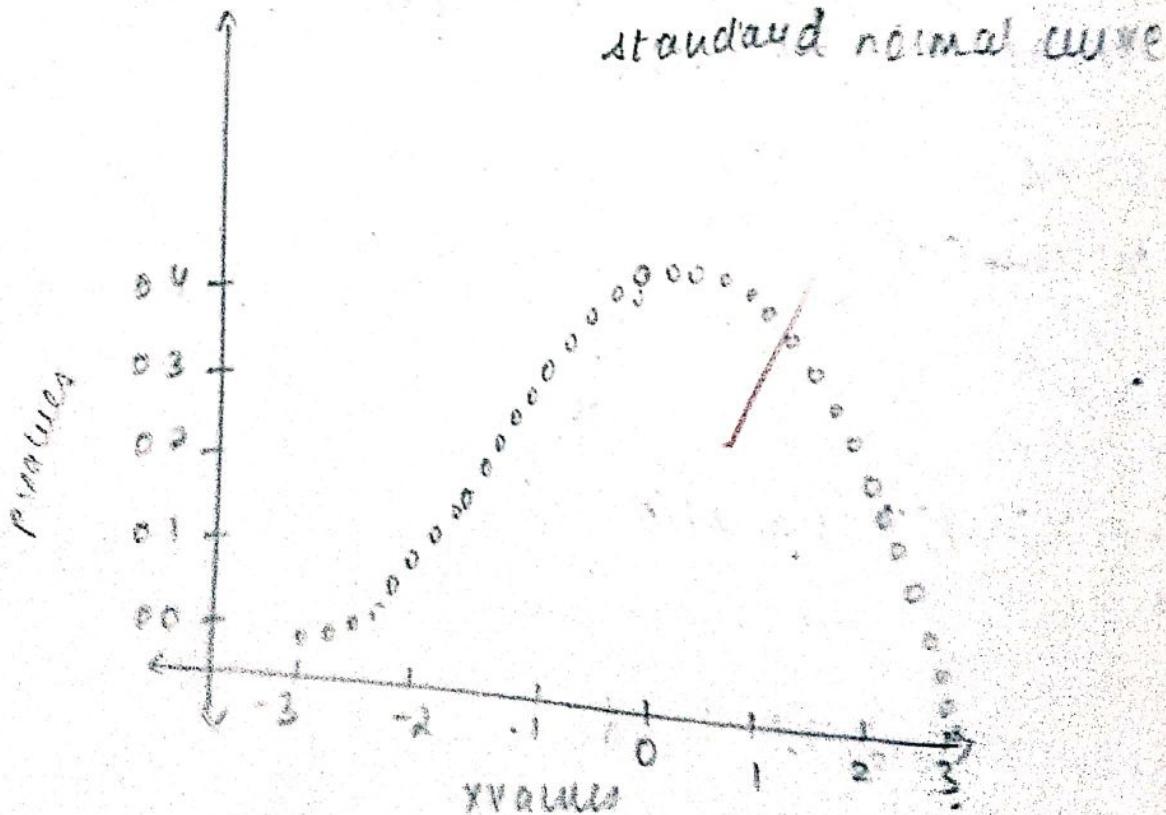
$$\gamma_{\text{cat}} ("p(95 < x_L < 110) v = "p4)$$

$$p(95 < x_L < 110) v = 0.74988137$$

$$\gamma_k = \text{pnorm}(0.9, 100, 6)$$

$$\gamma_{\text{cat}} ("p(x_L=0.9, k) v = "k)$$

$$p(x_L=k) = 0.9 k v = 107.68937$$



i) plot the standard normal curve.

$$x = seq(-3, 3, by=0.1)$$

$$y = dnorm(x)$$

plot(x, y, xlab = "x values", ylab = "probability", main = "standard normal curve")

$$x \sim N(50, 10^2)$$

$$\text{find i) } P(X \leq 60)$$

$$\text{ii) } P(X \geq 60)$$

$$\text{iii) } P(40 \leq X \leq 60)$$

$$p1 = pnorm(60, 50, 10)$$

$$cat("P(X \leq 60) is ", p1)$$

$$P(X \leq 60) \text{ is } 0.8413447$$

$$p2 = 1 - pnorm(60, 50, 10)$$

$$cat("P(X > 60) is ", p2)$$

$$P(X > 60) \text{ is } 0.668072$$

$$p3 = pnorm(60, 50, 10) - pnorm(40, 50, 10)$$

$$cat("P(40 \leq X \leq 60) is ", p3)$$

$$P(40 \leq X \leq 60) \text{ is } 0.8328072$$

PRACTICAL NO-6

z and t distribution sum

Test the hypothesis $H_0: \mu = 20$ against $H_1: \mu \neq 20$
 A sample of size 400 is selected and the sample
 mean is 20.2 and the standard deviation is 2.25
 Test at 5% level of significance

$$n = 400$$

$$m_0 = 20$$

$$m_x = 20.2$$

$$s_d = 2.25$$

$$z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$$

"calculated is ", z_{cal}

calculated is 1.777778

$$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

cat("pvalue is ", pvalue)

pvalue is 0.0754

$$\therefore 0.0754 > 0.05$$

$\therefore H_0: \mu = 20$ is accepted

1) Test the hypothesis $H_0: \mu = 250$ against $H_1: \mu \neq 250$
 A sample of size 100 has a mean of 275 & standard
 deviation 30. Check the hypothesis at 5% level of
 significance.

$$n = 100$$

$$m_0 = 250$$

$$m_x = 275$$

Q20.

$$sd = 30$$

$$z_{\text{cal}} = (m_x - m_0) / (sd / \sqrt{n})$$

z_{cal} ("z calculated is", z_{cal})

$x_{\text{calculated}}$ is 8.3333337

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

p_{value} is "pvalue", p value

P VALUE is 0.8

0 < 0.075

$H_0: \mu = 250$ is rejected

- Q3) We want to test the hypothesis $H_0: P = 0.2$ against $H_1: P \neq 0.2$ (P = population proportion). A sample of 400 is selected and the sample proportion is calculated 0.125. Test the hypothesis at 1% level of significance.

$$P = 0.2$$

$$Q = 1 - P$$

$$p = 0.125$$

$$n = 400$$

$$z_{\text{cal}} = (p - P) / \sqrt{P * Q / n}$$

x_{cal}

[1] -3.75

$$p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

p_{value} is "pvalue"

P VALUE is 0.0001768346

$\therefore P \text{ value} < 0.01$

$\therefore H_0: \mu = 0.2$ is rejected

out in a big city 325 men out of 800 men are self-employed. Does this information support the conclusion that exactly half of the men in the city are self-employed?

$$\gamma p = 325/800$$

$$\gamma p = 0.5$$

$$\gamma n = 800$$

$$\gamma q = 1 - p$$

$$\gamma z_{\text{cal}} = (p - q) / \sqrt{q(p+q)/n}$$

$$\gamma z_{\text{cal}}$$

$$[1] 2.041241$$

$$\gamma p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

γ cat["P VALUE IS", pvalue]

$$PVALUE IS 0.041222683 >$$

$$\therefore 0.0412 = 0.05$$

∴ It is rejected

Q5) Test the hypothesis $H_0: \mu = 50$ against $H_1: \mu \neq 50$

A sample of 30 is collected.
A sample of 30 is collected.
(50, 49, 52, 44, 45, 48, 46, 45, 49, 41, 45, 40, 47, 55, 54, 46, 58,
(50, 49, 52, 44, 45, 48, 46, 45, 49, 41, 45, 40, 47, 55, 54, 46, 58)
47, 44, 59, 60, 61, 41, 52, 44, 55, 56, 46, 45, 48, 49)

$$\gamma m0 = 50$$

$$\gamma x = [50, 49, 52, 44, 45, 48, 46, 45, 49, 41, 45, 40, 47, 55, 54, 46, 58]$$

$$\gamma n = \text{length}(x)$$

$$\gamma n$$

$$[1] 30$$

$$\gamma mx = \text{mean}(x)$$

$$\gamma mx$$

~~Q20~~
> variance = $(n - 1) * \text{var}(x) / n$

> variance

[1] 30.985

> sd = sqrt(variance)

> sd

[1] 5.563772

> z.cal

[1] -0.6562965

> pvalue = 2 * (1 - norm(labs(z.cal)))

> cal("pvalue is", pvalue)

PVALUE is 0.5116334

$\therefore 0.511 > 0.05$

$\therefore H_0: \mu = 50$ is accepted

~~BY
Y.D.~~

PRACTICAL NO. 7

LARGE SAMPLE TEST

Q1) Two random samples of size 1000 and 2000 are drawn from 2 population with standard deviation 2.3. Test the hypothesis that the two population means are equal to 5% level of significance. Sample means are 67 & 68 respectively.

$$H_0: \mu_1 = \mu_2 \text{ against } H_1: \mu_1 \neq \mu_2$$

$$\gamma n_1 = 1000$$

$$\gamma n_2 = 2000$$

$$\gamma m\bar{x}_1 = 67$$

$$\gamma m\bar{x}_2 = 68$$

$$\gamma s.d_1 = 2$$

$$\gamma s.d_2 = 3$$

$$\Rightarrow z_{cal} = (\bar{m}_1 - \bar{m}_2) / \sqrt{s.d_1^2/n_1 + s.d_2^2/n_2}$$

\times Cal. "z calculated is", z_{cal}

\times cal calculated is -10.8465^2

\times p value = $\Phi^{-1}(1 - \text{pnorm}(-z_{cal}))$

\times Cal "P value is", p_{value}

P value is 0

$$\therefore 0 < 0.05$$

\therefore It is rejected

Q2)

A study of noise level is done in two hospitals. Following data is calculated: first sample size = 84, mean = 61.2 , $s.d = 7.9$. Second sample size = 34, mean = 59.4 , $s.d = 7.8$. Test $H_0: \mu_1 = \mu_2$ at 1 level of significance.
 $H_0: \mu_1 = \mu_2$ against $\mu_1 \neq \mu_2$.

$$n_1 = 84$$

$$n_2 = 34$$

$$m_{x_1} = 61.2$$

$$m_{x_2} = 59.4$$

$$s.d_1 = 7.9$$

$$s.d_2 = 7.8$$

$$z_{cal} = ((m_{x_1} - m_{x_2}) / \sqrt{(s.d_1^2/n_1) + (s.d_2^2/n_2)})$$

"z calculated" is, "z_{cal}".

calculated is 1.131117

$$p\text{ value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$$

"cal" "p value" is, "pvalue".

pvalue is 0.258006

$$\therefore 0.25 > 0.05$$

∴ it is accepted.

pvalue is greater than 0.05

Q3) From each of the population of oranges the proportion of that oranges are equal to no. $n_1 = 250$, bad oranges are equal to no. $n_2 = 200$, bad oranges. Test: $p_1 = p_2$ against $p_1 \neq p_2$.

No. $p_1 = p_2$ against
 $H_1: p_1 \neq p_2$

0.64

$n_1 = 200$

$n_2 = 200$

$p_1 = 0.4 / 300$

$p_2 = 30 / 200$

$\Rightarrow (n_1 * p_1) + (n_2 * p_2) / (n_1 + n_2)$

$\Rightarrow p$

$(170 / 160) * 0.4 = 0.4375$

$\Rightarrow z = p - p$

$z = 0.8355356$

$\Rightarrow \text{value} = (p_1 / p_2) / \sqrt{p_1 * p_2 / (n_1 + n_2)}$

$\Rightarrow \text{calculated value} = 4.761$

$\Rightarrow \text{calculated} = 0.43935812$

$\Rightarrow \text{pvalue} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$

$\Rightarrow \text{calculated} \text{ pvalue} = ?$, pvalue

$\Rightarrow \text{pvalue} = 0.40968962$

\Rightarrow we accept the $H_0: p_1 = p_2$

we accept the $H_0: p_1 = p_2$

out random sample of 400 men & 600 females were asked whether they want an ACH. Among 400 males, 200 male & 390 female said in favour of the proposal. Test the hypothesis that the population of male and female favours on the proposal are equal or not at 5% level of significance.

$H_0: p_1 = p_2$ against $p_1 \neq p_2$

$$n_1 = 400$$

$$n_2 = 600$$

$$p_1 = 200/400$$

$$p_2 = 390/600$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$\chi^2$$

$$[1] 0.59$$

$$\gamma = 1 - \alpha$$

$$z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z_{\text{cal}}$$

$$[1] 4.7247$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$\gamma \text{pvalue}$$

$$[1] 2.303972e-06$$

∴ pvalue is less than 0.05, we reject $H_0: p_1 = p_2$.

Q5) Following are the two independent samples from two populations. Test equality of two population means at 5% level of significance.

$$S_1 = [74, 77, 74, 73, 79, 76, 82, 72, 75, 78, 77, 78, 76, 77]$$

$$S_2 = [70, 76, 74, 70, 70, 78, 70, 72, 75, 79, 79, 74, 76, 76]$$

$H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 \neq \mu_2$

$x_1 = [74, 77, 74, \dots, 76, 70]$

$n_1 = \text{length}(x_1)$

$m_{x_1} = \text{mean}(x_1)$

$\text{variance} = (n_1 - 1) * \text{var}(x_1)/n_1$

variance

[1] 0.4808

$s_{d1} = \sqrt{\text{variance}}$

s_{d1}

[1] 0.6714

$x_2 = [72, 76, 74, \dots, 79, 80]$

$n_2 = \text{length}(x_2)$

$m_{x_2} = \text{mean}(x_2)$

$\text{variance} = (n_2 - 1) * \text{var}(x_2)/n_2$

variance

[1] 0.6163

$s_{d2} = \sqrt{\text{variance}}$

s_{d2}

[1] 0.7800

$t_{\text{cal}} = (m_{x_1} - m_{x_2}) / \sqrt{(s_{d1}^2/n_1 + s_{d2}^2/n_2)}$

t_{cal}

[1] 1.485

t_{cal} ("t calculated is;" + (a))

(1) + calculated is: 1.485

"t test (P(T < 2))

pvalue = 0.1387

~~M
27.01¹⁰~~

it is accepted

780

PRACTICAL - 8

Aim : sample test
small

Q1) We random sample of 15 observations are given by 80, 100, 110, 105, 122, 70, 110, 100, 88, 95, 89, 107, 125. Do this data support the assumption that population mean is 100?

$\rightarrow >x = c(80, 100, 110, 105, 122, 70, 120, 110, 101, 88,$
 $83, 95, 87, 107, 125)$

$>a = \text{length}(x)$

$>a$

[1] 15

$>t = \text{t.test}(x)$

One sample t-test

data: x

$t = 24.029$, $df = 14$. p-value = 8.819×10^{-13}

alternative hypothesis: true mean is not equal to 100. 95 percent confidence interval:
 91.37775 , 109.28892

Sample estimates

mean of x

100.8333

8.819×10^{-13}
 20.05

$H_0: \mu = 100$ is rejected at 5% level of significance

10 groups of 10 students score the following marks
group 1: 18, 22, 21, 17, 20, 17, 23, 20, 22, 21
group 2: 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

Test the hypothesis that there is no significant difference
between the scores at 1% level of significance

$$g_1 = \{18, 22, 21, 17, 20, 17, 23, 20, 22, 21\}$$

$$g_2 = \{16, 20, 14, 21, 20, 18, 13, 15, 17, 21\}$$

$$gt \cdot \text{ttest}(g_1, g_2)$$

Welch two sample t-test

data: g_1 and g_2

$$t = 2.2573, df = 16.376, p\text{-value} = 0.03798$$

alternative hypothesis: true difference in means is
not equal to 0

95 percent confidence interval

$$0.1628205 \quad 5.0371795$$

sample estimates:

mean of x mean of y

$$20.1 \quad 17.5$$

$$\therefore 0.03798 > 0.01$$

∴ $H_0: \mu_x = \mu_y$ is accepted at 1% level of significance

Two types of medicines are used on 547 patients for
reducing their weight. The decrease in the weight
after using the medicines are given below.

$$A = \{10, 12, 13, 11, 14\}$$

$$B = \{8, 9, 12, 14, 15, 10, 9\}$$

To test if there is significant difference in the efficiency

$$\begin{aligned} H_0: \mu_1 = \mu_2 \\ -m_1 = C(10, 12, 13, 14, 11) \\ -m_2 = C(8, 9, 12, 14, 15, 10, 9) \end{aligned}$$

t-test (m_1, m_2)
Welch two sample t-test

data: m_1 & m_2

$t = 0.80384$, $df = 9.7594$, p-value = 0.4406

alternative hypothesis: true difference in mean
is not equal to 0

95 percent confidence interval:

-1.781171 3.781171

sample estimate

mean of x & mean of y .

12 11

$\therefore 0.4406 > 0.05$

$\therefore H_0: \mu_1 = \mu_2$ is accepted at 5% level of significance.

Q4) The weight reducing diet program is conducted & observations are noted for 10 participants. Test whether the program is effective or not.

Before - 120, 125, 115, 130, 123, 119, 122, 127, 128, 118

After - 111, 114, 107, 120, 115, 112, 112, 120, 119, 112

H_0 : there is no significance difference in weight
 H_1 : the diet program reduced weight

$$\begin{aligned} b = C(120, 125, 115, 130, 123, 119, 122, 127, 128, 118) \\ a = C(111, 114, 107, 120, 115, 112, 112, 120, 119, 112) \end{aligned}$$

t-test (b, a, paired) = 7, alternative (p = "less")

paired t-test

$t = 1.7$, df = 9, p-value =

alternative hypothesis: true difference in means
is not equal to

95 percent confidence interval:

inf 3.416556

sample estimates:

mean of the difference

8.5

± 17.05

H_0 is accepted at 5% level of significance.

sample A: 66, 67, 75, 76, 82, 84, 89, 90, 92

sample B: 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97

test the population mean are equal or not.

$H_0: \bar{x}_A = \bar{x}_B$

$\bar{x}_A = \text{c}(66, 67, 75, 76, 82, 84, 89, 90, 92)$

$\bar{x}_B = \text{c}(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

$t = \text{tstat}(9, 8)$

welch two sample t-test

data = a \cup b

$t = -1.05$, $p = 17.906$ p-value = 0.5973

alternative hypothesis: true difference in means is
not equal to 0

95 percent confidence interval:

-12.79 $\leq \bar{x}_A - \bar{x}_B \leq 1.01822$

-12.79

sample estimates $\bar{x}_A - \bar{x}_B$

80.1111

83.0000

0.54777055

520

H_0 at 5% level of significance is accepted
if following all the marks before & after a training program test whether the program is effective or not

No. 77
before - 71, 72, 74, 69, 70, 74, 76, 70, 73, 75
after - 74, 77, 74, 73, 79, 76, 82, 72, 75, 78

$\rightarrow T_B = C(71, 72, 74, 69, 70, 74, 76, 70, 73, 75)$
 $T_A = C(74, 77, 74, 73, 79, 76, 82, 72, 75, 78)$
 T_B - test (b, a, paired = 9), alternative = "less"

paired t-test

data = 62.5

$t = -4.4691$, $d_f = 9$, p-value = 0.00077284
alternative hypothesis: true diff in means is less than

$-Sty = 2.12331$

sample estimates:

mean of the differences

$\therefore 0.00077041 \pm 0.05$

H_0 is rejected at 5% level of significance

~~AM~~
03.02.20

PRACTICAL NO-9
LARGE AND SMALL SAMPLE TEST

059

- Q1) The arithmetic mean of a sample of no. of items from a large population is 52. If standard deviation is 1, test the hypothesis that the population mean is 55 against the alternative more than 55 at 5% level of significance.
- Q2) In a big city 850 out of 1000 males are found to be smokers. Does this info supports that exactly half of males in the city are smokers? Test at 1% level of significance.
- Q3) Thousand articles from a factory A are found to have 2% defectives. 1500 articles from a factory B are found to have 1% defectives. Test at 5% level that the two factories are similar or not.
- Q4) A sample of size 400 was drawn and sample mean is 99 at 5% level that the sample that comes from a population of mean 100 & variance 64?
- Q5) The flower stems are selected and heights are found to be (in cm) 63, 63, 78, 69, 71, 72. Test the hypothesis that mean height is 66 or not at 1% level of significance.
- Q6) 100 random samples were drawn from 2 normal populations. Their values are - A - 66, 67, 75, 71, 82, 84, 89, 90, 92
B - 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97
The populations have same variance at 5% level of significance.

E80

1)

$$> n = 100$$

$$> m_x = 52$$

$$> m_{\bar{x}} = 51$$

$$> s_d = 7$$

$$> z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$$

> cat("z calculated is ", z.cal)

$$\sim 4.285714$$

$$> pvalue = 2 * (1 - pnorm(zabs(z.cal)))$$

> cat("pvalue is ", pvalue)

$$pvalue \approx 1.82153 \times 10^{-5}$$

$$\therefore 1.82153 \times 10^{-5} < 0.05$$

H0: H = 55 is rejected

2.

$$> p = 0.5$$

$$> \phi = 1 - p$$

$$> p = 350/700$$

$$> n = 700$$

$$> z_{cal} = (p - P) / \sqrt{p(1-p)/n}$$

> cat("z calculated is ", z.cal)

z calculated is 0

$$> pvalue = 2 * (1 - pnorm(zabs(z.cal)))$$

> cat("pvalue is ", pvalue)

$$pvalue \approx 1$$

$$\rightarrow 0.01$$

∴ it is accepted

$$\begin{aligned} \gamma n_1 &= 1000 \\ \gamma n_2 &= 1500 \\ \gamma p_1 &= 20/1000 \\ \gamma p_2 &= 15/1500 \end{aligned}$$

$$\gamma P = (c_{n_1} * p_1) + (c_{n_2} * p_2) / (c_{n_1} + c_{n_2})$$

γP

$$[1] 0.016$$

$$\gamma q = 1 - P$$

γq

$$[1] 0.984$$

$$\gamma z_{\text{cal}} = (P_1 - P_2) / \sqrt{s_{\text{q}}} \text{ where } s_{\text{q}} = \sqrt{q * (1/q + 1/(n_1 + n_2))}$$

γ cat("z calculated is", zcal)

$$\gamma z_{\text{calculated}} \approx 2.084842$$

$$\gamma p_{\text{value}} = 2 * (1 - \text{pnorm}(abs(z_{\text{cal}})))$$

γ cat("p value is", pvalue)

$$pvalue \approx 0.03708364$$

$$\therefore 0.037 < 0.05$$

$\therefore H_0: \mu$ is rejected

$$(v) \gamma n = 400$$

$$\gamma mx = 97$$

$$\gamma mo = 100$$

$$\gamma var = 64$$

$$\gamma s^d = \sqrt{var}$$

$$\gamma z_{\text{al}} = (mx - mo) / \sqrt{var} / \sqrt{n}$$

γ cat("z calculated is", zal)

$$\gamma$$
 cat("calculated n = ", n)

γ zal ≈ 2.57

~~0.00~~
Pvalue is 0.012419337

$\therefore 0.01241 < 0.05$
H₀ is rejected at 5% level

H₀: μ

v) >x=c(63, 63.68, 69, 71, 71.72)

>a= length(x)

>a

[1] 7

>t-test(x)

One sample t-test

data : x

t = 47.94, df = 26, p-value = 5.522e-05

alternative hypothesis: true mean is not equal to
95 percent confidence interval

64.61477 71.62092

sample estimate

mean of x

18.14256

$\therefore 0.00000000572 < 0.05$

$\therefore H_0: \mu = 18.14256 \rightarrow \text{accepted}$

PRACTICAL-10

ANOVA & Chi-square test

1) Use the following data to test whether the cleanliness of home & clearness of the child independent or not

	clean	Dirty
clean	70	50
fairly clean	80	20
dirty	35	45

-> Mo & CC & CH

? $x = c(20, 80, 35, 50, 20, 45)$

? $m = 3$ (rows)

? $n = 2$ (columns)

? $y = matrix(x, nrow = m, ncol = n)$

? y

$[4,1] [1,2]$

[1,1]	70	50
[2,1]	80	20
[3,1]	35	45

? $PV = \text{chisq.test}(y)$

? PV

Pearson's chi-sq test

data: y
 χ^2 -squared = 25.646, df = 2, p-value = 2.698e-06
 \because p-value is less than 0.05, we reject
 $H_0: CC \perp CH$

Q2) use the following data to find if vaccination and a particular disease are independent or not.
 D_{ij}

Aff Not Aff

Vaccination	20	30
Given		

Not given	25	35

$\rightarrow H_0: \text{Vaccination} \perp \text{disease}$ are independent

$\rightarrow x = c(20, 25, 30, 35)$

$\rightarrow m = 2$

$\rightarrow n = 2$

$\rightarrow y = \text{matrix}(x, n = 10, m = 2, \text{ncol} = 2)$

$\rightarrow y$

	[1, 1]	[1, 2]
[1,]	20	30
[2,]	25	35

$\rightarrow py = \text{chisq.test}(y)$

Pearson's
contingency

chi-squared test with Yates' continuity

4. If all σ_i^2 are equal & H_0 : $\mu_1 = \mu_2 = \dots = \mu_k$, p-value = 1.
If p-value is greater than 0.05, we accept
 H_0 . vaccination & disease are independent. 062

No. perform a ANOVA for the following data

values	Observations
A	50, 52
B	53, 55, 53
C	60, 68, 57, 56
D	52, 54, 54, 55

H0: the means of the values are equal

X1: C (60, 57)

X2: C (53, 58, 53)

X3: C (60, 58, 57, 60)

X4: C (52, 54, 54, 55)

H1: $\exists i \neq j$ such that $\mu_i \neq \mu_j$ (i.e. $b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4$)

one way test / values ~ iid, data = d, var.equal = T

one-way analysis of means

data: values ~ iid

F = 11.735, num df = 3, denom df = 9, p-value = 0.00185

ANOVA = aov(values ~ iid, data = d)

ANOVA

all:

aov(formula = values ~ iid, data = d)

		residuals
11.735	18.16667	
11.06410	9	
3		

little do we

Residual standard error: 1.420746
Estimated effects may be unbalanced

Since p-value is less than 0.05, we reject

H₀: The means of the varieties are equal.

Q4) The following data gives the life of four brands of bulbs

Type Observation

A 20, 23, 18, 17, 18, 22, 24

B 19, 15, 17, 20, 16, 17

C 21, 19, 22, 17, 20

D 15, 14, 16, 18, 14, 16

- Test the hypothesis that the average life for the four brands are same

→ H₀: Avg life of 4 brands are same

$$\bar{x}_1 = C(20, 23, 18, 17, 18, 22, 24)$$

$$\bar{x}_2 = C(19, 15, 17, 20, 16, 17)$$

$$\bar{x}_3 = C(21, 19, 22, 17, 20)$$

$$\bar{x}_4 = C(15, 14, 16, 18, 14, 16)$$

> a = stack (list (t1 = x1, t2 = x2, t3 = x3, t4 = x4))

> names(a)

> om may test (names and, data = a, var.equi)

data = values, var.equi

$$F = 6.8945, \text{num df} = 3, \text{denom} = 12$$

One-way analysis of means

anova = 0.9 (values ~ ind. data = d)

a nor 9
call:

a o4 / formula = values ~ ind. data = d?

turns

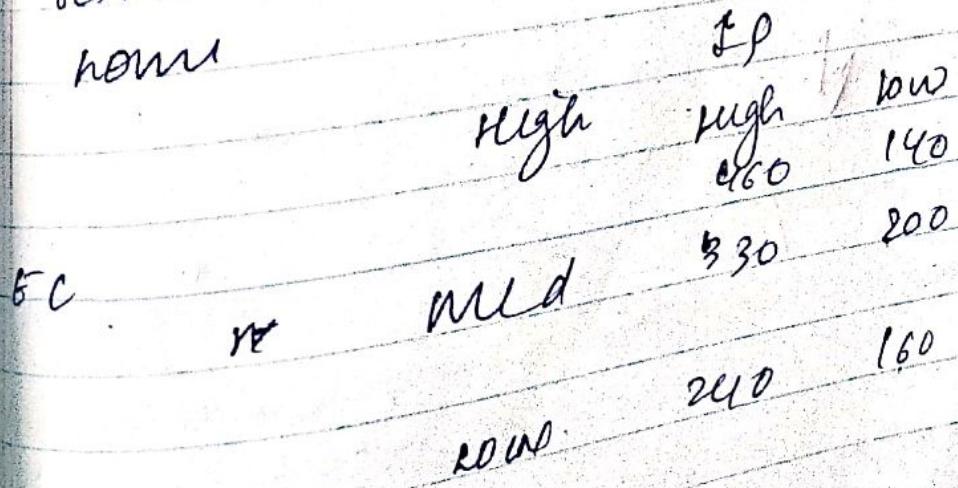
	sum of sqs	Residuals
deg of freedom	3	20
	91.4381	89.0619

residual standard error: 2.110237

estimated effects may be unbalanced

i.e. this p-value is less than 0.05, we reject H₀: all 4 types of land are same

If one thousand students of a college are graded according to their IQ and the economic condition of their home. Check that is there any association between IQ & their economic condition often home



680

→ H_0 : EC & IOP are independent

? $X = C(460, 330, 240, 140, 200, 160)$

? $M = 3$

? $n = 2$

? $y = \text{matrix}(x, nrow = M, ncol = n)$

? y

	[1, 1]	[1, 2]
[1,]	460	140
[2,]	330	200
[3,]	240	160

? $pV \equiv \text{chisq.test}(y)$

? pV

Pearson's chi-squared test

data: y

0 - square = 39.726, df = 2, p-value = 2.364e-05

∴ p-value is less than 0.05, we reject

H_0 : EC & IOP are independent.

AM

NON - Parametric test
following all the amounts of sulphur ⁰⁶⁴ and emitted
by industries. In 20 days Apply sign test. To test the
hypothesis that the population median is 21.5
 $17, 15, 20, 29, 19, 18, 22, 1, 20, 28, 9, 24, 20, 17, 6, 24, 14,$
 $18, 25, 24, 26$

H_0 : population median is 21.5

? DCC Data

? median = 21.5

? n = length (x (k, m))

? n = sptsh

? $\bar{x}_p = \text{length}(x(k, m))$

? n

? \bar{x}_p

? $p = p_{\text{fionom}}(g_p, n, 0.5)$

? p

(1) 0.419015

Since $p < \alpha$ and α more than 0.05 we accept H_0 : population
median is 21.5

Following are the 10 observation 612, 619, 631, 628, 643,
640, 655, 640, 670, 663

Apply sign test for hypothesis the population
median is 625 against the alternative th is greater
than 625 at 1% level.

One way if the alternative is greater than population
median is 625

100
? \bar{x} = c (data)

? $m_{ed} = 62.5$

? $s_n = \text{length}(\mathbf{x}(\mathbf{x} > m_{ed}))$

? $s_p = \text{length}(\mathbf{x}(\mathbf{x} < m_{ed}))$

? $n = s_p + s_n$

[1] 10

? $p_v = \text{ptnom}(s_n, n, 0.5)$

? p_x

(17) 0.0546875

∴ Since p-value is more than 0.01. ∴ we accept the H_0 population median is 62.5.

* 10 observations are

36, 32, 21, 30, 24, 25, 20, 22, 20, 18

using sign test. Test the hypothesis is 25 against the alternative it is less than 25 at 5% level

SOLN:-

H_0 : population median is 25

? $\mathbf{x} = \mathbf{c}(\text{data})$

? $m_{ed} = 25$

? $s_p = \text{length}(\mathbf{x}(\mathbf{x} > m_{ed}))$

? $s_n = \text{length}(\mathbf{x}(\mathbf{x} < m_{ed}))$

? $n = s_p + s_n$

? n

[17] 9

? $p_v = \text{ptnom}(s_n, n, 0.5)$

? p_x

[1] 0.25 390(3)

if p-value is more than 0.05 we accept H₀: population median is 25

for the following are same mean moments -
 63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39, 72, 5
 using wilcoxon signed rank test. test H₀:
 hypothesis that the population median is 60
 against the alternative it is greater than 60 at
 5% LOS

H₀: population median is 60
 7 DEC (Data)

wilcox : test (n, alt = "grate", mu=60)

wilcoxon signed rank test with continuity
 correction

data : x

n=68, p-value = 0.06181

alternative hypothesis: true location is greater than
 60

since p-value is greater than 0.05, we accept

H₀: population median is 60

15, 17, 29, 125, 120, 21, 32, 28, 12, 25, 24, 21
 wilcoxon signed rank test. test the hypothesis
 that the population median is 20 against H₁
 alternative it is less than 20 at 5% LOS

- solⁿ:
- ✓ H_0 : population median is 20
 - ✓ $x = C(\text{Data})$
 - ✓ wilcoxon test (X , alt = "less", $\mu_0 = 20$)
 - wilcoxon signed rank test with continuity correction
 - data: x
 - $V = 48.5$ p-value = 0.932
 - alternative hypothesis: true location is less than 20.
 - since, p-value is greater than 0.05, we accept H_0 : population median is 20

Q) $(20, 25, 27, 30, 18)$ Test the hypothesis that the population median is 25, against the alternative, is not 25

- ✓ $x = C(20, 25, 27, 30, 18)$
- ✓ wilcoxon test (X , alt = "two.sided", $\mu_0 = 25$)
- wilcoxon signed Rank Test with continuity correction

data: x

$$V = 3.5, \text{ p-value} = 0.7127$$

alternative hypothesis: true location is not equal to

$$\therefore 0.7127 > 0.05$$

$\therefore H_0$ is accepted $\cancel{H_1}$ $\alpha = 0.05$