

Inverse power method :-

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{bmatrix} \quad X_0 = (1, 1, 1)^T, \quad \sigma = 9$$

[I] $X_0 = (1, 1, 1)^T$

$$AX = [6 \quad 9 \quad 12]^T$$

{ divide by smallest value }

Thus,

$$\lambda^{(1)} = 6$$

$$\hat{X}^{(1)} = [1 \quad 1.5 \quad 2]^T$$

$$X^{(1)} = \frac{\hat{X}^{(1)}}{\|X^{(1)}\|_2} = \frac{1}{2.693} [0.371 \quad 0.557 \quad 0.742]^T$$

sum =

$$[\text{II}] \quad AX^{(1)} = [3.714 \quad 5.385 \quad 7.056]^T$$

$$\lambda^{(2)} = 3.714$$

$$\hat{X}^{(2)} = [1 \quad \overset{1.449}{\cancel{0.684}} \quad 1.899]^T \quad \& \quad \|\hat{X}\|_2 = 2.589$$

$$X^{(2)} = \frac{\hat{X}^{(2)}}{\|\hat{X}\|_2} = \begin{bmatrix} \cancel{0.443} & \cancel{0.305} & \cancel{0.841} \\ 0.386 & 0.559 & 0.733 \end{bmatrix}^T$$