

1. (a)

$$\begin{aligned}
 T(n) &= T\left(\frac{n}{2}\right) + 10 \\
 T\left(\frac{n}{2}\right) &= T\left(\frac{n}{4}\right) + 10 \\
 &\dots \\
 T\left(\frac{n}{n \div 2}\right) &= T\left(\frac{n}{n}\right) + 10 \\
 T\left(\frac{n}{n}\right) &= a \\
 T\left(\frac{n}{n \div 2}\right) &= a + 10 \\
 T\left(\frac{n}{n \div 4}\right) &= (a + 10) + 10 \\
 &\dots \\
 T(n) &= a + 10 \log_2 n
 \end{aligned}$$

$$\begin{aligned}
 F(n) &= \log_2 n \\
 T(n) &\text{ is } O(F(n))
 \end{aligned}$$

(b)

$$\begin{aligned}
 T(n) &= T\left(\frac{n}{2}\right) + n^2 \\
 T\left(\frac{n}{2}\right) &= T\left(\frac{n}{4}\right) + \left(\frac{n}{2}\right)^2 \\
 &\dots \\
 T\left(\frac{n}{n \div 2}\right) &= T\left(\frac{n}{n}\right) + \left(\frac{n}{n \div 2}\right)^2 \\
 T\left(\frac{n}{n}\right) &= a \\
 &\dots \\
 T\left(\frac{n}{n \div 2}\right) &= a + \left(\frac{n}{n \div 2}\right)^2 \\
 T\left(\frac{n}{n \div 4}\right) &= \left(a + \left(\frac{n}{n \div 2}\right)^2\right) + \left(\frac{n}{n \div 4}\right)^2 \\
 &\dots \\
 T(n) &= n^2 + \left(a + \left(\frac{n}{n \div 2}\right)^2\right) + \left(\frac{n}{n \div 4}\right)^2 + \left(\frac{n}{n \div 8}\right)^2 + \dots
 \end{aligned}$$

$$\begin{aligned}
 F(n) &= n^2 \\
 T(n) &\text{ is } O(F(n))
 \end{aligned}$$

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2. int[]arr = { ...};
   int n = arr.length;
   int result = ArraySum( arr, n );
   ArraySum( arr, n ) = ArraySum( arr, n - 1 ) + arr[ n - 1 ]
   ArraySum( arr, n - 1 ) = ArraySum( arr, n - 2 ) + arr[ n - 2 ]
   ...
   ArraySum( arr, n - (n - 2)) = ArraySum( arr, n - (n - 1)) + arr[1]
   ArraySum( arr, n - (n - 1) = arr[0]

   ArraySum(arr, n - (n - 2)) = arr[0] + arr[1];
   ...
   ArraySum(arr, n - 1) = (arr[n - 3] + arr[n - 4] + ... + arr[0]) + arr[n - 2]
   ArraySum(arr, n) = (arr[n - 2] + arr[n - 3] + ... + arr[0]) + arr[n - 1]

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Then, $result = arr[n - 1] + arr[n - 2] + \dots + arr[0]$

There are 2 process when call the ArraySum() ① the return ② the summation.

Let R is the return time, and S is the summation time.

Answer $T(\text{ArraySum}(\text{arr}, n)) = nR + (n - 1)S$