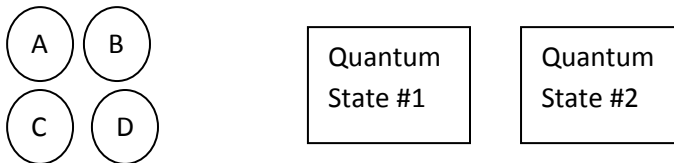


Problem Set #5: Statistical Mechanics

1.

- (a) Explain the difference(s) in the conditions of particles that can be described by the Maxwell-Boltzmann, Fermi-Dirac, and Bose-Einstein distributions.
- (b) Provide an example of a particle which obeys (i) Maxwell-Boltzmann distribution, (ii) Fermi-Dirac distribution, and (iii) Bose-Einstein distribution.
- (c) There exists an isolated system consisting of four particles which can occupy two distinct quantum states. Assuming these particles obey Maxwell-Boltzmann statistics, determine the probability of *each* possible distribution of the four particles among the two quantum states. Assume no degeneracy.



2. Consider the density of states per unit energy, $g(E)$, of a free-electron gas is given below. Calculate the number of states in a 1cm^3 volume between the energies of 0 and 1eV :

$$g(E)dE = \frac{8\sqrt{2}\pi V}{h^3} m^{3/2} \sqrt{E} dE$$

where V is the volume containing the gas and m is the mass of an electron.

3. Show that for a particle which obeys Fermi-Dirac statistics, the probability of a state a distance ΔE above E_f being filled is the same as the probability of a state a distance ΔE below E_f being empty.