# Linear Regression - US State Environmental Impact

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# Exercise 1: Least Squares Regression

Use the /states.rds/ data set. Fit a model predicting energy consumed per capita (energy) from the percentage of residents living in metropolitan areas (metro). Be sure to:

- 1. Examine/plot the data before fitting the model
- 2. Print and interpret the model 'summary'
- 3. 'plot' the model to look for deviations from modeling assumptions

Select one or more additional predictors to add to your model and repeat steps 1-3. Is this model significantly better than the model with /metro/ as the only predictor?

Load the required library.

```
library(ggplot2)
```

#### **Data Examination**

The dataset is some general US states statistical data from 1990-1991 that appears to be used to examine each of the state's environmental impact based on some of the potential key statistical characteristics. The data includes geographical information such as general population (in square miles, % in metropolitan area), and land area; environmental impact information such as per capita solid waste, energy consumed, toxics released, greenhouse gas; political voting performance in both house and senate (see this link); people's educational level such as mean SAT scores, % of adult high school and college graduates; and some financial details such as per pupil expenditures (primary & secondary schools) (see this link) and household incomes.

This exercise can be found on this website.

Loading the data:

```
# Set working directory
setwd("C:/Users/Chinpei/Documents/GitHub/Springboard_FDS/linear_regression")
# Read the states data. Note that the data is is RDS format
states.data <- readRDS("dataSets/states.rds")</pre>
```

Examining the data:

```
str(states.data)
```

```
## $ energy : int 393 991 258 330 246 273 234 349 NA 237 ...
## $ miles : num 10.5 7.2 9.7 8.9 8.7 ...
## $ toxic : num 27.86 37.41 19.65 24.6 3.26 ...
## $ green : num 29.2 NA 18.4 26 15.6 ...
   $ house : int 30 0 13 25 50 36 64 69 NA 45 ...
## $ senate : int 10 20 33 37 47 58 87 83 NA 47 ...
  $ csat : int 991 920 932 1005 897 959 897 892 840 882 ...
##
   $ vsat
           : int 476 439 442 482 415 453 429 428 405 416 ...
##
   $ msat : int 515 481 490 523 482 506 468 464 435 466 ...
   $ percent: int 8 41 26 6 47 29 81 61 71 48 ...
   $ expense: int 3627 8330 4309 3700 4491 5064 7602 5865 9259 5276 ...
   $ income : num 27.5 48.3 32.1 24.6 41.7 ...
## $ high : num 66.9 86.6 78.7 66.3 76.2 ...
## $ college: num 15.7 23 20.3 13.3 23.4 ...
   - attr(*, "datalabel")= chr "U.S. states data 1990-91"
   - attr(*, "time.stamp")= chr " 6 Apr 2012 08:40"
   - attr(*, "formats")= chr "%20s" "%9.0g" "%9.0g" "%9.0g" ...
   - attr(*, "types")= int 20 251 254 254 254 254 254 252 254 254 ...
  - attr(*, "val.labels")= chr "" "region" "" "" ...
   - attr(*, "var.labels")= chr "State" "Geographical region" "1990 population" "Land area, square mi
##
  - attr(*, "expansion.fields")=List of 4
    ..$ : chr "_dta" "_lang_c" "default"
    ..$ : chr "_dta" "_lang_list" "default"
##
    ..$ : chr "_dta" "__xi__Vars__To__Drop__" "_Iregion_2 _Iregion_3 _Iregion_4 _IregXperce_2 _IregXp
    ..$ : chr "_dta" "__xi__Vars__Prefix__" "_I _I _I _I _I _I"
  - attr(*, "version")= int 12
  - attr(*, "label.table")=List of 1
##
    ..$ region: Named int 1 2 3 4
     ....- attr(*, "names")= chr "West" "N. East" "South" "Midwest"
```

#### summary(states.data)

```
##
      state
                         region
                                     pop
                                                       area
                                                   Min. : 1045
  Length:51
                     West :13
                                 Min. : 454000
                                 1st Qu.: 1299750
                                                   1st Qu.: 36802
## Class :character
                     N. East: 9
## Mode :character
                     South:16
                                 Median : 3390500
                                                   Median : 54156
##
                                 Mean : 4962040
                                                   Mean : 70759
                     Midwest:12
##
                     NA's : 1
                                 3rd Qu.: 5898000
                                                   3rd Qu.: 81272
##
                                 Max. :29760000
                                                   Max. :570374
##
                                 NA's
                                      :1
                                                   NA's
                                                         : 1
##
      density
                       metro
                                       waste
                                                       energy
   Min. : 0.96
                    Min. : 20.40
                                   Min. :0.5400
                                                   Min. :200.0
   1st Qu.: 31.88
##
                    1st Qu.: 46.98
                                    1st Qu.:0.8225
                                                   1st Qu.:285.0
  Median : 75.76
##
                    Median : 67.55
                                    Median :0.9600
                                                   Median :320.0
        : 166.04
                    Mean : 64.07
                                    Mean :0.9888
                                                    Mean :354.5
   Mean
   3rd Qu.: 170.29
                    3rd Qu.: 81.58
                                    3rd Qu.:1.1450
                                                    3rd Qu.:371.5
##
        :1041.92
                    Max. :100.00
                                    Max. :1.5100
                                                          :991.0
   Max.
                                                    Max.
                    NA's :1
                                    NA's :1
##
  NA's
                                                    NA's
         :1
                                                         :1
##
       miles
                       toxic
                                       green
                                                       house
## Min. : 5.900
                   Min. : 0.770
                                    Min. : 11.76
                                                   Min. : 0.00
## 1st Qu.: 8.500
                                    1st Qu.: 16.98
                                                   1st Qu.:31.00
                  1st Qu.: 6.737
## Median : 9.100
                   Median : 11.705
                                    Median : 21.38
                                                   Median :44.50
## Mean : 9.046
                   Mean : 17.606
                                    Mean : 25.11
                                                    Mean :44.82
## 3rd Qu.: 9.700 3rd Qu.: 21.488
                                    3rd Qu.: 26.34
                                                   3rd Qu.:59.25
```

```
:12.800
                               :101.280
                                                                      :85.00
##
    Max.
                       Max.
                                           Max.
                                                   :114.40
                                                              Max.
            :1
##
    NA's
                       NA's
                                           NA's
                                                   :3
                                                              NA's
                               :1
                                                                      :1
##
        senate
                            csat
                                               vsat
                                                                msat
                              : 832.0
##
    Min.
            :10.00
                      Min.
                                         Min.
                                                 :395.0
                                                           Min.
                                                                   :435.0
##
    1st Qu.:27.00
                      1st Qu.: 888.0
                                         1st Qu.:421.0
                                                           1st Qu.:467.0
                      Median: 926.0
                                         Median :441.0
                                                           Median :485.0
##
    Median :51.00
##
    Mean
            :49.78
                      Mean
                              : 944.1
                                         Mean
                                                 :447.8
                                                           Mean
                                                                   :496.3
##
    3rd Qu.:67.00
                      3rd Qu.: 997.0
                                         3rd Qu.:476.0
                                                           3rd Qu.:521.5
##
    Max.
            :97.00
                      Max.
                              :1093.0
                                         Max.
                                                 :515.0
                                                           Max.
                                                                   :578.0
##
    NA's
            :1
##
       percent
                                           income
                                                              high
                         expense
##
    Min.
            : 4.00
                      Min.
                              :2960
                                       Min.
                                               :23.46
                                                        Min.
                                                                :64.30
                      1st Qu.:4352
                                       1st Qu.:29.88
##
    1st Qu.:11.00
                                                        1st Qu.:73.50
                                       Median :33.45
##
    Median :26.00
                      Median:5000
                                                        Median :76.70
##
    Mean
            :35.76
                      Mean
                              :5236
                                       Mean
                                               :33.96
                                                        Mean
                                                                :76.26
##
    3rd Qu.:60.50
                      3rd Qu.:5794
                                       3rd Qu.:36.92
                                                        3rd Qu.:80.10
##
    Max.
            :81.00
                              :9259
                                       Max.
                                               :48.62
                                                                 :86.60
                      Max.
                                                        Max.
##
##
       college
##
    Min.
            :12.30
##
    1st Qu.:17.30
    Median :19.30
##
##
    Mean
            :20.02
##
    3rd Qu.:22.90
##
    Max.
            :33.30
##
```

Upon examining the data frame, it is found that there are attributes that describing the dataset. The following command was used to examine what the attributes mean:

```
states.info <- data.frame(attributes(states.data)[c("datalabel", "time.stamp",
    "formats", "types", "val.labels", "var.labels", "expansion.fields", "version", "names")])</pre>
```

The author is unable to examine the "label.table" attributes. However, the rest of the attributes look like the following:

- datalabel: basically just says that these are U.S. states data in 1990-1991.
- time.stamp: the time the data is downloaded. They are all on Apr 6, 2012.
- formats: the data format: string, number format with the number of digits and decimal points.
- types: not exactly sure, but it looks like the amount of memory required.
- region: not exactly sure either, but there is only one data entry for "Geograhical region".
- var.labels: these labels explains what each of the name of the variable means, which is important.
- expansion.field: not exactly sure, but it looks like more attributes to each of the variable.
- version: probably the version of this dataset, which is 12 for all of them.
- names: the variable names, which is important.

```
data.frame(attributes(states.data)[c("names", "var.labels")])
```

```
## names var.labels
## 1 state State
## 2 region Geographical region
## 3 pop 1990 population
```

```
## 4
                      Land area, square miles
         area
## 5
                       People per square mile
      density
## 6
        metro Metropolitan area population, %
## 7
                 Per capita solid waste, tons
        waste
## 8
       energy Per capita energy consumed, Btu
## 9
        miles
                 Per capita miles/year, 1,000
        toxic Per capita toxics released, lbs
## 10
        green Per capita greenhouse gas, tons
## 11
## 12
        house
                 House '91 environ. voting, %
## 13
       senate
                Senate '91 environ. voting, %
## 14
                     Mean composite SAT score
         csat
                        Mean verbal SAT score
## 15
         vsat
## 16
                          Mean math SAT score
         msat
     percent
                    % HS graduates taking SAT
## 17
     expense Per pupil expenditures prim&sec
## 18
       income Median household income, $1,000
## 20
         high
                           % adults HS diploma
## 21 college
                      % adults college degree
```

Now, we look into the energy consumed per capita (energy) from the percentage of residents living in metropolitan areas (metro).

For analysis convenience, gather the states.data with only the numerical values into states.data.num, also removed all the NA's.

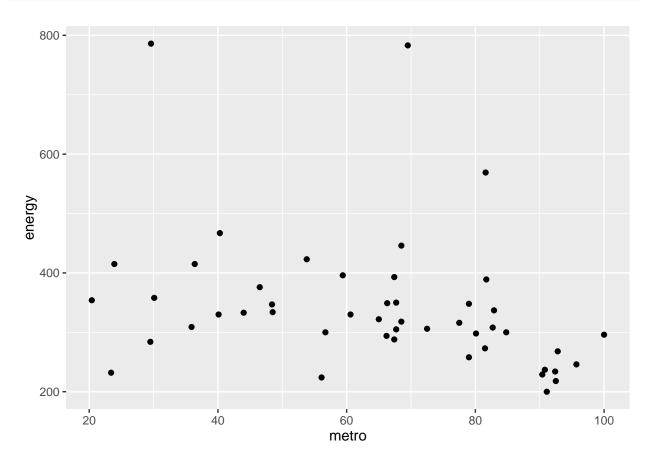
```
states.data.num <- states.data[c("pop", "area", "density", "metro", "waste", "energy",
"miles", "toxic", "green", "house", "senate", "csat", "vsat", "msat", "percent",
"expense", "income", "high", "college")]
states.data.num <- na.omit(states.data.num)
summary(states.data.num)</pre>
```

```
##
         pop
                              area
                                              density
                                                                  metro
##
                                : 1045
                                                      4.68
                                                                     : 20.40
    Min.
              454000
                        Min.
                                          Min.
                                                              Min.
    1st Qu.: 1562250
                        1st Qu.: 38666
                                           1st Qu.:
                                                     32.13
                                                              1st Qu.: 47.92
                                                              Median : 67.55
    Median : 3576000
                        Median : 54156
                                          Median :
                                                    75.76
##
##
    Mean
           : 5134250
                        Mean
                                : 61691
                                          Mean
                                                 : 169.35
                                                              Mean
                                                                     : 64.31
##
    3rd Qu.: 6058750
                        3rd Qu.: 80169
                                          3rd Qu.: 170.41
                                                              3rd Qu.: 81.62
##
    Max.
           :29760000
                        Max.
                                :261914
                                          Max.
                                                  :1041.92
                                                              Max.
                                                                     :100.00
##
        waste
                          energy
                                            miles
                                                              toxic
##
            :0.5400
                              :200.0
                                               : 5.900
                                                                 : 1.810
    Min.
                      Min.
                                       Min.
                                                         Min.
##
    1st Qu.:0.8150
                      1st Qu.:287.0
                                       1st Qu.: 8.500
                                                          1st Qu.: 7.232
##
    Median :0.9600
                      Median :320.0
                                       Median : 9.150
                                                         Median: 11.705
##
    Mean
            :0.9867
                      Mean
                              :343.6
                                       Mean
                                               : 9.121
                                                         Mean
                                                                 : 17.544
##
                      3rd Qu.:362.5
                                       3rd Qu.: 9.725
    3rd Qu.:1.1350
                                                          3rd Qu.: 21.363
##
    Max.
           :1.5100
                      Max.
                              :786.0
                                       Max.
                                               :12.800
                                                          Max.
                                                                 :101.280
##
        green
                          house
                                            senate
                                                              csat
##
           : 11.76
                              : 0.00
                                               :10.00
                                                                : 832.0
    Min.
                      Min.
                                       Min.
                                                         Min.
##
    1st Qu.: 16.98
                      1st Qu.:31.00
                                       1st Qu.:27.00
                                                         1st Qu.: 890.0
    Median : 21.38
                      Median :44.50
                                       Median :52.50
                                                         Median: 939.0
##
    Mean
           : 25.11
                      Mean
                              :44.92
                                       Mean
                                               :50.40
                                                         Mean
                                                                : 948.0
    3rd Qu.: 26.34
                      3rd Qu.:57.75
                                       3rd Qu.:67.75
                                                         3rd Qu.: 998.2
##
                                                                :1093.0
##
    Max.
            :114.40
                      Max.
                              :85.00
                                       Max.
                                               :97.00
                                                         Max.
                                         percent
##
         vsat
                          msat
                                                           expense
                                      Min.
##
                                              : 4.00
                                                               :2960
    Min.
            :395.0
                     Min.
                             :437.0
                                                       Min.
```

```
1st Qu.:423.2
                    1st Qu.:467.5
                                     1st Qu.:11.00
                                                     1st Qu.:4340
##
    Median :446.0
                    Median :493.0
                                     Median :23.50
                                                     Median:4920
                    Mean
                                     Mean
                                           :34.52
                                                      Mean
                                                             :5089
##
           :449.8
                           :498.2
    3rd Qu.:476.0
                    3rd Qu.:522.2
                                     3rd Qu.:60.25
                                                      3rd Qu.:5693
##
##
    Max.
           :515.0
                    Max.
                            :578.0
                                     Max.
                                            :81.00
                                                      Max.
                                                             :8645
##
        income
                         high
                                        college
##
           :23.46
                            :64.30
                                            :12.30
    Min.
                    Min.
                                     Min.
    1st Qu.:29.30
                    1st Qu.:73.45
                                     1st Qu.:17.15
##
##
    Median :32.28
                    Median :76.70
                                     Median :18.85
           :33.38
                                           :19.62
##
    Mean
                    Mean
                            :76.03
                                     Mean
    3rd Qu.:36.20
                    3rd Qu.:80.03
                                     3rd Qu.:21.92
           :48.62
                            :85.10
                                            :27.20
##
    Max.
                    Max.
                                     Max.
```

Look at the scattered plot and correlation between metro and energy data.

```
energy.metro.baseplot <- ggplot(states.data.num, aes(x = metro, y = energy)) + geom_point(size = 1.5)
energy.metro.baseplot</pre>
```



```
cor(subset(states.data.num, select = c("metro", "energy")))
```

```
## metro energy
## metro 1.0000000 -0.3116753
## energy -0.3116753 1.0000000
```

It can be noticed that there are not too much correlations.

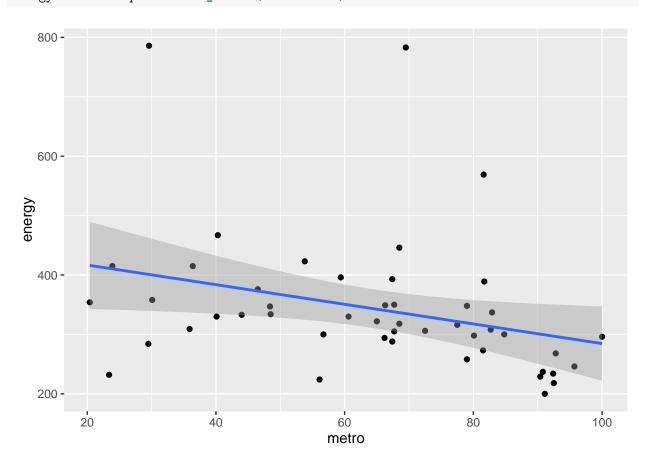
## Linear Regression

Perform a linear regression between energy and metro:

```
summary(lm(energy~metro, data = states.data.num))
```

```
##
## Call:
## lm(formula = energy ~ metro, data = states.data.num)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -179.17 -54.21 -21.64
                            15.07 448.02
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                                    8.917 1.37e-11 ***
## (Intercept) 449.8382
                          50.4472
                                             0.031 *
               -1.6526
                           0.7428 -2.225
## metro
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 112.3 on 46 degrees of freedom
## Multiple R-squared: 0.09714, Adjusted R-squared: 0.07751
## F-statistic: 4.949 on 1 and 46 DF, p-value: 0.03105
```

#### energy.metro.baseplot + stat\_smooth(method = lm)



Now, look the correlation between energy and all the other variables.

```
summary(lm(energy ~ ., data = states.data.num))
##
## Call:
## lm(formula = energy ~ ., data = states.data.num)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -126.554 -27.297
                        0.968
                                21.840
                                       159.899
##
## Coefficients: (1 not defined because of singularities)
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -4.536e+01 5.083e+02 -0.089 0.929477
              -1.707e-06 3.568e-06 -0.478 0.635888
## pop
               6.663e-04 3.708e-04
## area
                                      1.797 0.082403 .
## density
              -1.279e-02 8.882e-02 -0.144 0.886504
## metro
               6.069e-01 9.384e-01
                                       0.647 0.522692
## waste
               1.316e+01 5.415e+01
                                       0.243 0.809631
## miles
               1.188e+01 1.511e+01
                                       0.786 0.438014
## toxic
               2.759e+00 6.682e-01
                                      4.130 0.000267 ***
               4.426e+00 9.524e-01
                                      4.647 6.3e-05 ***
## green
## house
               1.071e-01 9.896e-01 0.108 0.914513
               1.348e-01 6.385e-01
                                      0.211 0.834171
## senate
## csat
               -2.084e-01
                          2.055e+00 -0.101 0.919910
## vsat
               7.732e-01
                          4.314e+00
                                       0.179 0.858958
## msat
                      NA
                                 NA
                                         NA
                                                   NA
               8.668e-01
## percent
                          1.463e+00
                                       0.593 0.557933
## expense
               1.244e-02
                          1.558e-02
                                      0.799 0.430823
## income
               9.697e-01
                          4.671e+00
                                       0.208 0.836945
## high
              -1.582e+00 3.545e+00 -0.446 0.658682
              -6.541e+00 5.768e+00 -1.134 0.265771
## college
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 63.12 on 30 degrees of freedom
## Multiple R-squared: 0.8141, Adjusted R-squared: 0.7087
## F-statistic: 7.726 on 17 and 30 DF, p-value: 7.656e-07
Progressively removing the variable that has low correlations:
summary(lm(energy ~ . - msat,
          data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat, data = states.data.num)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -126.554 -27.297
                        0.968
                               21.840
                                       159.899
##
```

```
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.536e+01 5.083e+02 -0.089 0.929477
## pop
             -1.707e-06 3.568e-06 -0.478 0.635888
## area
              6.663e-04 3.708e-04
                                    1.797 0.082403 .
              -1.279e-02 8.882e-02 -0.144 0.886504
## density
## metro
              6.069e-01 9.384e-01 0.647 0.522692
              1.316e+01 5.415e+01 0.243 0.809631
## waste
              1.188e+01 1.511e+01 0.786 0.438014
## miles
## toxic
              2.759e+00 6.682e-01 4.130 0.000267 ***
## green
              4.426e+00 9.524e-01 4.647 6.3e-05 ***
              1.071e-01 9.896e-01 0.108 0.914513
## house
## senate
              1.348e-01 6.385e-01 0.211 0.834171
## csat
              -2.084e-01 2.055e+00 -0.101 0.919910
## vsat
              7.732e-01 4.314e+00 0.179 0.858958
## percent
              8.668e-01 1.463e+00 0.593 0.557933
             1.244e-02 1.558e-02
                                   0.799 0.430823
## expense
## income
              9.697e-01 4.671e+00
                                     0.208 0.836945
              -1.582e+00 3.545e+00 -0.446 0.658682
## high
## college
              -6.541e+00 5.768e+00 -1.134 0.265771
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 63.12 on 30 degrees of freedom
## Multiple R-squared: 0.8141, Adjusted R-squared: 0.7087
## F-statistic: 7.726 on 17 and 30 DF, p-value: 7.656e-07
summary(lm(energy ~ . - msat - csat,
          data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat, data = states.data.num)
## Residuals:
       Min
                 1Q
                     Median
                                  3Q
                      0.531
## -125.408 -26.758
                              21.956 159.236
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.718e+01 4.998e+02 -0.094
                                           0.9254
## pop
              -1.870e-06 3.133e-06 -0.597
                                            0.5550
## area
              6.596e-04 3.590e-04
                                    1.838
                                            0.0757 .
              -1.197e-02 8.703e-02 -0.138
                                            0.8915
## density
## metro
              6.107e-01 9.226e-01 0.662
                                            0.5129
## waste
              1.410e+01 5.249e+01 0.269
                                            0.7901
## miles
              1.213e+01 1.465e+01 0.828
                                            0.4139
## toxic
              2.784e+00 6.130e-01 4.541 7.96e-05 ***
## green
              4.405e+00 9.154e-01 4.812 3.68e-05 ***
              8.952e-02 9.586e-01 0.093
## house
                                            0.9262
## senate
              1.303e-01 6.267e-01
                                     0.208
                                            0.8366
## vsat
              3.466e-01 9.358e-01 0.370
                                            0.7137
## percent
              9.070e-01 1.385e+00
                                     0.655
                                            0.5175
              1.221e-02 1.517e-02 0.805 0.4268
## expense
```

```
## income
             9.456e-01 4.590e+00 0.206
                                           0.8381
             -1.640e+00 3.443e+00 -0.476
## high
                                           0.6373
## college
             -6.548e+00 5.675e+00 -1.154
                                           0.2574
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 62.11 on 31 degrees of freedom
## Multiple R-squared: 0.814, Adjusted R-squared: 0.718
## F-statistic: 8.479 on 16 and 31 DF, p-value: 2.551e-07
summary(lm(energy ~ . - msat - csat - house,
   data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house, data = states.data.num)
##
## Residuals:
##
       Min
                1Q
                   Median
                                 3Q
                                         Max
## -124.337 -26.903 0.999
                             22.001 159.290
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.396e+01 4.908e+02 -0.090 0.9292
             -1.843e-06 3.071e-06 -0.600 0.5527
## pop
## area
              6.515e-04 3.429e-04
                                   1.900 0.0665 .
## density
             -9.338e-03 8.106e-02 -0.115 0.9090
## metro
             5.834e-01 8.612e-01 0.677
                                          0.5030
             1.529e+01 5.011e+01 0.305
## waste
                                           0.7622
## miles
             1.239e+01 1.416e+01 0.875
                                           0.3881
## toxic
             2.783e+00 6.034e-01 4.612 6.11e-05 ***
             4.360e+00 7.637e-01 5.709 2.53e-06 ***
## green
             1.514e-01 5.754e-01 0.263 0.7941
## senate
             3.343e-01 9.121e-01 0.367
## vsat
                                          0.7164
## percent
             9.077e-01 1.364e+00 0.666 0.5105
             1.224e-02 1.493e-02 0.820 0.4182
## expense
## income
              8.993e-01 4.492e+00 0.200
                                           0.8426
## high
             -1.560e+00 3.284e+00 -0.475 0.6380
## college
             -6.554e+00 5.586e+00 -1.173 0.2494
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 61.14 on 32 degrees of freedom
## Multiple R-squared: 0.814, Adjusted R-squared: 0.7267
## F-statistic: 9.333 on 15 and 32 DF, p-value: 8.099e-08
summary(lm(energy ~ . - msat - csat - house - density,
    data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density, data = states.data.num)
##
```

```
## Residuals:
                1Q Median
##
       Min
                                 3Q
                                         Max
## -124.852 -27.320 0.665 22.770 159.910
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.811e+01 4.821e+02 -0.100 0.9211
             -1.726e-06 2.854e-06 -0.605
## pop
                                          0.5495
## area
              6.491e-04 3.371e-04
                                   1.925
                                           0.0628 .
             5.663e-01 8.356e-01 0.678
## metro
                                          0.5027
## waste
             1.452e+01 4.891e+01 0.297 0.7684
              1.281e+01 1.348e+01 0.951
## miles
                                           0.3487
## toxic
              2.779e+00 5.933e-01 4.684 4.67e-05 ***
## green
              4.344e+00 7.398e-01 5.871 1.41e-06 ***
## senate
             1.454e-01 5.644e-01 0.258
                                           0.7983
## vsat
              3.235e-01 8.936e-01
                                    0.362
                                            0.7197
             8.894e-01 1.334e+00 0.667
                                            0.5096
## percent
## expense
             1.174e-02 1.406e-02 0.835
                                            0.4097
## income
             7.519e-01 4.241e+00 0.177
                                            0.8603
             -1.353e+00 2.704e+00 -0.500
## high
                                           0.6203
## college
             -6.650e+00 5.440e+00 -1.222 0.2302
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 60.22 on 33 degrees of freedom
## Multiple R-squared: 0.8139, Adjusted R-squared: 0.7349
## F-statistic: 10.31 on 14 and 33 DF, p-value: 2.451e-08
summary(lm(energy ~ . - msat - csat - house - density - income,
          data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income,
##
      data = states.data.num)
## Residuals:
       Min
                1Q Median
                                 30
## -123.810 -26.606
                   -0.543
                             22.380 158.698
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.924e+01 4.712e+02 -0.126
                                           0.9007
## pop
             -1.616e-06 2.747e-06 -0.589
                                            0.5601
## area
              6.282e-04 3.115e-04 2.017
                                           0.0516 .
## metro
              6.490e-01 6.835e-01 0.949
                                            0.3491
## waste
              1.395e+01 4.810e+01 0.290
                                            0.7736
## miles
             1.338e+01 1.291e+01 1.036
                                            0.3074
## toxic
             2.762e+00 5.772e-01 4.785 3.26e-05 ***
             4.345e+00 7.292e-01 5.959 9.75e-07 ***
## green
## senate
              1.647e-01 5.458e-01 0.302
                                           0.7647
## vsat
              3.342e-01 8.787e-01 0.380
                                            0.7061
## percent
              9.221e-01 1.302e+00 0.708
                                          0.4838
             1.204e-02 1.375e-02 0.876 0.3873
## expense
```

```
## high
              -1.195e+00 2.517e+00 -0.475
## college
             -6.301e+00 5.000e+00 -1.260
                                            0.2162
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 59.35 on 34 degrees of freedom
## Multiple R-squared: 0.8137, Adjusted R-squared: 0.7425
## F-statistic: 11.42 on 13 and 34 DF, p-value: 7.1e-09
summary(lm(energy ~ . - msat - csat - house - density - income - waste,
          data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste, data = states.data.num)
##
## Residuals:
##
       Min
                 1Q Median
                                  3Q
                                         Max
## -125.889 -27.884 -0.994 22.113 158.780
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.380e+01 4.646e+02 -0.116 0.9085
             -1.287e-06 2.468e-06 -0.522 0.6053
## pop
## area
              6.064e-04 2.982e-04 2.033
                                           0.0497 *
             7.011e-01 6.508e-01 1.077 0.2887
## metro
## miles
              1.405e+01 1.253e+01 1.121 0.2698
## toxic
              2.725e+00 5.557e-01 4.904 2.14e-05 ***
              4.311e+00 7.105e-01 6.068 6.28e-07 ***
## green
## senate
             1.550e-01 5.376e-01 0.288 0.7748
              3.376e-01 8.671e-01 0.389
## vsat
                                           0.6993
## percent
             9.025e-01 1.284e+00 0.703
                                            0.4867
## expense
             1.190e-02 1.356e-02 0.878 0.3861
## high
              -1.183e+00 2.483e+00 -0.477 0.6367
## college
             -6.330e+00 4.933e+00 -1.283 0.2079
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 58.57 on 35 degrees of freedom
## Multiple R-squared: 0.8132, Adjusted R-squared: 0.7492
## F-statistic: 12.7 on 12 and 35 DF, p-value: 1.998e-09
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate,
          data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate, data = states.data.num)
##
## Residuals:
##
       Min
                1Q Median
                                  3Q
                                         Max
```

```
## -127.815 -27.301
                      0.462 23.246 158.859
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.751e+01 4.497e+02 -0.061 0.9516
             -1.344e-06 2.429e-06 -0.553 0.5834
## pop
             5.851e-04 2.853e-04 2.051 0.0476 *
## area
              6.848e-01 6.400e-01 1.070
## metro
                                           0.2918
## miles
              1.323e+01 1.205e+01 1.098
                                            0.2794
## toxic
              2.686e+00 5.314e-01 5.054 1.28e-05 ***
## green
              4.283e+00 6.948e-01 6.165 4.19e-07 ***
              2.945e-01 8.431e-01 0.349
                                           0.7289
## vsat
## percent
              8.412e-01 1.250e+00 0.673
                                           0.5052
                                          0.3055
## expense
              1.317e-02 1.267e-02 1.040
              -1.156e+00 2.450e+00 -0.472
                                            0.6398
## high
## college
              -6.020e+00 4.753e+00 -1.267
                                            0.2134
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 57.82 on 36 degrees of freedom
## Multiple R-squared: 0.8128, Adjusted R-squared: 0.7556
## F-statistic: 14.21 on 11 and 36 DF, p-value: 5.307e-10
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
    - vsat, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat, data = states.data.num)
##
## Residuals:
       \mathtt{Min}
                 1Q
                    Median
                                  3Q
                                         Max
## -128.589 -27.684
                     -1.736
                              21.869 158.678
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.138e+02 1.940e+02 0.587 0.5611
             -1.487e-06 2.365e-06 -0.628
                                           0.5336
## pop
                                           0.0448 *
## area
              5.518e-04 2.656e-04 2.077
## metro
              6.104e-01 5.964e-01 1.024
                                           0.3127
## miles
              1.206e+01 1.144e+01 1.055
                                            0.2983
              2.700e+00 5.234e-01 5.159 8.62e-06 ***
## toxic
## green
              4.274e+00 6.860e-01 6.230 3.07e-07 ***
## percent
               4.519e-01 5.583e-01 0.809
                                           0.4235
## expense
                                            0.2838
              1.356e-02 1.247e-02
                                     1.088
## high
              -1.096e+00 2.414e+00 -0.454
                                            0.6526
## college
              -5.194e+00 4.073e+00 -1.275
                                            0.2102
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 57.13 on 37 degrees of freedom
## Multiple R-squared: 0.8122, Adjusted R-squared: 0.7614
## F-statistic: 16 on 10 and 37 DF, p-value: 1.351e-10
```

```
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
      - vsat - high, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high, data = states.data.num)
##
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
## -136.21 -26.01 -0.32
                           23.72 160.11
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 5.223e+01 1.373e+02 0.381 0.7057
## pop
             -1.127e-06 2.205e-06 -0.511 0.6123
## area
              5.086e-04 2.453e-04 2.073 0.0450 *
## metro
              6.339e-01 5.879e-01 1.078
                                           0.2877
## miles
              1.250e+01 1.128e+01 1.109
                                           0.2744
## toxic
              2.738e+00 5.115e-01 5.353 4.39e-06 ***
              4.257e+00 6.778e-01 6.280 2.35e-07 ***
## green
## percent
              5.116e-01 5.369e-01 0.953 0.3466
## expense
             1.236e-02 1.206e-02 1.025
                                            0.3116
## college
             -6.348e+00 3.148e+00 -2.016
                                            0.0509 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 56.53 on 38 degrees of freedom
## Multiple R-squared: 0.8111, Adjusted R-squared: 0.7664
## F-statistic: 18.13 on 9 and 38 DF, p-value: 3.358e-11
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
##
      waste - senate - vsat - high - pop, data = states.data.num)
##
## Residuals:
       Min
                 1Q
                    Median
                                  30
## -133.431 -26.533
                      0.072
                              22.267 158.721
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.268e+01 1.347e+02 0.317 0.7530
              4.414e-04 2.052e-04 2.151 0.0377 *
## area
## metro
              5.088e-01 5.294e-01 0.961
                                            0.3424
## miles
              1.364e+01 1.095e+01 1.246
                                            0.2201
## toxic
              2.760e+00 5.047e-01 5.469 2.82e-06 ***
              4.251e+00 6.712e-01 6.333 1.79e-07 ***
## green
## percent
              4.473e-01 5.169e-01 0.865 0.3922
```

```
## expense
               1.214e-02 1.193e-02
                                    1.017
              -5.906e+00 2.999e+00 -1.970
                                             0.0560 .
## college
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 55.99 on 39 degrees of freedom
## Multiple R-squared: 0.8098, Adjusted R-squared: 0.7708
## F-statistic: 20.76 on 8 and 39 DF, p-value: 7.987e-12
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop - percent, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high - pop - percent, data = states.data.num)
##
## Residuals:
       Min
##
                 1Q
                    Median
                                   3Q
                                           Max
## -134.599 -27.269 -1.304
                               21.873 159.145
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.792e+00 1.221e+02 -0.047
                                            0.9624
               4.004e-04 1.990e-04
## area
                                     2.011
                                             0.0511 .
## metro
              6.108e-01 5.146e-01
                                    1.187
                                             0.2422
              1.686e+01 1.026e+01 1.643
                                             0.1083
## miles
## toxic
              2.726e+00 5.016e-01 5.435 2.93e-06 ***
## green
               4.045e+00 6.259e-01 6.463 1.06e-07 ***
                                     1.610
## expense
              1.695e-02 1.053e-02
                                             0.1153
## college
              -5.303e+00 2.907e+00 -1.824
                                             0.0756 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 55.81 on 40 degrees of freedom
## Multiple R-squared: 0.8062, Adjusted R-squared: 0.7722
## F-statistic: 23.77 on 7 and 40 DF, p-value: 2.233e-12
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop - percent - metro, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high - pop - percent - metro, data = states.data.num)
##
## Residuals:
                      Median
       Min
                 1Q
                                   3Q
## -132.727 -30.155
                       1.581
                               21.121 164.617
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.549e+01 1.112e+02 0.499 0.6204
```

```
4.446e-04 1.965e-04 2.263 0.0290 *
## area
## miles
             1.155e+01 9.284e+00 1.244 0.2205
## toxic
              2.766e+00 5.029e-01 5.500 2.22e-06 ***
              3.946e+00 6.233e-01 6.330 1.47e-07 ***
## green
## expense
               1.825e-02 1.052e-02
                                    1.734
                                           0.0904 .
              -4.343e+00 2.807e+00 -1.547
                                           0.1295
## college
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 56.09 on 41 degrees of freedom
## Multiple R-squared: 0.7993, Adjusted R-squared: 0.77
## F-statistic: 27.22 on 6 and 41 DF, p-value: 7.94e-13
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop - percent - metro - miles, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high - pop - percent - metro - miles,
##
      data = states.data.num)
## Residuals:
       Min
                 1Q Median
                                  30
                                          Max
## -149.366 -25.937 -3.356
                              23.853 159.998
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.721e+02 6.020e+01 2.859 0.00658 **
              4.476e-04 1.978e-04 2.264 0.02883 *
## area
## toxic
              2.682e+00 5.016e-01 5.347 3.43e-06 ***
              4.334e+00 5.429e-01 7.983 5.90e-10 ***
## green
## expense
              1.234e-02 9.452e-03 1.306 0.19878
              -3.816e+00 2.792e+00 -1.366 0.17906
## college
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 56.46 on 42 degrees of freedom
## Multiple R-squared: 0.7918, Adjusted R-squared: 0.767
## F-statistic: 31.94 on 5 and 42 DF, p-value: 2.773e-13
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop - percent - metro - miles - expense, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high - pop - percent - metro - miles -
      expense, data = states.data.num)
##
##
## Residuals:
                 1Q Median
       Min
                                  3Q
## -166.285 -24.407 -2.312 21.667 170.718
```

```
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.054e+02 5.499e+01 3.735 0.000547 ***
## area
               3.409e-04 1.815e-04
                                     1.878 0.067214 .
               2.458e+00 4.753e-01 5.172 5.75e-06 ***
## toxic
               4.421e+00 5.432e-01 8.139 3.02e-10 ***
## green
              -1.886e+00 2.388e+00 -0.790 0.434086
## college
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 56.92 on 43 degrees of freedom
## Multiple R-squared: 0.7833, Adjusted R-squared: 0.7631
## F-statistic: 38.86 on 4 and 43 DF, p-value: 9.379e-14
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop - percent - metro - miles - expense - college, data = states.data.num))
##
## Call:
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high - pop - percent - metro - miles -
##
      expense - college, data = states.data.num)
##
## Residuals:
       Min
                 1Q
                    Median
                                   3Q
                                           Max
## -176.556 -27.333 -5.631
                               24.405 167.922
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.643e+02 1.774e+01 9.262 6.72e-12 ***
              3.383e-04 1.807e-04 1.872 0.0678 .
## area
                                   5.577 1.41e-06 ***
## toxic
              2.553e+00 4.578e-01
              4.523e+00 5.255e-01 8.608 5.50e-11 ***
## green
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 56.67 on 44 degrees of freedom
## Multiple R-squared: 0.7802, Adjusted R-squared: 0.7652
## F-statistic: 52.05 on 3 and 44 DF, p-value: 1.607e-14
summary(lm(energy ~ . - msat - csat - house - density - income - waste - senate
          - vsat - high - pop - percent - metro - miles - expense - college - area, data = states.data
##
## lm(formula = energy ~ . - msat - csat - house - density - income -
      waste - senate - vsat - high - pop - percent - metro - miles -
##
      expense - college - area, data = states.data.num)
##
## Residuals:
                 1Q Median
       Min
                                   3Q
```

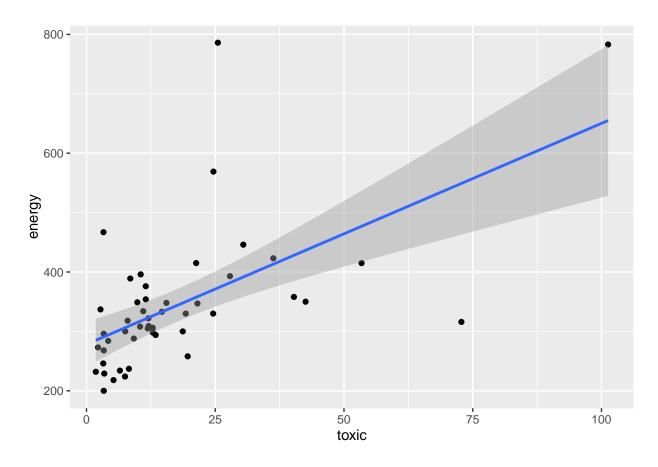
## -174.763 -28.685 -3.589 17.280 196.598

```
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 179.8260
                          16.1194 11.156 1.51e-14 ***
## toxic
                2.6455
                           0.4676
                                    5.657 1.01e-06 ***
                4.6722
                           0.5336
                                    8.756 2.81e-11 ***
## green
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 58.23 on 45 degrees of freedom
## Multiple R-squared: 0.7627, Adjusted R-squared: 0.7521
## F-statistic: 72.3 on 2 and 45 DF, p-value: 8.835e-15
```

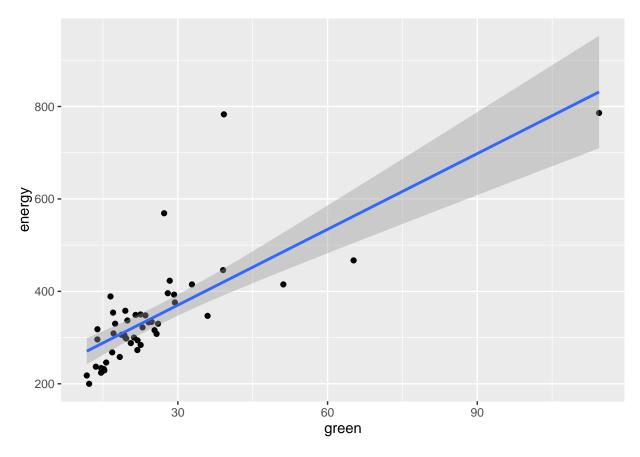
We can see that per capita toxics and greenhouse gas released have very strong correlation with the energy consumed per capita. The correlation makes sense, but the causality may be reversed since it is the energy consumption that cause the releases of toxic and greenhouse gas. We can plot the graphs to show the trends.

```
summary(lm(energy ~ toxic + green, data = states.data.num))
```

```
##
## Call:
## lm(formula = energy ~ toxic + green, data = states.data.num)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
                       -3.589
                                        196.598
##
  -174.763 -28.685
                                17.280
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 179.8260
                           16.1194 11.156 1.51e-14 ***
                                     5.657 1.01e-06 ***
## toxic
                 2.6455
                            0.4676
## green
                 4.6722
                            0.5336
                                     8.756 2.81e-11 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 58.23 on 45 degrees of freedom
## Multiple R-squared: 0.7627, Adjusted R-squared: 0.7521
## F-statistic: 72.3 on 2 and 45 DF, p-value: 8.835e-15
ggplot(states.data.num, aes(x = toxic, y = energy)) + geom_point(size = 1.5) + stat_smooth(method = lm)
```



ggplot(states.data.num, aes(x = green, y = energy)) + geom\_point(size = 1.5) + stat\_smooth(method = lm)



However, let's see if we take out toxic and green to see if there is any other factors that may have better correlation that cause higher energy consumption.

```
summary(lm(energy ~ . - msat - toxic - green, data = states.data.num))
```

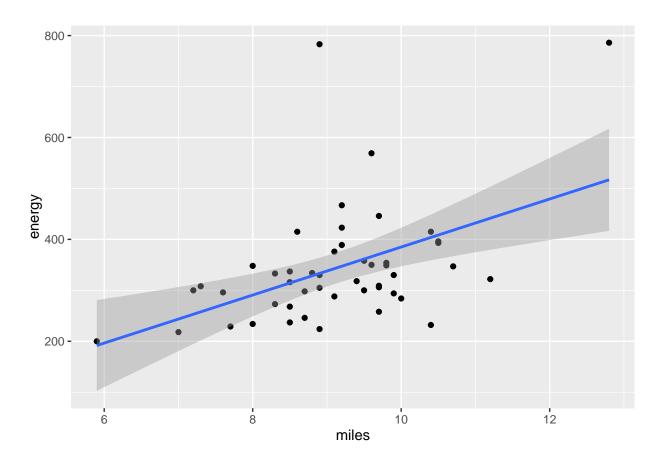
```
##
## Call:
## lm(formula = energy ~ . - msat - toxic - green, data = states.data.num)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
  -193.85 -45.33
                    -13.95
                             34.41
##
                                     343.16
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                1.096e+02 7.800e+02
                                        0.141
                                                0.8891
## pop
                2.415e-06
                           5.381e-06
                                        0.449
                                                0.6566
                1.860e-04
                           5.570e-04
                                        0.334
                                                0.7406
## area
## density
                1.551e-01
                           1.288e-01
                                        1.205
                                                0.2372
                3.197e-01
                           1.405e+00
                                        0.228
                                                0.8215
## metro
## waste
               -5.220e+01
                           8.034e+01
                                       -0.650
                                                0.5205
                                                0.0377 *
## miles
                4.465e+01
                           2.059e+01
                                        2.169
## house
               -2.588e+00
                           1.273e+00
                                       -2.033
                                                0.0504 .
## senate
               -2.015e-01 9.695e-01
                                       -0.208
                                                0.8367
## csat
               -1.521e+00 2.906e+00
                                       -0.523
                                                0.6043
                2.919e+00 6.072e+00
                                        0.481
                                                0.6340
## vsat
```

```
## percent
              -8.182e-01 2.219e+00
                                     -0.369
                                              0.7147
                                              0.2259
## expense
               2.859e-02 2.316e-02
                                      1.235
                                     -0.695
## income
              -4.906e+00
                         7.060e+00
                                              0.4921
               2.982e+00 5.326e+00
                                              0.5794
## high
                                      0.560
## college
              -5.976e+00 8.801e+00
                                     -0.679
                                              0.5020
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 97.16 on 32 degrees of freedom
## Multiple R-squared: 0.5301, Adjusted R-squared: 0.3099
## F-statistic: 2.407 on 15 and 32 DF, p-value: 0.01815
```

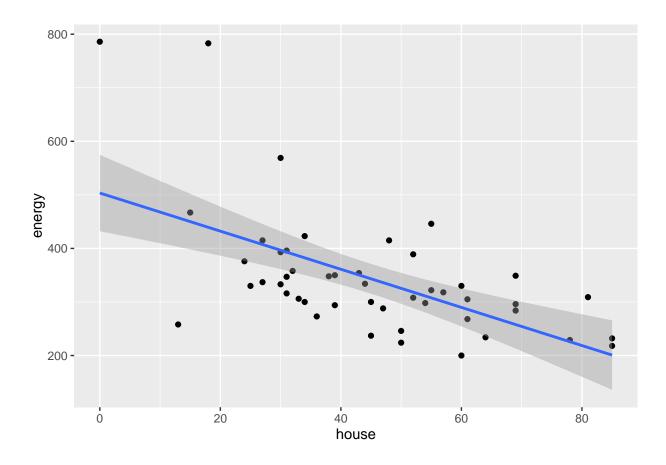
It turned out that the miles of roads built and the house voting on environmental bill have pretty high impact on the energy consumption. The interesting part is the correlation between the house bill voted is negative to the energy consumption, which means that the more energy bill voted, the less energy consumption will be. Here are the correlation plots:

```
summary(lm(energy ~ miles + house, data = states.data.num))
```

```
##
## Call:
## lm(formula = energy ~ miles + house, data = states.data.num)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
                   -16.69
##
  -197.69
           -48.78
                             35.51
                                    367.35
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 186.5377
                          122.3020
                                     1.525 0.134202
## miles
                31.6854
                           11.7671
                                     2.693 0.009920 **
                -2.9382
                            0.7192 -4.085 0.000179 ***
## house
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 89.89 on 45 degrees of freedom
## Multiple R-squared: 0.4344, Adjusted R-squared: 0.4093
## F-statistic: 17.28 on 2 and 45 DF, p-value: 2.695e-06
ggplot(states.data.num, aes(x = miles, y = energy)) + geom_point(size = 1.5) + stat_smooth(method = lm)
```



ggplot(states.data.num, aes(x = house, y = energy)) + geom\_point(size = 1.5) + stat\_smooth(method = lm)



# Exercise 1: Interactions and Factors

Use the states data set.

- 1. Add on to the regression equation that you created in exercise 1 by generating an interaction term and testing the interaction.
- 2. Try adding region to the model. Are there significant differences across the four regions?

## Interactions

Let's say we looked at miles and house we explored in the previous exercise:

```
summary(lm(energy ~ miles*house, data = states.data.num))
```

```
##
## Call:
## lm(formula = energy ~ miles * house, data = states.data.num)
##
## Residuals:
## Min    1Q Median   3Q Max
## -198.80   -39.03   -11.31   32.91   383.33
##
## Coefficients:
```

```
##
               Estimate Std. Error t value Pr(>|t|)
                          211.9374 -0.648 0.52045
## (Intercept) -137.3030
                65.4747
## miles
                           21.5839
                                     3.033 0.00405 **
                                     1.077 0.28733
                 4.2680
                            3.9627
## house
## miles:house
                -0.7652
                            0.4141
                                   -1.848 0.07139
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 87.57 on 44 degrees of freedom
## Multiple R-squared: 0.4752, Adjusted R-squared: 0.4394
## F-statistic: 13.28 on 3 and 44 DF, p-value: 2.63e-06
```

We can see that independently miles of road have higher impact to the energy consumption than house bill voted. Additional of house bill voted to the miles built has negative impact to miles built factor, and vice versa.

## Region

First, let's look at the region data:

```
summary(states.data$region)
```

```
## West N. East South Midwest NA's ## 13 9 16 12 1
```

If we look at the correlation of the energy consumption to the region:

```
summary(lm(energy ~ region, data = states.data))
```

```
##
## lm(formula = energy ~ region, data = states.data)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -162.62 -58.49 -30.62
                            12.00 585.38
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   405.62
                              39.23 10.339
                                            1.4e-13 ***
## regionN. East
                 -156.50
                              61.34 -2.552
                                              0.0141 *
## regionSouth
                   -25.49
                              52.82 -0.483
                                              0.6317
                                              0.2822
                   -61.62
                              56.63 -1.088
## regionMidwest
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 141.5 on 46 degrees of freedom
     (1 observation deleted due to missingness)
## Multiple R-squared: 0.1367, Adjusted R-squared: 0.08041
## F-statistic: 2.428 on 3 and 46 DF, p-value: 0.07737
```

We can see that the North East region has higher impact on the energy consumption per capita in the US.