

Binary Search : Searching words in a dictionary.

Divide into 2 parts.

Eg

0	1	2	3	4	5
3	10	17	18	24	32

$N \rightarrow N/2 \rightarrow N/4 \rightarrow N/8 \rightarrow \dots \rightarrow 1$

$\log_2 n$

Q1) Given sorted array with distinct elements, search for K . If K is not present (return index) return -1

0	1	2	3	4	5	6	7	8	9
3	6	9	12	14	19	20	23	25	27

Idea : Use binary search

$K = 20$

Case 1 : $arr[mid] == K$ return mid

Case 2 : $arr[mid] < K$ goto right

$[mid+1 \dots K]$

Case 3 : $arr[mid] > K$ goto left

$\downarrow \downarrow$

0 1 2 3 4 5 6 7 8 9
3 6 9 12 14 19 20 23 25 27

l h mid K=20
0 9 4 goto right
5 9 7
5 6 5
6 6 6 return 6

↓ ↓

Code

```
int search ( int ar[], int N, int k ) {
```

```
    l = 0          h = n - 1
```

```
    while ( l <= h ) {
```

```
        mid = (l + h) / 2
```

```
        if ( ar[mid] == k ) return mid
```

```
        if ( ar[mid] < k ) l = mid + 1
```

```
        else h = mid - 1
```

```
    }
```

```
    return -1
```

TC: $O(\log n)$

SC: $O(1)$

y

Q2 Sorted array, find index of first occurrence of elem K .

0	1	2	3	4	5	6	7	8	9	10
-5	-5	-3	0	0	1	1	5	5	5	5

$K = 5$ 7

$K = 0$ 3

$K = -3$ 2

Use Binary Search

Case I $ar[mid] == k$

$k \mid k \mid \text{mid} \mid k \mid k \mid k$

$ans = mid$

$goto = left$

Case II $ar[mid] < k$

$\text{mid} \mid k$

$ans =$

$goto \text{ right}$

Case III $ar[mid] > k$

$k \mid \text{mid}$

$ans =$

$goto \text{ left}$

	0	1	2	3	4	5	6	7	8	9	10
	-5	-5	-3	0	0	1	1	5	5	5	5
l											
h											
m											
											$k=5$
	0	10			5				right		
	6	10			8				ans=8		
	6	7			6				right		
	7	7			7				ans=7		
	7	6			<u>STOP</u>						

Code

```

int search ( int arr[], int N, int k ) {
    l = 0          h = n-1          ans = -1
    while ( l <= h ) {
        mid = (l+h)/2
    }
}

```

```

if (ar[mid] == k) <
    ans = mid
    h = mid - 1
}
else if (ar[mid] < k) l = mid + 1
else h = mid - 1
}
return ans
}

```

TC: $O(\log n)$
SC: $O(1)$

- For last occ


```

if (ar[mid] == k) <
    ans = mid
    l = mid + 1
}

```

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Q3 Find any local maxima
Peak elem, $a[i]$ is maxima if
 \geq both neighbours.
 $a[0]$ & $a[n-1]$ have only 1 neighbour

Eg1 $a[7] = [9, 6, 3, 14, 5, 7, 4]$

Eg2 $a[7] = [24, 21, 19, 17, 15, 9, 2]$

Brute: Iterate on each elem. &
check.

TC: $O(n)$

$a[i] \geq a[i-1]$ $a[i] \geq a[i+1]$

Idea: For any elem $a[mid]$

1) If \geq both neighbours \Rightarrow

return $a[mid]$

2) If left neighbour bigger \Rightarrow
goto left

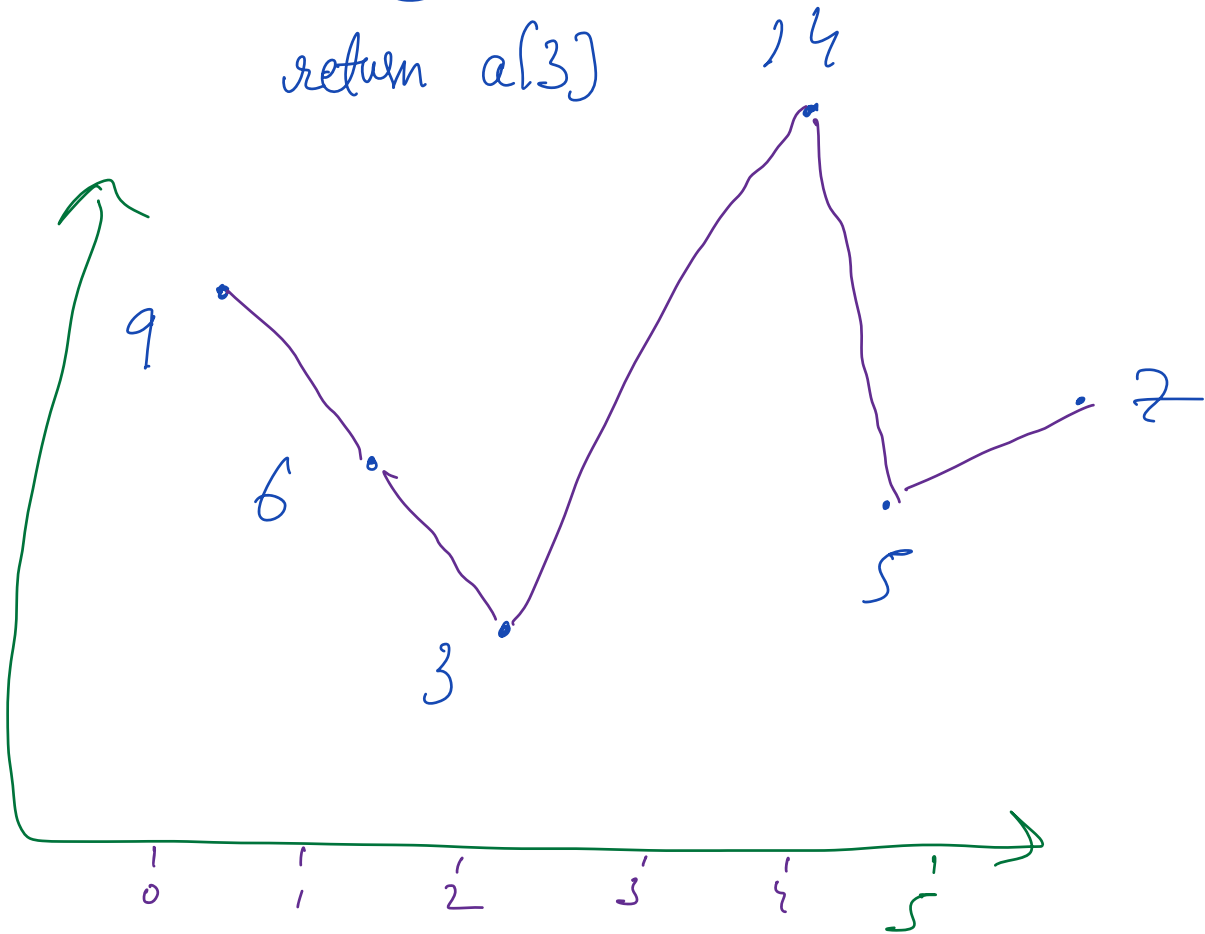
6 8 10
↑↑

3) If right neighbour bigger \Rightarrow
goto right

0 1 2 3 4 5
[9, 6, 3, 14, 5, 7]

l	h	m	
0	5	2	Can goto either side
3	5	4	lets go right $l = mid + 1$
3	3	3	left $h = mid - 1$

return a[3] 14



Code

```
int peak (int a[]) {  
    l = 0          h = n-1  
    while (l <= h) {  
        mid = (l+h)/2  mid != 0  
        if (a[mid] > a[mid-1] &&  
            a[mid] > a[mid+1])  
            mid !=  
            n-1 return a[mid]  
        else if (a[mid-1] > a[mid]) {  
            h = mid - 1  
        }  
        else {  
            l = mid + 1  
        }  
    }  
}
```

TC : $\log n$
SC : $O(1)$

Q4 Every element occurs twice except 1 which appears once. Find unique element. Note: Duplicates are adjacent

Eg- 0 1 2 3 4 5 6 7 8 9 10
 3 3 1 1 8 8 10 10 19 6 6

Idea : xor of all elem

Tc: $O(n)$

Obs: Before unique elem \rightarrow All 1's+
occurences at even idex
After unique elem \rightarrow All 1's+
occurences at odd idex

Hence binary search

target \Rightarrow Unique elem

what to search \Rightarrow indexes of the array

Case I $ar[mid] \Rightarrow \text{unique}$ **return** $ar[mid]$

Case II if $(ar[mid] == ar[mid-1])$ \downarrow
A A
mid-1 mid

new_mid --

if (new_mid is even)

goto right $l = mid + 1$

else

goto left $h = mid - 1$

0	1	2	3	4	5	6	7	8	9	10
3	3	1	1	8	8	10	10	19	6	6

l h m

0 10 5

6 10 8

return $a[8]$

19 17 17

0 2 1
0 0 0

Code

```
int findUnique ( int arr [], int N) {
```

```
    l = 0    h = n-1
```

```
    if (n == 1) return a[0]
```

```
    if (arr[0] != arr[1])
```

```
        return a[0]
```

```
    if (arr[n-1] != arr[n-2])
```

19 19 17

```
        return a[n-1]
```

```
    while (l <= h) {
```

```
        m = (l+h)/2
```

```
        if ( a[m] != a[m-1] & a[m] != a[m+1] ) { handle
```

for arr
n-1

```
            return a[m]
```

```
        new_mid = m
```

```
        if (a[m] == a[m-1]) new_mid--
```

```
        if (new_mid > 0) l = m+1
```

```
        else h = m-1
```

```
    }
```

```
    return arr[m]
```

```
}
```

TC: $O(\log n)$
SC: $O(1)$

↓ {don}

0	1	2	3	4	5	6
3	3	19	8	8	1	1

0	6	3
0	2	1
2	2	

—

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