

# `int arr[5];`

↓                      ↓

Type                      Size of the array.

0	1	2	3	4
4	3	2	5	6

Quiz-1

`int arr[N]`

0	1	2	3	...	N-2	N-1
			10			

Quiz-2

Index of first element  $\Rightarrow 0$

Index of last element  $\Rightarrow \underline{\underline{N-1}}$

# Print the array elements:-

3

`for(i=0; i < N; i++){`

`print(arr[i]);`

↓

$O(N)$

Quiz-3:

Access TC of `arr[i]`  $\Rightarrow O(1)$

$\Rightarrow$  Arrays are most frequently used data structure because it provides  $O(1)$  access & update TC.

Q. Given N array elements, Count the no. of elements having at least one element greater than itself.

A[7]: { <sup>0</sup>-3, <sup>1</sup>-2, <sup>2</sup>6, <sup>3</sup>8, <sup>4</sup>4, <sup>5</sup>8, <sup>6</sup>5 }  $\Rightarrow$  5

✓   ✓   ✓   ✗   ✓   ✗   ✓

Quiz

N=10

A: { 2, 5, 1, 4, 8, 0, 8, 1, 3, 8 }

✓   ✓   ✓   ✓   ✗   ✓   ✗   ✓   ✓   ✗

$\Rightarrow$  7

Count(8) = 3

ans = 10 - 3 = 7

Observations

- 1) For max element, there won't be any element greater than that.
- 2) Get the count / frequency of max element  
= Count
- 3) return N - Count;

1) Find max of the array.

```
max = INT_MIN
for (i = 0; i < N; i++) {
    if (a[i] > max)
        max = a[i]
}
```

3 } N

2) Get the freq. of max

```
count = 0
for (i = 0; i < N; i++) {
    if (a[i] == max)
        count++
}
```

} N

3) return N - count;

# of iterations =  $2N$

TC:  $O(N)$

SC:  $O(1)$  { constant extra space }

Todo:- Try to do in single loop.  $\Rightarrow$  30 mins

Q.2 Given N array elements, check if there exists a pair  $i, j$  s.t  $arr[i] + arr[j] = k$  &  $i \neq j$ .  $i, j$  are indices &  $k$  is the target sum. (TWO SUM)

$A[]: \{ 3, -2, 1, 4, 3, 6, 8 \} \quad k=10$

$\underbrace{\hspace{10em}}_{\text{Sum} = 10}$

→ True

$A[]: \{ 2, 4, -3, 7 \} \quad k=8$

→ False

Idea 1:- Check all possible pairs.

N=5

0	1	2	3	4

	$i, i+1$				
(0,0)	(0,1)	(0,2)	(0,3)	(0,4)	
(1,0)	(1,1)	(1,2)	(1,3)	(1,4)	
(2,0)	(2,1)	(2,2)	(2,3)	(2,4)	
(3,0)	(3,1)	(3,2)	(3,3)	(3,4)	
(4,0)	(4,1)	(4,2)	(4,3)	(4,4)	

Upper triangular

Lower triangular matrix

```

for (i = 0; i < N; i++) {
    for (j = 0; j < N; j++) {
        if (a[i] + a[j] == K and i != j) {
            return true;
        }
    }
}
return false;

```

# of iterations =  $N^2$

TC:  $O(N^2)$

SC:  $O(1)$

$$a[i] + a[j] = a[j] + a[i]$$

```

for (i = 0; i < N; i++) {
    for (j = i+1; j < N; j++) {
        if (a[i] + a[j] == K and i != j) {
            return true;
        }
    }
}
return false;

```

i	j	# of iteration
0	[1, N-1]	N-1
1	[2, N-1]	N-2
2	[3, N-1]	N-3
⋮	⋮	⋮
N-2	[N-1, N-1]	1
N-1	[N, N-1]	0

x

$$1 + 2 + 3 + \dots + (N-1)$$

Sum of (N-1) natural no's

$$\Rightarrow \frac{N(N-1)}{2} = \frac{N^2}{2} - \frac{N}{2}$$

$$TC: \underline{\underline{O(N^2)}}$$

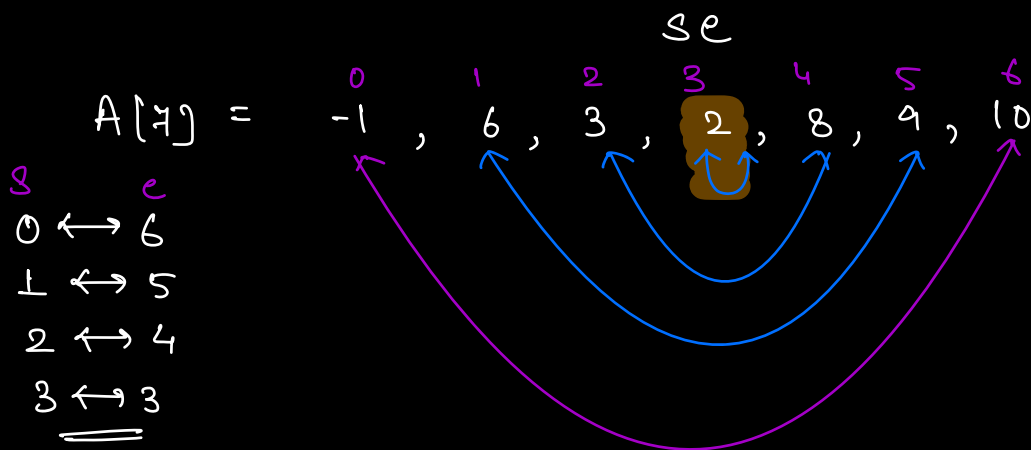
$$SC: \underline{\underline{O(1)}}$$

Q.  
Amazon  
MS

Given an Array, Reverse the entire array.  
{ Expected SC:  $O(1)$  }

$A[8]: \overset{0}{-1}, \overset{1}{4}, \overset{2}{7}, \overset{3}{6}, \overset{4}{-2}, \overset{5}{7}, \overset{6}{8}, \overset{7}{10}$

$\Rightarrow \{10, 8, 7, -2, 6, 7, 4, -1\}$



$A[8]: \overset{0}{-1}, \overset{1}{4}, \overset{2}{7}, \overset{3}{6}, \overset{4}{-2}, \overset{5}{7}, \overset{6}{8}, \overset{7}{10}$

$s=0, e=7 \Rightarrow \text{swap}$

$s=1, e=6 \Rightarrow \text{swap}$

$s=2, e=5 \Rightarrow \text{swap}$

$s=3, e=4 \Rightarrow \text{swap}$

$s=4, e=3 \Rightarrow \text{Break the while loop.}$

$A[7] = \overset{0}{-1}, \overset{1}{6}, \overset{2}{3}, \overset{3}{2}, \overset{4}{8}, \overset{5}{9}, \overset{6}{10}$

$s=0, e=6 \Rightarrow \text{swap}$

$s=1, e=5 \Rightarrow \text{swap}$

$s=2, e=4 \Rightarrow \text{swap}$

$s=3, e=3 \times \times \times \text{Break}$

```
void reverse ( A[], N) {
```

```
    start = 0
```

```
    end = N-1
```

```
    while ( start < end ) {
```

```
        swap (a[start], a[end]);
```

```
        start++;
```

```
        end--;
```

3

3

# of iterations =  $\frac{N}{2}$

Todo Implement swap  
without using  
temp variable.

TC:  $O(N)$

SC:  $O(1)$

Q: Given an Array  $A [S_i \text{ to } S_j]$ , Reverse array  
from  $S_i$  to  $S_j$  [ $S_i \leq S_j$ ]

A:     0     1     2     3     4     5     6     7     8  
     -3     4     2     8     7     4     6     2     10

$S_i = 3$

$S_j = 7$

A:     -3     4     2     2     6     4     7     8     10



```

void reversePart(A[], N, Si, Sj) {
    start = Si;
    end = Sj;
    while (start < end) {
        swap(a[start], a[end]);
        start++;
        end--;
    }
}

```

3

$$\underline{\underline{[Si, Sj] \Rightarrow Sj - Si + 1}}$$

$$\# \text{ of iterations} = \frac{Sj - Si + 1}{2}$$

Worst Case :  $Si = 0, Sj = N - 1$

$$\# \text{ of iter} = \frac{N}{2}$$

$$TC: \underline{\underline{O(N)}}$$

$$SC: O(1)$$

Q. Given N array elements, Rotate the array from last to first by k times.  
 {SC:  $O(1)$ }

A[7]:      0      1      2      3      4      5      6  
              3      -2      1      4      6      9      8

k=1      8      3      -2      1      4      6      9

k=2      9      8      3      -2      1      4      6

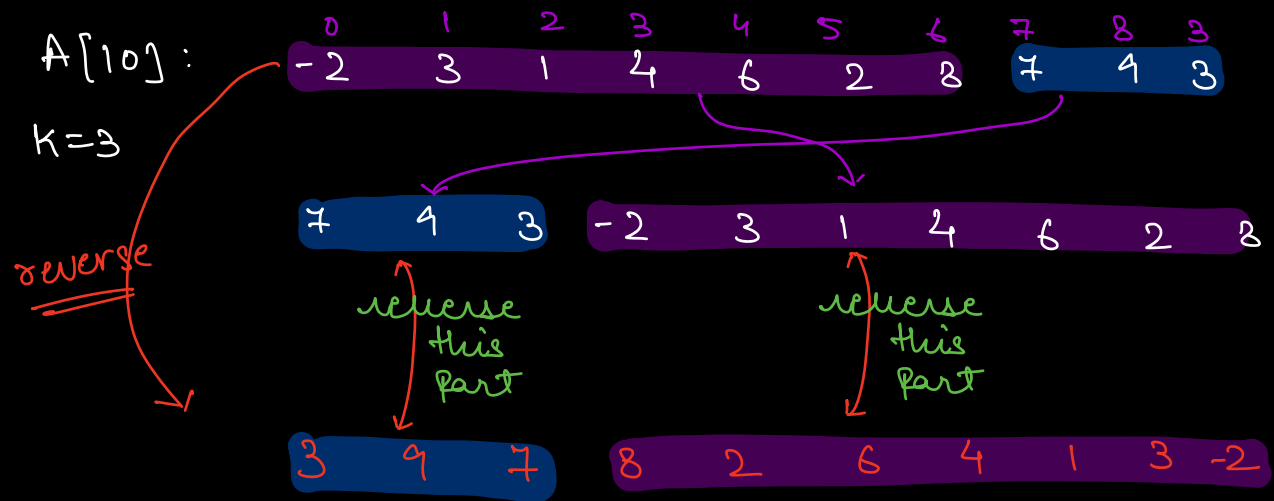
k=3      6      9      8      3      -2      1      4

k=4      4      6      9      8      3      -2      1

A[9]:      N-k      K  
              4      1      6      9      2      14      7      8      3  
 k=4  
              14      7      8      3      4      1      6      9      2

⇒ last 4 elements ⇒ first 4 elements after rotation.

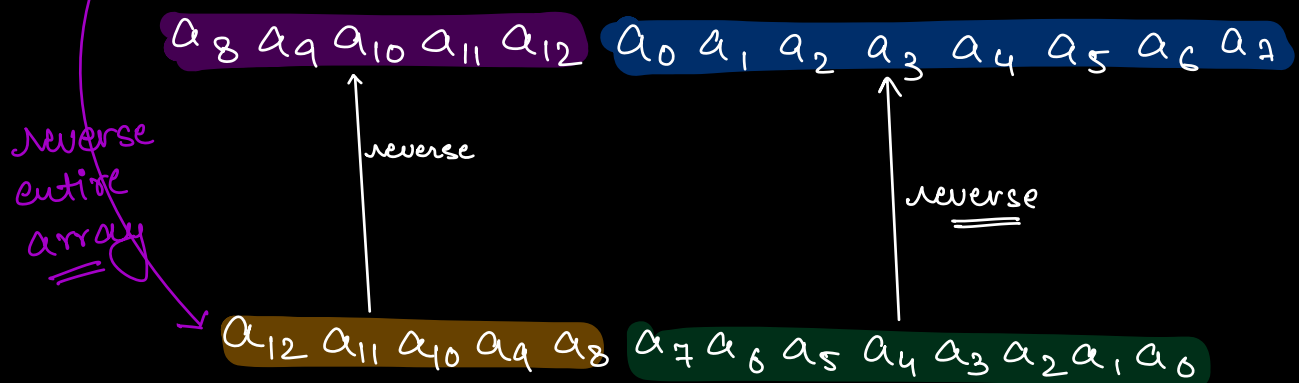
⇒ first 5 elements ⇒ last 5 elements after rotation.



General

$A[13]$ :  $a_0 a_1 a_2 a_3 a_4 a_5 a_6 a_7 a_8 a_9 a_{10} a_{11} a_{12}$

$k=5$



Steps

- 1) Reverse the entire array
- 2) Reverse first  $k$  elements
- 3) Reverse last  $N-k$  elements.

## Pseudo Code

- 1)  $\text{reversePart}(\text{arr}, N, 0, N-1) \Rightarrow \frac{N}{2}$
- 2)  $\text{reversePart}(\text{arr}, N, 0, K-1) \Rightarrow \frac{K}{2}$
- 3)  $\text{reversePart}(\text{arr}, N, K, N-1) \Rightarrow \frac{N-K}{2}$

$$\begin{aligned}\text{Total no. of iterations} &= \frac{N}{2} + \frac{K}{2} + \frac{N-K}{2} \\ &= \underline{\underline{N}}\end{aligned}$$

$$\left\{ \begin{array}{l} \text{TC: } O(N) \\ \text{SC: } \underline{\underline{O(1)}} \end{array} \right\}$$

K = N

- 1)  $\text{reversePart}(\text{arr}, N, 0, N-1)$
- 2)  $\text{reversePart}(\text{arr}, N, 0, N-1)$
- 3)  $\text{reversePart}(\text{arr}, N, N, N-1)$

K > N

↳ Array Index Out of bound Exception

$A[6]:$	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$N=6$
$k=0$	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	6, 12, 18
$k=1$	$a_5$	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	7, 13, 19
$k=2$	$a_4$	$a_5$	$a_0$	$a_1$	$a_2$	$a_3$	8, 14, 20
$k=3$	$a_3$	$a_4$	$a_5$	$a_0$	$a_1$	$a_2$	9, 15, 21
$k=4$	$a_2$	$a_3$	$a_4$	$a_5$	$a_0$	$a_1$	10, 16, 22
$k=5$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_0$	11, 17, 23
$k=6$	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	
$k=7$	$a_5$	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	

if ( $k > N$ )

$$k = k \% N$$

Quiz

$A: \{a_0 a_1 a_2 a_3 a_4 a_5\} \quad N=6$

$k=9$

$$k > N \Rightarrow k \% N$$

$$= 9 \% 6 = 3$$

$\{a_3 a_4 a_5 a_0 a_1 a_2\}$

# `int arr[5];`  
                     5 size  
`int arr[N];` ⇒ N elements } Static Array

## Dynamic Array

C++ : Vector

Java : ArrayList

Python : List

C# : ArrayList

JS : Array

C : Upgrade to C++

⇒ `vector<int> v; | list<int> l;`

`v.push-back(10) | l.insert(10)`

`v.push-back(20) | l.insert(20)`

`v.push-back(30) | l.insert(30)`

`v.size() ⇒ 3`

`l.size() ⇒ 3`

TC of insert =  $O(1)$