

# corVis: An R Package for Visualising Associations and Conditional Associations

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**Abstract** Correlation matrix displays are important tools to explore multivariate datasets prior to modeling. These displays with other measures of association can summarize interesting patterns to an analyst and assist them in framing right questions while performing exploratory data analysis. In this paper, we present new visualisation techniques to visualise association between all the variable pairs in a dataset in a single plot, which is something existing displays lack. We extend these displays to regression and classification settings, where these could be used to find out variables with high predictive power. Also, we propose new methods to visualise trivariate relationship summaries using conditioning. We use different layouts like: matrix or linear, to name a few, for our displays which have their own advantages and disadvantages. We use seriation in our displays which helps in highlighting interesting patterns easily. The R package *corVis* provides an implementation.

## Section 1: Introduction

Exploratory Data Analysis (EDA) is an important step to explore multivariate datasets prior to modeling. One of the important tools used for EDA is correlation matrix display, also known as *corrgram* (Friendly, 2002). This display is produced by first calculating the correlation among the variables and then plotting these calculated values in a matrix display. Effective ordering techniques are also used with these displays to highlight interesting relationships. The display is useful to quickly find highly associated variables which are explored further and are taken into consideration during the modeling step.

The correlation displays are generally used with one of the Pearson's, Spearman's or Kendall's correlation coefficient and are therefore limited to quantitative variables. An analyst can use one-hot encoding of the qualitative variables in order to use these displays but will need to deal with the high dimensions produced by the encoding. The existing method to quickly explore association among qualitative variables, and mixed variables in a dataset include using proportions or counts with different graphical displays like boxplots or barplots depending on the variable types. This means that the analyst will have to explore quantitative, qualitative and mixed variables separately and thus calls for a tool which can summarize relationships among all the variables in a single step.

MANY ASSOCIATION measures have been proposed to summarize different types of relationships among two variables. The most commonly used measure is Pearson's correlation coefficient which captures any linear trend present between the variables. Other popular measures include Kendall's or Spearman's rank correlation coefficient which are non-parametric measures and looks for monotonic relationship among the variables. The distance correlation (Székely et al., 2007) is an important measure useful in exploring non-linear relationships. The information theory measure maximal information coefficient (Reshef et al., 2011) is capable of summarizing complex relationships. These multiple measures are useful for explaining complex relationships in a dataset compared to using a single measure. With effective displaying techniques, the multiple measures of association provide a comparison tool that assist an analyst in discovering interesting variable pairs.

The association measures calculated at different levels of a factor variable for a variable pair help in finding patterns like Simpson's paradox and displaying these conditional associations using graphical representation will help explain these patterns.

In this paper, we propose extensions of these displays and new visualizations which look at variables of mixed type, multiple association measures and conditional associations. These displays are implemented in the R package *corVis*. The paper is organised in the following way: first a review of existing packages/methods to calculate and display association with a quick overview of some association measures used in the package, then our approach to calculate the association measures, then visualizations of associations and conditional associations, followed by a discussion.

## Section 2: Background

The correlation matrix display is an important tool to explore association among variables in a multivariate analysis. It was first introduced by Murdoch and Chow (1996) in which they replaced the numerical entries of a correlation matrix with ellipses and then popularized by (Friendly, 2002) who called them *corrgrams*, wherein he rendered the correlation values with shaded squares, bars, ellipses,

or circular ‘pac-man’ symbols. The main goal of these displays is to describe the bivariate patterns in a dataset. This section provides a brief review of correlation displays and the association measures which are used to explore interesting relationships.

## Section 2.1: Literature Review on Correlation Displays

There are packages available in R which can be used to create correlation matrix displays. The R package `corrgram` provides these displays with shaded squares, bars, ellipses, or circular ‘pac-man’ glyphs. The package includes various variable ordering methods which assist in detecting patterns of relations among the variables. The package `corr` produces correlation matrix in a tidy structure, which then can be used to create correlation displays. In addition to matrix display, the package also plots the correlation values in a network display which is useful when dealing with high-dimensional datasets. There have been other extensions to correlation displays like: (Buja et al., 2016) and `sCorrPlot`, which have been proposed mainly for exploring correlations among the numeric variables for a high dimensional dataset. We introduce a display which includes all the variables of a dataset, irrespective of the data type, displaying every pairwise association. This saves the effort and time of an analyst for exploring relationship among all the variable pairs. Kuhn et al. (2013) have proposed display techniques to compare multiple association measures for every pair of output variable and a predictor to measure the importance of each predictor. This can help in summarizing a complex relationship more efficiently as compared to using just one measure like Pearson’s correlation which can only find linear associations. In a similar way, we propose different visualization techniques to compare multiple association measures for all the variable pairs in a dataset which can assist a user in finding interesting patterns.

## Section 2.2: Literature Review on Association Measures

An association measure can be defined as a numerical summary quantifying relationship between two or more variables. For example, Pearson’s correlation coefficient summarizes the strength and direction of the linear relationship present between two *numeric* variables and is in the range  $[-1, 1]$ . Similarly, distance correlation coefficient measures the non-linear association between two *numeric* variables and summarizes it in  $[0, 1]$  where 0 suggests no non-linear relationship and 1 suggests very high non-linear relationship. The package provides a collection of various measures of association which can be used to quantify the relationship between two variables and could be used to explore patterns prior to modeling. The measures available in the package are not limited to *numeric* variables only and can be used with *categorical* and *ordinal* variables as well.

- Pearson’s correlation
- Spearman’s rank correlation.
- Kendall’s rank correlation.
- Distance correlation.
- Canonical correlations.
- Maximal-information based non-parametric exploration (MINE) statistics.

The package provides a collection of various measures of association which is used to quantify the relationship between two variables and is used to explore patterns prior to modeling. The measures available in the package are not limited to *numeric* variables and are used with *categorical* and *ordinal* variables as well. Table @ref(tab:association\_measures) lists the different measures of association provided in the package with the variable types they can be used with, the package used for calculation, the information on whether the measure is symmetric, and the minimum and maximum value of the measure.

funName	typeX	typeY	from	symmetric	min	max
tbl_cor	numeric	numeric	stats::cor	TRUE	-1	1
tbl_dcor	numeric	numeric	energy::dcor2d	TRUE	0	1
tbl_mine	numeric	numeric	minerva::mine	TRUE	0	1
tbl_polycor	ordinal	ordinal	polycor::polychor	TRUE	-1	1
tbl_tau	ordinal	ordinal	DescTools::KendalTauA,B,C,W	TRUE	-1	1
tbl_gkTau	nominal	nominal	DescTools::GoodmanKruskalTau	FALSE	0	1
tbl_gkLambda	nominal	nominal	DescTools::GoodmanKruskalTau	TRUE	0	1
tbl_gkGamma	nominal	nominal	DescTools::GoodmanKruskalTau	TRUE	0	1
tbl_uncertainty	nominal	nominal	DescTools::UncertCoef	TRUE	0	1
tbl_chi	nominal	nominal	DescTools::ContCoef	TRUE	0	1
tbl_cancel	nominal	nominal	corVis	TRUE	0	1
tbl_cancel	nominal	numerical	corVis	TRUE	0	1
tbl_nmi	any	any	corVis	TRUE	0	1
tbl_easy	any	any	correlation::correlation	TRUE	-1	1

### Section 3: corVis: Calculating Association

We introduce a method which creates a tibble structure for the variable pairs in a dataset along with calculated association measure. The package contains various functions (shown in Table 1) for different association measures in the form `tbl_*` to calculate them. For example, a user might be interested in calculating distance correlation for numeric pair of variables in a dataset. This can be done by using `tbl_dcor`.

```
df <- penguins
distance <- tbl_dcor(df)
head(distance)

#> # A tibble: 6 x 4
#>   x           y      measure measure_type
#>   <chr>      <chr>    <dbl> <chr>
#> 1 bill_depth_mm bill_length_mm 0.387 dcor
#> 2 flipper_length_mm bill_length_mm 0.666 dcor
#> 3 body_mass_g      bill_length_mm 0.587 dcor
#> 4 year            bill_length_mm 0.0784 dcor
#> 5 flipper_length_mm bill_depth_mm 0.704 dcor
#> 6 body_mass_g      bill_depth_mm 0.614 dcor
```

Similarly, one can use `tbl_nmi` to calculate normalised mutual information for numeric, nominal and mixed pair of variables.

```
nmi <- tbl_nmi(df)
head(nmi)

#> # A tibble: 6 x 4
#>   x           y      measure measure_type
#>   <chr>      <chr>    <dbl> <chr>
#> 1 island      species 0.507 nmi
#> 2 bill_length_mm species 0.353 nmi
#> 3 bill_depth_mm species 0.315 nmi
#> 4 flipper_length_mm species 0.343 nmi
#> 5 body_mass_g      species 0.300 nmi
#> 6 sex           species 0.0000854 nmi
```

These functions return a tibble with the variable pairs and calculated measure, and also with additional classes `pairwise` and `data.frame`. With the pairwise measures of association in a tibble or dataframe structure, the output of these functions can then be used with packages like `dplyr`, `ggplot2` for further exploration of association measures.

```
class(distance)

#> [1] "pairwise" "tbl_df" "tbl" "data.frame"
```

The function `matrix_assoc` helps in converting the tibble of association measure to matrix structure. The function takes a tibble or dataframe of the variable pairs of the dataset along with the calculated association measures and returns a symmetric matrix of the variables.

```
head(matrix_assoc(distance))
```

```
#>               bill_length_mm bill_depth_mm flipper_length_mm body_mass_g
#> bill_length_mm             NA      0.3872021      0.6664558  0.5871319
#> bill_depth_mm      0.3872021             NA      0.7039636  0.6141631
#> flipper_length_mm  0.6664557      0.7039636             NA  0.8674122
#> body_mass_g        0.58713186  0.6141631      0.8674122             NA
#> year                0.07842516  0.1117057      0.1643876  0.0790560
#>               year
#> bill_length_mm  0.07842516
#> bill_depth_mm  0.11170568
#> flipper_length_mm 0.16438763
#> body_mass_g     0.07905600
#> year            NA
```

The function outputs a matrix even if any variable pair is missing in the input tibble with NA for corresponding variable pair cell in the matrix output.

```
distance <- distance[-1,]
matrix_assoc(distance)
```

```
#>               bill_length_mm bill_depth_mm flipper_length_mm body_mass_g
#> bill_length_mm             NA             NA      0.6664558  0.5871319
#> bill_depth_mm      NA             NA      0.7039636  0.6141631
#> flipper_length_mm  0.6664557      0.7039636             NA  0.8674122
#> body_mass_g        0.58713186  0.6141631      0.8674122             NA
#> year                0.07842516  0.1117057      0.1643876  0.0790560
#>               year
#> bill_length_mm  0.07842516
#> bill_depth_mm  0.11170568
#> flipper_length_mm 0.16438763
#> body_mass_g     0.07905600
#> year            NA
```

The function has an additional argument called `group` which represents the level of the grouping categorical variable for which the matrix output needs to be calculated and is set to `overall` as default.

## Calculating association measures for whole dataset

`calc_assoc` can be used to calculate association measures for all the variable pairs in the dataset at once in a tibble structure. In addition to tibble structure, the output also has `pairwise` and `data.frame` class which are important class attributes for producing visual summaries in this package.

```
complete_assoc <- calc_assoc(df)
glimpse(complete_assoc)
```

```
#> Rows: 28
#> Columns: 4
#> $ x      <chr> "island", "bill_length_mm", "bill_depth_mm", "flipper_len~
#> $ y      <chr> "species", "species", "species", "species", "species", "s~
#> $ measure <dbl> 0.81328762, 0.84131393, 0.82447508, 0.88217284, 0.8183348~
#> $ measure_type <chr> "cancor", "cancor", "cancor", "cancor", "cancor", "cancor~
```

```
class(complete_assoc)
```

```
#> [1] "pairwise" "tbl_df"      "tbl"        "data.frame"
```

The function has a `types` argument which is basically a tibble of the association measure to be calculated for different variable pairs. The default tibble of measures is `default_assoc()` which calculates Pearson's correlation if both the variables are numeric, Kendall's tau-b if both the variables are ordinal, canonical correlation if one is factor and other is numeric and canonical correlation for the rest of the variable pairs.

```
default_measures <- update_assoc()
default_measures

#> # A tibble: 4 x 4
#>   funName   typeX   typeY   argList
#>   <chr>     <chr>   <chr>   <list>
#> 1 tbl_cor   numeric numeric <NULL>
#> 2 tbl_tau   ordered ordered <NULL>
#> 3 tbl_cancor factor  numeric <NULL>
#> 4 tbl_cancor other   other   <NULL>
```

An analyst can update these measures using the `update_assoc` function where one can specify a `tbl_*` function to calculate association measure depending on the variable pair in the dataset and a method if it calculates more than one measure.

```
updated_assoc <- update_assoc(num_pair = "tbl_cor",
                             num_pair_argList = "spearman",
                             mixed_pair = "tbl_cancor",
                             other_pair = "tbl_nmi")

updated_assoc

#> # A tibble: 4 x 4
#>   funName   typeX   typeY   argList
#>   <chr>     <chr>   <chr>   <list>
#> 1 tbl_cor   numeric numeric <chr [1]>
#> 2 tbl_tau   ordered ordered <NULL>
#> 3 tbl_cancor factor  numeric <NULL>
#> 4 tbl_nmi   other   other   <NULL>

updated_complete_assoc <- calc_assoc(df, types = updated_assoc)
head(updated_complete_assoc)

#> # A tibble: 6 x 4
#>   x           y      measure measure_type
#>   <chr>       <chr>    <dbl>   <chr>
#> 1 island      species 0.507     nmi
#> 2 bill_length_mm species 0.841     cancel
#> 3 bill_depth_mm species 0.824     cancel
#> 4 flipper_length_mm species 0.882     cancel
#> 5 body_mass_g species 0.818     cancel
#> 6 sex         species 0.0000854 nmi
```

The tibble output for `calc_assoc` has the following structure:

- `x` and `y` representing a pair of variables
- `measure` representing the calculated value for association measure
- `measure_type` representing the association measure calculated for `x` and `y` pair.

The variable pairs in the output are unique pairs and a subset of all the variable pairs of a dataset where  $x \neq y$ . As explained earlier, the `measure_type` represents the association measure calculated for a specific type of variable pair. A user can be interested in calculating multiple association measures for a type of variable pair. This can be done by using the `calc_assoc` and `update_assoc` together for calculating different association measures and then merging the output tibbles.

### Calculating conditional association

`calc_assoc_by` can be used to calculate association measures for all the variable pairs at different levels of a categorical variable. This can help in exploring the conditional associations and find out interesting patterns in the data prior to modeling. The output of this function is a tibble structure with `pairwise` and `data.frame` as additional class attributes. The `by` argument is used for the grouping variable which needs to be categorical.

```
complete_assoc_by <- calc_assoc_by(df, by = "sex")
```

The function also has a `types` argument which can be updated similarly to `calc_assoc`.

```

updated_assoc <- update_assoc(num_pair = "tbl_cor",
                             num_pair_argList = "spearman",
                             mixed_pair = "tbl_cancor",
                             other_pair = "tbl_nmi")
updated_complete_assoc_by <- calc_assoc_by(df, by = "sex", types = updated_assoc)
head(updated_complete_assoc_by)

#> # A tibble: 6 x 5
#>   x           y      measure measure_type by
#>   <chr>      <chr>    <dbl> <chr>      <fct>
#> 1 island    species  0.502 nmi        female
#> 2 bill_length_mm species  0.885 cancort female
#> 3 bill_depth_mm species  0.900 cancort female
#> 4 flipper_length_mm species  0.914 cancort female
#> 5 body_mass_g species  0.911 cancort female
#> 6 year      species  0.0457 cancort female

```

By default, the function calculates the association measures for all the variable pairs at different levels of the grouping variable and the pairwise association measures for the ungrouped data (*overall*). This behavior can be changed by setting `include.overall` to `FALSE`.

```
complete_assoc_by <- calc_assoc_by(df, by = "sex", include.overall = FALSE)
```

The tibble output for `calc_assoc_by` has the following structure:

- `x` and `y` representing a pair of variables
- `measure` representing the calculated value for association measure
- `measure_type` representing the association measure calculated for `x` and `y` pair.
- `by` representing the levels of the categorical variable used in the function.

The variable pairs in the output are repeated for every level of `by` variable. At present the function doesn't allow multiple `by` variables to be used for conditioning but is something which can be done by using the `calc_assoc_by` function multiple times and then merging the multiple outputs. For calculating multiple measures for a specific variable type, one can use `update_assoc` with `calc_assoc_by` and then can merge these multiple tibble outputs.

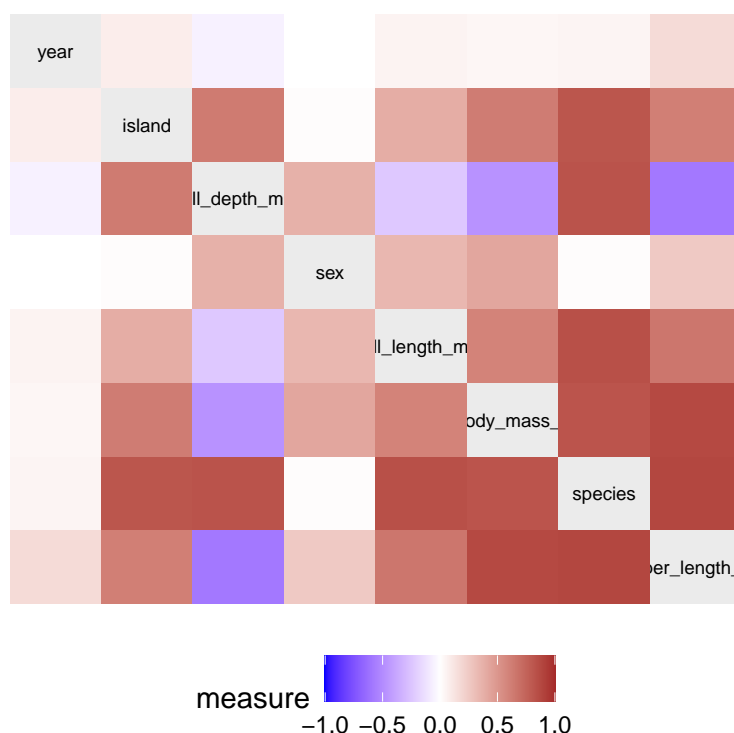
## Creating Your Own Association Measure

We introduce a new structure for calculating association measures which can be used to add other existing or new measures in the package. These measures can then be analysed and visualised using the plot functions present in the package. For example, Cramer's V is a measure to summarize association between two categorical variables using the Chi-square test statistic. If a user wants to add Cramer's V to the package, they can write a simple function and then can use it for their analysis.

## Section 4: corVis: Visualising Association

We propose novel visualisations to display association for every variable pair in a dataset in a single plot and show multiple bivariate measures of association simultaneously to find out interesting patterns. Efficient seriation techniques have been included to order and highlight interesting relationships. These ordered association and conditional association displays can help find interesting patterns in the dataset. While designing these displays we considered matrix-type, linear and network-based layouts. A matrix-type layout simplifies lookup, and different measures may be displayed on the upper and lower diagonal. Linear layouts are more space-efficient than matrix plots, but lookup is more challenging. Variable pairs can be ordered by relevance (usually difference in measures of association or across the factor levels), and less relevant pairs can be omitted. Linear displays are also suitable to display associations between the response and predictors only. Our selection criteria for a better display were based on :

- Number of variables
- Easier pixel-variable or variable-pixel look up
- Number of levels of a factor for conditional association displays



**Figure 1:** Association matrix display for penguins data showing Pearson's correlation for numeric variable pairs, canonical correlation for mixed variable pairs and categorical variable pairs.

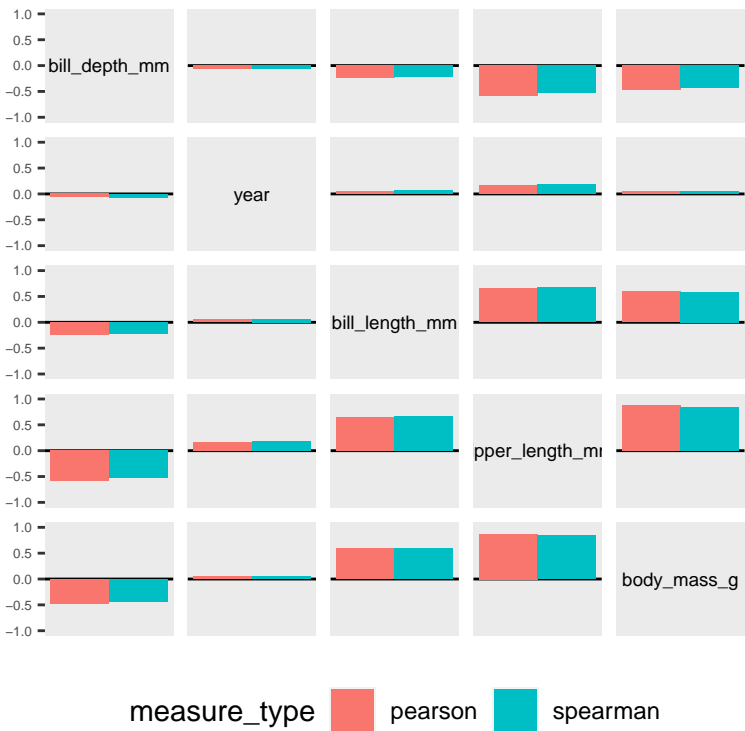
Figure 1 shows this display for every variable pair in the *penguins* dataset from the *palmerpenguins* package. It shows a high positive Pearson's correlation among flipper\_length\_mm and body\_mass\_g, flipper\_length\_mm and bill\_length\_mm, and bill\_length\_mm and bodymass.g. There seems to be a strong negative Pearson's correlation between flipper\_length\_mm and bill\_depth\_mm, and bill\_depth\_mm and body\_mass.g. The plot also shows that there is a high canonical correlation between species and other variables except year and sex, and a high canonical correlation between island and species, which traditional correlation matrix display would omit as they are limited to numeric variable pairs only. The variables in the display are ordered using average linkage clustering method to find out highly associated variables quickly.

We can also calculate multiple association measures for all the variable pairs in the dataset and compare them. This will help in finding out pairs of variables with a high difference among different measures and one can investigate these bivariate relationships in more detail. The `pairwise_summary_plot` function can be used to compare various measures using the matrix layout. It plots multiple measures among the variable pairs as bars, where each bar represents one measure of association. Figure 2 shows a matrix layout comparing Pearson's and Spearman's correlation coefficient for the numeric variable pairs in *penguins* data.

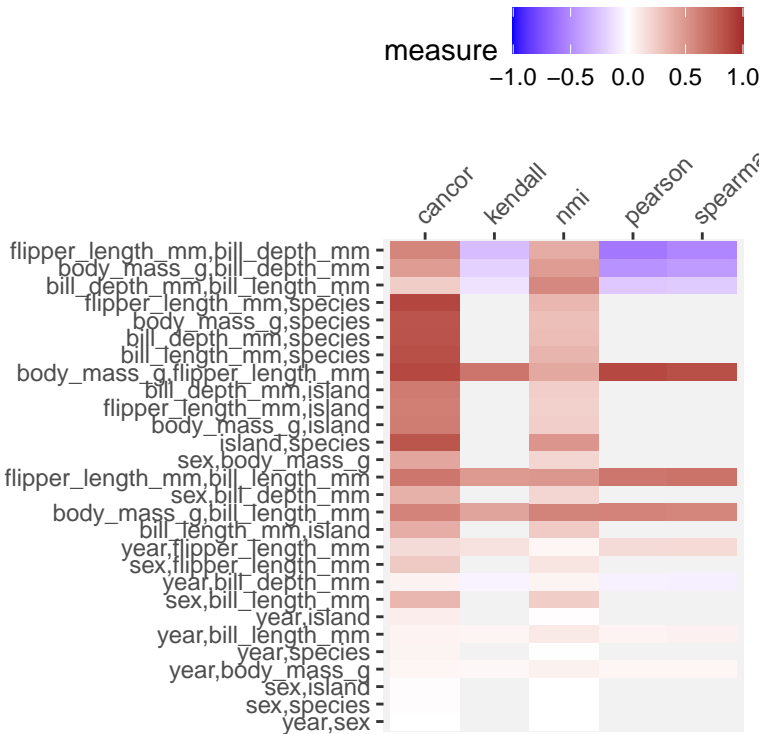
In addition to matrix layout, we can also use linear layouts for comparing multiple measures. Figure 3 shows a linear layout comparing multiple association measures for all the variable pairs in the penguins data. Linear layouts seems to be more suitable when comparing high number of association measures.

## Visualising Conditional Association

The package includes a function `calc_assoc_by` which calculates the pairwise association at different levels of a categorical conditioning variable. This helps in finding out interesting variable triples which can be explored further prior to modeling. Figure 4 shows a conditional association plot for the *penguins* data. Each cell corresponding to a variable pair shows three bars which correspond to the association measure (Pearson's correlation for numeric pair and Normalized mutual information for other combination of variables) calculated at the levels of conditioning variable *island*. The dashed line represents the overall association measure. The plot shows that there is a high value for normalised mutual information between bill\_length\_mm and species for the penguins which lived in *Biscoe* island compared to the penguins which lived in *Dream* island. It can also be seen that the cell corresponding to variable pair flipper\_length\_mm and bill\_depth\_mm has a high negative overall Pearson's correlation



**Figure 2:** Matrix display comparing Pearson’s and Spearman’s correlation coefficient. All the variable pairs have similar values for both correlations.



**Figure 3:** Comparing multiple association measures using a linear layout. The display has variable pairs on the Y-axis and association measures on the X-axis. The cell corresponding to a variable pair and an association measure has been colored grey showing that the measure is not defined for corresponding pair.



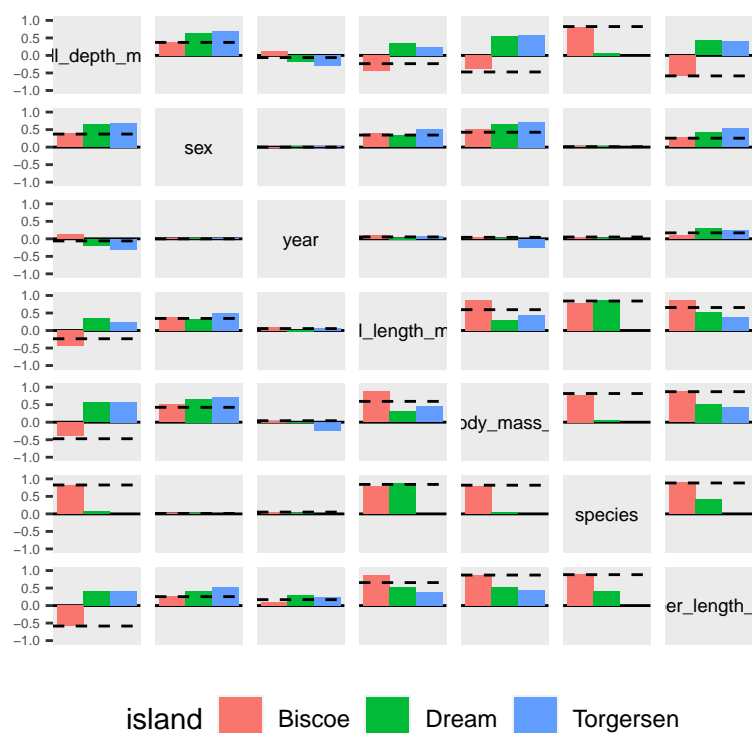


Figure 4: Conditional Association plot

and for the penguins which lived in *Biscoe* island but positive correlation for penguins which lived in *Dream* and *Torgersen* island. This is an instance of Simpson's paradox which can be taken into account during the modeling step.

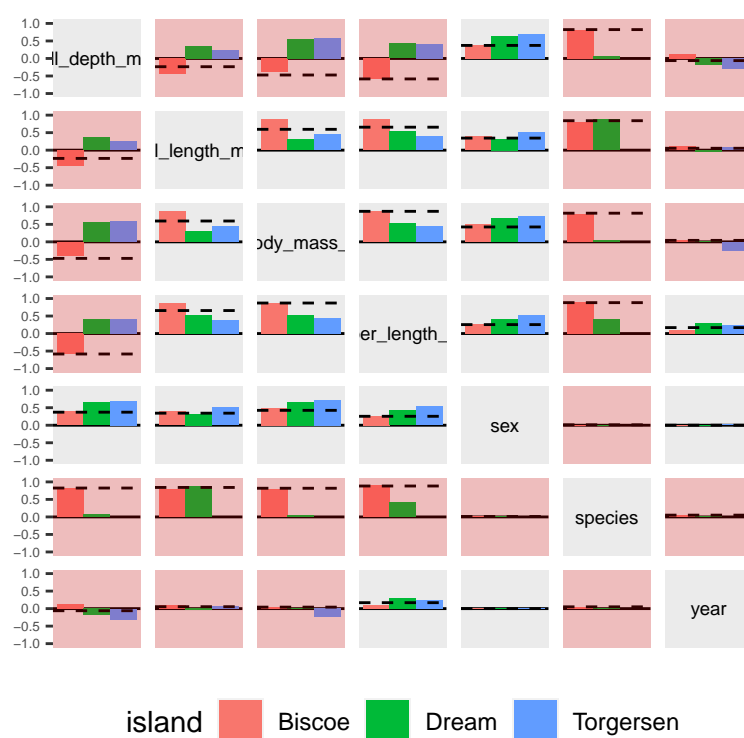
We also provide a functionality for highlighting interesting patterns like Simpson's paradox. Figure 5 shows the matrix plot with highlighted cells for the variable pairs where Simpson's paradox is present.

The cells can also be highlighted on the basis of a score calculated by the user. This can be done by providing a dataframe with pairs of variables to highlight and a score for highlighting variable pairs. The cells with high score will have a thicker border compared to cells with low score. Figure 6 shows highlighted cells on the basis of a score provided for a subset of variable pairs.

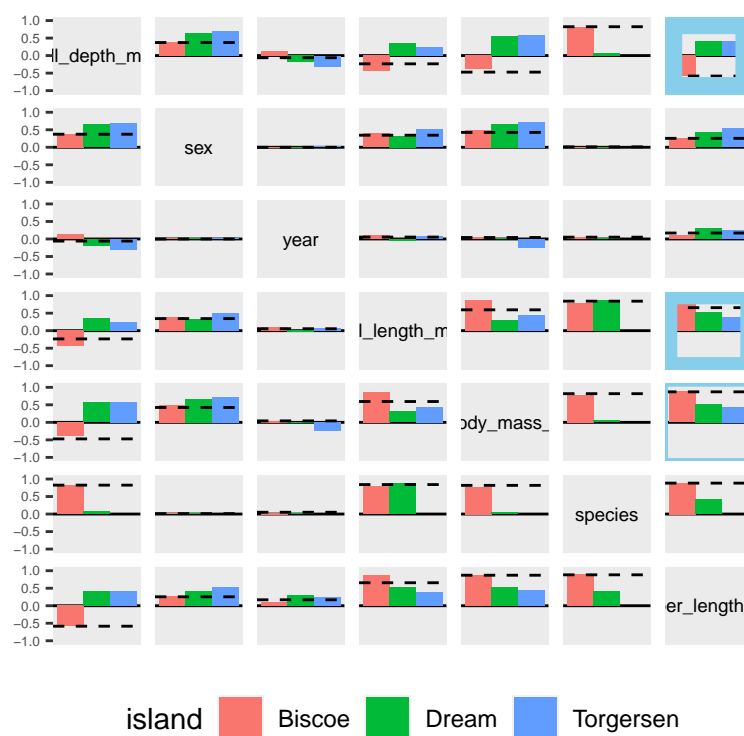
We can also use linear layouts for displaying conditional association. Figure 7 shows a funnel-like linear display for conditional association measures with all the variable pairs on the y-axis, the value of association measure on x-axis and color of the points representing the level of the grouping variable. The linear layout becomes more useful over the matrix layout when the number of variables and number of levels of grouping variable are high.

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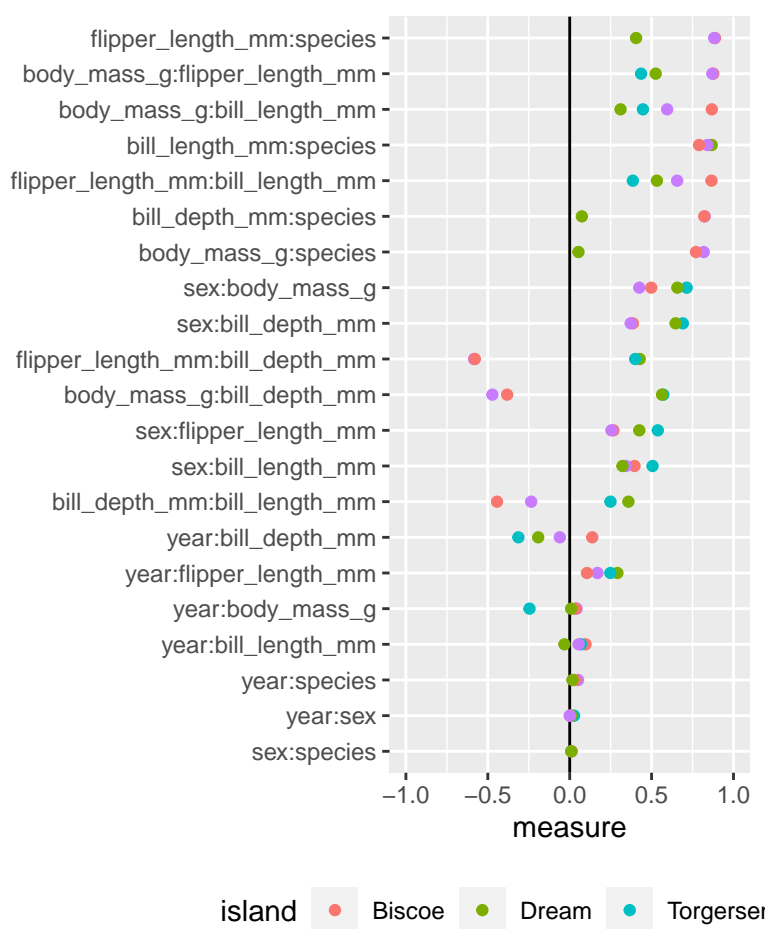
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**Figure 5:** Conditional Association plot with Simpson's paradox



**Figure 6:** Conditional Association plot with manual highlighting



**Figure 7:** Conditional Association plot using linear layout

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