

HW1

Profit Maximization Problem by recursive and non-recursive version program

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Recursive :

程式摘要：

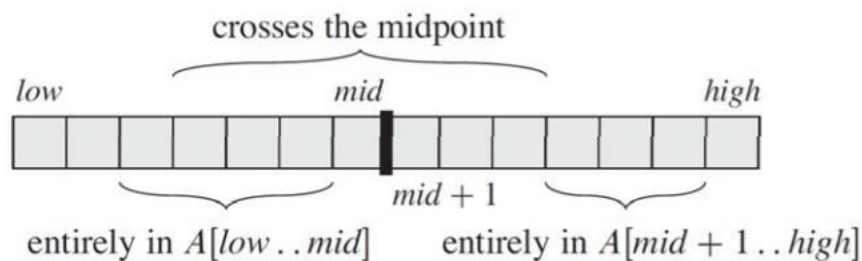
此程式用 C++ 語言

用 struct 存取 Subarray 中的三個值，起始、結束、總和

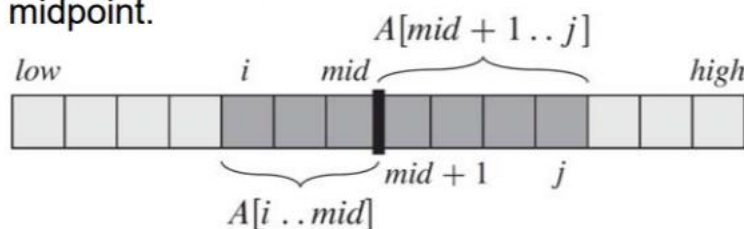
用 Divide and Conquer 方法做遞迴運算，把原本的 array 分成數個 subarray，再藉由 subarrays 間，互相比較取的的最大區間，從而得出整個 array 的最大區間

程式內容說明：

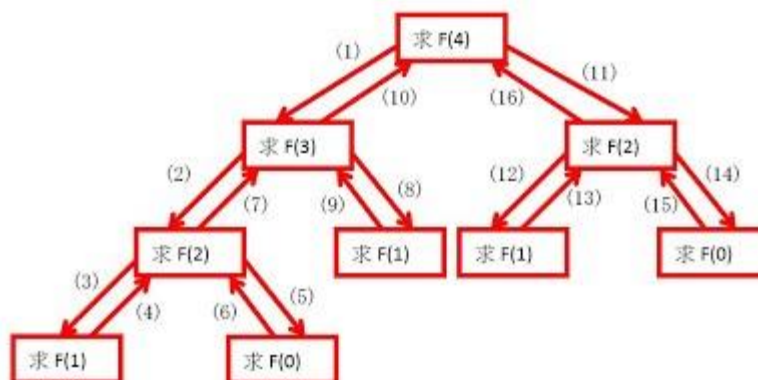
圖解：



midpoint.



- We just need to find maximum subarrays of the form $A[i \dots \text{mid}]$ and $A[\text{mid} + 1 \dots j]$ and then combine them.



虛擬碼:

```
1 Find_Max_Crossing_Subarray(A, low, mid, high)
2   left_sum = -∞
3   sum = 0
4   for i = mid to low
5       sum = sum + A[i]
6       if sum > left_sum
7           left_sum = sum
8           max_left = i
9   right_sum = -∞
10  sum = 0
11  for j = mid + 1 to high
12      sum = sum + A[j]
13      if sum > right_sum
14          right_sum = sum
15          max_right = j
16  return (max_left, max_right, left_sum + right_sum)
```

```
1 Find_Maxium_Subarray( A, low, high)
2   if high == low
3       return (low, high, A[low])
4   else mid = (low + high)/2
5       (left_low, left_high, left_sum) =
           Find_Maxium_Subarray(A, low, mid)
6       (right_low, cross_high, cross_sum) =
           Find_Maxium_Subarray(A, mid+1, high)
7       (cross_low, cross_high, cross_sum) =
           Find_Max_Crossing_Subarray(A, low, mid, high)
8   if left_sum >= right_sum and left_sum >= cross_sum
9       return (left_low, left_high, left_sum)
10  elseif right_sum >= left_sum and right_sum >= cross_sum
11      return(right_low, right_high, right_sum)
12  else return(corss_low, cross_high, cross_sum)
```

程式:

```
1 // Name: B10532011高婷雅
2 // Date: March 21, 2018
3 // Last Update: March 21, 2018
4 // Problem statement: Profit Maximization Problem by recursive method
5 // A Divide and Conquer based program for maximum subarray sum problem
6 #include <stdio.h>
7 #include <limits.h>
8 #include <iostream>
9 using namespace std;
10
11 //用struct存答案的三個值，start，end，sum
12 struct ANS{int low, high, sum;};
13
14 //找出橫跨中間的最大值
15 ANS maxCrossingSum(int *arr, int l, int m, int h)
16 {
17     // Include elements on left of mid.
18     int sum = 0;
19     int left_sum = INT_MIN;
20     int maxlow=0;
21     for (int i = m; i >= l; i--)
22     {
23         sum = sum + arr[i];
24         if (sum > left_sum){
25             left_sum = sum;
26             maxlow=i;
27         }
28     }
29     // Include elements on right of mid
30     sum = 0;
31     int right_sum = INT_MIN;
32     int maxhigh=0;
33     for (int i = m+1; i <= h; i++)
34     {
35         sum = sum + arr[i];
36         if (sum > right_sum){
37             right_sum = sum;
38             maxhigh=i;
39         }
40     }
41     ANS array;
42     array.low=maxlow;
43     array.high=maxhigh;
44     array.sum=left_sum + right_sum;
45     // Return sum of elements on Left and right of mid
46     return array;
47 }
48
```

```

49 // Returns sum of maximum sum subarray in arr[l..h]
50 ANS maxSubArraySum(int *arr, int l, int h)
51 {
52     ANS subarrayleft, subarrayright, subarraycross;
53     // Base Case: Only one element
54     if (l == h) {
55         subarrayleft.low = l;
56         subarrayleft.high = h;
57         subarrayleft.sum = arr[l];
58         return subarrayleft;
59     } else {
60
61         // 找出中間值
62         int m = (l + h) / 2;
63
64         subarrayleft = maxSubArraySum(arr, l, m);
65         subarrayright = maxSubArraySum(arr, m + 1, h);
66         subarraycross = maxCrossingSum(arr, l, m, h);
67
68         if (subarrayleft.sum >= subarrayright.sum && subarrayleft.sum >= subarraycross.sum)
69             return subarrayleft;
70         else if (subarrayright.sum >= subarrayleft.sum && subarrayright.sum >= subarraycross.sum)
71             return subarrayright;
72         else
73             return subarraycross;
74     }
75 }
76
77
78 int main() {
79     ANS answer;
80     int n; // while 迴圈可以不斷輸入
81     while (cin >> n) {
82         int *arr = new int[n];
83         for (int i = 0; i < n; i++) {
84             cin >> arr[i];
85         }
86         // 將整個arr代進function，傳回max_sum
87         answer = maxSubArraySum(arr, 0, n - 1);
88         cout << answer.low << " " << answer.high << " " << answer.sum << endl;
89         delete[] arr;
90     }
91     return 0;
92 }

```

Non-recursive:

程式摘要：

此程式用 C++ 語言

將所輸入的值做累加的，當有比較大的值則存入 Max

當累加的值突然遠小於之前的值，則歸零，並將 start 位置移到下一個位置

程式內容說明：

圖解:

Ex. N = 8 array = {7, -3, 1, -9, 10, 7, 6, 0}

對整個陣列往下累加，遇到某個加上去的極小值，則歸零

number	TempStart	TempEnd	TempSum	Start	End	Sum
7	0	0	7	0	0	7
-3	0	1	4	0	0	7
1	0	2	5	0	0	7
-9	0 -> 3+1 (起始位置 往後)	3	-4 -> 0 (歸零)	0	0	7
10	4	4	10	4	4	10
7	4	5	17	4	5	17
-6	4	6	11	4	5	17
0	4	7	11	4	5	17

虛擬碼:

```
1 maxSubSeqSum(A[], n)
2   for i=0 to n
3       temp = temp + A[i]
4       if temp<0
5           temp = 0
6           tempi=i+1
7       elseif temp>max
8           max = temp
9           maxi = tempi
10          maxj = i
11  return (maxi, maxj, max)
```

程式:

```
1 // Name: 810532011高靖雅
2 // Date: March 6, 2019
3 // Last Update: March 6, 2019
4 // Problem statement: Profit Maximization Problem by non-recursive method
5
6 #include<iostream>
7 using namespace std;
8 //宣告一個function找出最大subarray
9 int maxSubSeqSum(int arr[],int n);
10
11 int main() {
12     int n; //while迴圈可以不斷輸入
13     while (cin >> n) {
14         int arr[n];
15         for (int i = 0; i < n; i++) {
16             cin >> arr[i];
17         }
18         //將整個arr代進function
19         maxSubSeqSum(arr,n);
20     }
21     return 0;
22 }
23
24 int maxSubSeqSum(int arr[],int n){
25     int temp=0, tempi=0;
26     int max=0, maxi=0, maxj=0;
27
28     for(int i=0; i < n; i++)
29     { //arr一個一個加上去
30         temp=temp+arr[i];
31         //當加到某一個數使得整個值遠小於之前的值，則歸零
32         //（這邊設定成當值變為負的時候來判斷）
33         if(temp<0)
34         {
35             temp=0;
36             tempi=i+1; //此時start位置從for迴圈往後一個
37         }
38         //當新的值大於之前儲存的最大值，則更新最大值
39         //且同時儲存位置
40         else if(temp > max)
41         {
42             max = temp;
43             maxi = tempi; //start位置為陣列開始加的位置
44             maxj = i; //end位置為for迴圈所加的位置
45         }
46     }
47     cout<<maxi<<" "<<maxj<<" "<<max<<endl;
48 }
```