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## PRACTICE SET

### Questions

- Q6-1.** In *synchronous TDM*, each input has a reserved slot in the output frame. This can be inefficient if some input lines have no data to send. In *statistical TDM*, slots are dynamically allocated to improve bandwidth efficiency. Only when an input line has a slot's worth of data to send is it given a slot in the output frame.
- Q6-2.** In *spread spectrum*, we spread the bandwidth of a signal into a larger bandwidth. Spread spectrum techniques add redundancy; they spread the original spectrum needed for each station. The expanded bandwidth allows the source to wrap its message in a protective envelope for a more secure transmission. We discussed frequency hopping spread spectrum (FHSS) and direct sequence spread spectrum (DSSS).
- Q6-3.** The *frequency hopping spread spectrum* (FHSS) technique uses M different carrier frequencies that are modulated by the source signal. At one moment, the signal modulates one carrier frequency; at the next moment, the signal modulates another carrier frequency.
- Q6-4.** To maximize the efficiency of their infrastructure, telephone companies have traditionally multiplexed digital signals from lower data rate lines onto higher data rate lines. The *digital hierarchy* uses DS-0 (64 Kbps), DS-1 (1.544 Mbps), DS-2 (6.312 Mbps), DS-3 (44.376 Mbps), and DS-4 (274.176 Mbps).
- Q6-5.** *Multiplexing* is the set of techniques that allows the simultaneous transmission of multiple signals across a single data link.
- Q6-6.** FDM and WDM are used to combine analog signals; the bandwidth is shared. TDM is used to combine digital signals; the time is shared.
- Q6-7.** WDM is common for multiplexing *optical signals* because it allows the multiplexing of signals with a very high frequency.

- Q6-8.** In *multilevel TDM*, some lower-rate lines are combined to make a new line with the same data rate as the other lines. *Multiple slot TDM*, on the other hand, uses multiple slots for higher data rate lines to make them compatible with the lower data rate line. *Pulse stuffing TDM* is used when the data rates of some lines are not an integral multiple of other lines.
- Q6-9.** In *multiplexing*, the word *link* refers to the physical path. The word *channel* refers to the portion of a link that carries a transmission between a given pair of lines. One link can have many ( $n$ ) channels.
- Q6-10.** We discussed *frequency-division multiplexing* (FDM), *wave-division multiplexing* (WDM), and *time-division multiplexing* (TDM).
- Q6-11.** To maximize the efficiency of their infrastructure, telephone companies have traditionally multiplexed analog signals from lower-bandwidth lines onto higher-bandwidth lines. The *analog hierarchy* uses voice channels (4 KHz), *groups* (48 KHz), *supergroups* (240 KHz), *master groups* (2.4 MHz), and *jumbo groups* (15.12 MHz).
- Q6-12.** The *direct sequence spread spectrum* (DSSS) technique expands the bandwidth of the original signal. It replaces each data bit with  $n$  bits using a spread-impulse code.

## Problems

### P6-1.

- Each output frame carries 2 bits from each source plus one extra bit for synchronization. Frame size =  $20 \times 2 + 1 = 41$  bits.
- Each frame carries 2 bit from each source. Frame rate =  $200,000/2 = 100,000$  frames/s.
- Frame duration =  $1 / (\text{frame rate}) = 1 / 100,000 = 10$  ms.
- Data rate =  $(100,000 \text{ frames/s}) \times (41 \text{ bits/frame}) = 41$  Mbps.
- In each frame 40 bits out of 41 are useful. Efficiency =  $40/41 = 97.5\%$ .

### P6-2.

- The frame carries 6 bits from each of the first two sources and 3 bits from each of the second two sources. Frame size =  $6 \times 2 + 3 \times 2 = 18$  bits.
- Each frame carries 6 bit from each 300-kbps source or 3 bits from each 150 kbps. Frame rate =  $300,000 / 6 = 150,000 / 3 = 50,000$  frames/s.

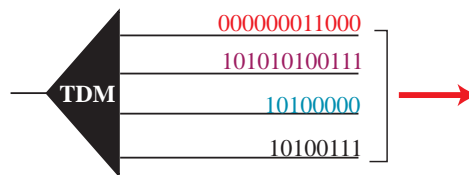
- c. Frame duration =  $1 / (\text{frame rate}) = 1 / 50,000 = 20 \text{ ms}$ .
- d. Output data rate =  $(50,000 \text{ frames/s}) \times (18 \text{ bits/frame}) = 900 \text{ kbps}$ . We can also calculate the output data rate as the sum of input data rates because there are no synchronization bits. Output data rate =  $2 \times 300 + 2 \times 150 = 900 \text{ kbps}$ .

**P6-3.**

- a. Group level: overhead =  $48 \text{ KHz} - (12 \times 4 \text{ KHz}) = 0 \text{ Hz}$ .
- b. Supergroup level: overhead =  $240 \text{ KHz} - (5 \times 48 \text{ KHz}) = 0 \text{ Hz}$ .
- c. Master group: overhead =  $2520 \text{ KHz} - (10 \times 240 \text{ KHz}) = 120 \text{ KHz}$ .
- d. Jumbo Group: overhead =  $16.984 \text{ MHz} - (6 \times 2.52 \text{ MHz}) = 1.864 \text{ MHz}$ .

**P6-4.**

- a. Frame size =  $6 \times (8 + 4) = 72 \text{ bits}$ .
- b. We can assume that we have only 6 input lines. Each frame needs to carry one character from each of these lines. This means that the frame rate is 500 frames/s.
- c. Frame duration =  $1 / (\text{frame rate}) = 1 / 500 = 2 \text{ ms}$ .
- d. Data rate =  $(500 \text{ frames/s}) \times (72 \text{ bits/frame}) = 36 \text{ kbps}$ .

**P6-5.** See the following figure.**P6-6.**

- a.  $2^4 = 16 \text{ hops}$
- b.  $(64 \text{ bits/s}) / 4 \text{ bits} = 16 \text{ cycles}$

**P6-7.** Random numbers are 11, 13, 10, 6, 12, 3, 8, 9 as calculated below:

$$\begin{aligned}
 N_1 &= 11 \\
 N_2 &= (5 + 7 \times 11) \bmod 17 - 1 = 13 \\
 N_3 &= (5 + 7 \times 13) \bmod 17 - 1 = 10 \\
 N_4 &= (5 + 7 \times 10) \bmod 17 - 1 = 6 \\
 N_5 &= (5 + 7 \times 6) \bmod 17 - 1 = 12 \\
 N_6 &= (5 + 7 \times 12) \bmod 17 - 1 = 3 \\
 N_7 &= (5 + 7 \times 3) \bmod 17 - 1 = 8 \\
 N_8 &= (5 + 7 \times 8) \bmod 17 - 1 = 9
 \end{aligned}$$

**P6-8.**

- a. DS-1 overhead = 1.544 Mbps – (24 × 64 kbps) = 8 kbps.
- b. DS-2 overhead = 6.312 Mbps – (4 × 1.544 Mbps) = 136 kbps.
- c. DS-3 overhead = 44.376 Mbps – (7 × 6.312 Mbps) = 192 kbps.
- d. DS-4 overhead = 274.176 Mbps – (6 × 44.376 Mbps) = 7.92 Mbps.

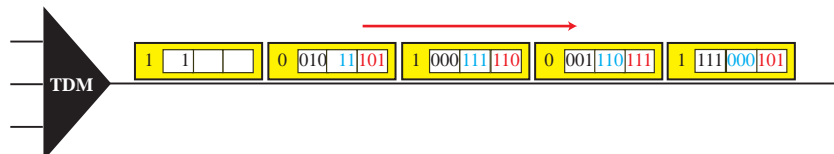
**P6-9.** The number of hops = 100 KHz/8 KHz = 12.5. So we need  $\log_2 12.5 = 3.64 \approx 4$  bits

**P6-10.**

- a. Each output frame carries 1 bit from each source plus one extra bit for synchronization. Frame size =  $40 \times 1 + 1 = 41$  bits.
- b. Each frame carries 1 bit from each source. Frame rate = 100,000 frames/s.
- c. Frame duration =  $1 / (\text{frame rate}) = 1 / 100,000 = 10$  ms.
- d. Data rate =  $(100,000 \text{ frames/s}) \times (41 \text{ bits/frame}) = 4.1 \text{ Mbps}$
- e. In each frame 40 bits out of 41 are useful. Efficiency =  $40/41 = 97.5\%$

**P6-11.** To multiplex 12 voice channels, we need eleven guard bands. The required bandwidth is then  $B = (4 \text{ KHz}) \times 12 + (500 \text{ Hz}) \times 11 = 53.5 \text{ KHz}$

**P6-12.** See the following figure.



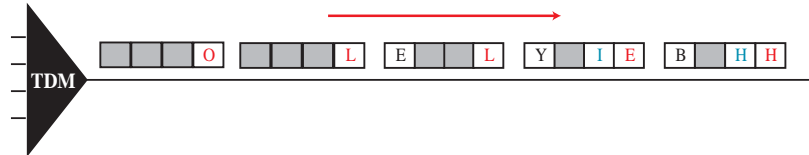
**P6-13.** We combine six 200-kbps sources into three 400-kbps. Now we have seven 400-kbps channel.

- Each output frame carries 1 bit from each of the seven 400-kbps line. Frame size =  $7 \times 1 = 7$  bits.
- Each frame carries 1 bit from each 400-kbps source. Frame rate = 400,000 frames/s.
- Frame duration =  $1 / (\text{frame rate}) = 1 / 400,000 = 2.5$  ms.
- Output data rate =  $(400,000 \text{ frames/s}) \times (7 \text{ bits/frame}) = 2.8 \text{ Mbps}$ . We can also calculate the output data rate as the sum of input data rate because there is no synchronizing bits. Output data rate =  $6 \times 200 + 4 \times 400 = 2.8 \text{ Mbps}$ .

**P6-14.**

- T-1 line sends 8000 frames/s. Frame duration =  $1/8000 = 125$  ms.
- Each frame carries one extra bit. Overhead =  $8000 \times 1 = 8 \text{ kbps}$

**P6-15.** See the following figure.



**P6-16.** The bandwidth allocated to each voice channel is  $30 \text{ KHz} / 100 = 300 \text{ Hz}$ . As we saw in the previous chapters, each digitized voice channel has a data rate of 64 Kbps ( $8000 \text{ sample} \times 8 \text{ bit/sample}$ ). This means that our modulation technique uses  $64,000/300 \approx 214 \text{ bits/Hz}$ .

**P6-17.** We need to add extra bits to the second source to make both rates = 190 kbps. Now we have two sources, each of 190 Kbps.

- The frame carries 1 bit from each source. Frame size =  $1 + 1 = 2$  bits.
- Each frame carries 1 bit from each 190-kbps source. Frame rate = 190,000 frames/s.
- Frame duration =  $1 / (\text{frame rate}) = 1 / 190,000 = 5.3$  ms.
- Output data rate =  $(190,000 \text{ frames/s}) \times (2 \text{ bits/frame}) = 380 \text{ kbps}$ . Here the output bit rate is greater than the sum of the input rates (370 kbps) because of extra bits added to the second source.

**P6-18.** The Barker chip is 11 bits, which means that it increases the bit rate 11 times. A voice channel of 64 kbps needs  $11 \times 64 \text{ kbps} = 704 \text{ kbps}$ . This means that the bandpass channel can carry  $(20 \text{ Mbps}) / (704 \text{ kbps})$  or approximately 28 channels.