

Stats.

- ① Chi Square Test
- ② ANOVA TEST (F Test).

Chi Square Test

- ① Chi Square Test claims about population proportions.

It is a non parametric test that is performed categorical (nominal or ordinal) data.

↳ Rank

- ② In the 2000 U.S Census the ages of individuals in a small town were found to be the following.

✓	✓	✓
<18	$18-35$	>35

20%	30%	50%
-----	-----	-----

In 2010, ages of $n=500$ individuals were sampled. Below are the results.

<18	$18-35$	>35
121	288	91

Using $\alpha=0.05$, would you conclude that the population distribution of ages has changed in the last 10 years?

Ans)

	<18	18-35	>35	
Expected	20%	30%	50%	↙

$$n=500$$

	<18	18-35	>35	
Observed	121	288	91	↙
Expected	100	150	250	↙
	200	2000	80	

- ① Null Hypothesis H_0 : The data meets the expected distribution
 H_1 : The data do not meet the " "

② $\alpha = 0.05 \quad C.I = 95\%$

$n=500 \rightarrow \text{Sample}$

③ Degree of freedom

(CHI SQUARED)

$$df = k - 1 = 3 - 1 = 2$$

2 Tailed Test

④ Decision Boundary $\Rightarrow 5.991$

$\chi^2 > 5.991$ Reject the H_0 .

⑤ Chi Square Test statistics

$$\chi^2 = \sum \frac{(f_o - f_e)^2}{f_e} = \frac{(121-100)^2}{100} + \frac{(288-150)^2}{150} + \frac{(91-250)^2}{250}.$$

$$\chi^2 = 232.494$$

$\chi^2 > 5.99$ Reject the H_0 .

- ④ 500 elementary school boys and girls are asked which is their favourite color: blue, green or pink. Results are shown below:

	Blue	Green	Pink	$\Rightarrow (3-1) = 2$
Boys	100	150	20	270
Girls	20	30	180	230
	120	180	200	500

Using $\alpha=0.05$, would you conclude that there is a relationship between gender and favorite color?

- ④ Null Hypothesis H_0 : Gender and favorite color are related ✓
 H_1 : . Not related.

- $$(f) \quad L = 0.05 \quad C.I = 95\%.$$

- ## Degree of freedom

$\Delta f = (\text{rows} - 1) (\text{columns} - 1)$

$$= (2-1) (3-1)$$

$$\therefore (1)(2) = \boxed{2}$$

- ④ Tut Stats = 5.991.

Q) Chi-square Test Statistics

$$\chi^2 = \sum \frac{(f_o - f_e)^2}{f_e}$$

		Blue	Green	Pink	
Observed	Boys	100	150	20	270
	Girls	20	30	180	230
		120	180	200	500

$$\Rightarrow (3-1) = 2$$

$$f_e = \frac{f_c f_r}{f_n}$$

$$= \frac{(100 - 64.8)^2}{64.8} + \frac{(150 - 97.2)^2}{97.2} +$$

		Blue	Green	Pink	
Expected	Boys	64.8	97.2	108	270
	Girls	55.2	82.8	92	230
		120	180	200	500

$$(Boy, Blue) = \frac{(120 \times 270)}{500} = 64.8$$

$$(Girl, Pink) = \frac{(200 \times 230)}{500}$$

$$(Boy, Green) = \frac{(180 \times 270)}{500} = 97.2$$

$$(Boy, Pink) = \frac{(200 \times 230)}{500} = 108$$

$$(Girl, Blue) = \frac{(120 \times 230)}{500} = 55.2$$

$$(Girl, Green) = \frac{(180 \times 230)}{500} = 82.8$$

$$\chi^2 = 259.78 > 5.99 \quad \text{Reject the H}_0.$$

{python}

(*) ANOVA Test (F Test) → {python}



Analysis of Variance

{ CHI SQUARE AND ANOVA }

Stats { python }

Interviews Questions

- ① Size of all the sharks in the world?

[C.I] ✓.

$$\begin{array}{l} n=25 \\ \hline \end{array} \quad \boxed{n = 40} \quad \boxed{\bar{x} = 5m} \quad \boxed{S = 0.5m}$$

$$\begin{array}{l} \alpha = 0.05 \\ \hline \end{array} \quad \boxed{n > 30} \rightarrow z_{\text{test}}$$

$Z_{\text{test}} = 0.7 + 1$

t test

$t_{\alpha/2}$

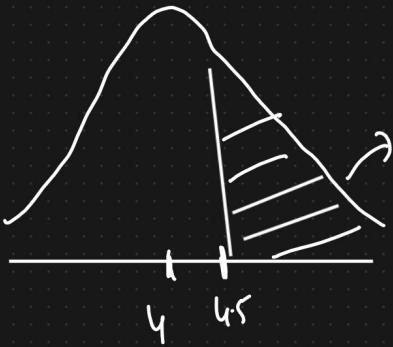
Point Estimate

$$\begin{array}{l} \bar{x} \pm \text{Margin of Error} \\ \bar{x} \pm Z_{\alpha/2} \left(\frac{S}{\sqrt{n}} \right). \end{array}$$

Amazon

Lower fence \longleftrightarrow Higher Fence

(*)



$\sigma = 0.5$

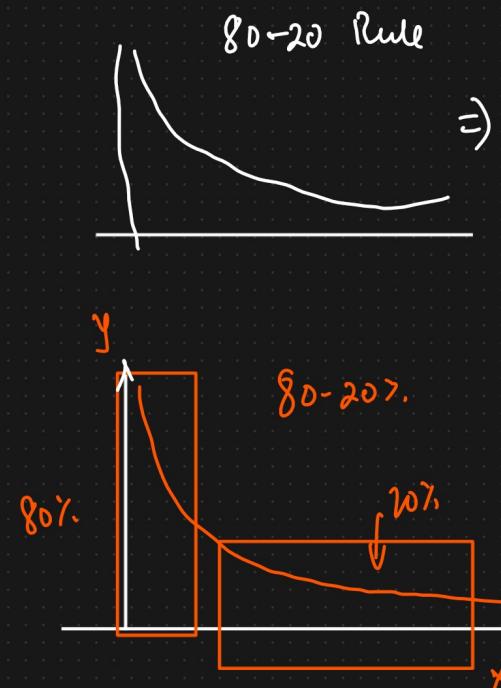
π Correlation

- ② Pearson & Spearman Rank Correlation

\downarrow
linear

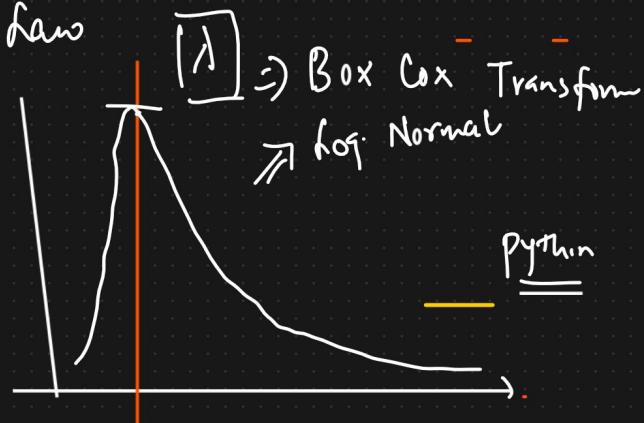
\downarrow
Non Linear Data.

Q) Oil Distribution in a place follows which distribution.

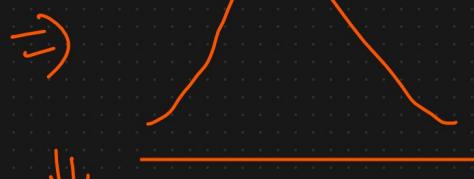
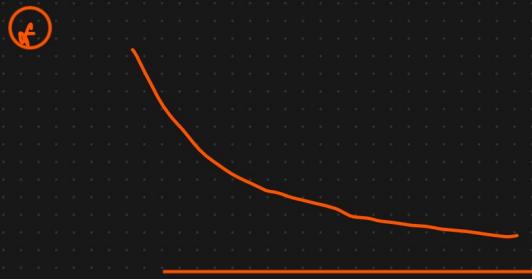


=> Pareto distribution

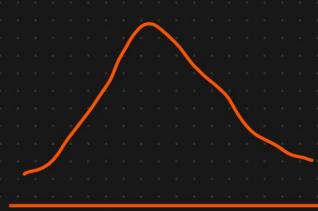
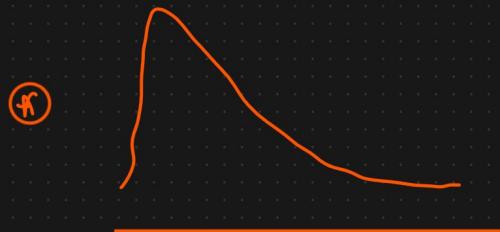
Power law



Eg:



Box Cox Transformation.





Normal values

④ Outliers := 5 Number Summary, Box plot

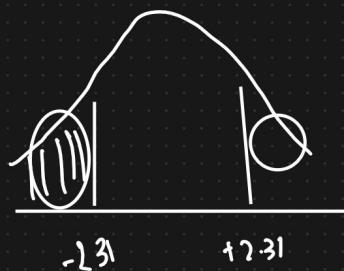
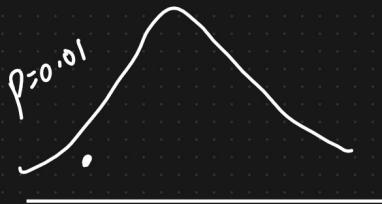
⑤ Z-score

⑥ Why variance by $n-1$? ^{Sample}

Bessel's correction Degrees of freedom



⑦ [CI] \Rightarrow P-value ✓



P-value is the probability
of the null hypothesis
to be True

⑧ f-test vs χ^2 -test

Bernoulli distribution {Binary} ^{outcomes.}

2 outcomes

Tossing coin \Rightarrow H or T

↓
Binomial distribution

$$P(H) = 0.5$$

$$P(T) = 0.5$$

Many Bernoulli experiments

$$P$$

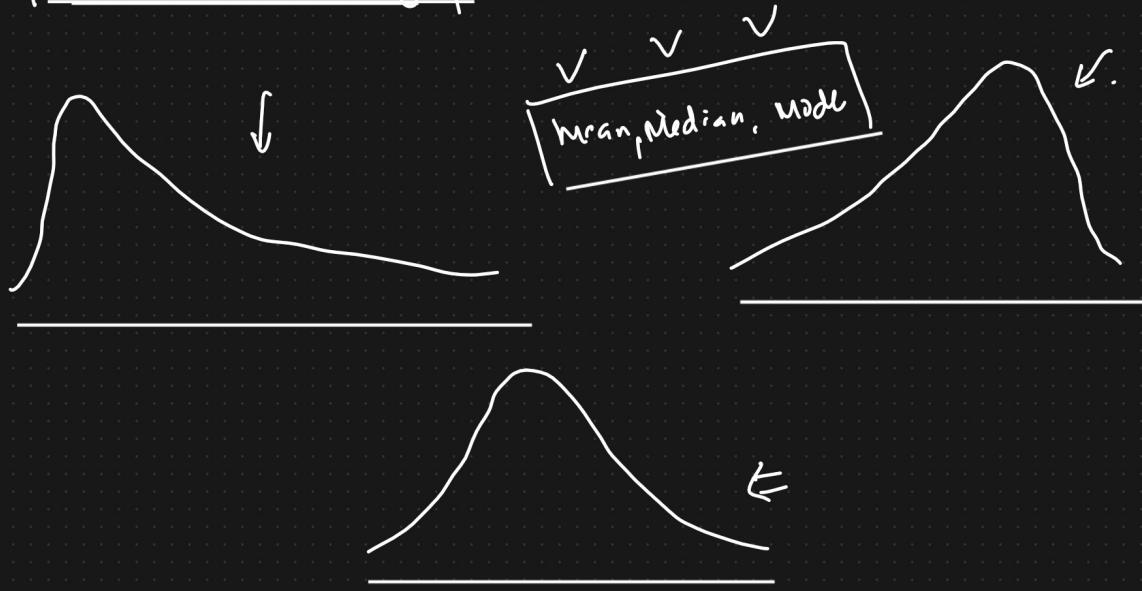
$$q = 1 - p$$

Tossing a coin 10 times



$$\{ \begin{matrix} P & P & P & P & P \\ q & q & q & q & q \end{matrix} \}$$

python programming



T-test for Proportion, Two Samples

① Researchers wants to test the effectiveness of a new anxiety medicine. In clinical testing, 64 out of 200 people taking the medicine report symptoms of anxiety. Of the people receiving a placebo, 92 out of 200 reports symptoms of anxiety. Is the medication working any different than the placebo? $\alpha = 0.05$ Test the claim?

1) Null hypothesis $H_0 = \boxed{P_1 = P_2}$

(k) Calculate Test Statistic

$$H_1 = \boxed{P_1 \neq P_2}$$

$$Z = \frac{\hat{P}_1 - \hat{P}_2}{\sqrt{\hat{P}(1-\hat{P})} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

$n_1 = 200$

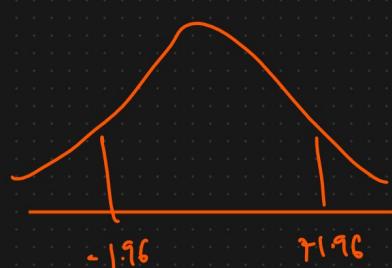
$n_2 = 200$

2) $\alpha = 0.05$ C.I: 95%

$$\hat{P}_1 = \frac{64}{200} = 0.32$$

$$\hat{P}_2 = \frac{92}{200} = 0.46$$

$$= -2.869$$



$$\hat{P} = \frac{n_1 + n_2}{n_1 + n_2} = \frac{64 + 92}{200 + 200} = 0.35$$

$-2.869 < -1.96$ Reject the Null Hypothesis