EE 238

Power Engineering - II

Power Electronics



Lecture 12

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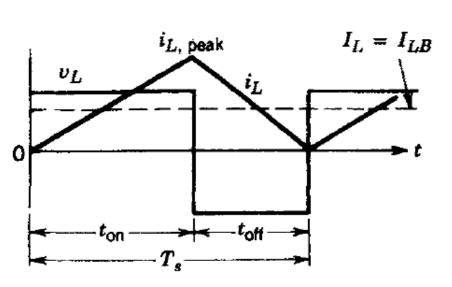
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BOOST CHOPPER

Boundary between Cont. and Discont. Modes

$$\frac{V_o}{V_d} = \frac{T_s}{t_{\text{off}}} = \frac{1}{1 - D}$$

$$\frac{I_o}{I_d} = (1 - D)$$



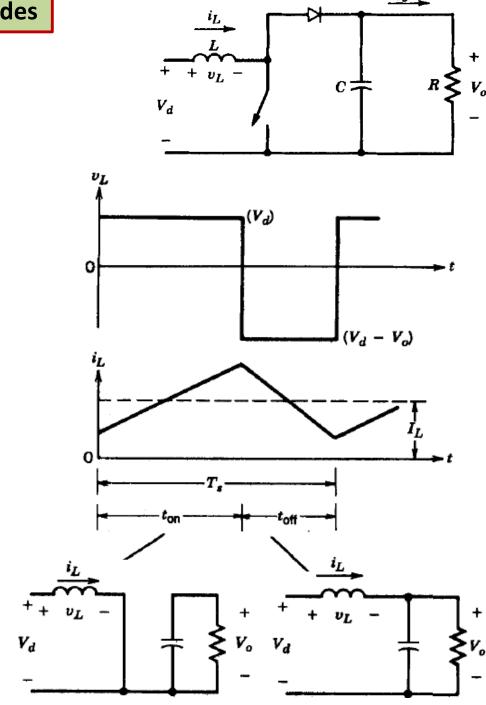
$$I_{LB} = \frac{1}{2} i_{L,\text{peak}}$$

$$= \frac{1}{2} \frac{V_d}{L} t_{\rm on}$$

$$= \frac{T_s V_o}{2L} D(1 - D)$$

The average output current at the edge of cont. cond. is $I_{oB} = \frac{T_s V_o}{2L} D(1 - D)^2$

$$I_{oB} = \frac{T_s V_o}{2L} D(1-D)^2$$



STEP-UP (BOOST) CONVERTER | Boundary between Cont. and Discont. Modes

$$I_{LB} = \frac{T_s V_o}{2L} D(1-D) \frac{I_o}{I_d} = (1-D) \frac{i_d = i_L}{I_d}$$

at the edge of cont. cond. is $I_{oB} = \frac{T_s V_o}{2L} D(1 - D)^2$ The average output current

$$I_{oB} = \frac{T_s V_o}{2L} D(1-D)^2$$

In most Boost converter applications, V_0 is kept constant.

$$I_{LB}$$
 reaches a maximum value at D = 0.5: $I_{LB,max} = \frac{T_s V_o}{8I_c}$

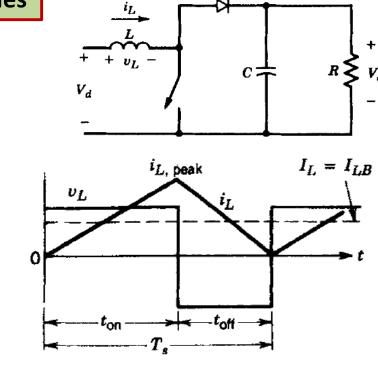
Also,
$$I_{0B}$$
 has its maximum at D = 0.333 $I_{oB,\text{max}} = \frac{2}{27} \frac{T_s V_o}{L} = 0.074 \frac{T_s V_o}{L}$

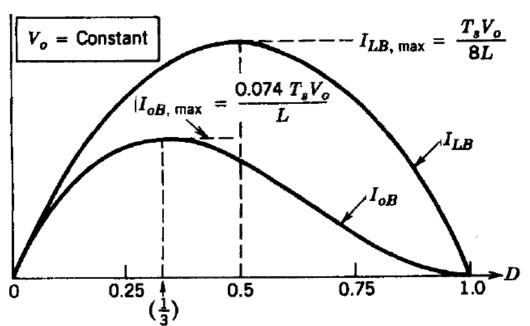
In terms of their maximum values,

$$I_{LB} = 4D(1 - D)I_{LB,\text{max}}$$

$$I_{oB} = \frac{27}{4}D(1 - D)^2I_{oB,\text{max}}$$

For a given D_r , with constant V_{0r} , if the average load current drops below I_{OB} (and, hence, the average inductor current below I_{LB}), the current conduction will become discontinuous.

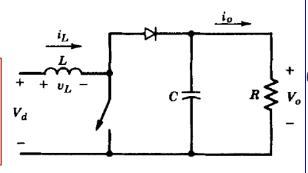


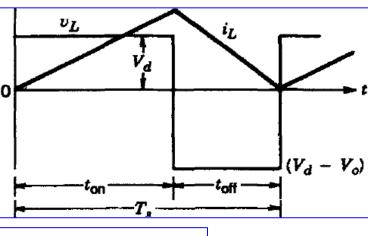


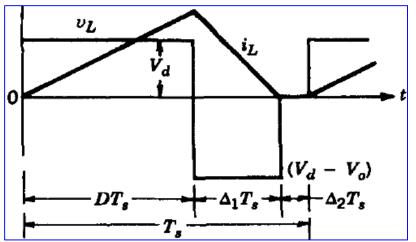
DISCONTINUOUS-CONDUCTION MODE

Assume that as the output load power decreases, Vd and D remain constant (even though, in practice, D would vary in order to keep Vo constant).

- The DCM occurs due to decreased Po (=Pd) and, hence, a lower I_1 (= I_d), since v_d is constant.
- Since i_{Lpeak} is the same in both modes, a lower value of I₁ (and, hence a discontinuous I₁) is possible only if Vo goes up.







If we equate the integral of the inductor $V_dDT_s + (V_d - V_o)\Delta_1T_s = 0$ voltage over one time period to zero,

$$\frac{I_o}{I_d} = \frac{\Delta_1}{\Delta_1 + D} \quad \text{(since } P_d = P_o\text{)}$$

$$\therefore \frac{V_o}{V_d} = \frac{\Delta_1 + D}{\Delta_1}$$

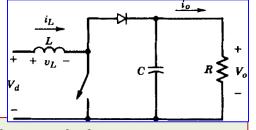
The average input current, which is also equal to the inductor current, is $I_d = \frac{V_d}{2L}DT_s(D + \Delta_1)$

$$I_d = \frac{V_d}{2L} DT_s(D + \Delta_1) \implies I_o = \left(\frac{T_s V_d}{2L}\right) D\Delta$$

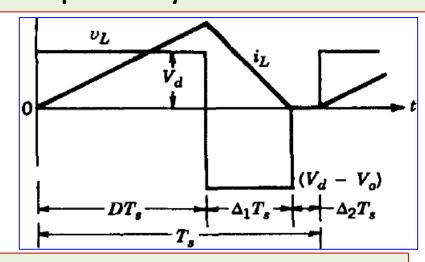
DISCONTINUOUS-CONDUCTION MODE

$$I_o = \left(\frac{T_s V_d}{2L}\right) D \Delta_1 \frac{V_o}{V_d} = \frac{\Delta_1 + D}{\Delta_1}$$

$$I_{oB,\text{max}} = \frac{2}{27} \frac{T_s V_o}{L} = 0.074 \frac{T_s V_o}{L}$$



In practice, since V_0 is held constant and D varies in response to the variation in V_0 , it is more useful to obtain the required duty ratio D as a function of load current for various values of V_0 / V_0 .



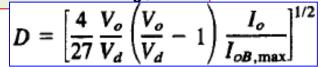
In the discontinuous mode, if V_0 is not controlled during each switching time period, at least $L_{:2}$

are transferred from the input to the $\frac{L}{2}i_{L,peak}^2 = \frac{(V_d DT_s)^2}{2L}$

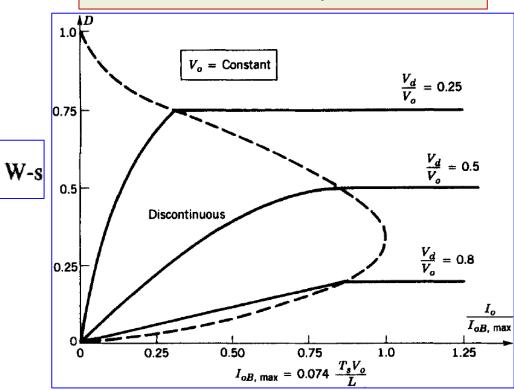
output capacitor and to the load.

For constant output voltage and variable input voltage applications

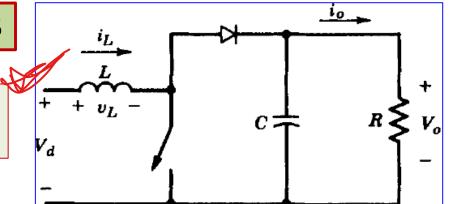
$$\left(1 - \frac{V_{in,max}}{V_o}\right) \le D \le \left(1 - \frac{V_{in,min}}{V_o}\right)$$



D is plotted as a function of Io/IoBmax for various values of Vd/V0.

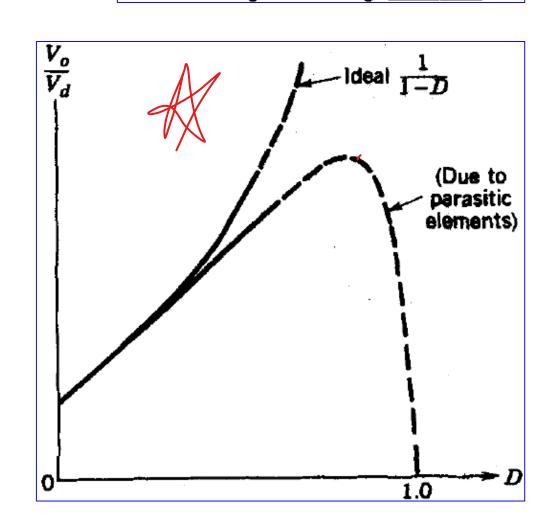


The parasitic elements in a step-up converter are due to the losses associated with the inductor, the capacitor, the switch, and the diode.



Unlike the ideal characteristic, in practice, V_0/V_d declines as D approaches unity.

These parasitic elements can be incorporated into circuit simulation programs on computers for designing such converters.



Inductor Resistance

- L should be designed to have small resistance to minimize power loss and maximize efficiency.
- The existence of a small inductor resistance does not substantially change the buck converter analysis:
- However, inductor resistance affects performance of the boost converter, especially at high duty ratios.

For analysis purpose, assume that iL is approximately constant.

Neglecting other losses. And applying power balance:

$$P_s = P_o + P_{r_L}$$
$$V_s I_L = V_o I_D + I_L^2 r_L$$

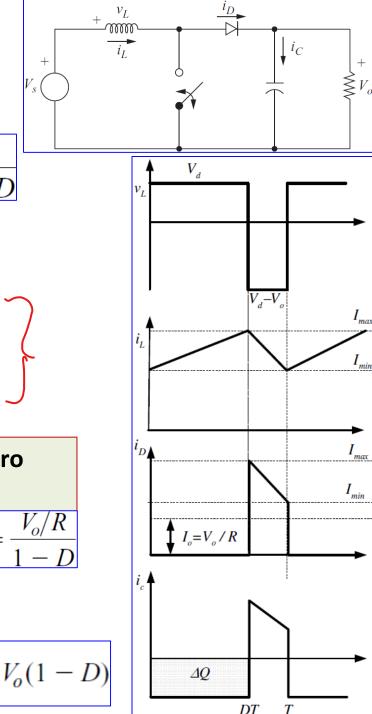
 r_L is the series resistance of L.

The diode current is equal to the inductor current when the switch is off and is zero when the switch is on. Therefore, the average diode current is $I_D = I_L(1-D)$

From above,
$$V_s I_L = V_o I_L (1 - D) + I_L^2 r_L$$

=> $V_s = V_o (1 - D) + I_L r_L$

Also,
$$I_L = \frac{I_D}{1 - D} = \frac{V_o/R}{1 - D}$$
 => $V_s = V_s = V_s$



Solving for V_a , This eqn. is similar to that for an ideal converter **Inductor Resistance** but includes a correction factor to account for rL. $V_s = \frac{V_o r_L}{R(1-D)} + V_o (1-D) \quad V_o = \left(\frac{V_s}{1-D}\right) \left(\frac{1}{1 + r_L/[R(1-D)^2]}\right)$ 10 \vdash V_o/V_s vs. D The inductor resistance also has an effect on the power efficiency of converters. Efficiency is the ratio of output power to output power plus losses. For the boost Ideal converter $\frac{P_o}{P_o + P_{\text{loss}}} = \frac{V_o^2 / R}{V_o^2 / R + I_L^2 r_L}$ $\frac{V_o^2/R + (V_o/R)^2/(1-D)r_L}{1+r_L[R(1-D)^2]}$ Nonideal Efficiency vs. D 1.0 As D increases, the Ideal converter efficiency 0.4D0.6 0.8 decreases. 0.8Output voltage of the boost converter with and without inductor resistance. 6.0 6.0 6.0 Nonideal Effect is dominant at high D Difficult to achieve large conversion ratios (> 10) 0.2 No power transfer at D = 1 0.2 D0.40.6 0.8

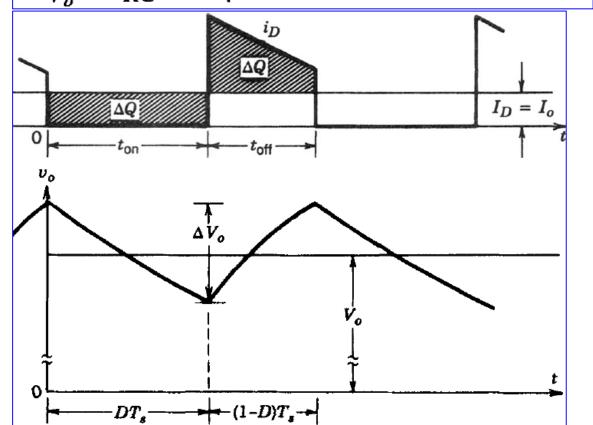
OUTPUT VOLTAGE RIPPLE (ΔV_0)

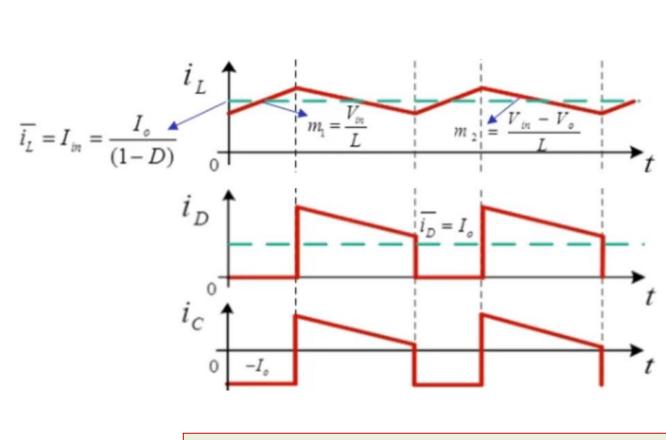
CCM: Assuming that all the ripple component i_D flows through C and its average value flows through the load resistor, the shaded area represents charge ΔQ .

Current-sec. balance principle:

$$\Delta V_o = \frac{\Delta Q}{C} = \frac{I_o D T_s}{C} = \frac{V_o}{R} \frac{D T}{C}$$

$$\therefore \frac{\Delta V_o}{V_o} = \frac{DT_s}{RC} = D\frac{T_s}{\tau} \quad \text{(where } \tau = RC \text{ time constant)}$$





A similar analysis can be performed for the discontinuous mode of conduction.

Buck-Boost Converter

The main application of a buck-boost converter is in regulated dc power supplies, where a negative-polarity output may be desired with respect to the common terminal of the input voltage, and the output voltage can be either higher or lower than the input voltage.

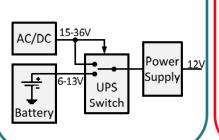
Buck-boost applications

Industrial PCs



Application needs

- 6 V-36 V_{IN} from AC-powered supply or battery
- 12 V output, 60 W-200 W

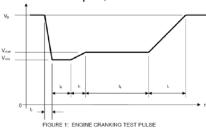


Automotive start/stop & DVRs



Application needs

- 9 V-16 V_{IN}, 3.5 V during start
- ~12 V output, 60 W-120 W



USB power delivery



Application needs

- 12 V bus or battery, 9V–16 V_{IN}
- 5/12/20 V_{OUT}, 10 W–100 W

USB Power Delivery profiles

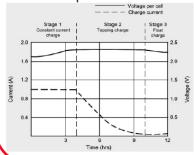
CCZ r oner Zentery premise			
Profile	+5 V	+12 V	+20 V
1	2.0 A, 10 W	N/A	N/A
2		1.5 A, 18 W	N/A
3		3.0 A, 36 W	N/A
4			3.0 A, 60 W
5		5.0 A, 60 W	5.0 A, 100 W

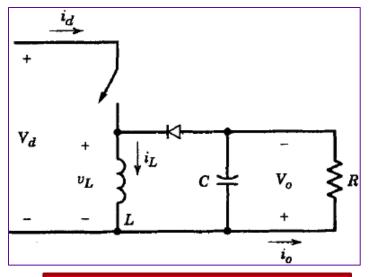
Industrial & battery chargers



Application needs

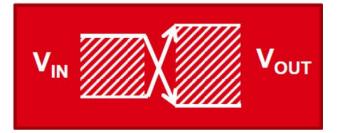
- 12 V or 24 V_{IN} or DC adapter
- CC/CV up to 200 W+



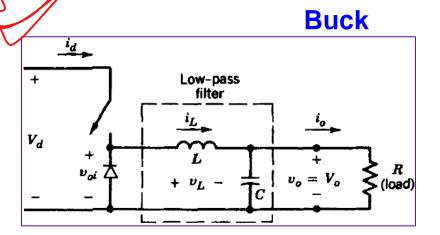


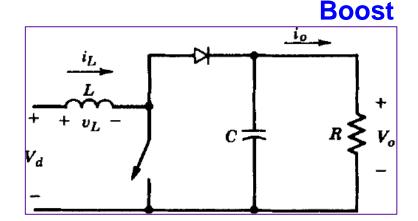




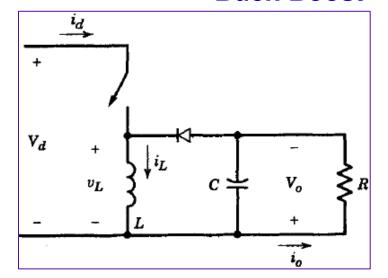


buck-boost converter can be obtained by the cascade connection of the two basic converters: the stepdown converter and the step-up converter.





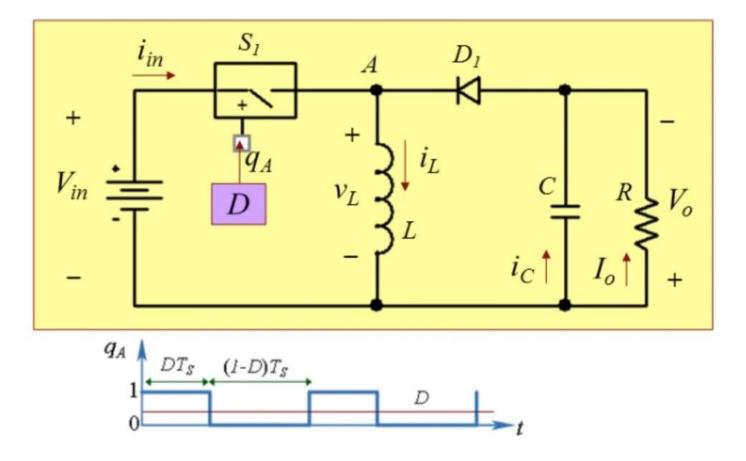
Buck-Boost



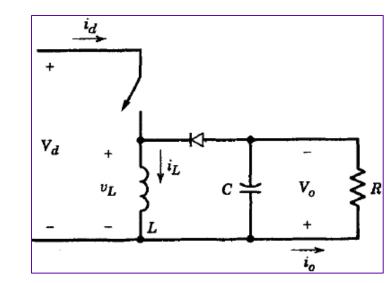
In steady state, the output-to-input voltage conversion ratio is the product of the conversion ratios of the two converters in cascade (assuming that switches in both converters have the same D):

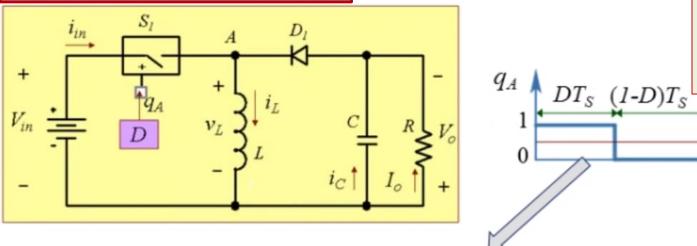
This allows the output voltage to be higher or lower than the input voltage, based on the duty ratio *D*.

$$\frac{V_o}{V_d} = D \frac{1}{1 - D}$$

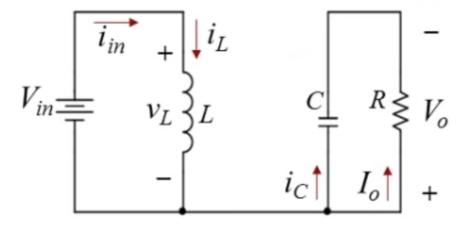


- Step up as well as step down depending on D
- Negative output (with respect to input ground)
- Isolated version flyback converter quite popular at low (~100 W) power level



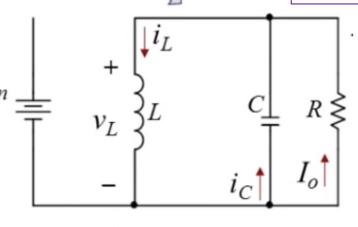


- When the switch is closed, the input provides energy to the inductor and the diode is reverse biased.
- When the switch is open, the energy stored in the inductor is transferred to the output.
- No energy is supplied by the input during this interval.

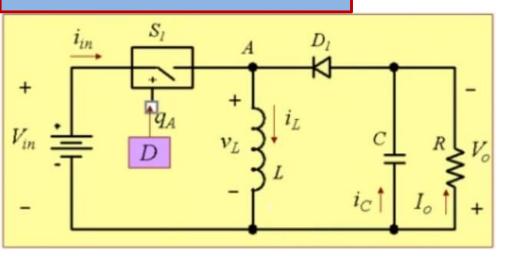


0

- $v_L = V_{in}$
- i_L and energy stored in L increase
- C supports load and discharges
- C large enough to maintain voltage almost constant (small ripple)



- $v_L = -V_0$
- i_L and energy stored in L decrease, energy fed to C and R
- i_C positive and C charges up
- C large enough to maintain voltage almost constant (small ripple)

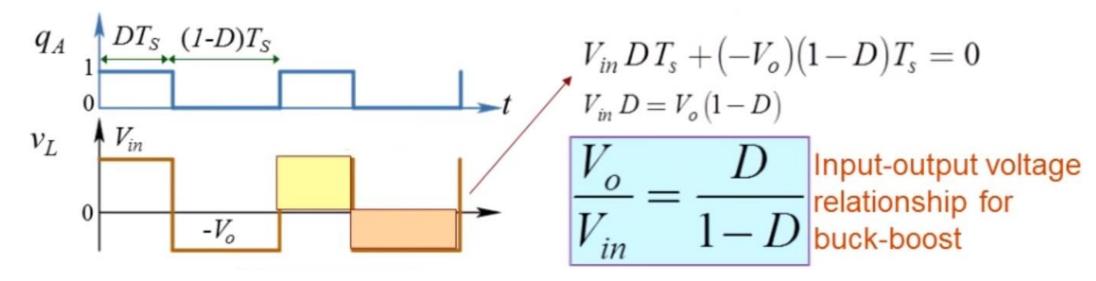


Buck operation for

$$D \le 0.5$$

Boost operation for

$$D \ge 0.5$$



$$\frac{I_{in}}{I_o} = \frac{D}{1 - D}$$

Input-output current relationship using power balance

Switch closed

$$v_L = Vd = L \frac{di_L}{dt}$$

$$\Rightarrow \frac{di_L}{dt} = \frac{V_d}{I_L}$$

$$\frac{\Delta i_L}{\Delta t} = \frac{\Delta i_L}{DT} = \frac{V_d}{L}$$

$$\Rightarrow (\Delta i_L)_{closed} = \frac{V_d DT}{L}$$

Switch opened

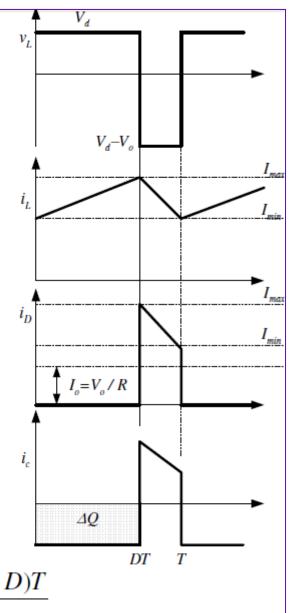
$$v_L = V_o = L \frac{di_L}{dt}$$

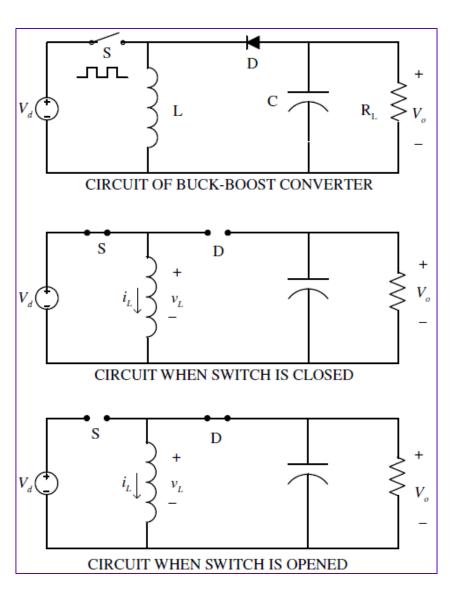
$$\Rightarrow \frac{di_L}{dt} = \frac{V_o}{I_c}$$

$$\frac{\Delta i_L}{\Delta t} = \frac{\Delta i_L}{(1-D)T} = \frac{V_o}{I_c}$$

$$\frac{\Delta i_L}{\Delta t} = \frac{\Delta i_L}{(1-D)T} = \frac{V_o}{L}$$

$$\Rightarrow (\Delta i_L)_{opened} = \frac{V_o(1-D)T}{L}$$





Steady state operation:

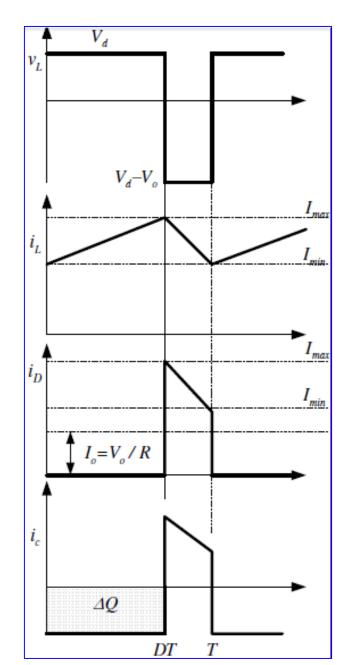
$$\Delta_{iL(closed)} + \Delta_{iL(opened)} = 0$$

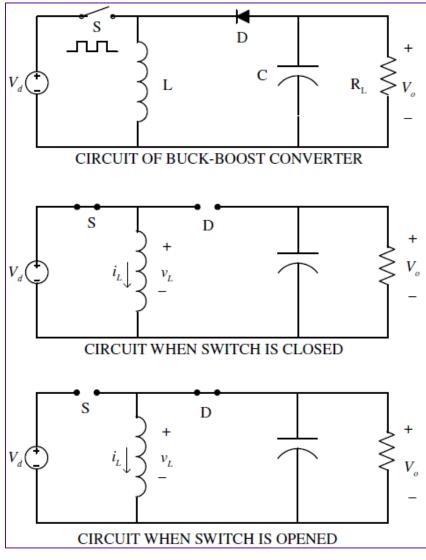
$$\Rightarrow \frac{V_d DT}{L} + \frac{V_o (1 - D)T}{L} = 0$$

Output voltage:

$$\Rightarrow$$
 V_o = $-V_s \left(\frac{D}{1 - D} \right)$

- NOTE: Output of a buck-boost converter either be higher or lower than input.
 - If D>0.5, output is higher than input
 - If D<0.5, output is lower input
- Output voltage is always negative.
- Note that output is never directly connected to load.
- Energy is stored in inductor when switch is closed and transferred to load when switch is opened.





Comparison of v₁ in Buck, Boost and Buck-Boost

