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1 ssm1 Theory

Built: 23 April 2019 Parent Theories: satList

1.1 Datatypes

```
configuration =
    CFG (('command inst, 'principal, 'd, 'e) Form -> bool)
        ('state -> ('command inst, 'principal, 'd, 'e) Form)
        (('command inst, 'principal, 'd, 'e) Form list)
        (('command inst, 'principal, 'd, 'e) Form list) 'state
        ('output list)

inst = SOME 'command | NONE

trType = discard | trap 'command | exec 'command
```

1.2 Definitions

```
[TR_def]
 ⊢ TR =
    (\lambda a_0 \ a_1 \ a_2 \ a_3.
        \forall TR'.
           (\forall a_0 \ a_1 \ a_2 \ a_3.
               (\exists input Test\ P\ NS\ M\ Oi\ Os\ Out\ s\ cert List\ state Interp
                    cmd ins outs.
                   (a_0 = (M, Oi, Os)) \land (a_1 = exec \ cmd) \land
                   (a_2 =
                    CFG inputTest stateInterp certList
                       (P says prop (SOME cmd)::ins) s outs) \land
                   (a_3 =
                    {\tt CFG}\ input Test\ state Interp\ cert List\ ins
                       (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs)) \ \land
                   inputTest (P says prop (SOME cmd)) \land
                  CFGInterpret (M, Oi, Os)
                     (CFG inputTest\ stateInterp\ certList
                         (P says prop (SOME cmd)::ins) s outs)) \lor
               (\exists input Test\ P\ NS\ M\ Oi\ Os\ Out\ s\ cert List\ state Interp
                    cmd ins outs.
                   (a_0 = (M, Oi, Os)) \land (a_1 = trap \ cmd) \land
                   (a_2 =
                    CFG inputTest stateInterp certList
                       (P says prop (SOME cmd)::ins) s outs) \land
```

SSM1 THEORY Theorems

```
(a_3 =
        CFG inputTest stateInterp certList ins
           (NS s (trap cmd)) (Out s (trap cmd)::outs)) \land
       inputTest (P says prop (SOME cmd)) \land
       CFGInterpret (M, Oi, Os)
          (CFG inputTest stateInterp certList
              (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs)) \ \lor
   (\exists input Test\ NS\ M\ Oi\ Os\ Out\ s\ cert List\ state Interp\ cmd
        x ins outs.
       (a_0 = (M, Oi, Os)) \wedge (a_1 = discard) \wedge
       (a_2 =
        CFG inputTest stateInterp certList (x::ins) s
           outs) \land
       (a_3 =
        CFG inputTest stateInterp certList ins
           (NS \ s \ \text{discard}) (Out \ s \ \text{discard}::outs)) \land
       \neg inputTest \ x) \Rightarrow
   TR' a_0 a_1 a_2 a_3) \Rightarrow
TR' a_0 a_1 a_2 a_3)
```

1.3 Theorems

```
[CFGInterpret_def]
 \vdash CFGInterpret (M, Oi, Os)
         (CFG inputTest stateInterp context (x::ins) state
             outStream) \iff
     (M,Oi,Os) satList context \land (M,Oi,Os) sat x \land (M,Oi,Os)
     (M, Oi, Os) sat stateInterp state
[CFGInterpret_ind]
  \vdash \forall P.
        (\forall M \ Oi \ Os \ input Test \ state Interp \ context \ x \ ins \ state
              outStream.
             P (M, Oi, Os)
                (CFG inputTest stateInterp context (x::ins) state
                    outStream)) \land
         (\forall v_{15} \ v_{10} \ v_{11} \ v_{12} \ v_{13} \ v_{14}.
             P \ v_{15} \ (CFG \ v_{10} \ v_{11} \ v_{12} \ [] \ v_{13} \ v_{14})) \ \Rightarrow
        \forall v \ v_1 \ v_2 \ v_3. P \ (v, v_1, v_2) \ v_3
[configuration_one_one]
 \vdash \forall a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_0' \ a_1' \ a_2' \ a_3' \ a_4' \ a_5'.
        (CFG a_0 a_1 a_2 a_3 a_4 a_5 = CFG a_0' a_1' a_2' a_3' a_4' a_5') \iff
        (a_0 = a_0') \wedge (a_1 = a_1') \wedge (a_2 = a_2') \wedge (a_3 = a_3') \wedge
        (a_4 = a'_4) \wedge (a_5 = a'_5)
```

Theorems SSM1 THEORY

```
[inst_distinct_clauses]
 \vdash \forall a. SOME a \neq \texttt{NONE}
[inst_one_one]
 \vdash \forall a \ a'. (SOME a = SOME \ a') \iff (a = a')
[TR_cases]
 \vdash \forall a_0 \ a_1 \ a_2 \ a_3.
      TR a_0 a_1 a_2 a_3 \iff
       (\exists input Test\ P\ NS\ M\ Oi\ Os\ Out\ s\ cert List\ state Interp\ cmd\ ins
           (a_0 = (M, Oi, Os)) \land (a_1 = exec \ cmd) \land
           (a_2 =
           {\tt CFG} \ input Test \ state Interp \ cert List
              (P says prop (SOME cmd)::ins) s outs) \land
           (a_3 =
           {\tt CFG} inputTest stateInterp certList ins
              (NS s (exec cmd)) (Out s (exec cmd)::outs)) \land
          inputTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG inputTest\ stateInterp\ certList
                 (P \text{ says prop (SOME } cmd)::ins) \ s \ outs)) \lor
       (\exists input Test P NS M Oi Os Out s certList stateInterp cmd ins
           (a_0 = (M, Oi, Os)) \land (a_1 = trap \ cmd) \land
           (a_2 =
           {\tt CFG} inputTest stateInterp certList
              (P says prop (SOME cmd)::ins) s outs) \land
           (a_3 =
           CFG inputTest stateInterp certList ins
              (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs)) \ \land
           inputTest (P says prop (SOME cmd)) \wedge
          CFGInterpret (M, Oi, Os)
             (CFG inputTest stateInterp certList
                 (P \text{ says prop (SOME } cmd)::ins) \ s \ outs)) \lor
       \exists inputTest\ NS\ M\ Oi\ Os\ Out\ s\ certList\ stateInterp\ cmd\ x\ ins
         (a_0 = (M, Oi, Os)) \land (a_1 = discard) \land
         (a_2 =
          CFG inputTest stateInterp certList (x::ins) s outs) \land
         (a_3 =
          CFG inputTest stateInterp certList ins (NS s discard)
             (Out \ s \ discard::outs)) \land \neg input Test \ x
```

SSM1 THEORY Theorems

```
[TR_discard_cmd_rule]
 \vdash TR (M, Oi, Os) discard
      (CFG inputTest stateInterp certList (x::ins) s outs)
      (CFG inputTest stateInterp certList ins (NS s discard)
          (Out \ s \ discard::outs)) \iff \neg input Test \ x
[TR_EQ_rules_thm]
 \vdash (TR (M,Oi,Os) (exec cmd)
       (CFG inputTest stateInterp certList
           (P says prop (SOME cmd)::ins) s outs)
       (CFG inputTest stateInterp certList ins (NS s (exec cmd))
           (Out \ s \ (exec \ cmd)::outs)) \iff
     inputTest (P says prop (SOME cmd)) \land
     CFGInterpret (M, Oi, Os)
       (CFG inputTest stateInterp certList
           (P \text{ says prop (SOME } cmd)::ins) \ s \ outs)) \land
    (TR (M, Oi, Os) (trap cmd)
       (CFG inputTest\ stateInterp\ certList
           (P says prop (SOME cmd)::ins) s outs)
       (CFG inputTest stateInterp certList ins (NS s (trap cmd))
           (Out \ s \ (trap \ cmd)::outs)) \iff
     inputTest (P says prop (SOME cmd)) \land
     CFGInterpret (M, Oi, Os)
       (CFG inputTest stateInterp certList
           (P says prop (SOME cmd)::ins) s outs)) \land
    (TR (M, Oi, Os) discard
       (CFG inputTest stateInterp certList (x::ins) s outs)
       (CFG inputTest stateInterp certList ins (NS s discard)
           (Out \ s \ discard::outs)) \iff \neg inputTest \ x)
[TR_exec_cmd_rule]
 \vdash \forall inputTest \ certList \ stateInterp \ P \ cmd \ ins \ s \ outs.
      (\forall M \ Oi \ Os.
          CFGInterpret (M, Oi, Os)
            (CFG inputTest\ stateInterp\ certList
                (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
          (M, Oi, Os) sat prop (SOME cmd)) \Rightarrow
      \forall NS \ Out \ M \ Oi \ Os.
        TR (M, Oi, Os) (exec cmd)
           (CFG inputTest stateInterp certList
               (P says prop (SOME cmd)::ins) s outs)
           (CFG inputTest stateInterp certList ins
              (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs)) \iff
         inputTest (P says prop (SOME cmd)) \wedge
```

Theorems SSM1 THEORY

```
CFGInterpret (M, Oi, Os)
             (CFG inputTest stateInterp certList
                 (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \ \land
          (M,Oi,Os) sat prop (SOME cmd)
[TR_ind]
 \vdash \forall TR'.
       (\forall \mathit{inputTest}\ P\ \mathit{NS}\ \mathit{M}\ \mathit{Oi}\ \mathit{Os}\ \mathit{Out}\ \mathit{s}\ \mathit{certList}\ \mathit{stateInterp}\ \mathit{cmd}\ \mathit{ins}
             outs.
           inputTest (P says prop (SOME cmd)) \land
           CFGInterpret (M, Oi, Os)
              (CFG inputTest stateInterp certList
                  (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
            TR' (M, Oi, Os) (exec cmd)
              (CFG inputTest stateInterp certList
                  (P says prop (SOME cmd)::ins) s outs)
              (CFG inputTest stateInterp certList ins
                  (NS\ s\ (exec\ cmd)) (Out\ s\ (exec\ cmd)::outs))) \land
       (\forall input Test \ P \ NS \ M \ Oi \ Os \ Out \ s \ cert List \ state Interp \ cmd \ ins
            outs.
           inputTest (P says prop (SOME cmd)) \land
           CFGInterpret (M, Oi, Os)
              (CFG inputTest stateInterp certList
                  (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
            TR' (M, Oi, Os) (trap cmd)
              (CFG inputTest\ stateInterp\ certList
                  (P says prop (SOME cmd)::ins) s outs)
              (CFG inputTest stateInterp certList ins
                  (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs))) \land
       (\forall input Test\ NS\ M\ Oi\ Os\ Out\ s\ cert List\ state Interp\ cmd\ x\ ins
            outs.
           \neg inputTest \ x \Rightarrow
            TR' (M, Oi, Os) discard
              (CFG inputTest stateInterp certList (x::ins) s outs)
              (CFG inputTest stateInterp certList ins (NS s discard)
                  (Out \ s \ discard::outs))) \Rightarrow
       \forall a_0 \ a_1 \ a_2 \ a_3. TR a_0 \ a_1 \ a_2 \ a_3 \Rightarrow TR' \ a_0 \ a_1 \ a_2 \ a_3
[TR_rules]
 \vdash (\forall inputTest\ P\ NS\ M\ Oi\ Os\ Out\ s\ certList\ stateInterp\ cmd\ ins
        inputTest (P says prop (SOME cmd)) \land
        CFGInterpret (M, Oi, Os)
           (CFG inputTest stateInterp certList
               (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
```

SSM1 THEORY Theorems

```
TR (M, Oi, Os) (exec cmd)
          (CFG inputTest stateInterp certList
              (P says prop (SOME cmd)::ins) s outs)
          (CFG inputTest\ stateInterp\ certList\ ins
              (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs))) \ \land
    (\forall input Test P NS M Oi Os Out s certList stateInterp cmd ins
        inputTest (P says prop (SOME cmd)) \land
        CFGInterpret (M, Oi, Os)
          (CFG inputTest stateInterp certList
              (P \text{ says prop (SOME } cmd)::ins) \ s \ outs) \Rightarrow
        TR (M, Oi, Os) (trap cmd)
          (CFG inputTest stateInterp certList
              (P says prop (SOME cmd)::ins) s outs)
          (CFG inputTest\ stateInterp\ certList\ ins
              (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs))) \ \land
    \forall inputTest\ NS\ M\ Oi\ Os\ Out\ s\ certList\ stateInterp\ cmd\ x\ ins
        outs.
      \neg inputTest \ x \Rightarrow
      TR (M, Oi, Os) discard
         (CFG inputTest stateInterp certList (x::ins) s outs)
         (CFG inputTest stateInterp certList ins (NS s discard)
             (Out s discard::outs))
[TR_strongind]
 \vdash \forall TR'.
       (\forall input Test \ P \ NS \ M \ Oi \ Os \ Out \ s \ cert List \ state Interp \ cmd \ ins
          inputTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG inputTest\ stateInterp\ certList
                 (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
          TR' (M,Oi,Os) (exec cmd)
             (CFG inputTest stateInterp certList
                 (P says prop (SOME cmd)::ins) s outs)
             (CFG inputTest stateInterp certList ins
                (NS \ s \ (exec \ cmd)) \ (Out \ s \ (exec \ cmd)::outs))) \ \land
       (\forall input Test \ P \ NS \ M \ Oi \ Os \ Out \ s \ cert List \ state Interp \ cmd \ ins
          inputTest (P says prop (SOME cmd)) \land
          CFGInterpret (M, Oi, Os)
             (CFG inputTest\ stateInterp\ certList
                 (P \text{ says prop } (SOME \ cmd)::ins) \ s \ outs) \Rightarrow
          TR' (M, Oi, Os) (trap \ cmd)
             (CFG inputTest stateInterp certList
```

Theorems SSM1 THEORY

```
(P says prop (SOME cmd)::ins) s outs)
             (CFG inputTest stateInterp certList ins
                (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs))) \ \land
       (\forall input Test\ NS\ M\ Oi\ Os\ Out\ s\ cert List\ state Interp\ x\ ins
           outs.
          \neg inputTest \ x \Rightarrow
          TR' (M,Oi,Os) discard
             (CFG inputTest stateInterp certList (x::ins) s outs)
             (CFG inputTest stateInterp certList ins (NS s discard)
                (Out \ s \ discard::outs))) \Rightarrow
      \forall a_0 \ a_1 \ a_2 \ a_3. TR a_0 \ a_1 \ a_2 \ a_3 \Rightarrow TR' \ a_0 \ a_1 \ a_2 \ a_3
[TR_trap_cmd_rule]
 \vdash \forall inputTest \ stateInterp \ certList \ P \ cmd \ ins \ s \ outs.
       (\forall M \ Oi \ Os.
          CFGInterpret (M, Oi, Os)
             (CFG inputTest stateInterp certList
                 (P \text{ says prop } (SOME \ cmd) :: ins) \ s \ outs) \Rightarrow
          (M, Oi, Os) sat prop NONE) \Rightarrow
      \forall NS \ Out \ M \ Oi \ Os.
         TR (M, Oi, Os) (trap cmd)
           (CFG inputTest\ stateInterp\ certList
               (P says prop (SOME cmd)::ins) s outs)
           (CFG inputTest stateInterp certList ins
               (NS \ s \ (trap \ cmd)) \ (Out \ s \ (trap \ cmd)::outs)) \iff
         inputTest (P says prop (SOME cmd)) \land
         CFGInterpret (M, Oi, Os)
           (CFG inputTest\ stateInterp\ certList
               (P says prop (SOME cmd)::ins) s outs) \land
         (M,Oi,Os) sat prop NONE
[TRrule0]
 \vdash TR (M, Oi, Os) (exec cmd)
      (CFG inputTest stateInterp certList
          (P says prop (SOME cmd)::ins) s outs)
       (CFG inputTest stateInterp certList ins (NS s (exec cmd))
          (Out \ s \ (exec \ cmd)::outs)) \iff
    inputTest (P says prop (SOME cmd)) \land
    CFGInterpret (M, Oi, Os)
       (CFG inputTest stateInterp certList
          (P says prop (SOME cmd)::ins) s outs)
[TRrule1]
 \vdash TR (M, Oi, Os) (trap cmd)
       (CFG inputTest stateInterp certList
```

```
(P says prop (SOME cmd)::ins) s outs)
       (CFG inputTest stateInterp certList ins (NS s (trap cmd))
          (Out \ s \ (trap \ cmd)::outs)) \iff
    inputTest (P says prop (SOME cmd)) \wedge
    CFGInterpret (M, Oi, Os)
       (CFG inputTest stateInterp certList
          (P says prop (SOME cmd)::ins) s outs)
[trType_distinct_clauses]
 \vdash (\forall a. discard \neq trap a) \land (\forall a. discard \neq exec a) \land
    \forall a' \ a. \ \mathsf{trap} \ a \neq \mathsf{exec} \ a'
[trType_one_one]
 \vdash (\forall a \ a'. (trap a = trap a') \iff (a = a')) \land
    \forall a \ a'. (exec a = \text{exec } a') \iff (a = a')
2
     satList Theory
Built: 23 April 2019
Parent Theories: aclDrules
2.1
      Definitions
[satList_def]
 \vdash \forall M \ Oi \ Os \ formList.
       (M,Oi,Os) satList formList \iff
      FOLDR (\lambda x \ y. \ x \land y) T (MAP (\lambda f. \ (M, Oi, Os) \ \text{sat} \ f) formList)
2.2
      Theorems
[satList_conj]
 \vdash \forall l_1 \ l_2 \ M \ Oi \ Os.
       (M,Oi,Os) satList l_1 \land (M,Oi,Os) satList l_2 \iff
       (M,Oi,Os) satList (l_1 ++ l_2)
[satList_CONS]
 \vdash \forall h \ t \ M \ Oi \ Os.
       (M,Oi,Os) satList (h::t) \iff
       (M,Oi,Os) sat h \wedge (M,Oi,Os) satList t
[satList_nil]
 \vdash (M, Oi, Os) satList []
```

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```