Homework 11

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Week 11

Abstract

This project is a part of HW11 of Assurance Foundations. The homework deals with integration of ML and HOL to LaTeX. The goal of this report is to show reproducibility which is the groundwork for credibility that I have done this on my own without any external help. Every Chapter demonstrates the following sections:

- Problem Statement
- Relevant Code
- Test Results

This project includes the following packages:

634format.sty A format style for this course

 $\boldsymbol{listings}$ Package for displaying and inputting ML source code

holtex HOL style files and commands to display in the report

This document also demonstrates my ability to :

- Easily generate a table of contents,
- Refer to chapter and section labels

My skills and my professional details can be found at https://www.linkedin.in/in/chiragsachdev.

Acknowledgments

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Executive Summary

All requirements for this project are satisfied. Specifically we prove the following theorems:

```
[Alice_npriv_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
         (Name Alice says prop (SOME (NP npriv))::ins) s outs) \Rightarrow
    (M,Oi,Os) sat prop (SOME (NP npriv))
[Alice_exec_npriv_justified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
        (CFG inputOK SMOStateInterp (certs cmd\ npriv\ privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s outs)
        (CFG inputOK SMOStateInterp (certs cmd\ npriv\ privcmd) ins
            (NS \ s \ (exec \ (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \iff
      inputOK (Name Alice says prop (SOME (NP npriv))) \wedge
      CFGInterpret (M, Oi, Os)
        (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s
            outs) \land (M, Oi, Os) sat prop (SOME (NP npriv))
[Alice_npriv_verified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
        (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s outs)
        (CFG inputOK SMOStateInterp (certs cmd npriv privcmd) ins
            (NS \ s \ (exec \ (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \Rightarrow
      (M, Oi, Os) sat prop (SOME (NP npriv))
[Alice_justified_npriv_exec_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os \ cmd \ npriv \ privcmd \ ins \ s \ outs.
      inputOK (Name Alice says prop (SOME (NP npriv))) \land
      CFGInterpret (M, Oi, Os)
        (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s
            outs) \Rightarrow
      TR (M, Oi, Os) (exec (NP npriv))
        (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s outs)
        (CFG inputOK SMOStateInterp (certs cmd\ npriv\ privcmd) ins
            (NS \ s \ (exec \ (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs))
```

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```
[Carol_npriv_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
          (Name Carol says prop (SOME (NP npriv))::ins) s outs) \Rightarrow
    (M,Oi,Os) sat prop (SOME (NP npriv))
[Carol_exec_npriv_justified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS \ s \ (exec (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \iff
      inputOK2 (Name Carol says prop (SOME (NP npriv))) \land
      CFGInterpret (M, Oi, Os)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s
            outs) \land (M, Oi, Os) sat prop (SOME (NP npriv))
[Carol_npriv_verified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS \ s \ (exec (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \Rightarrow
      (M, Oi, Os) sat prop (SOME (NP npriv))
[Carol_justified_npriv_exec_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os \ cmd \ npriv \ privcmd \ ins \ s \ outs.
      inputOK2 (Name Carol says prop (SOME (NP npriv))) \lambda
      CFGInterpret (M, Oi, Os)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s
            outs) \Rightarrow
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS \ s \ (exec (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs))
[Carol_privcmd_trap_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
          (Name Carol says prop (SOME (PR \mathit{privcmd}))::\mathit{ins}) s
          outs) \Rightarrow
    (M,Oi,Os) sat prop NONE
[Carol_justified_privcmd_trap_thm]
 \vdash \ \forall \mathit{NS} \ \mathit{Out} \ \mathit{M} \ \mathit{Oi} \ \mathit{Os} \ \mathit{cmd} \ \mathit{npriv} \ \mathit{privcmd} \ \mathit{ins} \ \mathit{s} \ \mathit{outs}.
      inputOK2 (Name Carol says prop (SOME (PR privemd))) \land
      CFGInterpret (M, Oi, Os)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (PR privemd))::ins) s
```

```
outs) \Rightarrow
      TR (M, Oi, Os) (trap (PR privend))
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (PR privend))::ins) s
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS s (trap (PR privemd)))
            (Out s (trap (PR privemd))::outs))
[Carol_privcmd_trapped_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (trap (PR privend))
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (PR privend))::ins) s
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS s (trap (PR privcmd)))
            (Out \ s \ (trap \ (PR \ privemd))::outs)) \Rightarrow
      (M,Oi,Os) sat prop NONE
[Carol_trap_privcmd_justified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (trap (PR privend))
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (PR privend))::ins) s
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS s (trap (PR privemd)))
            (Out \ s \ (trap \ (PR \ privcmd))::outs)) \iff
      inputOK2 (Name Carol says prop (SOME (PR privemd))) \land
      CFGInterpret (M, Oi, Os)
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (PR privend))::ins) s
            outs) \land (M,Oi,Os) sat prop NONE
[inputOK2_def]
 \vdash (inputOK2 (Name Carol says prop (SOME cmd)) \iff T) \land
    (inputOK2 TT \iff F) \land (inputOK2 FF \iff F) \land
    (inputOK2 (prop v) \iff F) \land (inputOK2 (notf v_1) \iff F) \land
    (inputOK2 (v_2 andf v_3) \iff F) \land (inputOK2 (v_4 orf v_5) \iff F) \land
    (inputOK2 (v_6 impf v_7) \iff F) \land (inputOK2 (v_8 eqf v_9) \iff F) \land
    (inputOK2 (v_{10} says TT) \iff F) \wedge
    (inputOK2 (v_{10} says FF) \iff F) \wedge
    (inputOK2 (Name Alice says prop (SOME v142)) \iff F) \land
    (inputOK2 (Name Bob says prop (SOME v142)) \iff F) \land
    (inputOK2 (Name v132 says prop NONE) \iff F) \land
    (inputOK2 (v133 meet v134 says prop v_{66}) \iff F) \land
    (inputOK2 (v135 quoting v136 says prop v_{66}) \iff F) \land
    (inputOK2 (v_{10} says notf v_{67}) \iff F) \wedge
    (inputOK2 (v_{10} says (v_{68} andf v_{69})) \iff F) \wedge
    (inputOK2 (v_{10} says (v_{70} orf v_{71})) \iff F) \land
    (inputOK2 (v_{10} says (v_{72} impf v_{73})) \iff F) \wedge
    (inputOK2 (v_{10} says (v_{74} eqf v_{75})) \iff F) \land
    (inputOK2 (v_{10} says v_{76} says v_{77}) \iff F) \land
    (inputOK2 (v_{10} says v_{78} speaks_for v_{79}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{80} controls v_{81}) \iff F) \wedge
    (inputOK2 (v_{10} says reps v_{82} v_{83} v_{84}) \iff F) \land
```

```
(inputOK2 (v_{10} says v_{85} domi v_{86}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{87} eqi v_{88}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{89} doms v_{90}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{91} eqs v_{92}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{93} eqn v_{94}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{95} lte v_{96}) \iff F) \wedge
    (inputOK2 (v_{10} says v_{97} lt v_{98}) \iff F) \wedge
    (inputOK2 (v_{12} speaks_for v_{13}) \iff F) \wedge
    (inputOK2 (v_{14} controls v_{15}) \iff F) \wedge
    (inputOK2 (reps v_{16} v_{17} v_{18}) \iff F) \wedge
    (inputOK2 (v_{19} domi v_{20}) \iff F) \wedge
    (inputOK2 (v_{21} eqi v_{22}) \iff F) \wedge
    (inputOK2 (v_{23} doms v_{24}) \iff F) \wedge
    (inputOK2 (v_{25} eqs v_{26}) \iff F) \wedge
    (inputOK2 (v_{27} eqn v_{28}) \iff F) \wedge
    (inputOK2 (v_{29} lte v_{30}) \iff F) \wedge (inputOK2 (v_{31} lt v_{32}) \iff F)
[certs2_def]
 \vdash \ \forall \ cmd \ npriv \ privemd.
       certs2 cmd npriv privcmd =
       [Name Carol controls prop (SOME (NP npriv));
        Name Carol says prop (SOME (PR privemd)) impf prop NONE]
```

[Reproducibility in ML and LATEX]

The ML and LATEX source files compile with no errors.

Excercise 17.3.1

2.1 Problem statement

Using inputOK and certs to authenticate and authorize commands, prove the following theorems that justify Alices request to execute a non-privileged command will be executed.

```
[Alice_npriv_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
          (Name Alice says prop (SOME (NP npriv))::ins) s outs) \Rightarrow
    (M, Oi, Os) sat prop (SOME (NP npriv))
[Alice_exec_npriv_justified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK SMOStateInterp (certs cmd npriv privcmd) ins
            (NS \ s \ (exec \ (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \iff
      inputOK (Name Alice says prop (SOME (NP npriv))) \wedge
      CFGInterpret (M, Oi, Os)
         (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s
            outs) \land (M, Oi, Os) sat prop (SOME (NP npriv))
[Alice_npriv_verified_thm]
  \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK SMOStateInterp (certs cmd\ npriv\ privcmd) ins
            (NS \ s \ (exec \ (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \Rightarrow
      (M, Oi, Os) sat prop (SOME (NP npriv))
[Alice_justified_npriv_exec_thm]
 \vdash \ \forall \mathit{NS} \ \mathit{Out} \ \mathit{M} \ \mathit{Oi} \ \mathit{Os} \ \mathit{cmd} \ \mathit{npriv} \ \mathit{privcmd} \ \mathit{ins} \ \mathit{s} \ \mathit{outs}.
      inputOK (Name Alice says prop (SOME (NP npriv))) \land
      CFGInterpret (M, Oi, Os)
         (CFG inputOK SMOStateInterp (certs cmd npriv privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s
            outs) \Rightarrow
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK SMOStateInterp (certs cmd\ npriv\ privcmd)
            (Name Alice says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK SMOStateInterp (certs cmd npriv privcmd) ins
            (NS \ s \ (exec \ (NP \ npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs))
```

2.2 Proof 17.3.1 A

2.2.1 Relevant Code

2.2.2 Session Transcript

```
# # # # # # # # # Meson search level: ....
                                                                                                                                  1
val Alice_npriv_lemma :
   |- CFGInterpret
     ((M :(command inst, 'b, staff, 'd, 'e) Kripke),(Oi :'d po),
      (Os :'e po))
     (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
        (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
        (certs (cmd :command) (npriv :npriv) (privcmd :privcmd) :
           (command inst, staff, 'd, 'e) Form list)
        (Name Alice says
         (prop (SOME (NP npriv) :command inst) :
            (command inst, staff, 'd, 'e) Form)::
   (ins :(command inst, staff, 'd, 'e) Form list)) (s :state)
        (outs :output list)) ==>
   (M,Oi,Os) sat
   (prop (SOME (NP npriv) :command inst) :
      (command inst, staff, 'd, 'e) Form):
   thm
```

2.3 Proof 17.3.1 B

2.3.1 Relevant Code

```
val Alice_exec_npriv_justified_thm =
let
val th1 = ISPECL
 [''inputOK:(command inst, staff,'d,'e)Form -> bool'',
  ''(certs cmd npriv privcmd):(command inst, staff, 'd, 'e)Form list '',
  "SMOStateInterp: state -> (command inst, staff, 'd, 'e) Form ",
  "Name Alice", "NP npriv", "ins:(command inst, staff, 'd, 'e)Form list",
  "s:state", "outs:output list" TR_exec_cmd_rule
TAC_PROOF(([],
''!(NS :state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\! >\ bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Alice says
              (prop (SOME (NP npriv) :command inst) :
                 (command inst, staff, 'd, 'e) Form)::
                  (ins :(command inst, staff, 'd, 'e) Form list)) (s :state)
             (outs :output list))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs cmd npriv privcmd :
                (command inst, staff, 'd, 'e) Form list) ins
             (NS s (exec (NP npriv)))
             (Out s (exec (NP npriv))::outs)) <=>
        inputOK
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)) /\
        CFGInterpret (M, Oi, Os)
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs cmd npriv privcmd:
                (command inst, staff, 'd, 'e) Form list)
             (Name Alice says
              (prop (SOME (NP npriv) :command inst) :
                 (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[th1, Alice_npriv_lemma])
end
val _ = save_thm("Alice_exec_npriv_justified_thm", Alice_exec_npriv_justified_thm)
```

2.3.2 Session Transcript

```
Meson search level: ....
                                                                                                                               2
val Alice_exec_npriv_justified_thm =
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
(M :(command inst, 'b, staff, 'd, 'e) Kripke) (Oi :'d po)
      (Os :'e po).
     TR (M,Oi,Os) (exec (NP (npriv :npriv)))
       (CFG (inputOK :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs (cmd :command) npriv (privcmd :privcmd) :
             (command inst, staff, 'd, 'e) Form list)
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::
               (ins :(command inst, staff, 'd, 'e) Form list))
          (s :state) (outs :output list))
       (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list) ins
          (NS s (exec (NP npriv))) (Out s (exec (NP npriv))::outs)) <=>
     inputOK
       (Name Alice says
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form)) /\
     CFGInterpret (M,Oi,Os)
       (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs cmd npriv privcmd :
            (command inst, staff, 'd, 'e) Form list)
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
     (M,Oi,Os) sat
     (prop (SOME (NP npriv) :command inst) :
        (command inst, staff, 'd, 'e) Form):
  thm
val it = (): unit
```

2.4 Proof 17.3.1 C

2.4.1 Relevant Code

```
val Alice_npriv_verified_thm=
TAC_PROOF(([].
         ''!(NS : state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os:'epo).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
           (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\!\!\!>\ bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\, ,\ 'e\, )\ Form\ -\! >\ bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                 (command inst, staff, 'd, 'e) Form list) ins
```

```
(NS s (exec (NP npriv)))
        (Out s (exec (NP npriv))::outs)) ==>
        (M,Oi,Os) sat
        (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)''),
              PROVE_TAC[Alice_exec_npriv_justified_thm])

val _ = save_thm("Alice_npriv_verified_thm", Alice_npriv_verified_thm)
```

2.4.2 Session Transcript

```
3
Meson search level: ..
val Alice_npriv_verified_thm :
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
      (M : (command inst, 'b, staff, 'd, 'e) Kripke) (Oi : 'd po)
      (Os :'e po).
     TR (M,Oi,Os) (exec (NP (npriv :npriv)))
       (CFG (inputOK :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs (cmd :command) npriv (privcmd :privcmd) :
             (command inst, staff, 'd, 'e) Form list)
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::
               (ins :(command inst, staff, 'd, 'e) Form list))
          (s :state) (outs :output list))
       (CFG (inputOK :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs {\tt cmd} {\tt npriv} {\tt priv}{\tt cmd} :
             (command inst, staff, 'd, 'e) Form list) ins
          (NS s (exec (NP npriv))) (Out s (exec (NP npriv))::outs)) ==>
     (M,Oi,Os) sat
     (prop (SOME (NP npriv) :command inst) :
        (command inst, staff, 'd, 'e) Form):
  t.hm
val it = (): unit
```

2.5 Proof 17.3.1 D

2.5.1 Relevant Code

```
val Alice_justified_npriv_exec_thm=
TAC_PROOF(([],
''!(NS : state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
          CFGInterpret (M, Oi, Os)
          (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\, ,\ 'e\, )\ Form\ -\! >\ bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) =>>
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
```

```
(CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  ({\tt command \ inst} \ , \ {\tt staff} \ , \ {\tt 'd} \ , \ {\tt 'e}) \ {\tt Form})::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                 (command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs))''),
             PROVE_TAC[Alice_exec_npriv_justified_thm ,inputOK_def , Alice_npriv_lemma
                 ])
val _ = save_thm("Alice_justified_npriv_exec_thm", Alice_justified_npriv_exec_thm)
```

2.5.2 Session Transcript

```
Meson search level: .....
                                                                                                                               4
val Alice_justified_npriv_exec_thm =
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
      (M : (command inst, 'b, staff, 'd, 'e) Kripke) (Oi : 'd po)
      (Os :'e po) (cmd :command) (npriv :npriv) (privcmd :privcmd)
      (ins: (command inst, staff, 'd, 'e) Form list) (s:state)
      (outs :output list).
     inputOK
       (Name Alice says
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form)) /\
     CFGInterpret (M,Oi,Os)
       (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs) ==>
     TR (M,Oi,Os) (exec (NP npriv))
       (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Alice savs
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs)
       (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs cmd npriv privcmd :
          (command inst, staff, 'd, 'e) Form list) ins
(NS s (exec (NP npriv))) (Out s (exec (NP npriv))::outs)):
  thm
val it = (): unit
```

Excercise 17.3.3

3.1 Problem statement

Devise two new definitions inputOK2 and certs2, within SM0Script.sml, that authenticate only Carol and authorize her to execute non-privileged instructions. The new definitions should reflect the fact that if Carol attempts to execute a privileged command, her request is trapped. Any inputs by Alice or Bob are rejected by inputOK2. Also, using inputOK2 and certs2, prove the following theorems that justify executing Carols request to execute a non-privileged command.

```
[Carol_npriv_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
          (Name Carol says prop (SOME (NP npriv))::ins) s outs) \Rightarrow
    (M,Oi,Os) sat prop (SOME (NP npriv))
[Carol_exec_npriv_justified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS s (exec (NP npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \iff
      inputOK2 (Name Carol says prop (SOME (NP npriv))) \lambda
      CFGInterpret (M, Oi, Os)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s
            outs) \land (M, Oi, Os) sat prop (SOME (NP npriv))
[Carol_npriv_verified_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (exec (NP npriv))
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s outs)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            ins (NS s (exec (NP npriv)))
            (Out \ s \ (exec \ (NP \ npriv))::outs)) \Rightarrow
      (M, Oi, Os) sat prop (SOME (NP npriv))
[Carol_justified_npriv_exec_thm]
 \vdash \ \forall \mathit{NS} \ \mathit{Out} \ \mathit{M} \ \mathit{Oi} \ \mathit{Os} \ \mathit{cmd} \ \mathit{npriv} \ \mathit{privcmd} \ \mathit{ins} \ \mathit{s} \ \mathit{outs}.
      inputOK2 (Name Carol says prop (SOME (NP npriv))) \wedge
      CFGInterpret (M, Oi, Os)
         (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
            (Name Carol says prop (SOME (NP npriv))::ins) s
            outs) \Rightarrow
      TR (M, Oi, Os) (exec (NP npriv))
```

```
(CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
   (Name Carol says prop (SOME (NP npriv))::ins) s outs)
(CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
   ins (NS s (exec (NP npriv)))
   (Out s (exec (NP npriv))::outs))
```

Using inputOK2 and certs2, prove the following theorems that justify trapping Carols request to execute a privileged command

```
[Carol_privcmd_trap_lemma]
 \vdash CFGInterpret (M, Oi, Os)
      (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
         (Name Carol says prop (SOME (PR privemd))::ins) s
         outs) \Rightarrow
    (M,Oi,Os) sat prop NONE
[Carol_trap_privcmd_justified_thm]
 \vdash \ \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (trap (PR privcmd))
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           (Name Carol says prop (SOME (PR privemd))::ins) s
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           ins (NS s (trap (PR privcmd)))
           (Out \ s \ (trap \ (PR \ privemd))::outs)) \iff
      inputOK2 (Name Carol says prop (SOME (PR privemd))) \land
      CFGInterpret (M, Oi, Os)
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           (Name Carol says prop (SOME (PR \mathit{privemd}))::\mathit{ins}) s
           outs) \land (M,Oi,Os) sat prop NONE
[Carol_privcmd_trapped_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os.
      TR (M, Oi, Os) (trap (PR privemd))
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           (Name Carol says prop (SOME (PR privemd))::ins) s
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           ins (NS s (trap (PR privemd)))
           (Out \ s \ (trap \ (PR \ priverd))::outs)) \Rightarrow
      (M,Oi,Os) sat prop NONE
[Carol_justified_privcmd_trap_thm]
 \vdash \forall NS \ Out \ M \ Oi \ Os \ cmd \ npriv \ privcmd \ ins \ s \ outs.
      inputOK2 (Name Carol says prop (SOME (PR privemd))) \land
      CFGInterpret (M, Oi, Os)
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           (Name Carol says prop (SOME (PR privend))::ins) s
           outs) \Rightarrow
      TR (M, Oi, Os) (trap (PR privcmd))
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           (Name Carol says prop (SOME (PR privcmd))::ins) s
           outs)
        (CFG inputOK2 SMOStateInterp (certs2 cmd npriv privcmd)
           ins (NS s (trap (PR privcmd)))
           (Out \ s \ (trap \ (PR \ privemd))::outs))
```

3.2 Proof 17.3.3 A

3.2.1 Relevant Code

```
val inputOK2_def =
Define
'(inputOK2 (((Name Carol) says (prop (SOME (cmd:command)))):(command inst, staff, 'd,' e)Form) = T) /\ (inputOK2 _ = F)'

val certs2_def =
Define
'certs2 (cmd:command)(npriv:npriv)(privcmd:privcmd) = [(Name Carol controls ((prop (SOME (NP npriv))):(command inst, staff, 'd, 'e)Form)); ((Name Carol) says (prop (SOME (PR privcmd)))) impf (prop NONE)]'
```

3.2.2 Session Transcript

```
# # # # # # # <<HOL message: mk_functional:
                                                                                                                             5
  pattern completion has added 40 clauses to the original specification.>>
Equations stored under "inputOK2_def".
Induction stored under "inputOK2_ind".
Definition has been stored under "certs2_def"
val certs2_def =
   |- !(cmd :command) (npriv :npriv) (privcmd :privcmd).
     (certs2 cmd npriv privcmd :
        (command inst, staff, 'd, 'e) Form list) =
     [Name Carol controls
      (prop (SOME (NP npriv) :command inst) :
         (command inst, staff, 'd, 'e) Form);
      Name Carol says
      (prop (SOME (PR privcmd) :command inst) :
         (command inst, staff, 'd, 'e) Form) impf
      (prop (NONE :command inst) :(command inst, staff, 'd, 'e) Form)]:
   |-!(v98 :num) (v97 :num) (v96 :num) (v95 :num) (v94 :num) (v93 :num)
      (v92 :(staff, 'e) SecLevel) (v91 :(staff, 'e) SecLevel)
      (v90 :(staff, 'e) SecLevel)
      (v9 :(command inst, staff, 'd, 'e) Form)
      (v89 :(staff, 'e) SecLevel) (v88 :(staff, 'd) IntLevel)
      (v87 :(staff, 'd) IntLevel) (v86 :(staff, 'd) IntLevel)
      (v85 :(staff, 'd) IntLevel)
      (v84 : (command inst, staff, 'd, 'e) Form) (v83 : staff Princ)
      (v82 :staff Princ) (v81 :(command inst, staff, 'd, 'e) Form)
      (v80 :staff Princ) (v8 :(command inst, staff, 'd, 'e) Form)
      (v79 :staff Princ) (v78 :staff Princ)
      (v77 :(command inst, staff, 'd, 'e) Form) (v76 :staff Princ)
      (v75:(command\ inst,\ staff,\ 'd,\ 'e)\ Form)
      (v74 :(command inst, staff, 'd, 'e) Form)
      (v73 : (command inst, staff, 'd, 'e) Form)
      (v72 :(command inst, staff, 'd, 'e) Form)
      (v71 :(command inst, staff, 'd, 'e) Form)
      (v70 :(command inst, staff, 'd, 'e) Form)
      (v7 :(command inst, staff, 'd, 'e) Form)
      (v69 :(command inst, staff, 'd, 'e) Form)
      (v68 :(command inst, staff, 'd, 'e) Form)
(v67 :(command inst, staff, 'd, 'e) Form) (v66 :command inst)
      (v6:(command inst, staff, 'd, 'e) Form)
(v5:(command inst, staff, 'd, 'e) Form)
      (v4 :(command inst, staff, 'd, 'e) Form) (v32 :num) (v31 :num)
      (v30 :num) (v3 :(command inst, staff, 'd, 'e) Form) (v29 :num)
      (v28 :num) (v27 :num) (v26 :(staff, 'e) SecLevel)
      (v25 :(staff, 'e) SecLevel) (v24 :(staff, 'e) SecLevel)
      (v23:(staff, 'e) SecLevel) (v22:(staff, 'd) IntLevel) (v21:(staff, 'd) IntLevel) (v20:(staff, 'd) IntLevel)
      (v2 :(command inst, staff, 'd, 'e) Form)
      (v19 :(staff, 'd) IntLevel)
      (v18 :(command inst, staff, 'd, 'e) Form) (v17 :staff Princ)
      (v16 :staff Princ) (v15 :(command inst, staff, 'd, 'e) Form)
      (v142 :command) (v14 :staff Princ) (v136 :staff Princ)
      (v135 :staff Princ) (v134 :staff Princ) (v133 :staff Princ)
      (v132 :staff) (v13 :staff Princ) (v12 :staff Princ)
      (v10 :staff Princ) (v1 :(command inst, staff, 'd, 'e) Form)
      (v :command inst) (cmd :command).
     (inputOK2
        (Name Carol says
         (prop (SOME cmd :command inst) :
            (command inst, staff, 'd, 'e) Form)) <=> T) /\
     (inputOK2 (TT :(command inst, staff, 'd, 'e) Form) <=> F) /\
     (inputOK2 (FF :(command inst, staff, 'd, 'e) Form) <=> F) /\
     (inputOK2 (prop v :(command inst, staff, 'd, 'e) Form) <=> F) /\
     (inputOK2 (notf v1) <=> F) /\ (inputOK2 (v2 andf v3) <=> F) /\
     (inputOK2 (v4 orf v5) <=> F) /\ (inputOK2 (v6 impf v7) <=> F) /\
     (inputOK2 (v8 eqf v9) <=> F) /\
     (inputOK2 (v10 says (TT :(command inst, staff, 'd, 'e) Form)) <=>
     (inputOK2 (v10 says (FF :(command inst, staff, 'd, 'e) Form)) <=>
      F) /\
     (inputOK2
        (Name Alice says
         (prop (SOME v142 :command inst) :
            (command inst, staff, 'd, 'e) Form)) <=> F) /\
     (inputOK2
        (Name Bob says
         (prop (SOME v142 :command inst) :
            (command inst, staff, 'd, 'e) Form)) <=> F) /\
     (inputOK2
         (Name v132 says
            (prop (NONE :command inst) :
     (inputOK2
        (v133 meet v134 says
```

3.3 Proof 17.3.3 B

3.3.1 Relevant Code

```
val Carol_npriv_lemma=
TAC_PROOF(([],
"CFGInterpret ((M: (command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os)
  (CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)
   (((Name Carol) says (prop (SOME (NP (npriv:npriv)))))::ins)
   s (outs:output list)) =>>
  ((M,Oi,Os) sat (prop (SOME(NP npriv))))''),
  REWRITE_TAC[CFGInterpret_def, certs2_def, SM0StateInterp_def, satList_CONS,
             satList_nil ,sat_TT | THEN PROVE_TAC[Controls])
val _ = save_thm("Carol_npriv_lemma", Carol_npriv_lemma)
val Carol_exec_npriv_justified_thm=
let
val th1 = ISPECL
[''inputOK2:(command inst, staff,'d,'e)Form -> bool'', ''(certs2 cmd npriv privcmd)
     :(command inst, staff,'d,'e)Form list'', ''SM0StateInterp:state->(command inst,
     staff, 'd, 'e) Form'', ''Name Carol'', ''NP npriv'', ''ins:(command inst, staff, 'd, 'e)
    Form list '', ''s:state'', ''outs:output list''| TR_exec_cmd_rule
in
TAC_PROOF(([],
       ''!(NS :state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
           (CFG\ (inputOK2\ : (command\ inst\ ,\ staff\ ,\ 'd\, ,\ 'e\, )\ Form\ -\! >\ bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (NP npriv) : command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 ({\tt command \ inst} \ , \ {\tt staff} \ , \ {\tt 'd} \ , \ {\tt 'e}) \ {\tt Form \ list} \ ) \ {\tt ins}
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs)) <=>
        inputOK2
           (Name Carol says
            (prop (SOME (NP npriv) : command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
        CFGInterpret (M, Oi, Os)
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (NP npriv) : command inst) :
```

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```
(command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) :command inst) :
           ({\tt command \ inst} \ , \ {\tt staff} \ , \ {\tt 'd} \ , \ {\tt 'e}) \ {\tt Form}) \ ``) \ ,
           PROVE_TAC[th1, Carol_npriv_lemma])
end
val _ = save_thm("Carol_exec_npriv_justified_thm", Carol_exec_npriv_justified_thm)
val Carol_npriv_verified_thm=
TAC_PROOF(([],
       ''!(NS :state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
              (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs)) ==>
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[Carol_exec_npriv_justified_thm])
val _ = save_thm("Carol_npriv_verified_thm", Carol_npriv_verified_thm)
val Carol_justified_npriv_exec_thm=
TAC_PROOF(([],
       ''!(NS : state -> command trType -> state)
         (Out : state -> command trTvpe -> output)
         (M:(command inst, 'b, staff, 'd, 'e) Kripke) (Oi:'d po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK2
          (Name Carol says
           (prop (SOME (NP npriv) : command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
          CFGInterpret (M, Oi, Os)
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (NP npriv) : command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) =>
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form \rightarrow bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
```

3.3.2 Session Transcript

```
6
Meson search level: ....
Meson search level: .....
Meson search level: ...
Meson search level: ....
val Carol_exec_npriv_justified_thm =
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
      (M : (command inst, 'b, staff, 'd, 'e) Kripke) (Oi : 'd po)
     TR (M,Oi,Os) (exec (NP (npriv :npriv)))
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 (cmd :command) npriv (privcmd :privcmd) :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::
               (ins:(command inst, staff, 'd, 'e) Form list))
          (s :state) (outs :output list))
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list) ins
          (NS s (exec (NP npriv))) (Out s (exec (NP npriv))::outs)) <=>
       (Name Carol says
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form)) /\
     CFGInterpret (M,Oi,Os)
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol savs
           (prop (SOME (\mbox{NP} npriv) :command inst) :
             (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
     (M,Oi,Os) sat
     (prop (SOME (NP npriv) :command inst) :
        (command inst, staff, 'd, 'e) Form):
  thm
val Carol_justified_npriv_exec_thm =
  |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
(M :(command inst, 'b, staff, 'd, 'e) Kripke) (Oi :'d po)
      (Os :'e po) (cmd :command) (npriv :npriv) (privcmd :privcmd)
      (ins :(command inst, staff, 'd, 'e) Form list) (s :state)
      (outs :output list).
     inputOK2
       (Name Carol says
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form)) /\
     CFGInterpret (M,Oi,Os)
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs) ==>
     TR (M,Oi,Os) (exec (NP npriv))
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs)
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list) ins
          (NS s (exec (NP npriv))) (Out s (exec (NP npriv))::outs)):
  thm
val Carol_npriv_lemma =
   |- CFGInterpret
     ((M :(command inst, 'b, staff, 'd, 'e) Kripke),(Oi :'d po),
     (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
        (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
        (certs2 (cmd :command) (npriv :npriv) (privcmd :privcmd) :
           (command inst, staff, 'd, 'e) Form Akist) RANCE FUNDAMENTALS
        (Name Carol savs
         (prop (SOME (NP npriv) :command inst) :
            (command inst, staff, 'd, 'e) Form)::
```

3.4 Proof 17.3.3 C

3.4.1 Relevant Code

```
val Carol_privcmd_trap_lemma=
TAC_PROOF(([],
"CFGInterpret ((M: (command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os)
  (CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)
   (((Name Carol) says (prop (SOME (PR (privemd:privemd)))))::ins)
   s (outs:output list)) =>>
  ((M,Oi,Os) sat (prop NONE))''),
  REWRITE_TAC[CFGInterpret_def, certs2_def, SM0StateInterp_def, satList_CONS,
      satList_nil ,sat_TT | THEN PROVE_TAC[Controls , Modus_Ponens])
val _ = save_thm("Carol_privcmd_trap_lemma", Carol_privcmd_trap_lemma)
val Carol_trap_privcmd_justified_thm=
let
val th1 = ISPECL
 [''inputOK2:(command inst, staff,'d,'e)Form -> bool'', 'SMOStateInterp:state->(
    command inst, staff, 'd, 'e)Form'', ''(certs2 cmd npriv privcmd):(command inst,
     staff, 'd, 'e) Form list '', ''Name Carol'', ''PR privcmd'', ''ins:(command inst, staff
     ,'d,'e)Form list'', ''s:state'',''outs:output list''] TR_trap_cmd_rule
in
TAC_PROOF(([],
      ''!(NS :state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (trap (PR (privcmd : privcmd)))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (PR privcmd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 ({\tt command \ inst} \ , \ {\tt staff} \ , \ {\tt 'd} \ , \ {\tt 'e}) \ {\tt Form \ list} \ ) \ {\tt ins}
              (NS s (trap (PR privcmd)))
              (Out s (trap (PR privcmd))::outs)) <=>
        inputOK2
           (Name Carol says
            (prop (SOME (PR privemd) : command inst) :
               (command inst, staff, 'd, 'e) Form)) / 
        CFGInterpret (M, Oi, Os)
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (PR privcmd) :command inst) :
```

```
(command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M,Oi,Os) sat (prop NONE): (command inst, staff, 'd, 'e) Form''),
PROVE_TAC[th1, Carol_privcmd_trap_lemma])
end
val _ = save_thm("Carol_trap_privcmd_justified_thm", Carol_trap_privcmd_justified_thm
val Carol_privcmd_trapped_thm=
TAC_PROOF(([],
      ''!(NS : state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (trap (PR (privcmd : privcmd)))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Carol says
              (prop (SOME (PR privcmd) :command inst) :
                 (command inst, staff, 'd, 'e) Form)::
                  (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
             (outs :output list))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 cmd npriv privcmd :
                (command inst, staff, 'd, 'e) Form list) ins
             (NS s (trap (PR privcmd)))
             (Out s (trap (PR privcmd))::outs)) =>>
        (M, Oi, Os) sat
        (prop NONE:
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[Carol_trap_privcmd_justified_thm])
val _ = save_thm("Carol_privcmd_trapped_thm", Carol_privcmd_trapped_thm)
val Carol_justified_privcmd_trap_thm=
TAC_PROOF(([],
      ''!(NS : state -> command trType -> state)
         (Out : state -> command trTvpe -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK2
          (Name Carol says
           (prop (SOME (PR privemd) : command inst) :
              (command inst, staff, 'd, 'e) Form)) /\
          CFGInterpret (M, Oi, Os)
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 cmd npriv privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Carol says
              (prop (SOME (PR privcmd) :command inst) :
                 (command inst, staff, 'd, 'e) Form)::ins) s outs) =>>
       TR (M, Oi, Os) (trap (PR (privcmd : privcmd)))
          (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
```

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3.4.2 Session Transcript

```
Meson search level: ....
                                                                                                                              7
Meson search level: .....
Meson search level: ...
Meson search level: .....
val Carol_justified_privcmd_trap_thm =
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
      (M : (command inst, 'b, staff, 'd, 'e) Kripke) (Oi : 'd po)
      (Os :'e po) (cmd :command) (npriv :npriv) (privcmd :privcmd)
      (ins :(command inst, staff, 'd, 'e) Form list) (s :state)
      (outs :output list).
     inputOK2
       (Name Carol says
        (prop (SOME (PR privcmd) :command inst) :
           (command inst, staff, 'd, 'e) Form)) /\
     CFGInterpret (M,Oi,Os)
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol says
           (prop (SOME (PR privcmd) :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs) ==>
     TR (M,Oi,Os) (trap (PR privcmd))
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol says
           (prop (SOME \stackrel{\cdot}{(PR\ privcmd)} :command inst) :
              (command inst, staff, 'd, 'e) Form)::ins) s outs)
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list) ins
          (NS s (trap (PR privcmd))) (Out s (trap (PR privcmd))::outs)):
  thm
val Carol_privcmd_trap_lemma =
   |- CFGInterpret
     ((M :(command inst, 'b, staff, 'd, 'e) Kripke),(Oi :'d po),
      (Os :'e po))
     (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
        (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form) (certs2 (cmd :command) (npriv :npriv) (privcmd :privcmd) :
           (command inst, staff, 'd, 'e) Form list)
        (Name Carol says
         (prop (SOME (PR privcmd) :command inst) :
    (command inst, staff, 'd, 'e) Form)::
             (ins :(command inst, staff, 'd, 'e) Form list)) (s :state)
        (outs :output list)) ==>
   (M,Oi,Os) sat
   (prop (NONE :command inst) :(command inst, staff, 'd, 'e) Form):
val Carol_privcmd_trapped_thm =
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
      (M :(command inst, 'b, staff, 'd, 'e) Kripke) (Oi :'d po)
     TR (M,Oi,Os) (trap (PR (privcmd :privcmd)))
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 (cmd :command) (npriv :npriv) privcmd :
             (command inst, staff, 'd, 'e) Form list)
          (Name Carol says
           (prop (SOME (PR privcmd) :command inst) :
              (command inst, staff, 'd, 'e) Form)::
               (ins :(command inst, staff, 'd, 'e) Form list))
          (s :state) (outs :output list))
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
          (certs2 cmd npriv privcmd :
             (command inst, staff, 'd, 'e) Form list) ins
          (NS s (trap (PR privcmd)))
          (Out s (trap (PR privcmd))::outs)) ==>
     (M,Oi,Os) sat
     (prop (NONE :command inst) :(command inst, staff, 'd, 'e) Form):
val Carol trap privcmd justified thm =
   |- !(NS :state -> command trType -> state)
      (Out :state -> command trType -> output)
      (M : (command inst, 'b, staff, 'd, 'e) Kripke) (Oi : 'd po)
     TR (M,Oi,Os) (trap (PR (privcmd :privcmd)))

(CFG (inputON2 :/c--
       (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form -> bool)
          (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
```

Source code: ssm1Script

```
(* Secure State Machine Theory: authentication, authorization, and state
(* interpretation.
(* Author: Shiu-Kai Chin
                                                                      *)
(* Date: 27 November 2015
structure ssm1Script = struct
app load ["TypeBase", "ssminfRules", "listTheory", "optionTheory", "acl_infRules",
         "satListTheory", "ssm1Theory"];
open\ TypeBase\ listTheory\ ssminfRules\ optionTheory\ acl\_infRules\ satListTheory
    ssm1Theory
==== end interactive mode ===== *)
open HolKernel boolLib Parse bossLib
open TypeBase listTheory optionTheory ssminfRules acl_infRules satListTheory
(*********
(* create a new theory *)
(**************************
val _ = new_theory "ssm1";
(* Define the type of transition: discard, execute, or trap. We discard from
(* the input stream those inputs that are not of the form P says command. We
                                                                      *)
(* execute commands that users and supervisors are authorized for. We trap
                                                                      *)
(* commands that users are not authorized to execute.
                                                                      *)
                                                                      *)
(* In keeping with virtual machine design principles as described by Popek
                                                                      *)
(* and Goldberg, we add a TRAP instruction to the commands by users.
                                                                      *)
(* In effect, we are LIFTING the commands available to users to include the
                                                                      *)
(* TRAP instruction used by the state machine to handle authorization errors. *)
val _ =
Datatype
'inst = SOME 'command | NONE'
val inst_distinct_clauses = distinct_of '': 'command inst''
val _ = save_thm("inst_distinct_clauses",inst_distinct_clauses)
val inst_one_one = one_one_of '': 'command inst ''
val _ = save_thm("inst_one_one",inst_one_one)
```

```
val =
Datatype
trType =
  discard | trap 'command | exec 'command'
val trType_distinct_clauses = distinct_of '': 'command trType''
val = save\_thm("trType\_distinct\_clauses", trType\_distinct\_clauses)
val trType_one_one = one_one_of '': 'command trType''
val _ = save_thm("trType_one_one", trType_one_one)
(* Define configuration to include the security context within which the
(* inputs are evaluated. The components are as follows: (1) the authentication*)
(* function, (2) the interretation of the state, (3) the security context,
                                                                               *)
(* (4) the input stream, (5) the state, and (6) the output stream.
                                                                                  *)
(* ----
                                                                                  *)
val_{-} =
Datatype
'configuration =
CFG
  (('command inst, 'principal, 'd, 'e)Form -> bool)
  (('state -> ('command inst, 'principal, 'd, 'e)Form))
  (('command inst, 'principal, 'd, 'e) Form list)
  (('command inst, 'principal, 'd, 'e)Form list)
  ('state)
  ('output list)'
(* Prove one-to-one properties of configuration
                                                                                  *)
(* ---
val configuration_one_one =
    one_one_of '': ('command inst,'d,'e,'output,'principal,'state)configuration ''
val _ = save_thm("configuration_one_one", configuration_one_one)
(* The interpretation of configuration is the conjunction of the formulas in
                                                                                 *)
(* the context and the first element of a non-empty input stream.
                                                                                  *)
(* ---
val CFGInterpret_def =
Define
'CFGInterpret
 ((M: ('command inst,'b,'principal,'d,'e) Kripke), Oi: 'd po, Os: 'e po)
 (CFG
  (inputTest:('command inst,'principal,'d,'e)Form -> bool)
  (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form)
  (context: ('command inst, 'principal, 'd, 'e) Form list)
  ((x:('command inst,'principal,'d,'e)Form)::ins)
  (state: 'state)
  (outStream: 'output list))
  ((M,Oi,Os) satList context) /\
  ((M, Oi, Os) sat x) / 
  ((M,Oi,Os) sat (stateInterp state))'
```

```
*)
(* Define transition relation among configurations. This definition is
                                                                                  *)
(* parameterized in terms of next-state transition function and output
                                                                                  *)
(* function.
                                                                                  *)
(* The first rule is set up with the expectation it is some principal P
(* ordering a command cmd be executed.
                                                                                  *)
(* -
val (TR\_rules, TR\_ind, TR\_cases) =
Hol_reln
'(!(inputTest:('command inst, 'principal, 'd, 'e)Form -> bool) (P: 'principal Princ)
    (NS: 'state -> 'command trType -> 'state) M Oi Os Out (s:'state)
    (certList:('command inst,'principal,'d,'e)Form list)
    (stateInterp: 'state -> ('command inst, 'principal, 'd, 'e)Form)
    (cmd: 'command) (ins: ('command inst, 'principal, 'd, 'e) Form list)
    (outs: 'output list).
 (inputTest ((P says (prop (SOME cmd))):('command inst,'principal,'d,'e)Form) /\
 (CFGInterpret (M, Oi, Os)
  (CFG inputTest stateInterp certList
       (((P says (prop (SOME cmd))):('command inst,'principal,'d,'e)Form)::ins)
       s outs))) \Longrightarrow
 (TR
  ((M:('command inst,'b,'principal,'d,'e)Kripke),Oi:'d po,Os:'e po) (exec cmd)
  (CFG inputTest stateInterp certList
       (((P says (prop (SOME cmd))):('command inst, 'principal, 'd, 'e)Form)::ins)
      s outs)
  (CFG inputTest stateInterp certList ins (NS s (exec cmd))
       ((Out s (exec cmd))::outs)))) /\
 (!(inputTest:('command inst,'principal,'d,'e)Form -> bool) (P:'principal Princ)
   (NS: 'state -> 'command trType -> 'state) M Oi Os Out (s: 'state)
   (certList:('command inst,'principal,'d,'e)Form list)
   (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form)
   (cmd: 'command) (ins: ('command inst, 'principal, 'd, 'e) Form list)
   (outs: 'output list).
 (inputTest ((P says (prop (SOME cmd))):('command inst,'principal,'d,'e)Form) /\
 (CFGInterpret (M, Oi, Os)
  (CFG inputTest stateInterp certList
       (((P says (prop (SOME cmd))):('command inst,'principal,'d,'e)Form)::ins)
       s outs))) ==>
 (TR
  ((M: ('command inst,'b,'principal,'d,'e)Kripke),Oi:'d po,Os:'e po) (trap cmd)
 (CFG inputTest stateInterp certList
      (((P says (prop (SOME cmd))):('command inst,'principal,'d,'e)Form)::ins)
      s outs)
 (CFG\ inputTest\ stateInterp\ certList\ ins\ (NS\ s\ (trap\ cmd))
      ((Out s (trap cmd))::outs)))) /\
 (!(inputTest:('command inst,'principal,'d,'e)Form -> bool)
   (NS: 'state -> 'command trType -> 'state)
  M Oi Os (Out: 'state -> 'command trType -> 'output) (s:'state)
   (certList:('command inst,'principal,'d,'e)Form list)
   (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form)
   (cmd: 'command) (x:('command inst, 'principal, 'd, 'e) Form)
   (ins:('command inst,'principal,'d,'e)Form list)
   (outs: 'output list).
 ~inputTest x ==>
 (TR
  ((M: ('command inst, 'b, 'principal, 'd, 'e) Kripke), Oi: 'd po, Os: 'e po)
  (discard: 'command trType)
```

```
(CFG inputTest stateInterp certList
     ((x:('command inst,'principal,'d,'e)Form)::ins) s outs)
 (CFG inputTest stateInterp certList ins (NS s discard)
     ((Out s discard)::outs))))'
(* Split up TR_rules into individual clauses
val [rule0, rule1, rule2] = CONJUNCTS TR_rules
(*\ Prove\ the\ converse\ of\ rule0\ ,\ rule1\ ,\ and\ rule2
val TR_lemma0 =
TAC_PROOF(([], flip_TR_rules rule0),
DISCH_TAC THEN
IMP_RES_TAC TR_cases THEN
PAT_ASSUM
 "
exec cmd = v"
 (fn th => ASSUME_TAC(REWRITE_RULE[trType_one_one,trType_distinct_clauses]th)) THEN
PROVE_TAC[configuration_one_one , list_11 , trType_distinct_clauses])
val TR_lemma1 =
TAC_PROOF(([], flip_TR_rules rule1),
DISCH_TAC THEN
IMP_RES_TAC TR_cases THEN
PAT_ASSUM
 ", trap cmd = v"
 (fn th => ASSUME_TAC(REWRITE_RULE[trType_one_one, trType_distinct_clauses]th)) THEN
PROVE_TAC[configuration_one_one, list_11, trType_distinct_clauses])
val TR_lemma2 =
TAC_PROOF(([], flip_TR_rules rule2),
DISCH_TAC THEN
IMP_RES_TAC TR_cases THEN
PAT_ASSUM
 ", discard = v"
 (fn th => ASSUME_TAC(REWRITE_RULE[trType_one_one,trType_distinct_clauses]th)) THEN
PROVETAC[configuration_one_one, list_11, trType_distinct_clauses])
val TR_rules_converse =
TAC_PROOF(([], flip_TR_rules TR_rules),
REWRITE_TAC[TR_lemma0, TR_lemma1, TR_lemma2])
val TR_EQ_rules_thm = TR_EQ_rules TR_rules TR_rules_converse
val _ = save_thm("TR_EQ_rules_thm",TR_EQ_rules_thm)
val [TRrule0, TRrule1, TR_discard_cmd_rule] = CONJUNCTS TR_EQ_rules_thm
val _ = save_thm("TRrule0", TRrule0)
val _ = save_thm("TRrule1",TRrule1)
val _ = save_thm("TR_discard_cmd_rule", TR_discard_cmd_rule)
```

```
(* If (CFGInterpret
                                                                                                *)
         (M, Oi, Os)
                                                                                                *)
(*
(*
         (C\!F\!G\ input Test\ state Interpret\ cert List
                                                                                                    *)
(*
               ((P \ says \ (prop \ (CMD \ cmd)))::ins) \ s \ outs) \Longrightarrow
                                                                                                *)
(*
       ((M, Oi, Os) \ sat \ (prop \ (CMD \ cmd))))
                                                                                                *)
(* is a valid inference rule, then executing cmd the exec(CMD cmd) transition
(* occurs if and only if prop (CMD cmd), inputTest, and
(* CFGInterpret (M, Oi, Os)
(* (CFG input Test state Interpret cert List (P says prop (CMD cmd)::ins) s outs)
(* are true.
                                                                                                *)
(* -
val TR_exec_cmd_rule =
TAC_PROOF(([],
"!inputTest certList stateInterp P cmd ins s outs.
 (!M Oi Os.
 (CFGInterpret
  ((M:('command inst, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po), (Os:'e po))
  (CFG inputTest
         (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form) certList
         (P says (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form)::ins)
         (s:'state) (outs:'output list)) =>
  (M,Oi,Os) sat (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form))) =>>
(!NS Out M Oi Os.
 TR
  ((M:('command inst, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po),
   (Os:'e po)) (exec (cmd:'command))
  (CFG (inputTest : ('command inst, 'principal, 'd, 'e) Form -> bool)
             (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form)
             (certList : ('command inst, 'principal, 'd, 'e) Form list)
             ((P:'principal Princ) says
               (\hspace{0.1cm} prop\hspace{0.1cm} \hspace{0.1cm} (\hspace{0.1cm} S\hspace{0.1cm} O\hspace{0.1cm} M\hspace{0.1cm} E\hspace{0.1cm} \hspace{0.1cm} cmd) \hspace{0.1cm} : (\hspace{0.1cm} {}^{\prime} command \hspace{0.1cm} inst \hspace{0.1cm}, \hspace{0.1cm} {}^{\prime} principal \hspace{0.1cm}, \hspace{0.1cm} {}^{\prime} d \hspace{0.1cm}, \hspace{0.1cm} {}^{\prime} e \hspace{0.1cm}) \hspace{0.1cm} Form) ::
                    (ins : ('command inst, 'principal, 'd, 'e) Form list))\\
             (s:'state) (outs:'output list))
    (CFG inputTest stateInterp certList ins
             ((NS: 'state -> 'command trType -> 'state) s (exec cmd))
             ((Out: 'state -> 'command trType -> 'output) s (exec cmd)::
                    outs)) <=>
   inputTest
     (P says (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form)) /
    (CFGInterpret (M, Oi, Os)
       inputTest stateInterp certList
       (P says (prop (SOME cmd): ('command inst, 'principal, 'd, 'e) Form)::ins)
       s outs)) /\
    (M, Oi, Os) sat (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form))''),
REWRITE_TAC[TRrule0] THEN
REPEAT STRIP_TAC THEN
EQ_TAC THEN
REPEAT STRIP_TAC THEN
PROVE_TAC[])
val _ = save_thm("TR_exec_cmd_rule", TR_exec_cmd_rule)
(* If (CFGInterpret
                                                                                                *)
(*
         (M, Oi, Os)
                                                                                                *)
         (CFG\ input Test\ state Interpret\ cert List
               ((P \ says \ (prop \ (CMD \ cmd))) :: ins) \ s \ outs) \Longrightarrow
```

```
(*
      ((M, Oi, Os) \ sat \ (prop TRAP)))
(*\ is\ a\ valid\ inference\ rule\ ,\ then\ executing\ cmd\ the\ exec\ (CMD\ cmd)\ transition
(* occurs if and only if prop TRAP, inputTest, and
(* CFGInterpret (M, Oi, Os)
                                                                                     *)
(* (CFG inputTest stateInterpret certList (P says prop (CMD cmd)::ins)
(*
          s outs) are true.
(* -
val TR_trap_cmd_rule =
TAC_PROOF(
([]]
 '!inputTest (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form) certList
   P cmd ins (s:'state) (outs:'output list).
  (!M Oi Os.
  CFGInterpret
   ((M:('command inst, 'b, 'principal, 'd, 'e) Kripke),(Oi:'d po), (Os:'e po))
   (CFG\ input Test\ state Interp\ cert List
         (P says (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form)::ins)
            s outs) \Longrightarrow
  (M, Oi, Os) sat (prop\ NONE : ('command\ inst, 'principal, 'd, 'e)\ Form)) =>>
(!NS Out M Oi Os.
TR
  ((M:(\ \text{'command inst}\ ,\ \ \text{'b}\ ,\ \ \text{'principal}\ ,\ \ \text{'d}\ ,\ \ \text{'e})\ Kripke)\ ,(Oi:\ \text{'d}\ po)\ ,
   (Os:'e po)) (trap (cmd:'command))
  (CFG (inputTest : ('command inst, 'principal, 'd, 'e) Form -> bool)
     (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form)
     (certList : ('command inst, 'principal, 'd, 'e) Form list)
     ((P:'principal Princ) says
      (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form)::
           (ins:('command inst, 'principal, 'd, 'e) Form list))
     (s:'state) outs)
  (CFG inputTest (stateInterp:'state -> ('command inst, 'principal, 'd, 'e)Form)
      certList ins
     ((NS: 'state -> 'command trType -> 'state) s (trap cmd))
     ((Out: 'state -> 'command trType -> 'output) s
         (trap cmd)::outs)) <=>
inputTest
  (P says
   (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form)) /\
CFGInterpret (M, Oi, Os)
  (CFG inputTest (stateInterp:'state -> ('command inst,'principal,'d,'e)Form)
      certList
     (P savs
      (prop (SOME cmd) : ('command inst, 'principal, 'd, 'e) Form)::ins)
     s outs) /\
(M, Oi, Os) sat (prop NONE)) ''),
REWRITE_TAC[TRrule1] THEN
REPEAT STRIP_TAC THEN
EQ_TAC THEN
REPEAT STRIP_TAC THEN
PROVE_TAC[])
val _ = save_thm("TR_trap_cmd_rule", TR_trap_cmd_rule)
(* ==== start here ====
 ==== end here ==== *)
val = export\_theory ();
val _ = print_theory "-";
```

end (* structure *)

Source code: SM0Script

```
(* Machine SMO example
(* Author: Shiu-Kai Chin
                                                                       *)
(* Date: 30 November 2015
structure SM0Script = struct
(* interactive mode
app load ["TypeBase", "ssm1Theory", "SM0Theory", "acl_infRules", "aclrulesTheory",
         "aclDrulesTheory", "SM0Theory"];
open TypeBase ssm1Theory acl_infRules aclrulesTheory
    acl Drules Theory \ satList Theory \ SM0 Theory
*)
open HolKernel boolLib Parse bossLib
open TypeBase ssm1Theory acl_infRules aclrulesTheory aclDrulesTheory
    \operatorname{satListTheory}
(*****
* create a new theory
*********
val _ = new_theory "SM0"
(* Define datatypes for commands and their properties
                                                                       *)
(* ---
Datatype 'privcmd = launch | reset'
val privcmd_distinct_clauses = distinct_of '': privcmd''
val _ = save_thm("privcmd_distinct_clauses", privcmd_distinct_clauses)
Datatype 'npriv = status'
val_{-} =
Datatype 'command = NP npriv | PR privcmd'
val command_distinct_clauses = distinct_of ':command''
val _ = save_thm("command_distinct_clauses", command_distinct_clauses)
val command_one_one = one_one_of '':command''
```

```
val _ = save_thm("command_one_one", command_one_one)
(* Define the states
(* -----
val_{-} =
Datatype 'state = STBY | ACTIVE'
val state_distinct_clauses = distinct_of ':state''
val _ = save_thm("state_distinct_clauses", state_distinct_clauses)
(* Define the outputs
                                                                                  *)
(* ----
val_{-} =
Datatype 'output = on | off '
val output_distinct_clauses = distinct_of '':output''
val _ = save_thm("output_distinct_clauses",output_distinct_clauses)
(* Define next-state function for machine MO
                                                                                  *)
val SM0ns_def =
Define
'(SMOns STBY (exec (PR reset)) = STBY) /\
 (SM0ns STBY (exec (PR launch)) = ACTIVE) /\
 (SM0ns STBY (exec (NP status)) = STBY) / 
 (SMOns ACTIVE (exec (PR reset)) = STBY) /\
 (SMOns ACTIVE (exec (PR launch)) = ACTIVE) / 
 (SM0ns ACTIVE (exec (NP status)) = ACTIVE) / 
 (SM0ns\ STBY\ (trap\ (PR\ reset)) = STBY)\ /\
 (SM0ns STBY (trap (PR launch)) = STBY) / 
 (SM0ns STBY (trap (NP status)) = STBY) / 
 (SM0ns ACTIVE (trap (PR reset)) = ACTIVE) / 
 (SMOns ACTIVE (trap (PR launch)) = ACTIVE) /\
 (SMOns ACTIVE (trap (NP status)) = ACTIVE) / 
 (SM0ns STBY discard = STBY) /\
 (SMOns ACTIVE discard = ACTIVE) '
                                                                                  *)
(* Define next-output function for machine MO
                                                                                  *)
(* ----
val SM0out_def =
Define
'(SMOout STBY (exec (PR reset)) = off) /\
 (SM0out STBY (exec (PR launch)) = on) / 
 (SM0out STBY (exec (NP status)) = off) /\
 (SM0out\ ACTIVE\ (exec\ (PR\ reset)) = off) / 
 (SM0out\ ACTIVE\ (exec\ (PR\ launch)) = on) / 
 (SM0out\ ACTIVE\ (exec\ (NP\ status)) = on) / 
 (SM0out STBY (trap (PR reset)) = off) / 
 (SM0out STBY (trap (PR launch)) = off) / 
 (SM0out STBY (trap (NP status)) = off) /\
 (SM0out\ ACTIVE\ (trap\ (PR\ reset)) = on)\ /\
 (SM0out ACTIVE (trap (PR launch)) = on) /\
 (SMOout ACTIVE (trap (NP status)) = on) /\
```

```
(SM0out STBY discard = off) /\
 (SM0out ACTIVE discard = on) '
(* ---
(* Define datatypes for principles and their properties
                                                                                   *)
(* -----
val_{-} =
Datatype 'staff = Alice | Bob | Carol'
val staff_distinct_clauses = distinct_of ':staff'
val _ = save_thm("staff_distinct_clauses", staff_distinct_clauses)
(* Input Authentication
                                                                                   *)
val inputOK_def =
Define
'(inputOK
  (((Name Alice) says
   (prop (SOME (cmd:command)))):(command inst, staff, 'd, 'e)Form) = T) /\
 (inputOK
  (((Name Bob) says
   (prop (SOME (cmd:command)))):(command inst, staff, 'd, 'e)Form) = T) /\
 (inputOK _{-} = F)
(* SM0StateInterp
val SM0StateInterp_def =
Define
'SMOStateInterp (state:state) = (TT:(command inst, staff, 'd, 'e)Form)'
(* certs definition
(* -----
\mathbf{val} \ \mathtt{certs\_def} =
Define
'certs (cmd:command)(npriv:npriv)(privcmd:privcmd) =
 [(Name Alice controls ((prop (SOME (NP npriv))):(command inst, staff, 'd, 'e)Form));
  Name Alice controls (prop (SOME (PR privemd)));
  Name Bob controls prop (SOME (NP npriv));
  ((Name Bob) says (prop (SOME (PR privemd)))) impf (prop NONE)]'
                                                                                  *)
(* Some theorems showing any message from Carol is rejected
                                                                                   *)
val Carol_rejected_lemma =
TAC_PROOF(([],
''~inputOK
   (((Name Carol) says (prop (SOME (cmd:command)))):(command inst, staff, 'd, 'e)Form)
PROVE_TAC[inputOK_def])
val _ = save_thm("Carol_rejected_lemma", Carol_rejected_lemma)
val Carol_discard_lemma =
TAC_PROOF(([],
"TR ((M:(command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os) discard
```

```
(CFG inputOK SM0StateInterp (certs cmd npriv privcmd)
   (((Name Carol) says (prop (SOME (cmd:command))))::ins)
   s (outs:output list))
  (CFG inputOK SM0StateInterp (certs cmd npriv privcmd) ins
  (SMOns s discard) ((SMOout s discard)::outs)) ''),
PROVE_TAC[Carol_rejected_lemma, TR_discard_cmd_rule])
val _ = save_thm("Carol_discard_lemma", Carol_discard_lemma)
(* Alice authorized on any privileged command
                                                                                 *)
val Alice_privcmd_lemma =
TAC_PROOF(([],
"CFGInterpret ((M: (command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os)
  (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)
   (((Name Alice) says (prop (SOME (PR (privcmd:privcmd)))))::ins)
   s (outs:output list)) ==>
  ((M,Oi,Os) sat (prop (SOME(PR privemd))))''),
REWRITE_TAC[CFGInterpret_def,certs_def,SM0StateInterp_def,satList_CONS,
            satList_nil, sat_TT] THEN
PROVE_TAC[Controls])
val _ = save_thm("Alice_privcmd_lemma", Alice_privcmd_lemma)
(* exec privemd occurs if and only if Alice's command is authenticated and
                                                                                *)
(* authorized
                                                                                 *)
(* ---
val Alice_exec_privcmd_justified_thm =
let
 val th1 =
 ISPECL
 [''inputOK:(command inst, staff,'d,'e)Form -> bool'',
  ''(certs cmd npriv privcmd):(command inst, staff, 'd, 'e)Form list'',
  "SMOStateInterp:state->(command inst, staff, 'd, 'e)Form',
  "'Name Alice", "PR privcmd", "ins:(command inst, staff, 'd, 'e)Form list",
  ''s:state'', ''outs:output list'']
 TR_exec_cmd_rule
in
TAC_PROOF(([],
    ''!(NS :state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (PR (privcmd : privcmd)))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Alice says
              (prop (SOME (PR privemd) : command inst) :
                 (command inst, staff, 'd, 'e) Form)::
                  (ins :(command inst, staff, 'd, 'e) Form list)) (s :state)
             (outs :output list))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
```

```
(certs cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (PR privcmd)))
              (Out s (exec (PR privcmd))::outs)) <=>
        inputOK
          (Name Alice says
           (prop (SOME (PR privcmd) :command inst) :
               (command inst, staff, 'd, 'e) Form)) / 
        CFGInterpret (M, Oi, Os)
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (PR privemd) :command inst) :
                 (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M, Oi, Os) sat
        (prop (SOME (PR privemd) :command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
PROVE_TAC[th1, Alice_privcmd_lemma])
end
val _ = save_thm("Alice_exec_privcmd_justified_thm", Alice_exec_privcmd_justified_thm
(*\ If\ Alice\ 's\ privileged\ command\ was\ executed\ ,\ then\ the\ request\ was\ verified\ .\ *)
val Alice_privcmd_verified_thm =
TAC_PROOF(([], ''!(NS :state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os : 'e po).
        TR (M, Oi, Os) (exec (PR (privcmd : privcmd)))
          (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\!\!\!>\ bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
              (prop (SOME (PR privcmd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
             (outs :output list))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                (command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (PR privcmd)))
              (Out s (exec (PR privcmd))::outs)) =>>
        (M, Oi, Os) sat
        (prop (SOME (PR privemd) :command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
PROVE_TAC[Alice_exec_privcmd_justified_thm])
val _ = save_thm("Alice_privcmd_verified_thm", Alice_privcmd_verified_thm)
```

```
(* If Alice's privileged command was authorized, then the command is executed *)
{\bf val}\ A {\tt lice\_justified\_privcmd\_exec\_thm}\ =
TAC_PROOF(([], ''!(NS :state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M:(command inst, 'b, staff, 'd, 'e) Kripke) (Oi:'d po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK
          (Name Alice says
           (prop (SOME (PR privcmd) :command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
          CFGInterpret (M, Oi, Os)
          (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\!\!\!>\ bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (PR privcmd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) =>>
        TR (M, Oi, Os) (exec (PR (privcmd : privcmd)))
           (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\!\!\!>\ bool)
              (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (PR privemd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                 (command inst , staff , 'd, 'e) Form list) ins
              (NS s (exec (PR privcmd)))
              (Out s (exec (PR privcmd))::outs))''),
PROVE_TAC[Alice_exec_privcmd_justified_thm ,inputOK_def ,Alice_privcmd_lemma])
val _ = save_thm("Alice_justified_privcmd_exec_thm", Alice_justified_privcmd_exec_thm
   )
val = export\_theory ()
val _ = print_theory "-"
end (* structure *)
```

Source code: SMOSolutionsScript

```
(* Solutions for Exercises 17.3.1, 17.3.2, and 17.3.3
(* Author: Shiu-Kai Chin
                                                                       *)
(* Date: 1 April 2017
structure SM0Solutions = struct
open HolKernel Parse boolLib bossLib;
open ssm1Theory SM0Theory acl_infRules aclrulesTheory
    aclDrulesTheory satListTheory
val _ = new_theory "SM0Solutions";
(* ==== start here ====*)
(* Exercise 17.3.1
                                                                       *)
(* Alice's non-privileged commands are executed and justified
                                                                       *)
(*a*)
val Alice_npriv_lemma=
TAC_PROOF(([],
"CFGInterpret ((M: (command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os)
  (CFG inputOK SM0StateInterp (certs cmd npriv privcmd)
  (((Name Alice) says (prop (SOME (NP (npriv:npriv)))))::ins)
  s (outs:output list)) ==>
  ((M,Oi,Os) sat (prop (SOME(NP npriv))))''),
 REWRITE_TAC[CFGInterpret_def,certs_def,SM0StateInterp_def,satList_CONS,
     satList_nil ,sat_TT | THEN PROVE_TAC[Controls])
val _ = save_thm("Alice_npriv_lemma", Alice_npriv_lemma)
(*b*)
val Alice_exec_npriv_justified_thm =
 val th1 = ISPECL
 [''inputOK:(command inst, staff,'d,'e)Form -> bool'',
  ``(certs cmd npriv privcmd):(command inst, staff, `d, `e)Form list ``,
  ''SMOStateInterp:state->(command inst, staff,'d,'e)Form'',
  ''Name Alice'', ''NP npriv'', ''ins:(command inst, staff, 'd, 'e)Form list'',
  "s:state", "outs:output list" TR_exec_cmd_rule
in
TAC_PROOF(([],
```

```
''!(NS : state -> command trType -> state)
          (Out : state -> command trType -> output)
          (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
          (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
           (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\,,\ 'e)\ Form\ -\!\!\!>\ bool)
              (SMOStateInterp : state \rightarrow (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                 (command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs)) <=>
        inputOK
           (Name Alice says
            (prop (SOME (NP npriv) : command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
        CFGInterpret (M, Oi, Os)
           (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M, Oi, Os) sat
         (prop (SOME (NP npriv) :command inst) :
             ({\tt command \ inst} \ , \ {\tt staff} \ , \ {\tt 'd} \ , \ {\tt 'e}) \ {\tt Form}) \ ``) \ , 
           PROVE_TAC[th1, Alice_npriv_lemma])
end
val _ = save_thm("Alice_exec_npriv_justified_thm", Alice_exec_npriv_justified_thm)
(*c*)
val Alice_npriv_verified_thm=
TAC_PROOF(([],
       ''!(NS : state -> command trType -> state)
         (Out :state -> command trType -> output)
          (M:(command inst, 'b, staff, 'd, 'e) Kripke) (Oi:'d po)
          (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
           (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
```

```
(outs :output list))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs cmd npriv privcmd :
                (command inst, staff, 'd, 'e) Form list) ins
             (NS s (exec (NP npriv)))
             (Out s (exec (NP npriv))::outs)) =>>
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) : command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[Alice_exec_npriv_justified_thm])
val _ = save_thm("Alice_npriv_verified_thm", Alice_npriv_verified_thm)
val Alice_npriv_verified_thm=
TAC_PROOF(([],
         ''!(NS :state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Alice says
              (prop (SOME (NP npriv) : command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
             (outs :output list))
          (CFG (inputOK :(command inst, staff, 'd, 'e) Form \rightarrow bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs cmd npriv privcmd:
                (command inst, staff, 'd, 'e) Form list) ins
             (NS s (exec (NP npriv)))
             (Out s (exec (NP npriv))::outs)) ==>
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[Alice_exec_npriv_justified_thm])
val _ = save_thm("Alice_npriv_verified_thm", Alice_npriv_verified_thm)
(*d*)
val Alice_justified_npriv_exec_thm=
TAC_PROOF(([],
''!(NS : state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK
          (Name Alice says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)) /\
          CFGInterpret (M, Oi, Os)
          (CFG (inputOK :(command inst, staff, 'd, 'e) Form \rightarrow bool)
             (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
```

```
(certs cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) =>>
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG\ (inputOK\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\! >\ bool)
              (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
              (certs (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Alice says
              (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
             (outs :output list))
          (CFG (inputOK : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs cmd npriv privcmd:
                (command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs))''),
             PROVE\_TAC[\ Alice\_exec\_npriv\_justified\_thm\ , inputOK\_def\ , Alice\_npriv\_lemma
                 ])
val _ = save_thm("Alice_justified_npriv_exec_thm", Alice_justified_npriv_exec_thm)
(* Exercise 17.3.3A
                                                                                  *)
(* inputOK2 and certs2 defined to authenticate Carol only. Carol is
                                                                                  *)
(* authorized solely on npriv commands, and trapped on privemd.
val inputOK2_def =
'(inputOK2 (((Name Carol) says (prop (SOME (cmd:command)))):(command inst, staff, 'd, '
   e)Form) = T) / (inputOK2 _ = F)
val certs2_def =
Define
'certs2 (cmd:command)(npriv:npriv)(privcmd:privcmd) = [(Name Carol controls ((prop (
   SOME (NP npriv))):(command inst, staff, 'd, 'e)Form)); ((Name Carol) says (prop (
   SOME (PR privcmd)))) impf (prop NONE)]
(* Exercise 17.3.3 B
                                                                                  *)
(* Carol can execute non-privileged commands using inputOK2 and certs2
(* -
val Carol_npriv_lemma=
TAC_PROOF(([],
"CFGInterpret ((M: (command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os)
  (CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)
```

```
(((Name Carol) says (prop (SOME (NP (npriv:npriv)))))::ins)
   s (outs:output list)) =>>
  ((M,Oi,Os) sat (prop (SOME(NP npriv))))''),
  REWRITE_TAC [ CFGInterpret_def , certs2_def , SM0StateInterp_def , satList_CONS ,
             satList_nil ,sat_TT] THEN PROVE_TAC[Controls])
val _ = save_thm("Carol_npriv_lemma", Carol_npriv_lemma)
val Carol_exec_npriv_justified_thm=
let
 val th1 = ISPECL
 [''inputOK2:(command inst, staff,'d,'e)Form -> bool'', ''(certs2 cmd npriv privcmd)
     :(command inst, staff,'d,'e)Form list'', ''SM0StateInterp:state->(command inst,
     staff, 'd, 'e) Form'', ''Name Carol'', ''NP npriv'', ''ins:(command inst, staff, 'd, 'e)
     Form list '', ''s:state'', ''outs:output list ''] TR_exec_cmd_rule
in
TACPROOF(([],
       ''!(NS : state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (NP npriv) : command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 ({\tt command \ inst} \ , \ {\tt staff} \ , \ {\tt 'd} \ , \ {\tt 'e}) \ {\tt Form \ list} \ ) \ {\tt ins}
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs)) <=>
        inputOK2
           (Name Carol says
            (prop (SOME (NP npriv) : command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
        CFGInterpret (M, Oi, Os)
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (NP npriv) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) :command inst) :
            (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[th1, Carol_npriv_lemma])
end
val _ = save_thm("Carol_exec_npriv_justified_thm", Carol_exec_npriv_justified_thm)
val Carol_npriv_verified_thm=
TAC_PROOF(([],
```

```
''!(NS : state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M:(command inst, 'b, staff, 'd, 'e) Kripke) (Oi:'d po)
         (Os: 'e po).
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form \rightarrow bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Carol says
              (prop (SOME (NP npriv) : command inst) :
                 (command inst, staff, 'd, 'e) Form)::
                  (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
             (outs :output list))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 cmd npriv privcmd :
                (command inst, staff, 'd, 'e) Form list) ins
             (NS s (exec (NP npriv)))
             (Out s (exec (NP npriv))::outs)) ==>
        (M, Oi, Os) sat
        (prop (SOME (NP npriv) :command inst) :
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[Carol_exec_npriv_justified_thm])
val _ = save_thm("Carol_npriv_verified_thm", Carol_npriv_verified_thm)
val Carol_justified_npriv_exec_thm=
TAC_PROOF(([],
       ''!(NS :state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK2
          (Name Carol says
           (prop (SOME (NP npriv) :command inst) :
              (command inst, staff, 'd, 'e) Form)) / 
          CFGInterpret (M, Oi, Os)
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 cmd npriv privcmd:
                (command inst, staff, 'd, 'e) Form list)
             (Name Carol says
              (prop (SOME (NP npriv) :command inst) :
                 (command inst, staff, 'd, 'e) Form)::ins) s outs) =>>
        TR (M, Oi, Os) (exec (NP (npriv :npriv)))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
             (Name Carol says
              (prop (SOME (NP npriv) : command inst) :
                 (command inst, staff, 'd, 'e) Form)::
                  (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
             (outs :output list))
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 cmd npriv privcmd :
```

```
(command inst, staff, 'd, 'e) Form list) ins
              (NS s (exec (NP npriv)))
              (Out s (exec (NP npriv))::outs)) ''),
             PROVE\_TAC[\ Carol\_exec\_npriv\_justified\_thm\ , inputOK2\_def\ , Carol\_npriv\_lemma
val _ = save_thm("Carol_justified_npriv_exec_thm", Carol_justified_npriv_exec_thm)
(* Exercise 17.3.3 C
                                                                                   *)
(* Carol's request to execute a privileged command is trapped
val Carol_privcmd_trap_lemma=
TAC_PROOF(([],
''CFGInterpret ((M: (command inst, 'b, staff, 'd, 'e) Kripke), Oi, Os)
  (CFG inputOK2 SM0StateInterp (certs2 cmd npriv privcmd)
   (((Name Carol) says (prop (SOME (PR (privcmd:privcmd)))))::ins)
   s (outs:output list)) ==>
  ((M,Oi,Os) sat (prop NONE))''),
  REWRITE_TAC[CFGInterpret_def,certs2_def,SM0StateInterp_def,satList_CONS,
      satList_nil ,sat_TT ] THEN PROVE_TAC[Controls , Modus_Ponens])
val _ = save_thm("Carol_privcmd_trap_lemma", Carol_privcmd_trap_lemma)
val Carol_trap_privcmd_justified_thm=
 val th1 = ISPECL
 [''inputOK2:(command inst, staff,'d,'e)Form -> bool'', ''SMOStateInterp:state ->(
    command inst, staff, 'd, 'e)Form'', ''(certs2 cmd npriv privcmd):(command inst,
     staff, 'd, 'e) Form list '', ''Name Carol'', ''PR privcmd'', ''ins:(command inst, staff
     ,'d,'e)Form list'', ''s:state'', ''outs:output list''] TR_trap_cmd_rule
in
TAC_PROOF(([],
       ''!(NS : state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (trap (PR (privemd : privemd)))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (PR privcmd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
(ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list) ins
              (NS s (trap (PR privemd)))
              (Out s (trap (PR privcmd))::outs)) <=>
        inputOK2
          (Name Carol says
           (prop (SOME (PR privcmd) :command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
        CFGInterpret (M, Oi, Os)
```

```
(CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (PR privcmd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) /\
        (M, Oi, Os) sat (prop NONE): (command inst, staff, 'd, 'e) Form',
PROVE_TAC[th1, Carol_privcmd_trap_lemma])
end
val _ = save_thm("Carol_trap_privcmd_justified_thm", Carol_trap_privcmd_justified_thm
val Carol_privcmd_trapped_thm=
TAC_PROOF(([],
       ''!(NS :state -> command trType -> state)
         (Out : state -> command trType -> output)
         (M: (command inst, 'b, staff, 'd, 'e) Kripke) (Oi: 'd po)
         (Os: 'e po).
        TR (M, Oi, Os) (trap (PR (privcmd : privcmd)))
          (CFG\ (inputOK2\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\!\!\!>\ bool)
             (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
             (certs2 (cmd :command) (npriv :npriv) privcmd :
                (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (PR privemd) : command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins :(command inst, staff, 'd, 'e) Form list)) (s :state)
              (outs :output list))
          (CFG (inputOK2 :(command inst, staff, 'd, 'e) Form \rightarrow bool)
             (SMOStateInterp :state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                (command inst, staff, 'd, 'e) Form list) ins
              (NS s (trap (PR privcmd)))
              (Out s (trap (PR privcmd))::outs)) =>>
        (M, Oi, Os) sat
        (prop NONE:
           (command inst, staff, 'd, 'e) Form) ''),
           PROVE_TAC[Carol_trap_privcmd_justified_thm])
val _ = save_thm("Carol_privcmd_trapped_thm", Carol_privcmd_trapped_thm)
val Carol_justified_privcmd_trap_thm=
TAC_PROOF(([],
       ''!(NS : state -> command trType -> state)
         (Out :state -> command trType -> output)
         (M:(command inst, 'b, staff, 'd, 'e) Kripke) (Oi:'d po)
         (Os: 'e po) cmd npriv privcmd ins s outs.
         inputOK2
          (Name Carol says
           (prop (SOME (PR privcmd) :command inst) :
               (command inst, staff, 'd, 'e) Form)) /\
          CFGInterpret (M, Oi, Os)
          (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd:
                 (command inst, staff, 'd, 'e) Form list)
```

```
(Name Carol says
               (prop (SOME (PR privemd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::ins) s outs) =>>
        TR (M,Oi,Os) (trap (PR (privcmd :privcmd)))
          (CFG\ (inputOK2\ : (command\ inst\ ,\ staff\ ,\ 'd\ ,\ 'e)\ Form\ -\!\!\!>\ bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 (cmd :command) (npriv :npriv) privcmd :
                 (command inst, staff, 'd, 'e) Form list)
              (Name Carol says
               (prop (SOME (PR privcmd) :command inst) :
                  (command inst, staff, 'd, 'e) Form)::
                   (ins:(command inst, staff, 'd, 'e) Form list)) (s:state)
              (outs :output list))
           (CFG (inputOK2 : (command inst, staff, 'd, 'e) Form -> bool)
              (SMOStateInterp : state -> (command inst, staff, 'd, 'e) Form)
              (certs2 cmd npriv privcmd :
                 (command inst, staff, 'd, 'e) Form list) ins
              (NS s (trap (PR privcmd)))
              (Out s (trap (PR privcmd))::outs))''),
PROVE_TAC[Carol_trap_privcmd_justified_thm ,inputOK2_def ,Carol_privcmd_trap_lemma])
\mathbf{val} \ \_ = \mathbf{save\_thm} \ ("Carol\_justified\_privcmd\_trap\_thm", Carol\_justified\_privcmd\_trap\_thm")
(*==== *)
val = export_theory();
end (* structure *)
```