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1 cipher Theory

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Parent Theories: indexedLists, patternMatches

1.1 Datatypes

```
asymMsg = Ea ('princ pKey) ('message option) 
 digest = hash ('message option) 
 pKey = pubK 'princ | privK 'princ 
 symKey = sym num 
 symMsg = Es symKey ('message option)
```

1.2 Definitions

1.3 Theorems

```
 [\operatorname{asymMsg\_one\_one}] \\ \vdash \forall a_0 \ a_1 \ a_0' \ a_1'. \\ \quad (\operatorname{Ea} \ a_0 \ a_1 = \operatorname{Ea} \ a_0' \ a_1') \iff (a_0 = a_0') \ \land \ (a_1 = a_1') \\ [\operatorname{deciphP\_clauses}] \\ \vdash (\forall P \ text. \\ \quad (\operatorname{deciphP} \ (\operatorname{pubK} \ P) \ (\operatorname{Ea} \ (\operatorname{privK} \ P) \ (\operatorname{SOME} \ text)) = \\ \quad \operatorname{SOME} \ text) \ \land \\ \quad (\operatorname{deciphP} \ (\operatorname{privK} \ P) \ (\operatorname{Ea} \ (\operatorname{pubK} \ P) \ (\operatorname{SOME} \ text)) = \\ \quad \operatorname{SOME} \ text)) \ \land \\ (\forall k \ P \ text. \\ \quad (\operatorname{deciphP} \ k \ (\operatorname{Ea} \ (\operatorname{privK} \ P) \ (\operatorname{SOME} \ text)) = \operatorname{SOME} \ text) \iff \\ \quad (k = \operatorname{pubK} \ P)) \ \land \\ (\forall k \ P \ text. \\ \end{aligned}
```

Theorems

```
(deciphP \ k \ (Ea \ (pubK \ P) \ (SOME \ text)) = SOME \ text) \iff
         (k = privK P)) \land
     (\forall x \ k_2 \ k_1 \ P_2 \ P_1.
         (deciphP (pubK P_1) (Ea (pubK P_2) (SOME x)) = NONE) \land
         (deciphP k_1 (Ea k_2 NONE) = NONE)) \wedge
    \forall x \ P_2 \ P_1. deciphP (privK P_1) (Ea (privK P_2) (SOME x)) = NONE
[deciphP_def]
 \vdash (deciphP key (Ea (privK P) (SOME x)) =
     if key = pubK P then SOME x else NONE) \wedge
     (deciphP \ key \ (Ea \ (pubK \ P) \ (SOME \ x)) =
     if key = privK P then SOME x else NONE) \wedge
     (deciphP k_1 (Ea k_2 NONE) = NONE)
[deciphP_ind]
 \vdash \forall P'.
       (\forall key \ P \ x. \ P' \ key \ (Ea \ (privK \ P) \ (SOME \ x))) \ \land
       (\forall key \ P \ x. \ P' \ key \ (Ea \ (pubK \ P) \ (SOME \ x))) \ \land
       (\forall k_1 \ k_2. \ P' \ k_1 \ (\texttt{Ea} \ k_2 \ \texttt{NONE})) \Rightarrow
       \forall v \ v_1 . \ P' \ v \ v_1
[deciphP_one_one]
 \vdash (\forall P_1 \ P_2 \ text_1 \ text_2.
        (deciphP (pubK P_1) (Ea (privK P_2) (SOME text_2)) =
          SOME text_1) \iff (P_1 = P_2) \land (text_1 = text_2)) \land
     (\forall P_1 \ P_2 \ text_1 \ text_2.
         (deciphP (privK P_1) (Ea (pubK P_2) (SOME text_2)) =
          SOME text_1) \iff (P_1 = P_2) \land (text_1 = text_2)) \land
     (\forall p \ c \ P \ msg.
         (deciphP (pubK P) (Ea p c) = SOME msg) \iff
         (p = privK P) \land (c = SOME msq)) \land
     (\forall enMsq \ P \ msg.
         (deciphP (pubK P) enMsg = SOME msg) \iff
         (enMsg = Ea (privK P) (SOME msg))) \land
     (\forall p \ c \ P \ msg.
         (deciphP (privK P) (Ea p c) = SOME msg) \iff
         (p = \text{pubK } P) \land (c = \text{SOME } msq)) \land
    \forall enMsg \ P \ msg.
       (deciphP (privK P) enMsg = SOME msg) \iff
       (enMsg = Ea (pubK P) (SOME msg))
[deciphS_clauses]
 \vdash (\forall k \ text. \ deciphS \ k (Es k (SOME text)) = SOME text) \land
     (\forall k_1 \ k_2 \ text.
```

```
(deciphS k_1 (Es k_2 (SOME text)) = SOME text) \iff
         (k_1 = k_2)) \wedge
     (\forall k_1 \ k_2 \ text.
         (deciphS k_1 (Es k_2 (SOME text)) = NONE) \iff k_1 \neq k_2) \land
     \forall k_1 \ k_2. deciphS k_1 (Es k_2 NONE) = NONE
[deciphS_def]
 \vdash (deciphS k_1 (Es k_2 (SOME x)) =
      if k_1 = k_2 then SOME x else NONE) \wedge
     (deciphS k_1 (Es k_2 NONE) = NONE)
[deciphS_ind]
 \vdash \forall P.
        (\forall k_1 \ k_2 \ x. \ P \ k_1 \ (\texttt{Es} \ k_2 \ (\texttt{SOME} \ x))) \ \land
        (\forall k_1 \ k_2. \ P \ k_1 \ (\texttt{Es} \ k_2 \ \texttt{NONE})) \Rightarrow
        \forall v \ v_1 . \ P \ v \ v_1
[deciphS_one_one]
 \vdash (\forall k_1 \ k_2 \ text_1 \ text_2.
         (deciphS k_1 (Es k_2 (SOME text_2)) = SOME text_1) \iff
         (k_1 = k_2) \wedge (text_1 = text_2)) \wedge
     \forall enMsq text key.
        (deciphS key\ enMsg = SOME text) \iff
        (enMsg = Es \ key \ (SOME \ text))
[digest_one_one]
 \vdash \forall a \ a'. (hash a = \text{hash } a') \iff (a = a')
[option_distinct]
 \vdash \forall x. \text{ NONE } \neq \text{SOME } x
[option_one_one]
 \vdash \forall x \ y. (SOME x = SOME \ y) \iff (x = y)
[pKey_distinct_clauses]
 \vdash (\forall a' \ a. pubK a \neq \text{privK } a') \land \forall a' \ a. privK a' \neq \text{pubK } a
[pKey_one_one]
 \vdash (\forall a \ a'. (pubK a = pubK a') \iff (a = a')) \land
     \forall a \ a'. (privK a = \text{privK } a') \iff (a = a')
```

```
[sign_one_one]
 \vdash \forall pubKey_1 \ pubKey_2 \ m_1 \ m_2.
       (sign pubKey_1 (hash m_1) = sign pubKey_2 (hash m_2)) \iff
       (pubKey_1 = pubKey_2) \land (m_1 = m_2)
[signVerify_one_one]
 \vdash (\forall P m_1 m_2.
        signVerify (pubK P) (Ea (privK P) (SOME (hash (SOME m_1))))
           (SOME m_2) \iff (m_1 = m_2)) \land
    (\forall signature \ P \ text.
        signVerify (pubK P) signature (SOME text) \iff
        (signature = sign (privK P) (hash (SOME text)))) \land
    \forall text_2 text_1 P_2 P_1.
      signVerify (pubK P_1) (sign (privK P_2) (hash (SOME text_2)))
         (SOME text_1) \iff (P_1 = P_2) \land (text_1 = text_2)
[signVerifyOK]
 \vdash \forall P \ msg.
      signVerify (pubK P) (sign (privK P) (hash (SOME <math>msg)))
         (SOME msq)
[symKey_one_one]
 \vdash \forall a \ a'. (sym a = \text{sym } a') \iff (a = a')
[symMsg_one_one]
 \vdash \forall a_0 \ a_1 \ a'_0 \ a'_1.
      (Es a_0 a_1 = Es a_0' a_1') \iff (a_0 = a_0') \land (a_1 = a_1')
     cryptoExercises Theory
```

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Parent Theories: cipher, string

2.1Theorems

```
[exercise15_6_1a_thm]
 \vdash \forall key \ enMsg \ message.
       (deciphS key \ enMsg = SOME \ message) \iff
       (enMsg = Es \ key \ (SOME \ message))
```

```
[exercise15_6_1b_thm]
 \vdash \forall keyAlice \ k \ text.
      (deciphS \ keyAlice \ (Es \ k \ (SOME \ text)) =
       SOME "This is from Alice") \iff
      (k = keyAlice) \land (text = "This is from Alice")
[exercise15_6_2a_thm]
 \vdash \forall P \; message.
      (deciphP (pubK P) enMsg = SOME message) \iff
      (enMsg = Ea (privK P) (SOME message))
[exercise15_6_2b_thm]
 \vdash \forall key text.
      (deciphP (pubK Alice) (Ea key (SOME text)) =
       SOME "This is from Alice") ←⇒
      (key = privK \ Alice) \land (text = "This is from Alice")
[exercise15_6_3_thm]
 \vdash \forall signature.
      signVerify (pubK Alice) signature
         (SOME "This is from Alice") \iff
      (signature =
       sign (privK Alice) (hash (SOME "This is from Alice")))
```

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