

```
// Swapping pairs make sum equal
```

```
// Given two arrays of integers A[] and B[] of size n and m,  
the task is to check if a pair of values (one value from  
each array) exists such that swapping the elements of the  
pair will make the sum of two arrays equal.
```

```
// Expected Time Complexity: O(mlogm+nlogn).
```

```
// Expected Auxiliary Space: O(1).
```

Idea: sA and sB are sum of all elements in array $A[]$ and array $B[]$ respectively. Here, if we are considering i^{th} element of A and j^{th} element of B , then it should satisfy a condition...

Handwritten derivation:

$$\begin{aligned} & \text{If } sA, sB; \text{ let say we are swapping } (i^{\text{th}}, j^{\text{th}}) \\ & sA - A[i] + B[j] = sB - B[j] + A[i] \\ \Rightarrow & sA + 2B[j] = sB + 2A[i] \\ & 2B[j] = sB - sA + 2A[i] \\ \Rightarrow & \text{If we run a loop for } A \text{ \& search } 2B[j] \text{ in } 2 \times B \text{ array} \end{aligned}$$

If we make i constant for a moment, we find that for a unique element in A , there exists a unique value in $2 \times B[]$ which will satisfy our condition. We can make all elements in $B[]$ twice and then, while traversing $A[]$ binary search for the element $sB - sA + 2A[i]$ in $2 \times B[]$.

Note: we will not find $(sB - sA + 2A[i]) / 2$ in $B[]$ array because the division of integers may cause some inaccuracies in the result.

```
int findSwapValues(int A[], int n, int B[], int m) //
```

```
Optimized: O(mlogm+nlogn)
```

```
{
```

```
    // sort it so that we can use binary search
```

```
    sort(B, B + m); // nlog(n)
```

```
    int sA = 0;
```

```
    int sB = 0;
```

```
    // sum of elements in A
```

```
    ----
```

```
    // sum of elements in B and multiplying its each element  
by 2.
```

```
for (int i = 0; i < n; i++)
{
    if (binary_search(B, B + m, sB - sA + 2 * A[i]))
        return 1;
}

return -1;
}
```