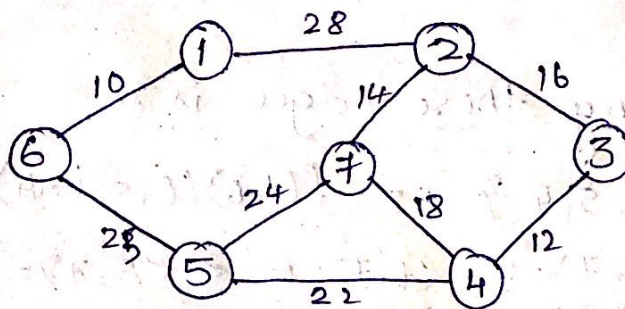


①

ADA AssignmentCHIRANJEEVI
IBM19CS403

Find the MST for following graph using
prim's algorithm



The cost adjacency matrix for above graph is

	1	2	3	4	5	6	7
1	-	28	∞	∞	∞	10	∞
2	28	-	16	∞	∞	∞	14
3	∞	16	-	12	∞	∞	∞
4	∞	∞	12	-	22	∞	18
5	∞	∞	∞	22	-	25	24
6	10	∞	∞	∞	25	-	∞
7	∞	14	∞	18	24	∞	-

$$\langle 1, 1 \rangle = 0$$

$$\langle 1, 2 \rangle = 28$$

$$\langle 1, 3 \rangle = \infty$$

$$\langle 1, 4 \rangle = \infty$$

$$\langle 1, 5 \rangle = \infty$$

$$\langle 1, 6 \rangle = 10$$

$$\langle 1, 7 \rangle = \infty$$

$$\langle 1, 1 \rangle = 0$$

$$\langle 1, 2 \rangle = 28$$

$$\langle 1, 3 \rangle = \infty$$

$$\langle 1, 4 \rangle = \infty$$

$$\langle 1, 5 \rangle = \infty$$

$$\langle 1, 7 \rangle = \infty$$

$$\langle 6, 2 \rangle = \infty$$

$$\langle 6, 3 \rangle = \infty$$

$$\langle 6, 4 \rangle = \infty$$

$$\langle 6, 5 \rangle = 25$$

$$\langle 6, 6 \rangle = 0$$

$$\langle 6, 7 \rangle = \infty$$

The least among these
edge is 10

$$V_T = \{1, 6\} \quad E_T = \{(1, 6)\}$$

The least among these edges is 25

$$V_T = \{1, 6, 5\} \quad E_T = \{(1, 6), (1, 5)\}$$

(2)

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$$\begin{aligned}
 \langle 1,1 \rangle &= 0 & \langle 1,7 \rangle &= \infty & \langle 6,7 \rangle &= \infty \\
 \langle 1,2 \rangle &= 28 & \langle 6,2 \rangle &= \infty & \langle 5,1 \rangle &= \infty & \langle 5,5 \rangle &= 0 \\
 \langle 1,3 \rangle &= \infty & \langle 6,3 \rangle &= \infty & \langle 5,2 \rangle &= \infty & \langle 5,7 \rangle &= 24 \\
 \langle 1,4 \rangle &= \infty & \langle 6,4 \rangle &= \infty & \langle 5,3 \rangle &= \infty \\
 \langle 1,5 \rangle &= \infty & \langle 6,6 \rangle &= 0 & \langle 5,4 \rangle &= 22
 \end{aligned}$$

The least among those edges is 22

$$\therefore V_T = \{1, 6, 5, 4\} \quad E_T = \{(1,6)(6,5)(5,4)(4,3)\}$$

$$\begin{aligned}
 \langle 1,1 \rangle &= 0 & \langle 1,7 \rangle &= \infty & \langle 6,7 \rangle &= \infty & \langle 5,7 \rangle &= 24 \\
 \langle 1,2 \rangle &= 28 & \langle 6,2 \rangle &= \infty & \langle 5,1 \rangle &= \infty & \langle 4,1 \rangle &= \infty \\
 \langle 1,3 \rangle &= \infty & \langle 6,3 \rangle &= \infty & \langle 5,2 \rangle &= \infty & \langle 4,2 \rangle &= \infty \\
 \langle 1,4 \rangle &= \infty & \langle 6,4 \rangle &= \infty & \langle 5,3 \rangle &= \infty & \langle 4,4 \rangle &= 0 \\
 \langle 1,5 \rangle &= \infty & \langle 6,6 \rangle &= 0 & \langle 5,5 \rangle &= 0 & \langle 4,6 \rangle &= \infty
 \end{aligned}$$

$$\begin{aligned}
 \langle 4,7 \rangle &= 18 & \langle 3,6 \rangle &= \infty \\
 \langle 3,1 \rangle &= \infty & \langle 3,7 \rangle &= \infty \\
 \langle 3,2 \rangle &= 16 \\
 \langle 3,3 \rangle &= 0 \\
 \langle 3,5 \rangle &= \infty
 \end{aligned}$$

The least among those edges is 16

$$\therefore V_T = \{1, 6, 5, 4, 3, 2\} \quad E_T = \{(1,6)(6,5)(5,4)(4,3)(3,2)\}$$

$$\begin{aligned}
 \langle 1,1 \rangle &= 0 & \langle 6,2 \rangle &= \infty & \langle 5,2 \rangle &= \infty & \langle 4,4 \rangle &= 0 \\
 \langle 1,2 \rangle &= 28 & \langle 6,3 \rangle &= \infty & \langle 5,3 \rangle &= \infty & \langle 4,6 \rangle &= \infty \\
 \langle 1,3 \rangle &= \infty & \langle 6,4 \rangle &= \infty & \langle 5,5 \rangle &= 0 & \langle 4,7 \rangle &= 18 \\
 \langle 1,4 \rangle &= \infty & \langle 6,6 \rangle &= 0 & \langle 5,7 \rangle &= 24 & \langle 3,1 \rangle &= \infty \\
 \langle 1,5 \rangle &= \infty & \langle 6,7 \rangle &= \infty & \langle 4,1 \rangle &= \infty & \langle 3,3 \rangle &= 0 \\
 \langle 1,7 \rangle &= \infty & \langle 5,1 \rangle &= \infty & \langle 4,3 \rangle &= \infty & \langle 3,5 \rangle &= \infty
 \end{aligned}$$

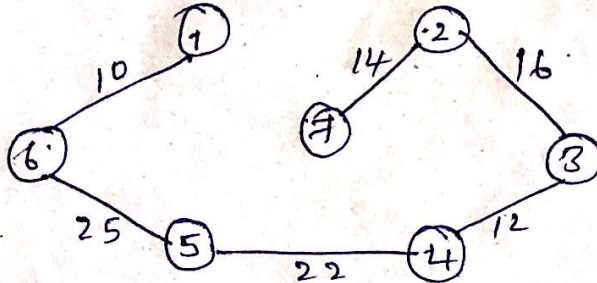
$$\begin{aligned}
 \langle 3,6 \rangle &= \infty & \langle 2,6 \rangle &= \infty \\
 \langle 3,7 \rangle &= \infty & \langle 2,7 \rangle &= 14 \\
 \langle 2,1 \rangle &= 28 \\
 \langle 2,2 \rangle &= 0 \\
 \langle 2,4 \rangle &= \infty \\
 \langle 2,5 \rangle &= \infty
 \end{aligned}$$

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The least among these edges is 14

$$\therefore V_T = \{1, 6, 5, 4, 3, 2, 7\} \quad E_T = \{(1,6), (6,5), (5,4), (4,3), (3,2), (2,7)\}$$

\therefore The minimum cost spanning tree is



The minimum cost is

$$\Rightarrow 10 + 25 + 22 + 12 + 16 + 14 = 99 \text{ units}$$