This document is a modified copy of the first five chapters of Basic Analysis: Introduction to Real Analysis, a free textbook included here for demonstration purposes.

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See https://www.jirka.org/ra/ for more information (including contact information, possible updates and errata).

The LaTeX source for the book is available for possible modification and customization at github: https://github.com/jirilebl/ra

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