

2026 r/mathmemes math contest

lets_clutch_this

To be Released Late 2025/Early 2026

1 Information

1. You will be allotted 48 hours of time to solve these 12 problems and submit your answers via the provided Google Form.
2. Since it would be impractical to restrict, any online calculators or aids will be allowed. However, you should subscribe to the honor code of solving the problems by yourself only.
3. Problems range in (roughly increasing) difficulty from early AMC to mid-late Putnam level.

2 Problems (WIP version)

1. James really wants to get a A on his number theory final exam, which is defined as a marked score of 90 or above. He is anxious, as he feels as if his performance was right around borderline. Fortunately for him, his professor is a very lenient grader - for any raw score r , his professor takes $\lceil r \rceil$ as the marked score so as long there exists some sequence of integers $a_1 > a_2 > \dots > a_k \geq 0$ such that when r is rounded up to the nearest 10^{-a_1} , then to the nearest 10^{-a_2} , and so on eventually to the nearest 10^{-a_k} , the score rounds to $\lceil r \rceil$. The maximum raw score R that James can score on the final exam yet not get a final grade of A can be expressed as $R = \frac{m}{n}$. Find $m + n$.
2. Jack is given a row of 2022 initially adjacent blocks, where each block is labeled either A or B . He can only move blocks labeled A to the left, and he can only move blocks labeled B to the right. If the expected value for the number of blocks Jack can possibly remove from the row is $\frac{m}{n}$ where m and n are positive integers such that $\gcd(m, n) = 1$, find the remainder when $m + n$ is divided by 1000.
3. Let a_1, a_2, \dots, a_{99} be a binary sequence such that for each $1 \leq k \leq 99$, a_k independently has a $k\%$ probability of being 1 and a $(100 - k)\%$ probability of being 0. Denote a *run* in a binary sequence as a maximal string of consecutive values. For instance, the binary string 100011100 has 4 distinct *runs*. What is the expected number of *runs* in the binary sequence a_1, a_2, \dots, a_{99} ?
4. You have a deck of $n > k$ cards, and you shuffle this deck by performing some finite number of k -swaps, where a k -swap consists of taking k cards at consecutive positions in the deck and placing the card that was originally the bottommost card among those k cards on the top of the $k - 1$ other cards. How many possible arrangements of the deck of n cards can you achieve?
5. For an ordered quadruple of integers (a, b, c, d) , define $f(0, 0, 0, 0) = 1$, $f(a, b, c, d) = f(a - 1, b, c, d) + f(a, b - 1, c, d) + f(a, b, c - 1, d) + f(a, b, c, d - 1)$ for all other nonnegative a, b, c, d , and $f(a, b, c, d) = 0$ if at least one of a, b, c, d are negative. For how many ordered quadruples of integers (a, b, c, d) such that $0 \leq a, b, c, d \leq 15$ is $f(a, b, c, d)$ odd?
6. The string $ABCDEFGHIJ$ is initially written on the board. Every iteration, one of the 10 letters in the string is uniformly randomly chosen, and this letter replaces an independently and uniformly random letter out of one of the 10 letters. What is the expected value for the number of iterations until $ABCDEFGHIJ$ becomes a 10-letter string of only one unique letter?

7. What is the least value of n such that for any sequence $a_1 < a_2 < \dots < a_n$ of distinct positive integers, we have that $\prod_{1 \leq i < j \leq n} (a_j - a_i)$ is divisible by 7^7 ?
8. Let $f_k(a, n) = \underbrace{a^a a^a \dots a^n}_{k \text{ a's}}$, and let $g(a)$ be the least positive integer k such that $f_k(a, n)$ is a constant function modulo $p = 65537$ in n , over all nonnegative integers n . Find $\max_{1 \leq a < 65537} g(a)$.
9. In a certain alien society living on the planet Zoumugn, there are two distinct races: Bazuworp and Trimazorp, and reproduction is sexual, except reproduction can be between any two aliens. It is given that a particular alien named Jejej, the fifth generation of his whole species, is exactly half-blooded Bazuworp and half-blooded Trimazorp. How many distinct family trees recording only direct ancestors of Jejej and exactly up to (and including) the generation 4 generations (the first generation of his whole species) before the subject are possible if Jejej is exactly half Bazuworp and half Trimazorp? Two family trees are considered identical if all members have the same proportion of Bazuworp blood in them. They are also considered identical if one is the gender flipped version of another, since all aliens are of the same gender.
10. Let $n = a_1 + a_2 + \dots + a_k$ be an ordered k -tuple of positive integers that sum to n . For all such (a_1, a_2, \dots, a_k) , define
- $$g(a_1, a_2, a_3, \dots, a_k) = \prod_{j=1}^{k-1} \binom{a_j + a_{j+1} - 2}{a_j - 1}$$
- if $k \geq 2$ and $g(a_1, a_2, \dots, a_k) = g(a_k) = g(a_1) = 1$ if $k = 1$.
- Let $F(n) = \sum_{\sum a_i \geq 1, k \geq 1, a_1 + a_2 + \dots + a_k = n} g(a_1, a_2, a_3, \dots, a_k)$. Find $\lim_{n \rightarrow \infty} \frac{F(n+1)}{F(n)}$.
11. Yvonne has 25 miniature houses, each of distinct dimensions in feet (i, j, k) , where $1 \leq i \leq j \leq k \leq 9$ are each integers. It is given that her 25 miniature houses can be arranged in an order H_1, H_2, \dots, H_{25} such that for each $1 \leq n < 25$, House H_n is fully contained inside House H_{n+1} . For any such set of 25 miniature houses $(H_1, H_2, \dots, H_{25})$ of distinct dimensions with those properties, let $M(H_1, H_2, \dots, H_{25})$ be the number of ways to arrange them such that (1) for each $1 \leq n < 25$, House H_n is fully contained inside House H_{n+1} and (2) for each miniature house, all of its edges are aligned with integer coordinates. Find the number of distinct possible values of $M(H_1, H_2, \dots, H_{25})$, assuming the coordinates of H_{25} are fixed. (Two arrangements are considered the same if in both arrangements, each of the 25 miniature houses H_1, H_2, \dots, H_{25} occupy pairwise the same space.)
12. Call a nonnegative rational number semi-dyadic if it can be expressed as

$$\frac{a}{2^b - 2^c}$$

where a , b , and c are nonnegative integers, and $b > c$. How many distinct semi dyadic numbers $\frac{m}{n}$ expressible in lowest terms $n < 2^{10}$ are there in the range $[0, 1]$?