

Lab-3

Task-4

BFS time complexity:

for adjacency list

Adjacency is a map of keys, where every ~~matrix~~ vertex is a key and points to a list of vertices which are incident from or adjacent to that key vertex.

In order to perform BFS, you have to put any vertex in queue and make it as ~~Q~~ visited, pop the queue to, pick the

Starting vertex, explore

all its adjacent vertices,
make them as visited
and put them all in
the queue and similarly
~~Pop the~~ similarly Pop
the queue [O] and explore
all the non-visited vertices
until the queue becomes empty.

For every vertex, you are
traversing through only
its adjacent non-visited
vertices (noting but edges)

So, the time complexity

visited = [] , queue [] $\rightarrow O(1)$

BFS (graph) : $O(V + E)$

$\left. \begin{array}{l} \text{---} \\ \text{---} \\ \text{---} \end{array} \right\} O(1)$

for vertices

While queue not empty: ~~do~~

$m \leftarrow \text{queue.pop}() \rightarrow O(1)$

Print(m)

Output = + --

If m = endpoint break

$\left. \begin{array}{l} O(1) \\ O(1) \\ O(1) \end{array} \right\} O(1)$

for each i of m in graph:

if i not visited

$\left. \begin{array}{l} \text{---} \\ \text{---} \end{array} \right\} O(E)$

for edges

Therefore, the time complexity

$$O(1) + \cancel{O(E)}$$

$$O(1) + O(c_1 V + c_2 E)$$

$$= O(V + E)$$

vertices

edges

for matrix:

In matrix representation,
for every vertex, you
have to traverse through
all the vertices and
check whether there is
a non-visited vertex.

since, for every vertex, we are traversing through all vertices,

the time complexity is, Θ

$$O(V^2)$$

DFS time complexity:

Adjacency list:

In worst case, DFS and BFS will give same time complexity in terms of adjacency list.

Since its a directed graph
its ^{edges} ~~vertices~~ will be

called once and ^{its} all
vertices will traverse
through.

hence, the time complexity
will be $O(V+E)$.

For matrix:

• An adjacency matrix is

• it is a $V \times V$ matrix

In worst case, the algorithm
will have to traverse
through entire $V \times V$ matrix.

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∴ the time complexity is

$$O(\cancel{v} \times v) = O(v^2)$$

Granny will get the victory
~~via~~ road first. Because,
ash have to go through
7 different cities from
the between source to
destination ^{city} or the other
hand, granny have to
go through 5 different
cities between source

to destination city,
 Although, BFS known
 as shortest path, in
 this case DFS's depth
 search ~~search~~ luckily found
 the destination city
 shortest. That is why Gary
 gets to the victory
 road first.

Ash:

1 → 2 → 3 → 4 → 5 → 7 → 11 → 6
 source → 12

Gary:

1 → 2 → 3 → 4 → 7 → 11 → 12
 source

destination