Chitramoy Mukherjee-DSC630-Week-08-Assignment 1

May 5, 2024

DSC-630-T302 Chitramoy Mukherjee Date : 05/01/2024 Week8 - Exercise 8.2 - Time Series Modeling

You will be using the dataset us_retail_sales.csv for this assignment. This data gives the total monthly retail sales in the US from January 1992 until June 2021. With this dataset, complete the following steps:

- * Plot the data with proper labeling and make some observations on the graph.
- st Split this data into a training and test set. Use the last year of data (July 2020 June 2021) of data as your

test set and the rest as your training set.

- * Use the training set to build a predictive model for the monthly retail sal
- * Use the model to predict the monthly retail sales on the last year of data.
- * Report the RMSE of the model predictions on the test set.

You can use R or Python to complete this assignment. Submit your code and output to the submission link. Make sure to add comments to all of your code and to document your steps, process, and analysis.

```
[9]: # import libraries
     import pandas as pd
     import numpy as np
     from numpy import sqrt
     import matplotlib.pyplot as plt
     import seaborn as sns
     from statsmodels.tsa.ar_model import AutoReg
     from statsmodels.tsa.statespace.sarimax import SARIMAX
     from sklearn.metrics import mean_squared_error
     from sklearn import metrics
     from datetime import datetime
     import warnings
     warnings.filterwarnings('ignore')
     from statsmodels.graphics.tsaplots import plot pacf
     from statsmodels.graphics.tsaplots import plot acf
     from statsmodels.tsa.holtwinters import ExponentialSmoothing
     from statsmodels.tsa.stattools import adfuller
     from tqdm import tqdm_notebook
     from itertools import product
     %matplotlib inline
```

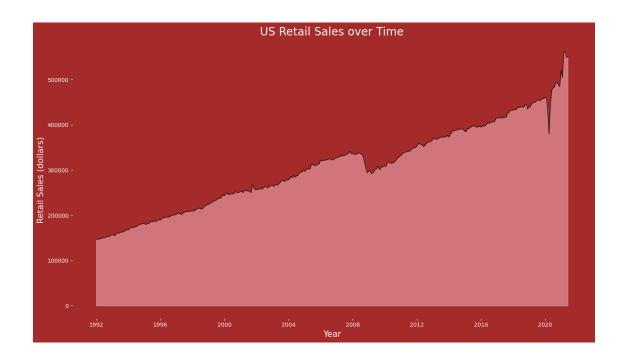
```
import statsmodels.api as sm
[10]: # Load the dataset
     df = pd.read_csv('C:

    \\Users\\Chitramoy\\Desktop\\MS-DSC\\DSC-630\\Week-8\\us_retail_sales.csv')
      # Preview the dataframe
     df.head(5)
[10]:
        YEAR
                 JAN
                         FEB
                                 MAR
                                         APR
                                                MAY
                                                        JUN
                                                                  JUL
                                                                            AUG \
     0 1992 146925 147223 146805 148032 149010 149800 150761.0 151067.0
     1 1993 157555 156266 154752 158979
                                             160605 160127 162816.0
                                                                      162506.0
     2 1994 167518 169649 172766 173106
                                             172329
                                                     174241 174781.0 177295.0
     3 1995 182413 179488 181013 181686
                                             183536 186081 185431.0 186806.0
     4 1996 189135 192266 194029 194744 196205 196136 196187.0 196218.0
             SEP
                       OCT
                                 NOV
                                          DEC
     0 152588.0 153521.0 153583.0 155614.0
     1 163258.0 164685.0 166594.0 168161.0
     2 178787.0 180561.0 180703.0 181524.0
     3 187366.0 186565.0 189055.0 190774.0
     4 198859.0 200509.0 200174.0 201284.0
[11]: #expand the dataframe
     df 2 = pd.melt(df, id vars=['YEAR'], var name="MONTH", value name="SALES")
      #convert months to numerical value
     df_2['Month'] = df_2['MONTH'].map({'JAN': 1, 'FEB': 2, 'MAR': 3, 'APR': 4, 'MAY':
      →5, 'JUN':6, 'JUL':7, 'AUG':8, 'SEP':9, 'OCT':10, 'NOV':11, 'DEC':12})
      #create year-month-date conversion
     df_2['DATE']=pd.to_datetime(df_2[['YEAR', 'Month']].assign(DAY=1))
      # create dataframe with only needed columns
     df_new = df_2[['DATE', 'SALES']].sort_values('DATE')
     df new = df new.dropna()
      # preview new dataframe
     df new.head(10)
[11]:
               DATE
                        SALES
         1992-01-01 146925.0
     30 1992-02-01 147223.0
     60 1992-03-01 146805.0
     90 1992-04-01 148032.0
     120 1992-05-01 149010.0
     150 1992-06-01 149800.0
     180 1992-07-01 150761.0
     210 1992-08-01 151067.0
     240 1992-09-01 152588.0
     270 1992-10-01 153521.0
```

```
[12]: # Check the shape of the dataframe. 354 records and 2 columns
      df_new.shape
[12]: (354, 2)
[14]: # Checking the dtypes of the variables
      df_new.info()
     <class 'pandas.core.frame.DataFrame'>
     Index: 354 entries, 0 to 179
     Data columns (total 2 columns):
          Column Non-Null Count Dtype
          DATE
                  354 non-null
                                  datetime64[ns]
      0
          SALES
                  354 non-null
                                  float64
      1
     dtypes: datetime64[ns](1), float64(1)
     memory usage: 8.3 KB
```

0.1 Plot the data with proper labeling and make some observations on the graph.

```
[15]: #create an area chart to show Sales vs Date
fig = plt.figure(figsize=(14,8), facecolor='brown')
plt.plot(df_new['DATE'], df_new['SALES'], linewidth=1, color='black')
plt.fill_between(df_new['DATE'], df_new['SALES'], color='pink', alpha=0.5)
plt.box(False)
plt.title('US Retail Sales over Time', fontsize=20, color='white')
plt.xlabel('Year', color='white', fontsize=15)
plt.ylabel('Retail Sales (dollars) ', color='white', fontsize=15)
plt.tick_params(axis='x', colors='white')
plt.tick_params(axis='y', colors='white')
plt.tight_layout()
plt.show()
```

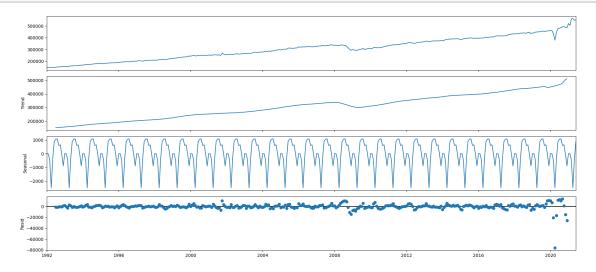


Clearly, the time series is not stationary, as its mean is not constant through time, and we see an increasing variance in the data, a sign of heteroscedasticity. The graph depicts a steady increase in retail revenue each year with an exception of 2008 and 2020. During the years of 2007 to 2009, the economy was entering a downturn due to the great recession due to lax lending in the mortgage housing market. In the year of 2020, the Covid-19 Pandemic slowed spending for many due to being in various lockdown situations. Definitely have upward sales trend.

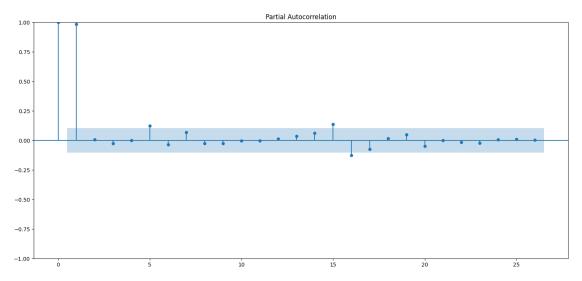
```
[16]: #set the date as the index
      df_new.set_index("DATE",inplace=True)
[17]: df_new.tail()
      #### Analyzing the chart, I can observe that the time-series has seasonality_
       ⇒pattern. There is an upward trend over the years as well.
[17]:
                     SALES
     DATE
      2021-02-01 504458.0
      2021-03-01 559871.0
      2021-04-01 562269.0
      2021-05-01 548987.0
      2021-06-01 550782.0
[18]: from pylab import rcParams
      rcParams['figure.figsize'] = 18, 8
      decomposition = sm.tsa.seasonal_decompose(df_new, model='additive')
      fig = decomposition.plot()
      plt.show()
```

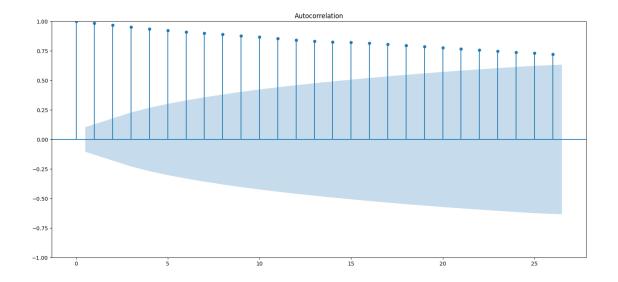
Using the "sm.tsa.seasonal_decompose" command from the pylab library I can decompose the time-series into three distinct components: trend,

seasonality, and noise. I can see upward sales trend over the year and also \Box \Rightarrow seasonality effect yearly by looking at the plot above.









```
[20]: # Again, no information can be deduced from those plots. I can further test for stationarity with the Augmented
# Dickey-Fuller test:
ad_fuller_result = adfuller(df_new['SALES'])
print(f'ADF Statistic: {ad_fuller_result[0]}')
print(f'p-value: {ad_fuller_result[1]}')
```

ADF Statistic: 1.4490526692726289 p-value: 0.9973259755033455

```
[21]: # Now, let's take the differencing in an effort to make it stationary:
    data = df_new.copy()
    data['Sales First Differencing'] = data['SALES'] - data['SALES'].shift(1)
    data['Seasonal First Differencing'] = data['SALES'] - data['SALES'].shift(12)
    data.head()
```

```
[21]:
                     SALES Sales First Differencing Seasonal First Differencing
     DATE
      1992-01-01 146925.0
                                                 NaN
                                                                              NaN
      1992-02-01 147223.0
                                               298.0
                                                                              NaN
      1992-03-01 146805.0
                                              -418.0
                                                                              NaN
      1992-04-01 148032.0
                                              1227.0
                                                                              NaN
      1992-05-01 149010.0
                                               978.0
                                                                              NaN
```

```
[22]: # Dickey-Fuller test:
    ad_fuller_result = adfuller(data['Seasonal First Differencing'].dropna())
    print(f'ADF Statistic: {ad_fuller_result[0]}')
    print(f'p-value: {ad_fuller_result[1]}')
```

ADF Statistic: -2.2393804106097703 p-value: 0.1922642410718154

```
[23]: # Dickey-Fuller test:
      ad fuller result = adfuller(data['Sales First Differencing'].dropna())
      print(f'ADF Statistic: {ad_fuller_result[0]}')
      print(f'p-value: {ad_fuller_result[1]}')
     ADF Statistic: -2.7280371246391555
     p-value: 0.06931100597169161
     0.1.1 Split this data into a training and test set. Use the last year of data (July 2020
           - June 2021) of data as your test set and the rest as your training set.
[24]: # build the train, test set
      train, test = df_new[df_new.index < '2020-07-01'], df_new[df_new.index >=_
       train.head()
[24]:
                     SALES
     DATE
      1992-01-01 146925.0
      1992-02-01 147223.0
      1992-03-01 146805.0
      1992-04-01 148032.0
      1992-05-01 149010.0
[19]: test.head()
[19]:
                     SALES
     DATE
      2020-07-01 481627.0
      2020-08-01 483716.0
      2020-09-01 493327.0
      2020-10-01 493991.0
      2020-11-01 488652.0
     0.1.2 Use the training set to build a predictive model for the monthly retail sales.
[25]: #Instantiate and fit the AR model with training data
      ar_model = AutoReg(train, lags=3).fit()
      #print summary
      print(ar_model.summary())
                                 AutoReg Model Results
     Dep. Variable:
                                     SALES
                                             No. Observations:
                                                                                 342
     Model:
                                AutoReg(3)
                                             Log Likelihood
                                                                           -3396.835
```

AIC

S.D. of innovations

5438.308

6803.670

Conditional MLE

Sun, 05 May 2024

Method:

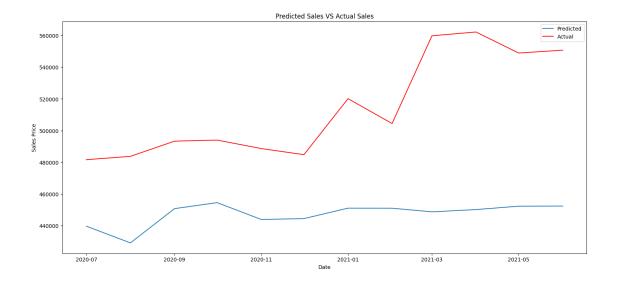
Date:

Time: Sample:		17:12 04-01-1 - 06-01-2	.992 HQIC			6822.800 6811.293
	coef	std err	z	P> z	[0.025	0.975]
const	2087.5148	1076.084	1.940	0.052	-21.572	4196.601
SALES.L1	0.8672	0.054	15.942	0.000	0.761	0.974
SALES.L2	-0.3893	0.076	-5.129	0.000	-0.538	-0.241
SALES.L3	0.5199	0.069	7.526	0.000	0.385	0.655
			Roots			
========	Real	Imaginary		Modulus		Frequency
AR.1	1.0013	-0.0000j		1.0013		-0.0000
AR.2	-0.1263	_	·1.3802j	1.3860		-0.2645
AR.3	-0.1263	+	·1.3802j	1.38	360	0.2645

0.1.3 Use the model to predict the monthly retail sales on the last year of data.

```
[26]: # Make the predictions
    pred = ar_model.predict(start=len(train), end=(len(df_new)-1), dynamic=False)
    # Plot the prediction vs test data
    from matplotlib import pyplot
    pyplot.plot(pred, label='Predicted')
    pyplot.plot(test, color='red', label='Actual')
    plt.title("Predicted Sales VS Actual Sales")
    plt.xlabel("Date")
    plt.ylabel("Sales Price")
    plt.legend()
```

[26]: <matplotlib.legend.Legend at 0x2364e293a40>



0.1.4 Report the RMSE of the model predictions on the test set.

```
[27]: # Find the square root of the mean of test sales value minus the predict test

→ sales values

rmse = sqrt(mean_squared_error(test, pred))

print('Test RMSE is %.3f' % rmse)
```

Test RMSE is 72691.589

Summary The unusual high RMSE value signifies that the autoregressive model is not optimal for this exercise. The important value is an indication of how close the predictions are to the actual values. Lower values of RMSE indicate a better fit. RMSE is a worthy measure of how accurately the model predicts the response. It can be the most important criterion for fit if the main purpose of the model is prediction. An explanation for the gap in prediction and actual could be that there was an unusual spike in sales during the period of prediction time frame.

0.1.5 Moving Average Model

```
df new['lag1'] = df new['SALES'].shift(1)
      df_new['Resid'] = df_new['SALES'] - df_new['lag1']
      df_new.reset_index(inplace=True)
[31]:
      df_new.head()
[31]:
              DATE
                        SALES
                                   lag1
                                           Resid
      0 1992-01-01
                     146925.0
                                     NaN
                                             NaN
      1 1992-02-01
                     147223.0
                               146925.0
                                           298.0
      2 1992-03-01
                     146805.0
                               147223.0
                                          -418.0
```

```
4 1992-05-01 149010.0 148032.0 978.0
[32]: train, test = df_new.Resid[df_new.DATE < '2020-07-01'], df_new.Resid[df_new.
     ⇔DATE >= '2020-07-01']
    train
[32]: 0
             NaN
    1
          298.0
    2
          -418.0
    3
          1227.0
          978.0
    337
          -976.0
    338
        -25329.0
    339
        -54389.0
    340
          64739.0
    341
          31712.0
    Name: Resid, Length: 342, dtype: float64
[34]: #Instantiate and fit the AR model with training data
    ar_model = AutoReg(train.iloc[1:], lags=3).fit()
[35]: #print summary
    print(ar_model.summary())
                          AutoReg Model Results
    ______
    Dep. Variable:
                             Resid No. Observations:
                                                               341
    Model:
                         AutoReg(3) Log Likelihood
                                                         -3386.071
    Method:
                    Conditional MLE S.D. of innovations
                                                           5426.349
    Date:
                    Sun, 05 May 2024 AIC
                                                           6782.141
                           17:13:04 BIC
    Time:
                                                           6801.256
                                   HQIC
    Sample:
                                3
                                                           6789.759
                               341
    ______
                                z P>|z|
                                                  [0.025
                       std err
      ______
                                                 960.244
            1577.0546 314.705
                                 5.011
                                         0.000
                                                           2193.865
    const

      0.055
      -2.680
      0.007

      0.071
      -6.975
      0.000

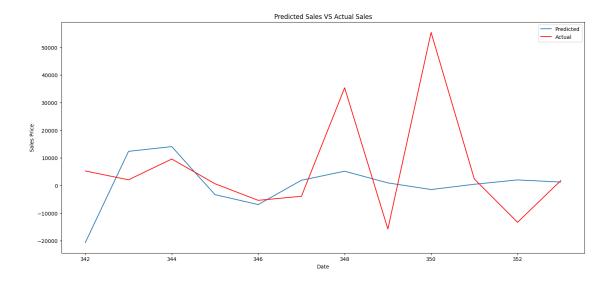
      0.095
      -1.699
      0.089

    Resid.L1
              -0.1476
                                                   -0.256
                                                            -0.040
                                                  -0.630
    Resid.L2
               -0.4918
                                                             -0.354
                       0.095
    Resid.L3
              -0.1612
                                                  -0.347
                                                             0.025
                                Roots
    ______
                            Imaginary
                                             Modulus
    AR.1
                0.1417
                             -1.3566j
                                             1.3639
                                                           -0.2334
                0.1417 +1.3566j 1.3639
    AR.2
                                                           0.2334
```

3 1992-04-01 148032.0 146805.0 1227.0

AR.3 -3.3338 -0.0000j 3.3338 -0.5000

[151]: # Make the predictions
pred = ar_model.predict(start=len(train), end=(len(df_new)-1), dynamic=False)
Plot the prediction vs test data
from matplotlib import pyplot
pyplot.plot(pred, label='Predicted')
pyplot.plot(test, color='red', label='Actual')
plt.title("Predicted Sales VS Actual Sales")
plt.xlabel("Date")
plt.ylabel("Sales Price")



```
[36]: # Find the square root of the mean of test sales value minus the predict test

→ sales values

rmse = sqrt(mean_squared_error(test, pred))

print('Test RMSE is %.3f' % rmse)
```

Test RMSE is 441541.556

plt.legend()
plt.show()

Summary With Moving Average Model, RMSE errors are reduced significantly. Since I used reseduals to predict future sales get some advantages.

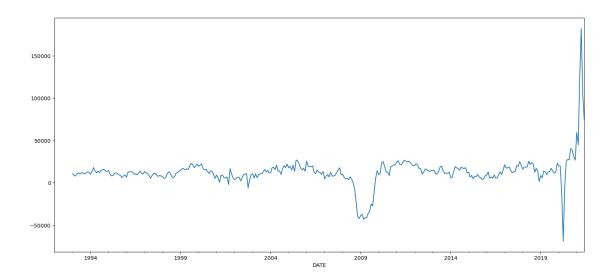
0.1.6 ARIMA model:

```
[37]: df_arima = df_new.copy() df_arima.head()
```

```
[37]:
              DATE
                       SALES
                                         Resid
                                  lag1
     0 1992-01-01 146925.0
                                   {\tt NaN}
                                           NaN
      1 1992-02-01 147223.0 146925.0
                                         298.0
      2 1992-03-01 146805.0 147223.0 -418.0
      3 1992-04-01 148032.0 146805.0 1227.0
      4 1992-05-01 149010.0 148032.0
                                         978.0
[38]: ### Testing For Stationarity
      from statsmodels.tsa.stattools import adfuller
[39]: test_result=adfuller(df_arima['SALES'])
[40]: def adfuller test(sales):
           result=adfuller(sales)
           labels = ['ADF Test Statistic', 'p-value', '#Lags Used', 'Number of
       ⇔Observations Used']
           for value, label in zip(result, labels):
               print(label+' : '+str(value) )
           if result[1] <= 0.05:</pre>
               print("strong evidence against the null hypothesis(Ho), reject the⊔
       onull hypothesis. Data has no unit root and is stationary")
           else:
               print("weak evidence against null hypothesis, time series has a unit⊔
       →root, indicating it is non-stationary ")
[41]: adfuller_test(df_arima['SALES'])
     ADF Test Statistic: 1.4490526692726289
     p-value: 0.9973259755033455
     #Lags Used : 12
     Number of Observations Used: 341
     weak evidence against null hypothesis, time series has a unit root, indicating
     it is non-stationary
[43]: # Differencinng
      df_arima['Sales First Difference'] = df_arima['SALES'] - df_arima['SALES'].
       ⇒shift(1)
[44]: df_arima['Seasonal First Difference']=df_arima['SALES']-df_arima['SALES'].
       ⇒shift(12)
[45]: df_arima.head(13)
[45]:
               DATE
                        SALES
                                          Resid Sales First Difference \
                                   lag1
      0 1992-01-01 146925.0
                                    {\tt NaN}
                                            {\tt NaN}
                                                                    NaN
                                                                  298.0
      1 1992-02-01 147223.0 146925.0
                                          298.0
      2 1992-03-01 146805.0 147223.0 -418.0
                                                                 -418.0
      3 1992-04-01 148032.0 146805.0 1227.0
                                                                 1227.0
```

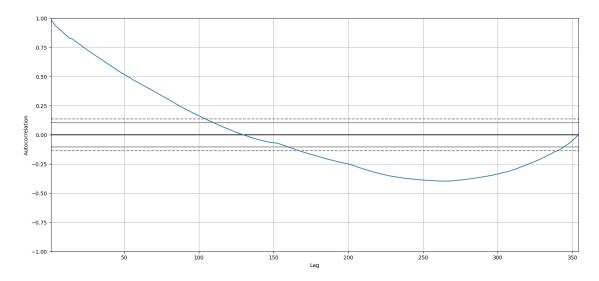
```
4 1992-05-01 149010.0 148032.0
                                          978.0
                                                                  978.0
                                          790.0
                                                                  790.0
      5 1992-06-01 149800.0 149010.0
      6 1992-07-01 150761.0 149800.0
                                          961.0
                                                                  961.0
      7 1992-08-01 151067.0 150761.0
                                           306.0
                                                                  306.0
      8 1992-09-01 152588.0 151067.0 1521.0
                                                                  1521.0
      9 1992-10-01
                     153521.0 152588.0
                                          933.0
                                                                  933.0
      10 1992-11-01 153583.0 153521.0
                                            62.0
                                                                   62.0
      11 1992-12-01 155614.0 153583.0
                                                                 2031.0
                                         2031.0
      12 1993-01-01 157555.0 155614.0 1941.0
                                                                  1941.0
          Seasonal First Difference
      0
                                NaN
                                NaN
      1
      2
                                NaN
      3
                                NaN
      4
                                NaN
      5
                                NaN
      6
                                NaN
      7
                                NaN
      8
                                NaN
      9
                                NaN
      10
                                NaN
      11
                                NaN
                            10630.0
      12
[165]: ## Again test dickey fuller test
      adfuller_test(df_arima['Seasonal First Difference'].dropna())
      ADF Test Statistic : -2.2393804106097703
      p-value : 0.1922642410718154
      #Lags Used : 16
      Number of Observations Used: 325
      weak evidence against null hypothesis, time series has a unit root, indicating
      it is non-stationary
[46]: df_arima.set_index("DATE")['Seasonal First Difference'].plot()
```

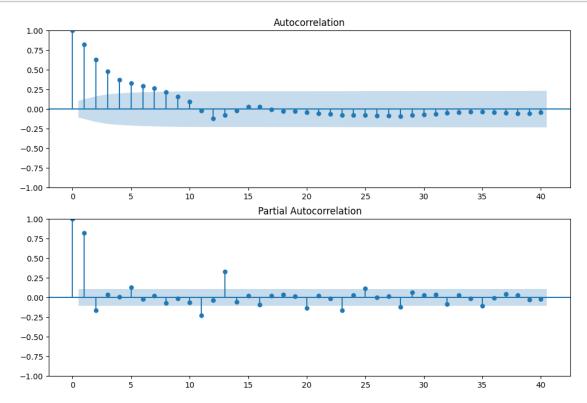
[46]: <Axes: xlabel='DATE'>



```
[46]: # Auto correlation Plot
from pandas.plotting import autocorrelation_plot
autocorrelation_plot(df_arima['SALES'])
```

[46]: <Axes: xlabel='Lag', ylabel='Autocorrelation'>





```
[49]: # For non-seasonal data
    #p=8, d=1, q=0 or 1
    from statsmodels.tsa.arima.model import ARIMA

[50]: df_arima = df_arima.set_index("DATE")

[57]: train, test = df_arima[df_arima.index < '2020-07-01'], df_arima[df_arima.index_u <> '2020-07-01'], df_arima[df_arima.index_u
```

Dep. Var	riable:	SALE	S	No. Obse	ervations:	342
Model:		ARIMA(8	, 1, 1)	Log Likel	ihood	-3436.232
Date:		Sun, 05 Ma	y 2024	AIC		6892.464
Time:		17:14:4	14	BIC		6930.782
Sample:		01-01-19	992	\mathbf{HQIC}		6907.730
		- 06-01-2	2020			
Covarian	ce Type:	opg				
	coef	std err	${f z}$	$\mathbf{P} > \mathbf{z} $	[0.025]	0.975]
ar.L1	0.9662	0.019	49.870	0.000	0.928	1.004
ar.L2	-0.0954	0.018	-5.198	0.000	-0.131	-0.059
ar.L3	0.0867	0.044	1.961	0.050	4.2e-05	0.173
ar.L4	0.0405	0.186	0.218	0.828	-0.324	0.405
ar.L5	-0.0080	0.238	-0.034	0.973	-0.474	0.458
ar.L6	0.0244	0.145	0.169	0.866	-0.259	0.308
ar.L7	-0.0067	0.115	-0.059	0.953	-0.233	0.219
ar.L8	-0.0077	0.087	-0.088	0.930	-0.179	0.164
ma.L1	-0.9991	0.028	-36.223	0.000	-1.053	-0.945
$\mathbf{sigma2}$	3.089e + 07	1.79e-08	1.73e + 1	5 0.000	3.09e + 07	3.09e + 07
Ljung	Ljung-Box (L1) (Q): 0.17 Jarque-Bera (JB): 49619.23					
$\operatorname{Prob}($	Q):	(0.68 P	rob(JB):		0.00
Heteroskedasticity (H):			4.81 S	kew:		0.28
Prob(H) (two-sid	led): (0.00 K	urtosis:		62.09

Warnings:

- [1] Covariance matrix calculated using the outer product of gradients (complex-step).
- [2] Covariance matrix is singular or near-singular, with condition number 6.69e+30. Standard errors may be unstable.

[54]:	DATE	SALES	lag1	Resid	Sales First Difference	\
	DATE	404407 0	474040	F004 0	5004.0	
	2020-07-01	481627.0	476343.0	5284.0	5284.0	
	2020-08-01	483716.0	481627.0	2089.0	2089.0	
	2020-09-01	493327.0	483716.0	9611.0	9611.0	
	2020-10-01	493991.0	493327.0	664.0	664.0	
	2020-11-01	488652.0	493991.0	-5339.0	-5339.0	
	2020-12-01	484782.0	488652.0	-3870.0	-3870.0	
	2021-01-01	520162.0	484782.0	35380.0	35380.0	
	2021-02-01	504458.0	520162.0	-15704.0	-15704.0	
	2021-03-01	559871.0	504458.0	55413.0	55413.0	
	2021-04-01	562269.0	559871.0	2398.0	2398.0	
	2021-05-01	548987.0	562269.0	-13282.0	-13282.0	
	2021-06-01	550782.0	548987.0	1795.0	1795.0	

Seasonal First Difference

DATE

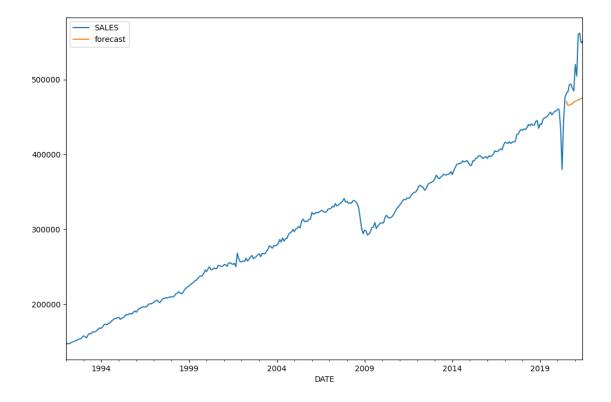
```
2020-07-01
                               27615.0
2020-08-01
                               27216.0
2020-09-01
                               40478.0
2020-10-01
                               38505.0
2020-11-01
                               30994.0
2020-12-01
                               26727.0
2021-01-01
                               59576.0
2021-02-01
                               44848.0
2021-03-01
                              125590.0
2021-04-01
                              182377.0
2021-05-01
                              104356.0
2021-06-01
                               74439.0
```

```
[59]: df_arima['forecast']=model_fit.

opredict(start='2020-07-01',end='2021-06-01',dynamic=True)

df_arima[['SALES','forecast']].plot(figsize=(12,8))
```

[59]: <Axes: xlabel='DATE'>



```
2020-07-01
            481627.0
                       476343.0
                                   5284.0
                                                             5284.0
                                   2089.0
2020-08-01
            483716.0
                       481627.0
                                                             2089.0
2020-09-01
            493327.0
                       483716.0
                                   9611.0
                                                             9611.0
2020-10-01
            493991.0
                       493327.0
                                    664.0
                                                              664.0
2020-11-01
            488652.0
                       493991.0
                                  -5339.0
                                                            -5339.0
2020-12-01
            484782.0
                       488652.0
                                  -3870.0
                                                            -3870.0
2021-01-01
            520162.0
                       484782.0
                                  35380.0
                                                            35380.0
2021-02-01
            504458.0
                       520162.0 -15704.0
                                                           -15704.0
2021-03-01
                       504458.0
                                  55413.0
                                                            55413.0
            559871.0
2021-04-01
            562269.0
                       559871.0
                                   2398.0
                                                             2398.0
2021-05-01
            548987.0
                       562269.0 -13282.0
                                                           -13282.0
2021-06-01
            550782.0
                       548987.0
                                   1795.0
                                                             1795.0
            Seasonal First Difference
                                               forecast
DATE
2020-07-01
                                27615.0
                                         470465.117037
2020-08-01
                                27216.0
                                          465331.907771
2020-09-01
                                40478.0
                                         466105.147904
2020-10-01
                                38505.0
                                         466443.805832
2020-11-01
                                30994.0
                                         467904.230481
2020-12-01
                                26727.0
                                         469946.603227
2021-01-01
                                59576.0
                                         471026.856631
                                         471680.073761
2021-02-01
                                44848.0
2021-03-01
                               125590.0
                                         472540.337572
2021-04-01
                               182377.0
                                         473516.319557
2021-05-01
                               104356.0
                                          474488.665292
2021-06-01
                                74439.0
                                         475464.865171
```

Conclusion: The unusual high RMSE value signifies that the autoregressive model is not optimal for this exercise. The important value is an indication of how close the predictions are to the actual values. Lower values of RMSE indicate a better fit. RMSE is a worthy measure of how accurately the model predicts the response. It can be the most important criterion for fit if the main purpose of the model is prediction. An explanation for the gap in prediction and actual could be that there was an unusual spike in sales during the period of prediction time frame. With Moving Average Model, RMSE errors are reduced significantly. Since I used reseduals to predict future sales get some advantages. ARIMA model doesn't consider seasanility causing the prediction is not good but SARIMA model can predict the sales more accurately because of the season consideration but the SARIMA model code execusion didn't gave any output because of that I couldn't compared the SARIMA output with other model output.

 $\label{lem:model} model = sm.tsa.statespace. SARIMAX (train.SALES, order = (8, 1, 1), seasonal_order = (8,1,1,12)) \\ results = model. fit() \\ df_arima[`forecast'] = results.predict(start = `2020-07-01', end = `2021-06-01', dynamic = True) \\ df_arima[[`SALES', `forecast']].plot(figsize = (12,8)) \\$