



## Department of Electronics & Telecommunication

CLASS : T. E. (E &TC)

SUBJECT : DC

EXPT. NO. : 9

DATE:

Roll NO. :32457

TITLE : Generation and reception of FSK in presence of noise

### PREREQUISITES

- FOR EXPT.** : 1. Different Line coding techniques  
2. Concept of ASK (amplitude shift keying)  
3. Concept of matched filter

- OBJECTIVE** : 1. To study the blocks in BFSK transmitter and receiver.  
2. To study the power spectrum of BFSK briefly.  
3. To understand difference between coherent and non coherent BFSK reception technique.

**APPARATUS** :

Sr. No.	Apparatus	Range
1.	FSK MOD /DEMOD kit	
2.	DSO	Dual Channel, 60 MHz

**THEORY** :

- In binary frequency shift keying (BFSK), the frequency of a sinusoidal carrier is shifted between two discrete values.
- One of these frequencies ( $f_H$ ) represents a binary “1” and other value ( $f_L$ ) represents a binary “0”.
- The representation of digital data using FSK is as shown in fig.1. Note that there’s no change in the amplitude and phase of the carrier.



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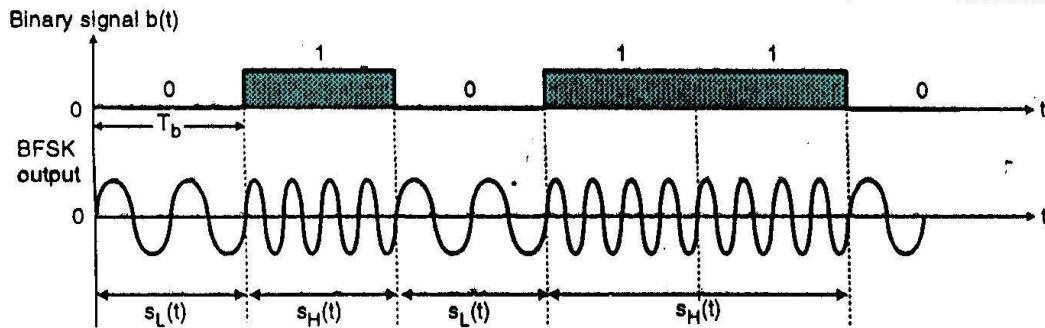


Fig.1 : Representation of digital signal using BFSK

- In BFSK the binary data waveform  $d(t)$  is used to generate a binary signal,

$$V_{BFSK}(t) = \sqrt{2P_s} \cos[\omega_c t + d(t)\Omega t] \quad 1$$

Where  $d(t)=\pm 1$  corresponding to the logic levels 1 and 0 at the input respectively.

- The transmitted BFSK signal is of constant amplitude  $\sqrt{2P_s}$  and is given by  
 $s_H(t) = v_{BFSK}(t) = \sqrt{2P_s} \cos[\omega_c + \Omega]t$  .....for logic "1" level input  
 $s_L(t) = v_{BFSK}(t) = \sqrt{2P_s} \cos[\omega_c - \Omega]t$  .....for logic "0" level input

If we call  $(\omega_c + \Omega) = \omega_H$  and  $(\omega_c - \Omega) = \omega_L$  then the above equations will be modified as

$$s_H(t) = \sqrt{2P_s} \cos \omega_H t \quad 2$$

$$\text{and} \quad s_L(t) = \sqrt{2P_s} \cos \omega_L t \quad 3$$

- As already mentioned,  $P_s = E_b/T_b$

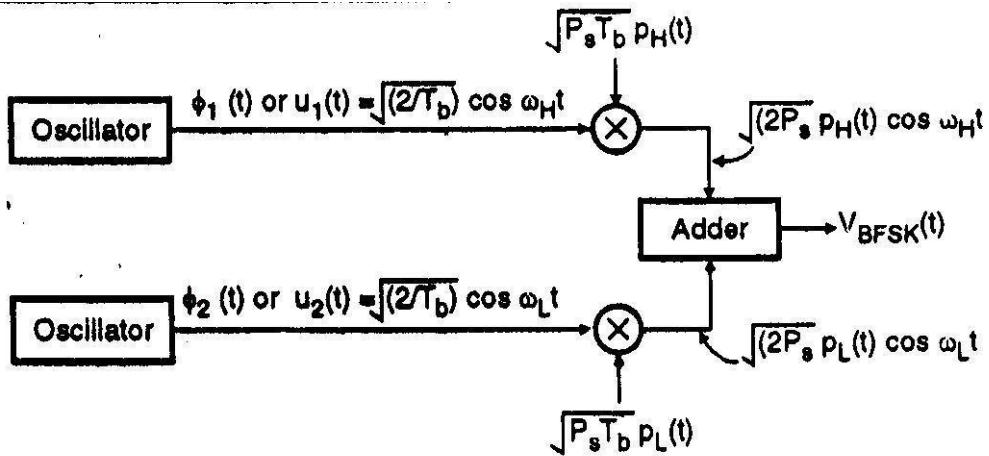
$$\text{therefore,} \quad s_H(t) = \sqrt{(2 E_b / T_b)} \cos \omega_H t \quad 4$$

$$\text{and} \quad s_L(t) = \sqrt{(2 E_b / T_b)} \cos \omega_L t \quad 5$$

### Generation of BFSK:

- The block diagram of BFSK generator is shown in fig 2. It consists of two oscillators, which produce carriers at frequencies  $f_H$  and  $f_L$  respectively.

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**Fig.2 : BFSK generation**

- The oscillator outputs are applied to the inputs of the multipliers (balance modulator). The other input to the two multipliers are the signals  $p_H(t)$  and  $p_L(t)$ .
- These signals are derived from the data bits  $d(t)$  as follows:

Data bit to be transmitted	Value of $d(t)$	$p_H(t)$	$p_L(t)$
Binary 0	-1V	0	1
Binary 1	+1V	1	0

- The other inputs to the two multipliers are the reference signals  $u_1(t)$  or  $\varphi_1(t)$  and  $u_2(t)$  or  $\varphi_2(t)$  which are generated by two oscillators  $u_1(t)=\varphi_1(t)=$

$$\sqrt{(2/T_b)} \cos \omega_H t \quad 6$$

$$u_2(t)=\varphi_2(t)=\sqrt{(2/T_b)} \cos \omega_L t \quad 7$$

- The multiplier outputs are then added to get the BFSK signal, given by equation 1
- Thus when binary 0 is to be transmitted,  $p_L(t)=1$  and  $p_H(t)=0$  and for a binary “1” to be transmitted  $p_H(t)=1$  and  $p_L(t)=0$ .
- Hence the transmitted frequency will have a frequency either  $f_H$  or  $f_L$ .

### Spectrum of BFSK:

- The BFSK output in terms of the variables  $p_H(t)$  and  $p_L(t)$  is given by,

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$$V_{BFSK}(t) = \sqrt{2P_s} p_H \cos[\omega_H t + \theta_H] + \sqrt{2P_s} p_L \cos[\omega_L t + \theta_L] \dots$$

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- ii. Each term in equation 8 looks like the signal  $\sqrt{2P_s} b(t) \cos\omega_C t$  which we have used in BPSK. The difference is that in BPSK, the signal  $b(t)$  is bipolar which alternates between +1 and -1. In BFSK the two signals  $p_H(t)$  and  $p_L(t)$  are alternating between 0 and +1 only.
- iii. So now let us write  $p_H$  and  $p_L$  in the form of sums of a constant and a bipolar variable as follows:

$$p_H(t) = \frac{1}{2} + \frac{1}{2} p'_H(t) \dots$$

9

$$p_L(t) = \frac{1}{2} + \frac{1}{2} p'_L(t) \dots$$

10

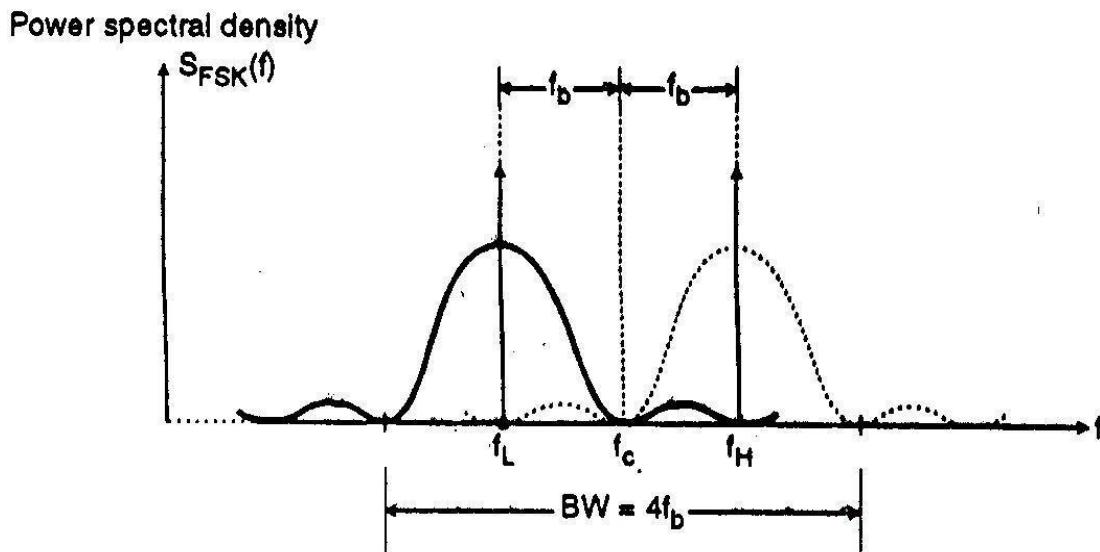
where  $p'_H(t)$  and  $p'_L(t)$  are bipolar variables, which alternate between +1 and -1. Also they are complementary signals i.e when  $p'_H=1$ ,  $p'_L=-1$  and vice versa.

- iv. Substituting the values of  $p_H(t)$  and  $p_L(t)$  from equations 9 and 10 into the expression for BFSK equation 8 we get,

$$v_{BFSK}(t) = \sqrt{P_s/2} \cos[\omega_H(t) + \theta_H] + \sqrt{P_s/2} \cos[\omega_L(t) + \theta_L] + \sqrt{P_s/2} \omega'_H \cos[\omega_H(t) + \theta_H] + \sqrt{P_s/2} \omega'_L \cos[\omega_H(t) + \theta_H]$$

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This expression will help us draw the spectrum of BFSK.



**Fig.3 : Spectrum of BFSK**



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- v. The first term in the expression 11 will produce a power spectral density, which consists of an impulse at  $f_H$ .
- Similarly the second term produces a power spectral density which consists of an impulse at  $f_L$
  - The third and fourth terms in the equation 11 together will produce the spectrum of a BFSK.
  - The individual power spectral density patterns of the last two terms in equation 11 are shown in fig 3.
  - Note that these patterns have been drawn with an assumption that  $f_H - f_L = 2f_b$
  - With this separation, the bandwidth of BFSK is,

$$BW(BFSK) = 4f_b$$

Note that this bandwidth is twice the bandwidth of BPSK.

### BFSK Reciever(coherent receiver):

- The BFSK receiver block diagram is as shown in fig 4. It is supposed to regenerate the original digital data form the BFSK signal at its input.
- The received BFSK signal is denoted by  $x(t)$ . It is applied to two correlators.
- These correlators are supplied with locally generated coherent reference signals  $\Phi_1$  (or  $u_1$ ) and  $\Phi_2$ (or  $u_2$ ).

$$\Phi_1(t) \text{ or } u_1(t) = \sqrt{(2/T_b)} \cos \omega_H t \quad 12$$

$$U_2(t) = \Phi_2(t) = \sqrt{(2/T_b)} \cos \omega_L t \quad 13$$

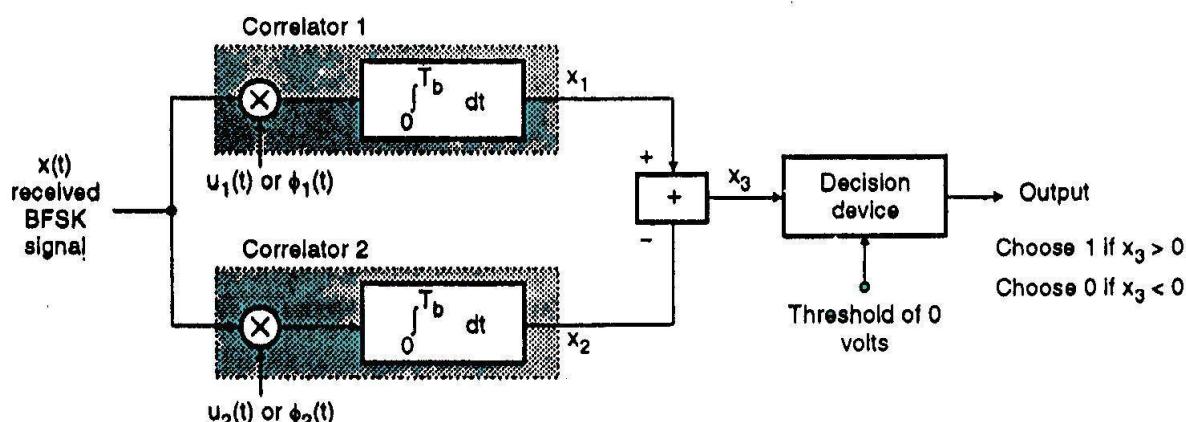


Fig. 4 : Coherent BFSK receiver



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- The outputs of the two correlators are then subtracted to get a signal  $x_3$  such that,  
$$x_3 = x_1 - x_2$$
- The signal  $x_3$  is then applied to a decision device which compares it with a threshold level of zero volts.
- If  $x_3 > 0$ , then the receiver decides that a 1 was transmitted whereas if  $x_3 < 0$  then a decision is made in favour of a zero.

### **Non coherent Binary Modulation Techniques :**

- Till now we have discussed the coherent modulation techniques in which the phase synchronous locally generated carrier was used for the purpose of detection.
- But practically sometimes it is not possible to have the knowledge of the carrier phase.
- Then we have to use the coherent binary systems.
- In this section we will consider the non coherent FSK system and the differential PSK or DPSK systems.

### **Non coherent BPSK :**

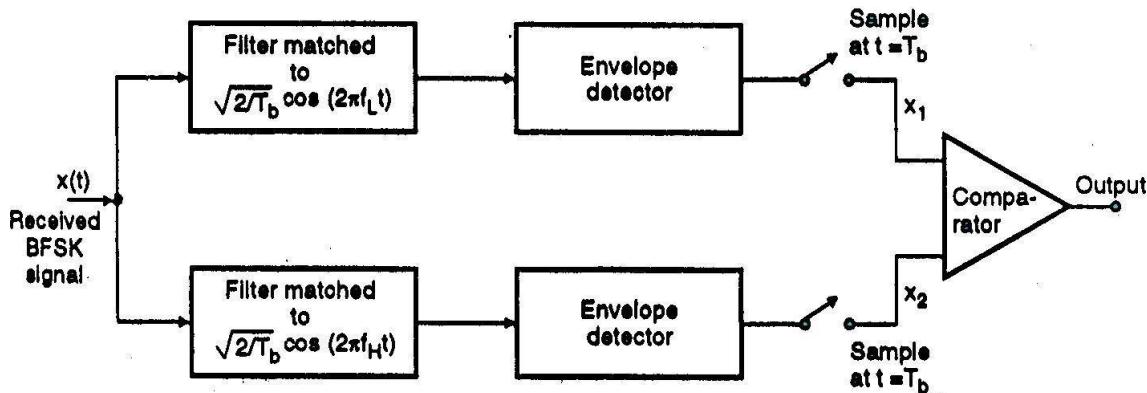
- In the binary FSK system, we know that the transmitted signal can be either  $s_H(t)$  and  $s_L(t)$  are given by,

$$s_H(t) = \sqrt{2 E_b / T_b} \cos(2\pi f_H t) \quad 14$$

$$s_L(t) = \sqrt{2 E_b / T_b} \cos(2\pi f_L t) \quad 15$$

- The transmission frequency  $f_H$  represents a logic 1 and  $f_L$  represents a logic 0.
- The non coherent receiver of BPSK is shown in fig 5.
- A pair of matched filters alongwith envelope detectors is being used.
- The matched filter in the upper path is matched to  $\sqrt{2/T_b} \cos(2\pi f_L t)$  whereas the filter in the lower path is matched to  $\sqrt{2/T_b} \cos(2\pi f_H t)$ .

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**Fig. 5 : Noncoherent BFSK receiver**

- The outputs of the envelope detector are sampled at  $t = T_b$  and a comparator is used for comparing their values  $x_1$  and  $x_2$ .
- If  $x_1 > x_2$  then the receiver decides that a logic 1 was transmitted whereas with  $x_1 < x_2$  the receiver's decision is in favour of a 0.
- The error probability of non coherent BFSK is

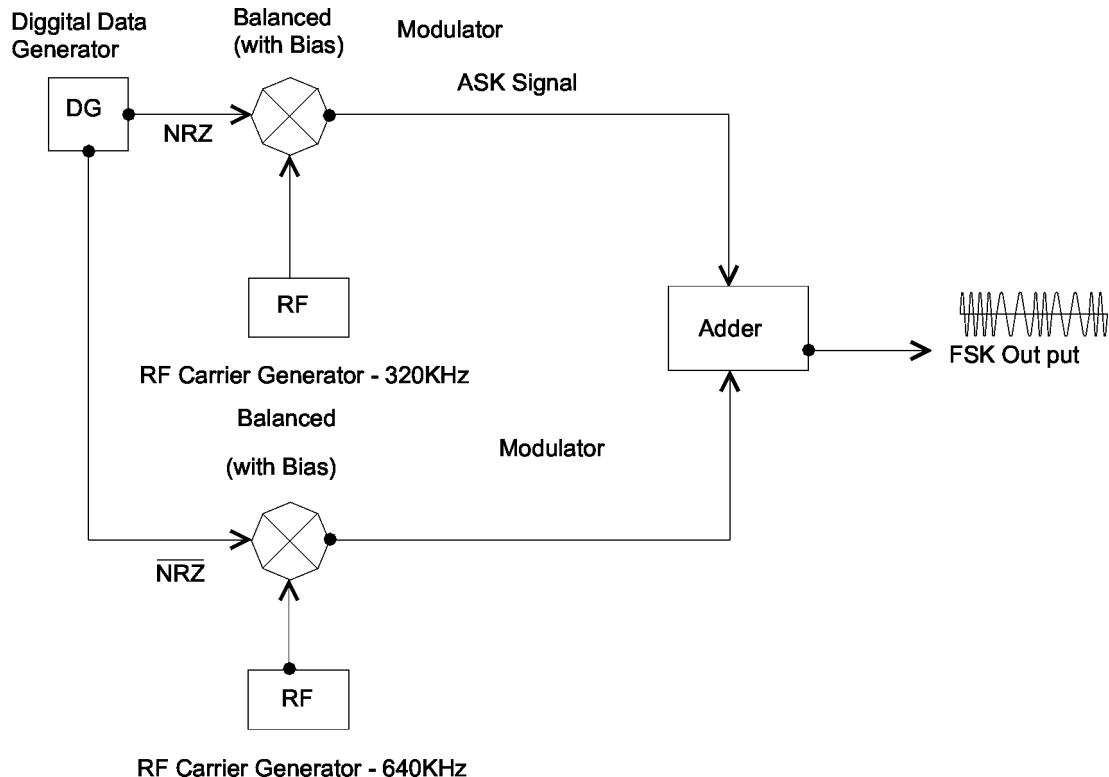
$$P_e = 1/2 e^{-(E_b/2N_0)}$$

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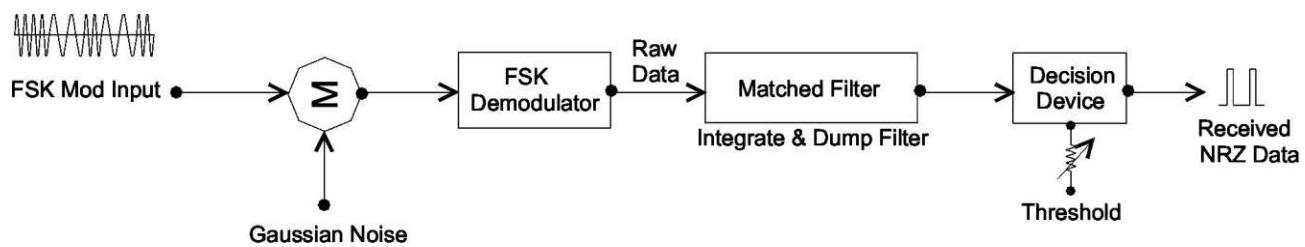
### **PRACTICAL BLOCK DIAGRAM OF FSK MODULATION/DEMODULATION :**

#### **FSK MODULATOR**

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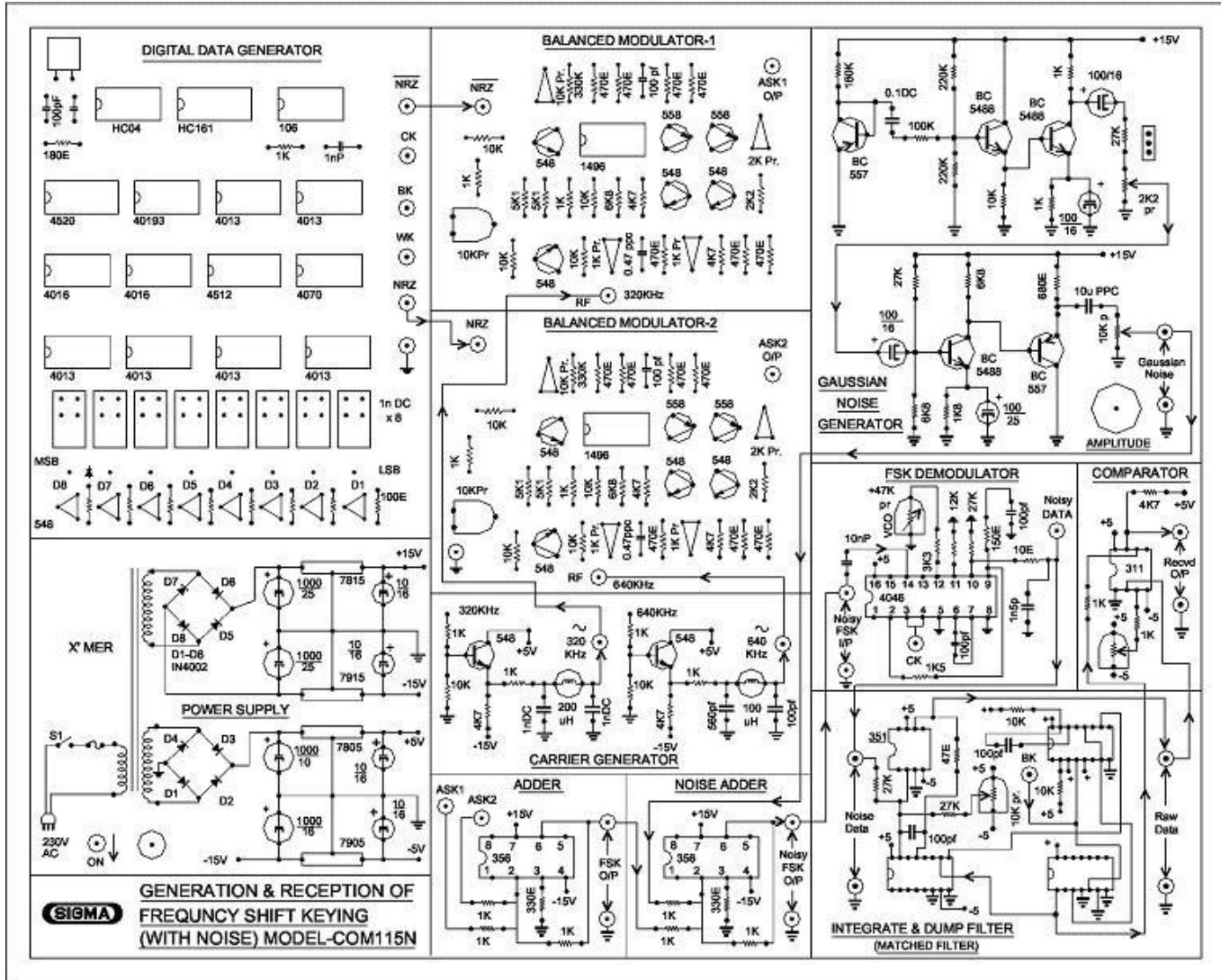
### FSK DEMODULATOR (RESONANT PHASE SHIFT DETECTOR)



### PROCEDURE:

To generate FSK signal and demodulate it by PLL detector: -

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1. Connect DSO channel 1 at carrier clock (Ck) socket and observe it ....(waveform T1).
2. Connect DSO channel 1 at bit clock(Bk) socket and observe it ....(waveform T2).
3. Connect DSO channel 1 at word clock(Wk) socket and observe it .....(waveform T3).
4. Connect DSO channel 1 at NRZ DATA(NRZ) socket and observe it .....(waveform T4).
5. Connect DSO channel 1 at NRZ\* DATA(NRZ') socket and observe it ... (waveform T5).



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6. Connect DSO channel 1 at RF carrier socket (in carrier generation section) for frequency 320kHz and 640kHz. Observe the waveforms on DSO for these two frequencies.
7. Connect DSO channel 1 at NRZ DATA (NRZ) socket.
8. Connect DSO channel 2 at the output of balanced modulator-1. Observe ASK output and draw its spectrum.
9. Same as, connect DSO channel 2 at the output of balanced modulator-2. Observe ASK output draw its spectrum.
10. Apply both output of balanced modulator 1 and balanced modulator 2 to adder section. Connect DSO channel 2 at output of the adder. Observe FSK output draw its spectrum.
11. Connect DSO channel 1 at Gaussian noise output and observe it. Keep noise level at minimum.
12. Observe received raw data signal at the output of FSK demodulator.
13. Observe received pure NRZ data at the output of data squarer.
14. Now add Gaussian noise by rotating noise level pot and observe its effect on all received signals.

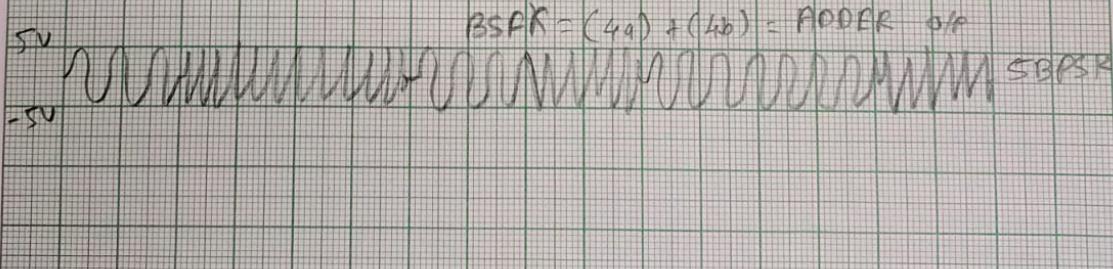
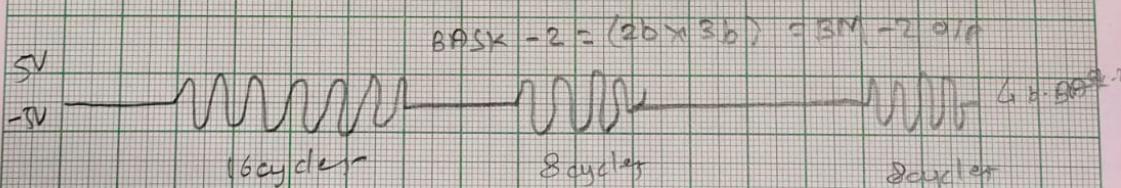
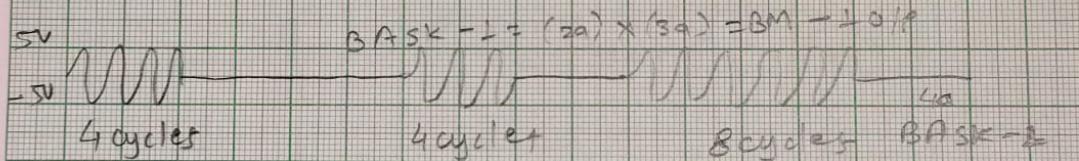
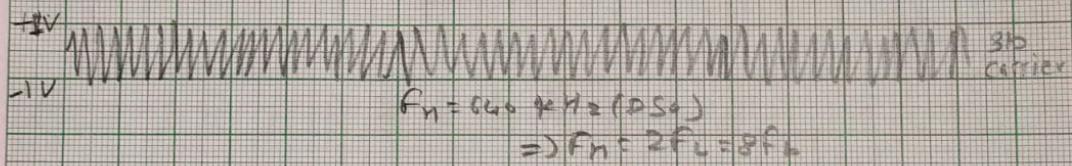
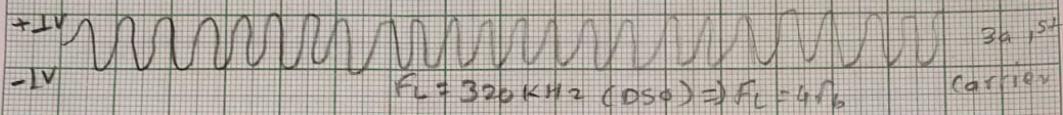
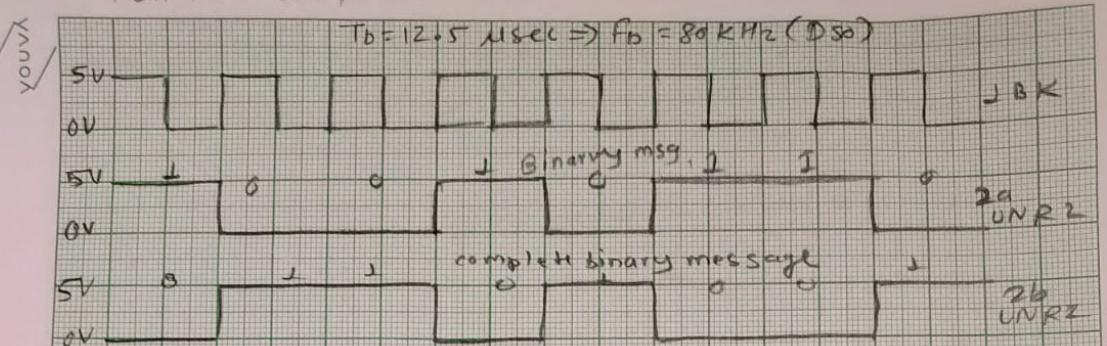
### OBSERVATIONS AND GRAPHS:

Observe and Plot the observed FSK modulator and demodulator waveform for given data input.



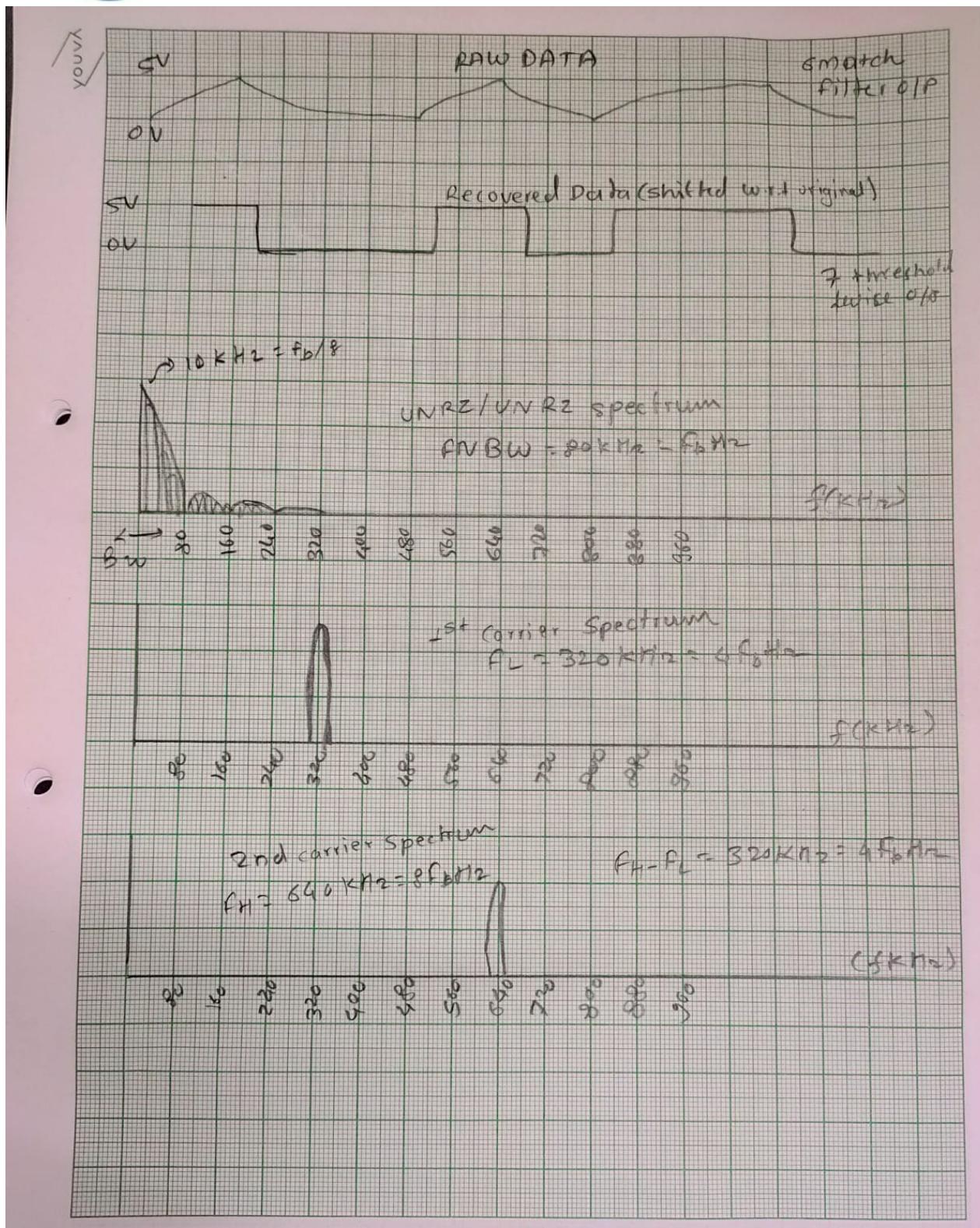
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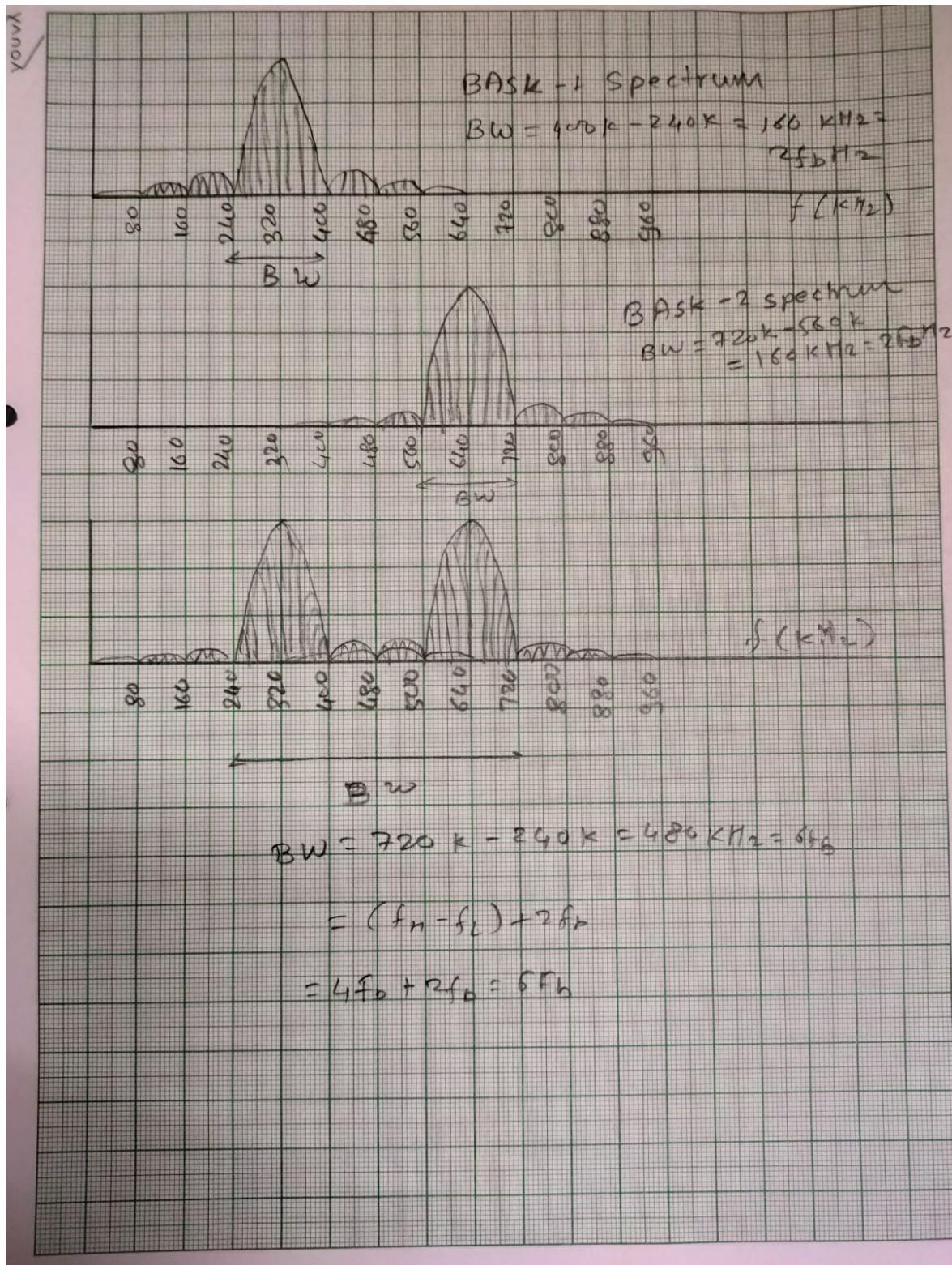


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### CONCLUSION:

- In this practical we studied the blocks in BFSK transmitter and receiver.
- We studied the power spectrum of BFSK briefly.
- We studied difference between coherent and non coherent BFSK reception technique.

### REFERENCES:

1. Modern Digital & Analog communication system-B.P.Lathi
2. “Communication Systems”- Carlson



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