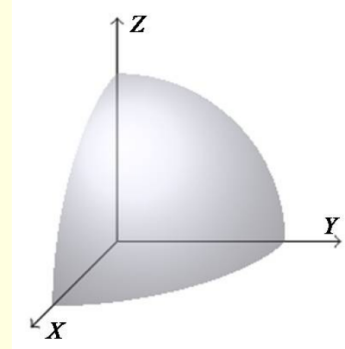


Ques1.

The value of the integral $\int_V (x^2 + y^2 + z^2) d\tau$, where V is the volume of a positive octant sphere (of radius 1) as shown in the figure, is π/n . The value of n is . Provide answer in the integer form.

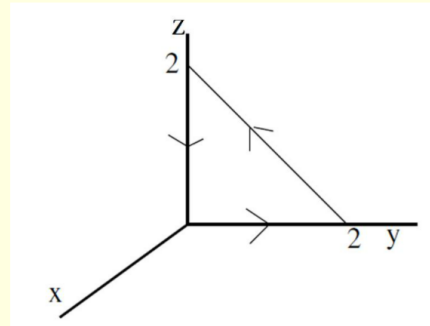


Ques2.

The value of the closed loop line integral $\oint (x^2y dx + 2xy dy)$ in a counterclockwise direction (as viewed from $+Z$ -axis) around the perimeter of the rectangle defined by $x = \pm 3, y = \pm 5$ is . Provide the answer in integer form.

Ques3.

The value of the surface integral $\int_S (\vec{\nabla} \times \vec{A}) \cdot d\vec{a}$ for the vector $\vec{A} = xy \hat{i} + 2yz \hat{j} + 3xz \hat{k}$, using the triangular area in the YZ plane (see figure), is . Round off the answer to two decimal places.



Ques4.

The value of the integral

$$I = \int_V \{r^4 + r^2(\vec{r} \cdot \vec{c}) + c^4\} \delta(\vec{r} - \vec{c}) d\tau,$$

where V is the volume of a sphere of radius 6 about the origin and $\vec{c} = 5\hat{i} + 3\hat{j} + 2\hat{k}$ and its magnitude $|\vec{c}| = c$, is . Round off the answer to the nearest integer.